

```
In [1]: from BSplineBase import BSplineBase  
        from utils import plotExampleBase, plot2DExample, plotSurface, generate_random_P  
        import numpy as np
```

# 绘制双三次B样条曲面

## B样条基函数

定义B样条基函数

```
import numpy as np

class BSplineBase:
    def __init__(self, U=np.asarray([0,0,0,0,0.5,1,1,1,1])):
        self.U=U
        # self.n=n
    def GetValue(self, u, i, degree=3):
        U=self.U
        p=degree
        if degree==0:
            if u>=U[i] and u<=U[i+1]:
                return 1
            else:
                return 0
        else:
            degree=degree-1
            if u>=U[i] and u<=U[i+p+1]:
                if U[i+p]!=U[i] and U[i+p+1]!=U[i+1]:
                    return (u-U[i])/(U[i+p]-U[i])*self.GetValue(u, i, degree)+(U[i+p+1]-u)/(U[i+p+1]-U[i+1])*self.GetValue(u, i+1, degree)
                elif U[i+p]!=U[i]:
                    return (u-U[i])/(U[i+p]-U[i])*self.GetValue(u, i, degree)
                elif U[i+p+1]!=U[i+1]:
                    return (U[i+p+1]-u)/(U[i+p+1]-U[i+1])*self.GetValue(u, i+1, degree)
                else:
                    return 0
            else:
                return 0
```

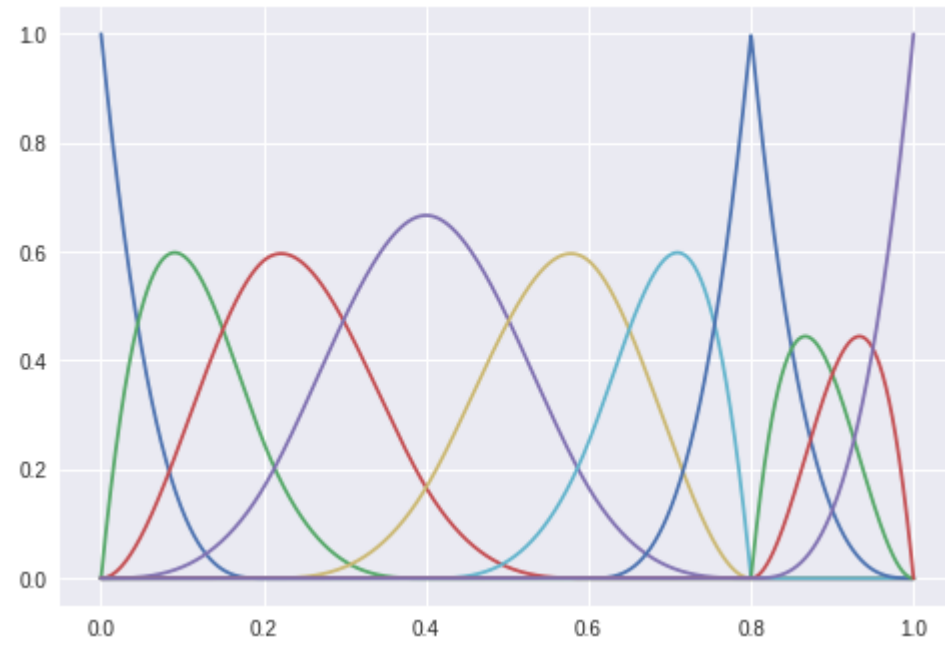
```
In [2]: U = np.array([0,0,0,0,0.2,0.4,0.6,0.8,0.8,0.8,1,1,1,1])  
        V = np.array([0,0,0,0,0.2,0.2,0.2,0.4,0.6,0.8,1,1,1,1])
```

