

# Lecture Presentation

## Advanced Multi-Well Formation Evaluation

### Shaly Sandstone Interpretation

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1

### Objectives:

1. To understand the influence of shale on the electrical resistivity of sands,
2. To introduce petrophysical models used to assess the various types of “shale emplacement” in sands,
3. To introduce the concepts of clay-bound water and cation-ion exchange capacity of clays,
4. To introduce the various petrophysical models used to describe the electrical resistivity of shaly sands, and
5. To introduce the governing factors and measurements thereof necessary to properly correct the influence of shale in the assessment of hydrocarbon saturation.

2

## Examples of Turbidites: Bouma Sequences



Thick-bedded turbidite sands



Thick-bedded turbidite sand with discontinuous shale-clast horizons

3

## Example of Laminated Sands in Distal Turbidite Systems



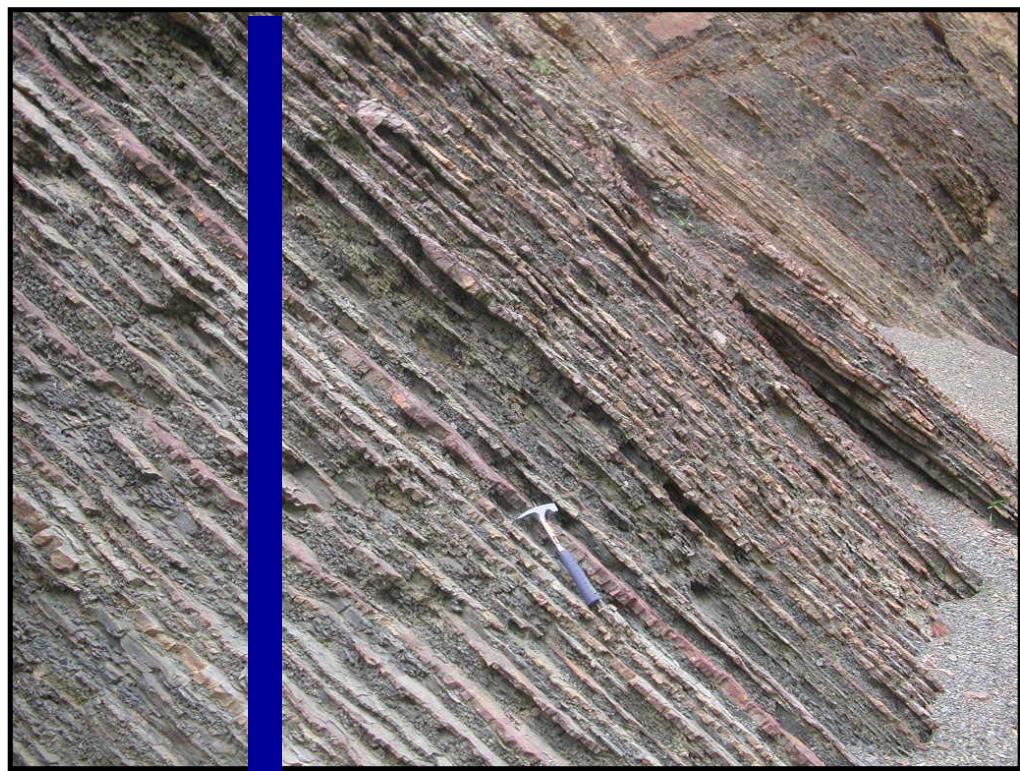
4

## Delta Front



5

## Bedding Orientation vs. Measurement Orientation

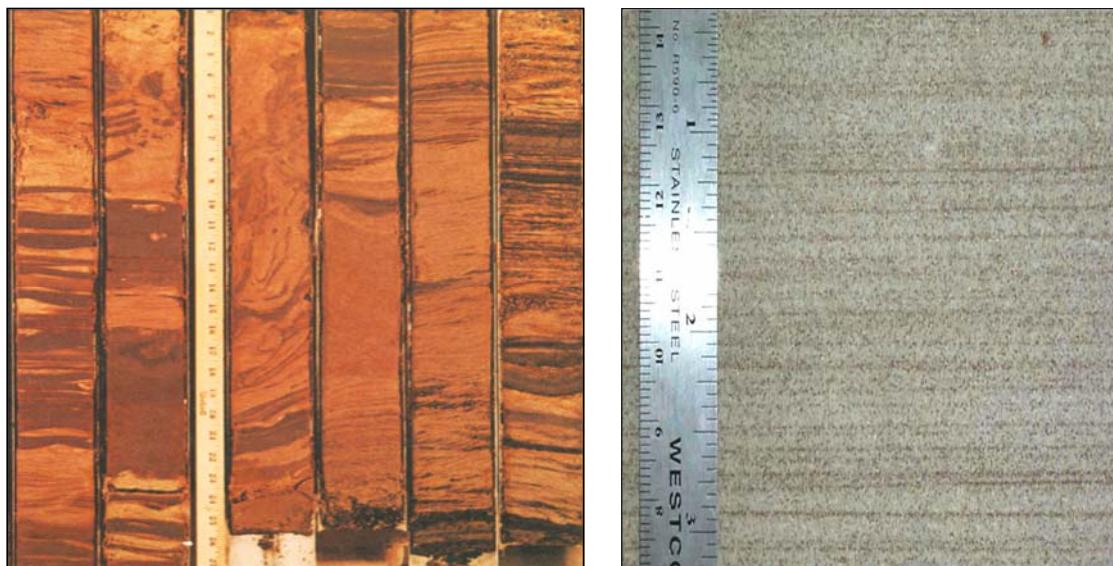