绘制的B样条基函数如下图所示

U 方向

```
In [3]: plotExampleBase(U=U,n=3)
```

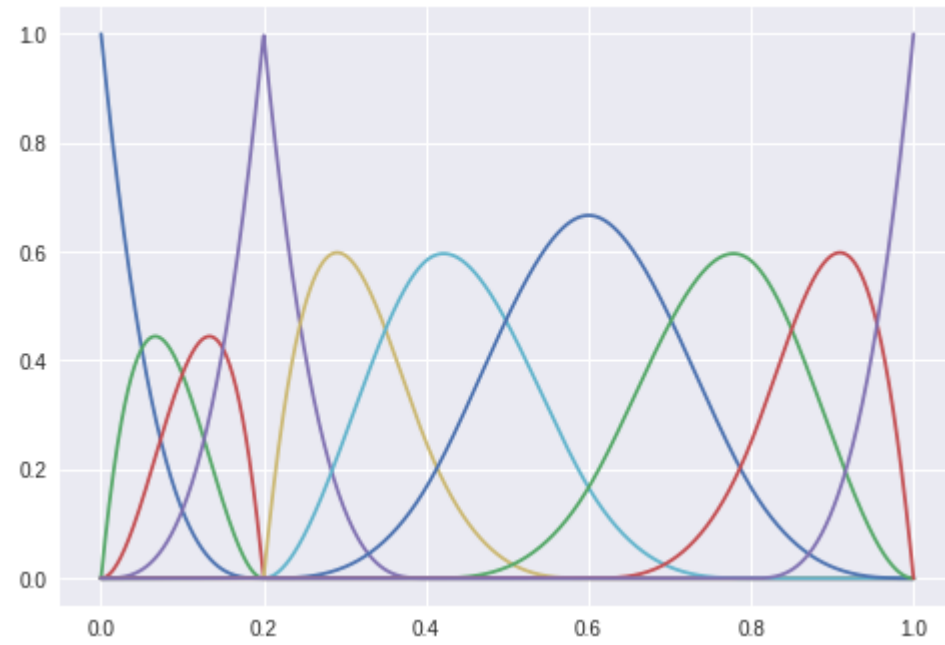
10



V 方向

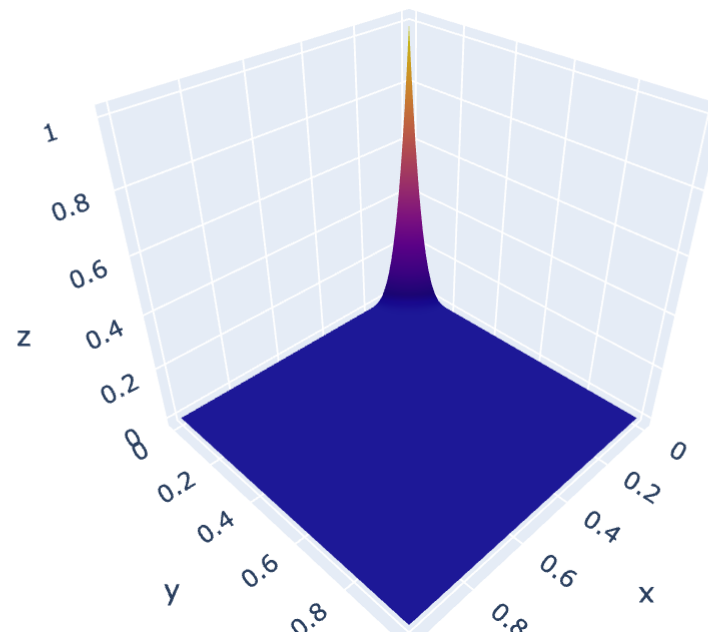
```
In [10]: plotExampleBase(U=V,n=3)
```

10

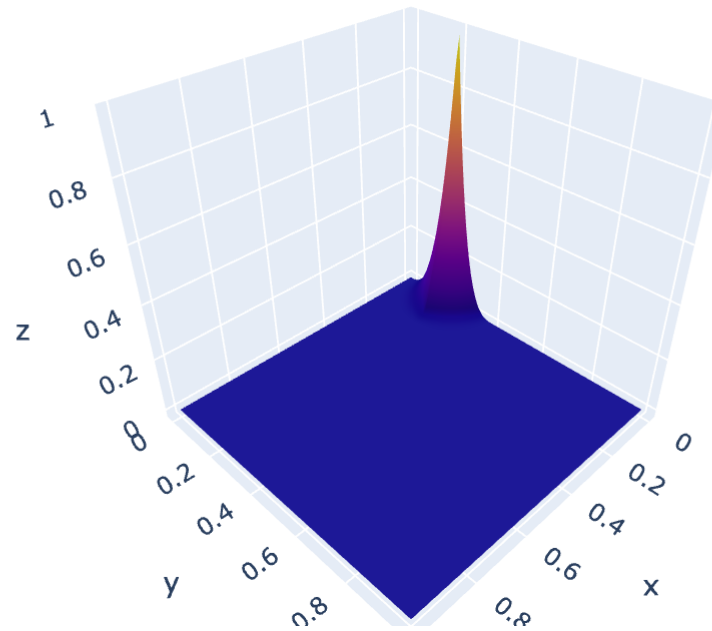


## 张量积基函数的绘制

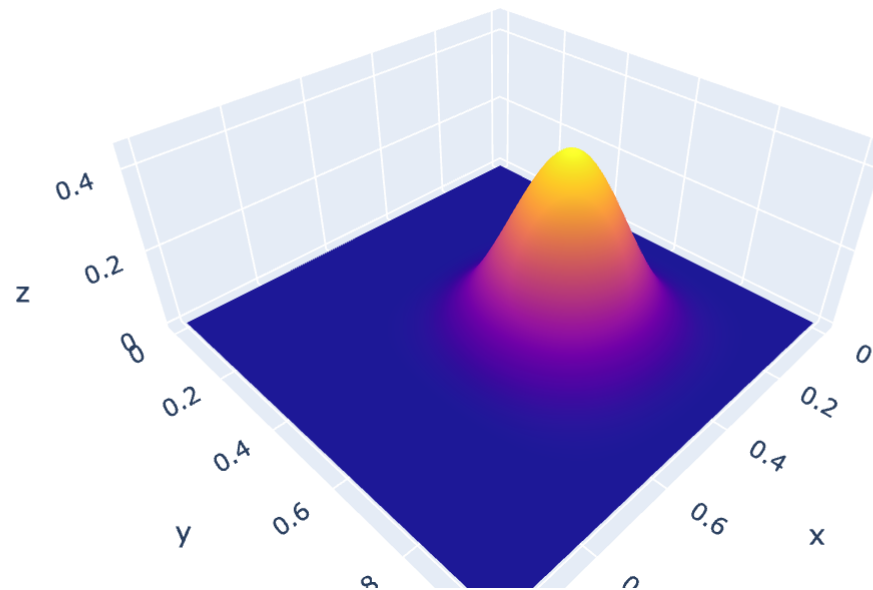
```
In [5]: plot2DExample(U,V,i=0,j=0)
```



```
In [6]: plot2DExample(U,V,i=0,j=3)
```



```
In [7]: plot2DExample(U,V,i=3,j=6)
```





## 双三次B样条曲面的绘制

随机生成的P

```
import numpy as np
import math
def generate_random_P():
    P = []
    for i in range(-5,5):
        tmp = []
        for j in range(-5,5):
            tmp.append([i,j,10-math.floor((i*i+j*j)/20)+np.random.rand()])
        P.append(tmp)
    P=np.asarray(P)
    return P
```

```
In [11]: P = generate_random_P()  
print(P)
```

```
[ [ [-5.      -5.      8.40345892 ]
  [-5.      -4.      8.44557891 ]
  [-5.      -3.      9.82681644 ]
  [-5.      -2.      9.86655201 ]
  [-5.      -1.      9.79615623 ]
  [-5.       0.      9.48181466 ]
  [-5.       1.      9.23705771 ]
  [-5.       2.      9.87263815 ]
  [-5.       3.      9.92803818 ]
  [-5.       4.      8.92057119 ] ]
```

```
[ [ [-4.      -5.      8.26126541 ]
  [-4.      -4.      9.20648574 ]
  [-4.      -3.      9.7903323  ]
  [-4.      -2.      9.84592371 ]
  [-4.      -1.     10.90397502 ]
  [-4.       0.     10.28341045 ]
  [-4.       1.     10.56462995 ]
  [-4.       2.      9.24712414 ]
  [-4.       3.      9.59711187 ]
  [-4.       4.      9.87036127 ] ]
```

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[ [ [-3.      -5.      9.41784256 ]
  [-3.      -4.      9.60266406 ]
  [-3.      -3.     10.99971199 ]
  [-3.      -2.     10.92796076 ]
  [-3.      -1.     10.51937373 ]
  [-3.       0.     10.86642652 ]
  [-3.       1.     10.92584685 ]
  [-3.       2.     10.00912443 ]
  [-3.       3.     10.27162369 ]
  [-3.       4.      9.71330262 ] ]
```