6

# Deltaic Sequences: Thinly-Bedded Rock Formations



## Origin of Electrical Anisotropy



- Laminated sand-shale sequences

- Different grain sizes
- Poor sorting

## Example of Fine Layering



9

## Origin of Electrical Anisotropy



Laminated  
sand-shale sequences



Sands With  
Different Grain Size

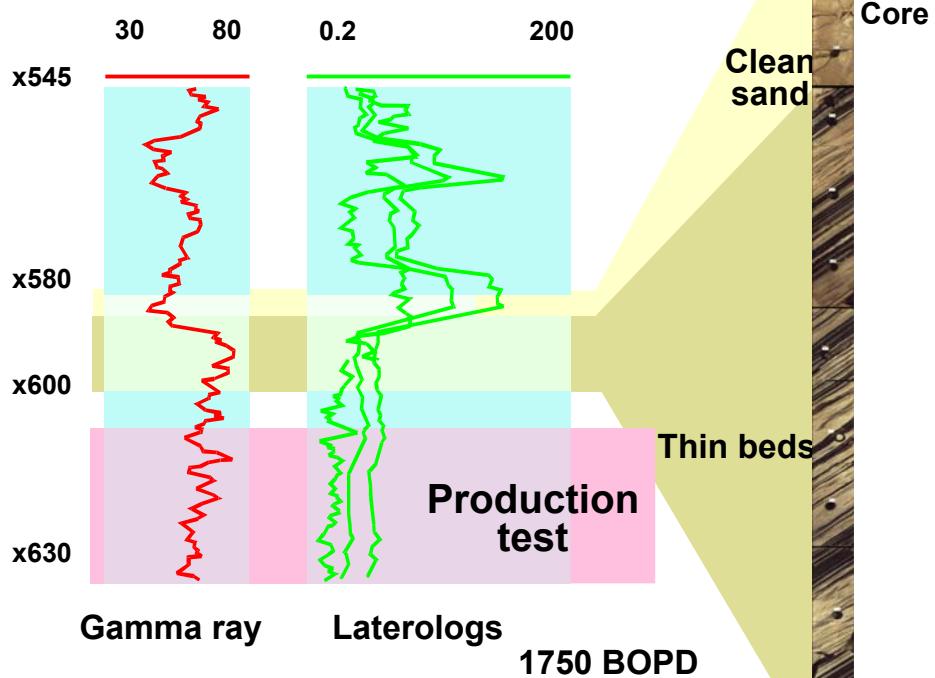


Thin resistive or  
conductive streaks

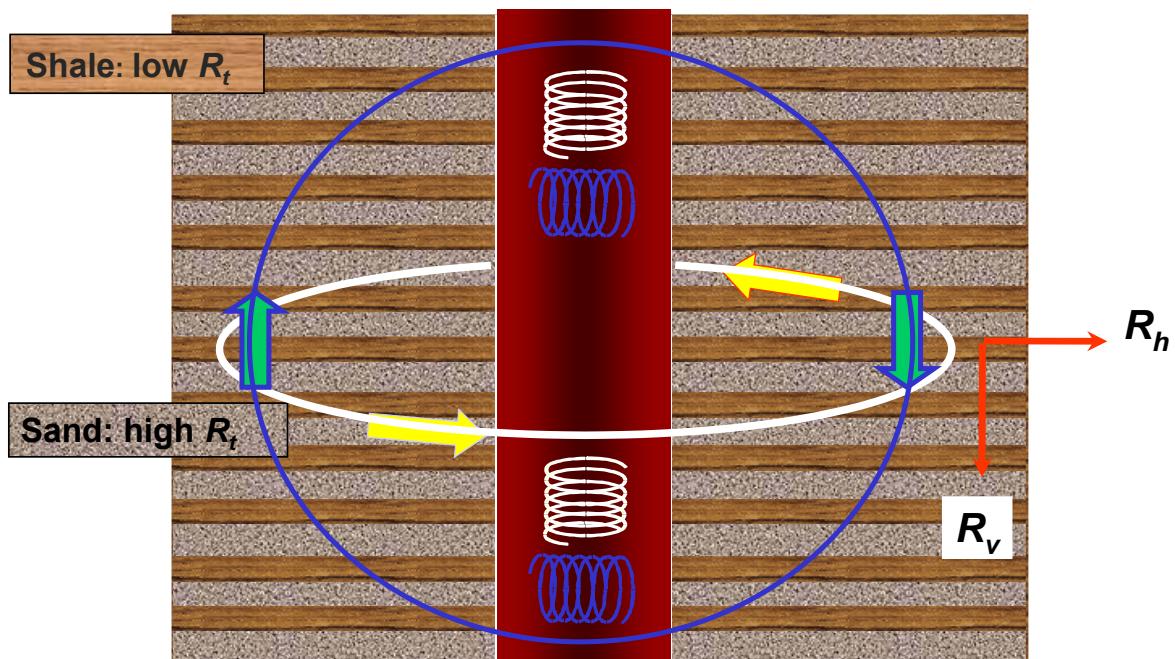
20-30% of global reserves in anisotropic reservoirs

10

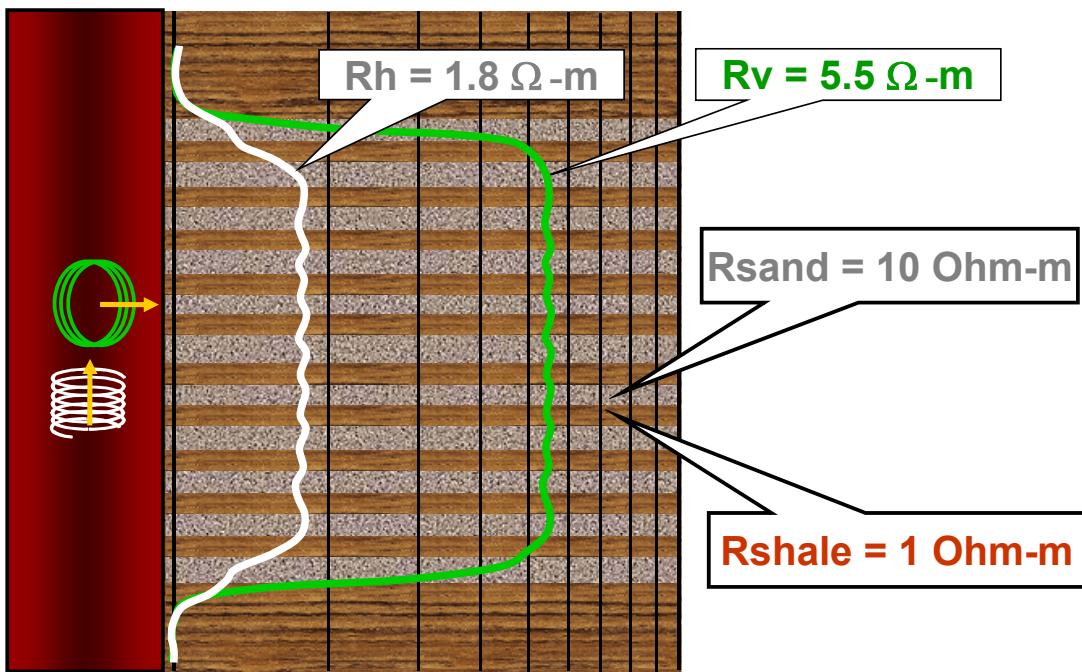
## Resistivity: example



## Measurement Principle

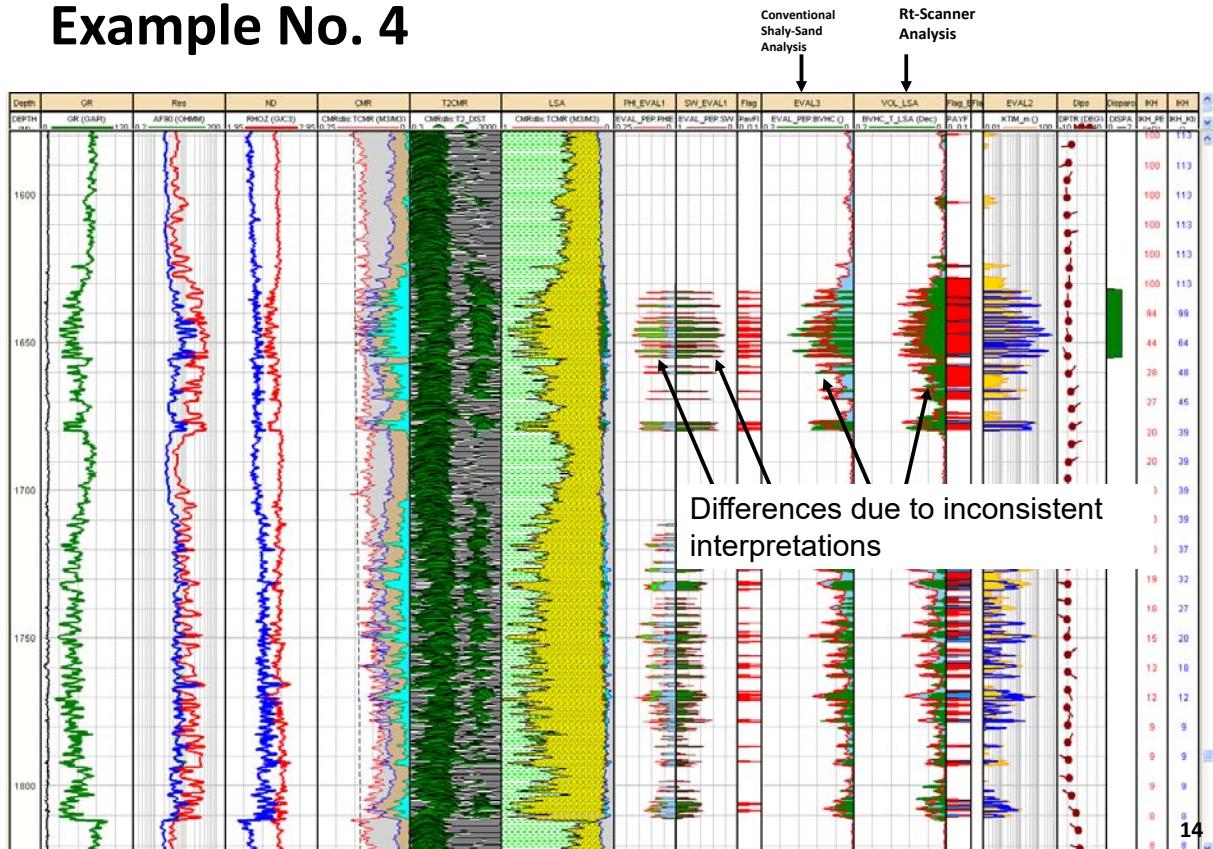


# Sand-Shale Resistivity Model



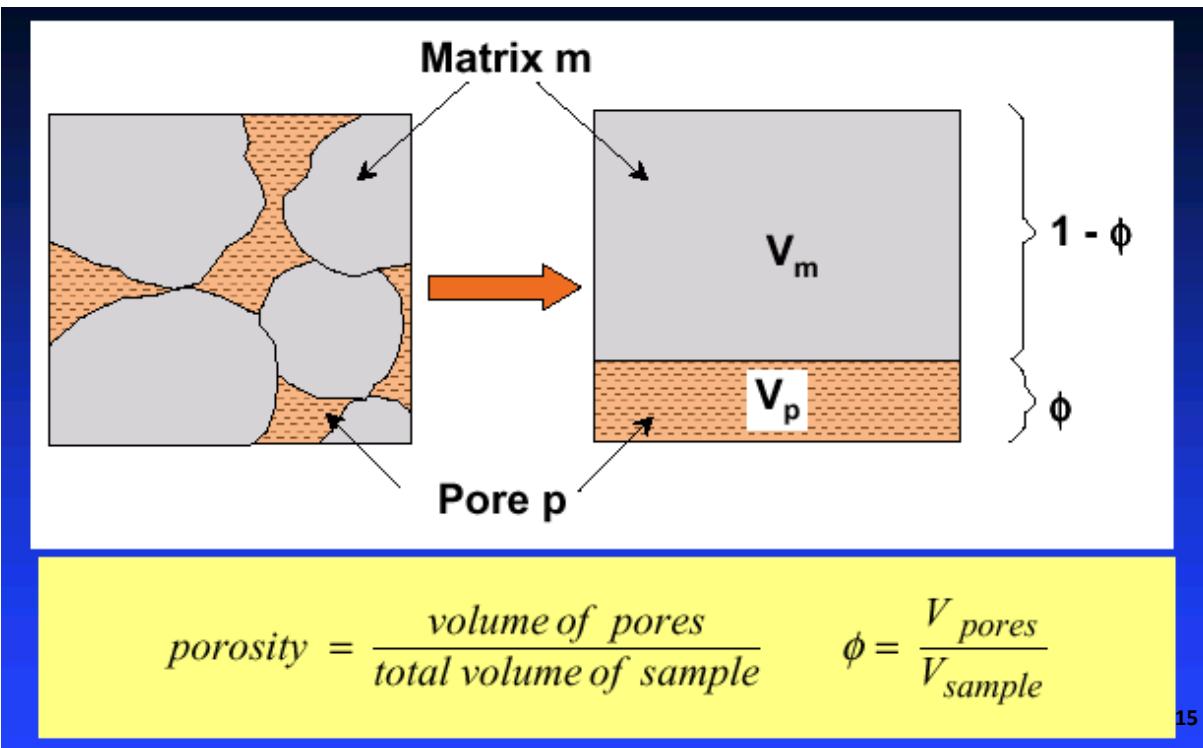
13

## Example No. 4



14

# Review: Definition of Porosity



## POROSITY

- TOTAL POROSITY?
- NON-SHALE POROSITY?
- EFFECTIVE POROSITY

## WATER SATURATION

- TOTAL WATER SATURATION?
- FREE (MOVABLE) WATER?
- IRREDUCIBLE WATER SATURATION (i.e. clay-bound water and capillary-bound water)?