```
[ [ [-2.      -5.      9.90670443 ]
  [-2.      -4.      9.1649982  ]
  [-2.      -3.     10.62553695 ]
  [-2.      -2.     10.22045737 ]
  [-2.      -1.     10.92299548 ]
  [-2.       0.     10.33666927 ]
  [-2.       1.     10.42686432 ]
```

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      [-2.      2.      10.50820218]
      [-2.      3.      10.67503104]
      [-2.      4.      9.93733606]]

[[ [-1.      -5.      9.3955832  ]
   [-1.      -4.      10.53858005]
   [-1.      -3.      10.04504879]
   [-1.      -2.      10.12469699]
   [-1.      -1.      10.35946259]
   [-1.       0.      10.69516686]
   [-1.       1.      10.66029895]
   [-1.       2.      10.82210764]
   [-1.       3.      10.15670177]
   [-1.       4.      10.0934782  ]]

[[ [ 0.      -5.      9.22254981]
   [ 0.      -4.      10.42248877]
   [ 0.      -3.      10.80476173]
   [ 0.      -2.      10.28647752]
   [ 0.      -1.      10.81628797]
   [ 0.       0.      10.8917794  ]
   [ 0.       1.      10.07694181]
   [ 0.       2.      10.64895834]
   [ 0.       3.      10.61080486]
   [ 0.       4.      10.80665907]]

[[ [ 1.      -5.      9.636292  ]
   [ 1.      -4.      10.61756828]
   [ 1.      -3.      10.53711928]
   [ 1.      -2.      10.12948602]
   [ 1.      -1.      10.83841346]
   [ 1.       0.      10.53625719]
   [ 1.       1.      10.77639787]
   [ 1.       2.      10.95344232]
   [ 1.       3.      10.76407113]
   [ 1.       4.      10.61515092]]

[[ [ 2.      -5.      9.71650097]
   [ 2.      -4.      9.71645262]
   [ 2.      -3.      10.85845072]
   [ 2.      -2.      10.00805556]

```

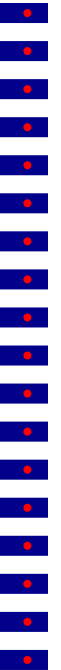
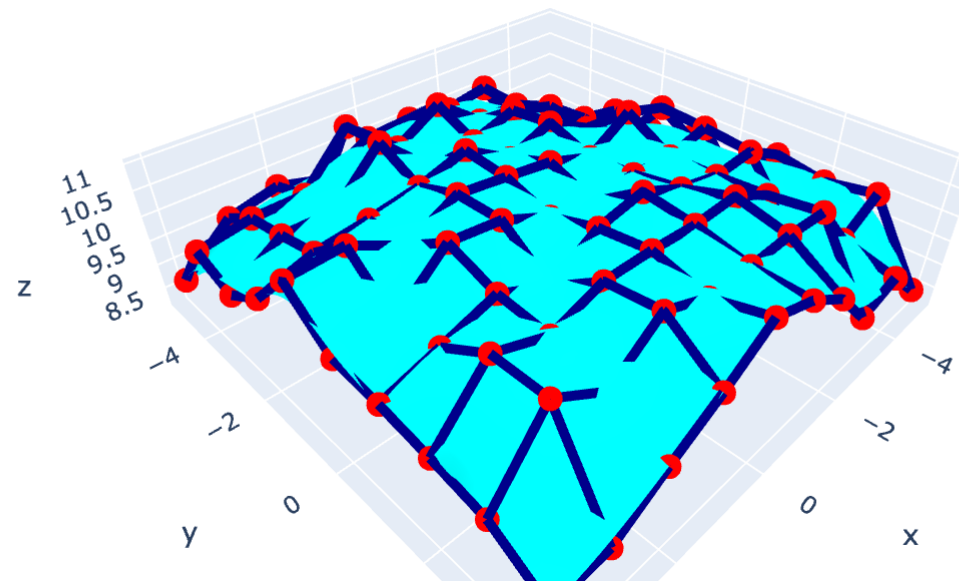
```
[ 2.      -1.      10.21107822 ]
[ 2.       0.      10.20454736 ]
[ 2.       1.      10.78479848 ]
[ 2.       2.      10.82884946 ]
[ 2.       3.      10.35044135 ]
[ 2.       4.       9.23355347 ] ]

[[ 3.      -5.       9.03241077 ]
 [ 3.      -4.       9.07150842 ]
 [ 3.      -3.      10.01823035 ]
 [ 3.      -2.      10.29600977 ]
 [ 3.      -1.      10.60321965 ]
 [ 3.       0.      10.49554577 ]
 [ 3.       1.      10.5792061  ]
 [ 3.       2.      10.70732042 ]
 [ 3.       3.      10.79169745 ]
 [ 3.       4.       9.45627108 ] ]

[[ 4.      -5.       8.6912883  ]
 [ 4.      -4.       9.3817444  ]
 [ 4.      -3.       9.56360327 ]
 [ 4.      -2.       9.67113859 ]
 [ 4.      -1.      10.9144551  ]
 [ 4.       0.      10.68233237 ]
 [ 4.       1.      10.3683772  ]
 [ 4.       2.       9.76501851 ]
 [ 4.       3.       9.69002243 ]
 [ 4.       4.       9.76769399 ] ] ]
```

开始绘制

```
In [9]: plotSurface(U,V,P)
```



```
In [ ]:
```