# Review: Fluids in the Pore Space

$$\text{saturation}_i = \frac{\text{volume fluid } i}{\text{pore volume}}$$

Bulk Volume Water

BVW

- fraction of pore volume occupied by water

Bulk Volume Irreducible

BVI

- fraction of pore volume occupied by immobile capillary-bound water

Clay Bound Water

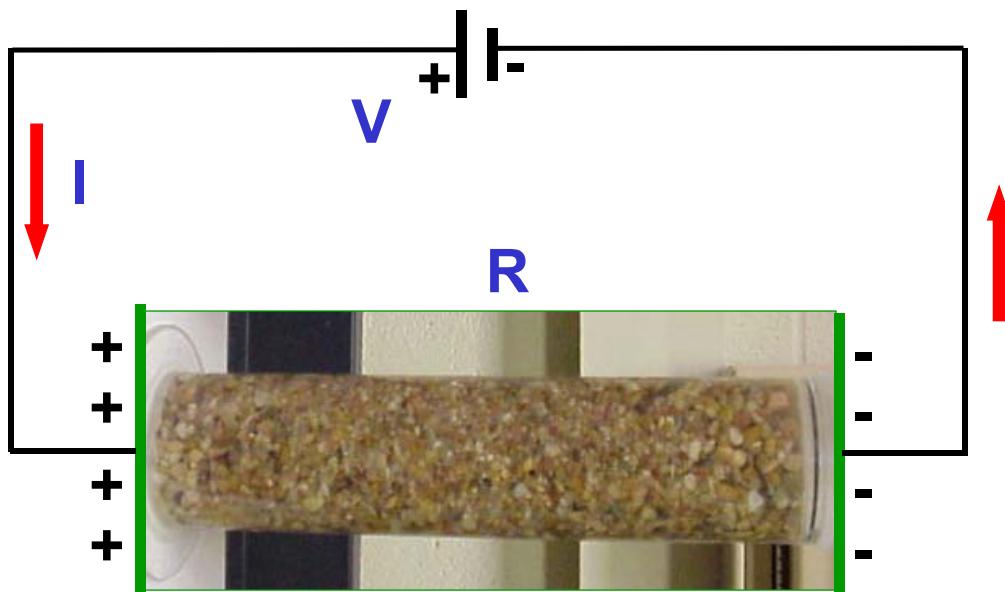
CBW

- water bound to negatively charged clay mineral surface

17

## LABORATORY SAMPLE

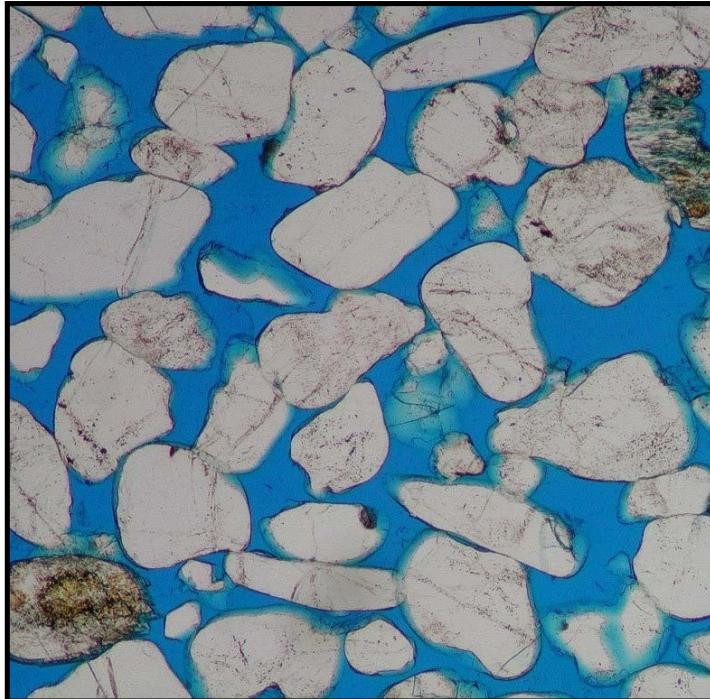
Brine-Water Saturation



$$R = \frac{V}{I}$$

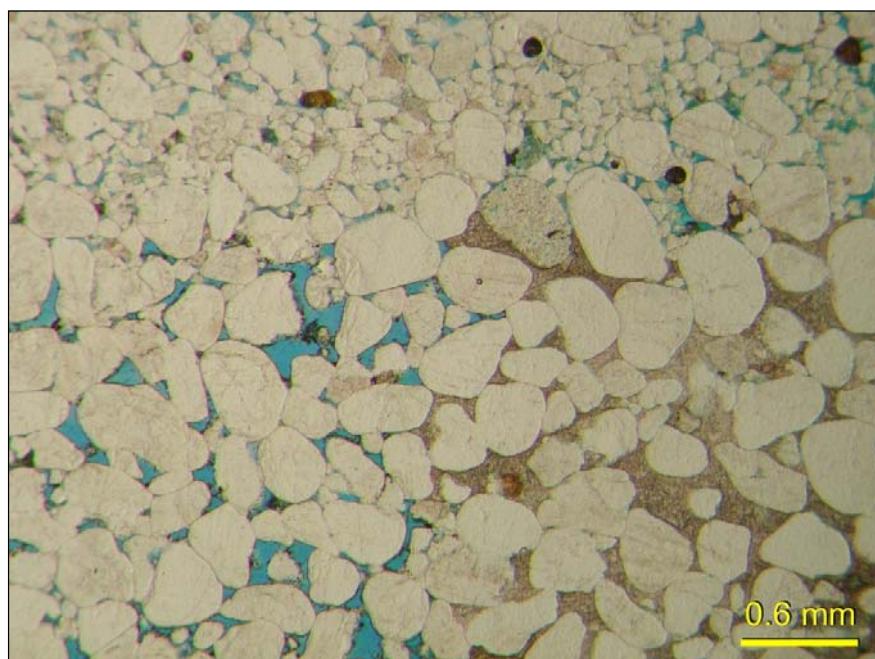
18

**DC ELECTRICAL CONDUCTION PHENOMENA IN  
POROUS MEDIA: Resistivity of Connate Water  
and Effective Porosity**



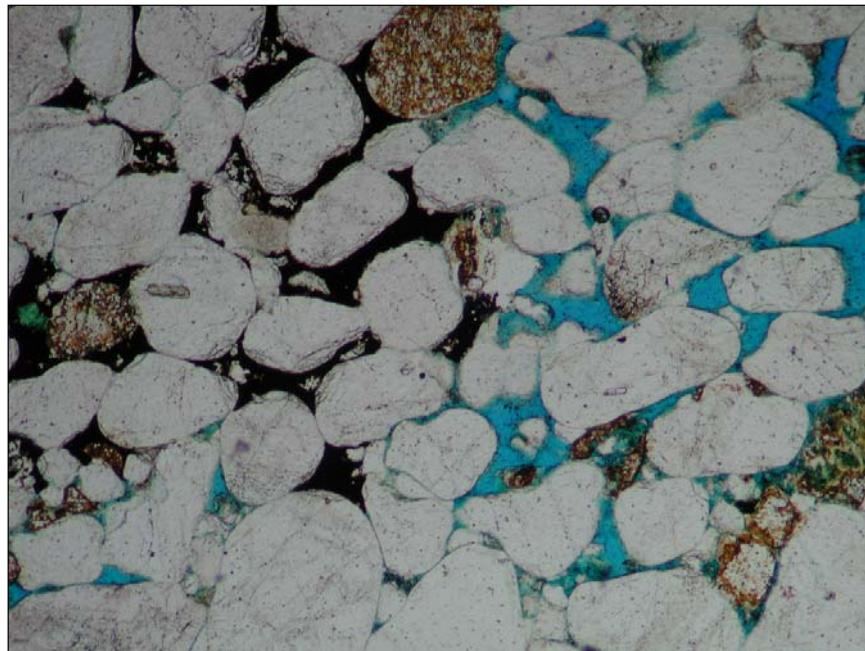
19

**DC ELECTRICAL CONDUCTION  
PHENOMENA IN POROUS MEDIA: Path of  
Electrical Conduction and Cementation**



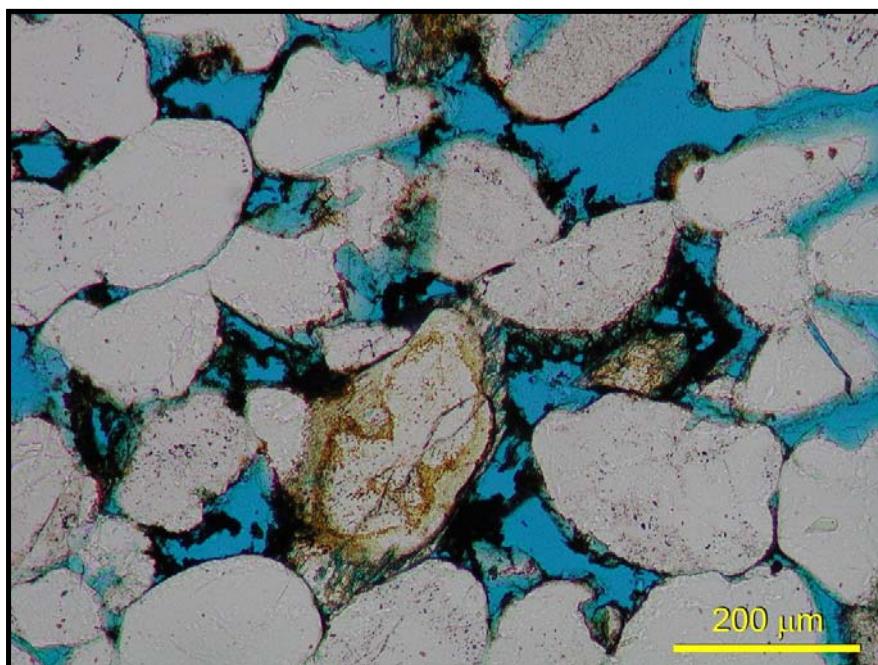
20

**DC ELECTRICAL CONDUCTION  
PHENOMENA IN POROUS MEDIA: Blockage  
of Conduction Paths by Hydrocarbons**



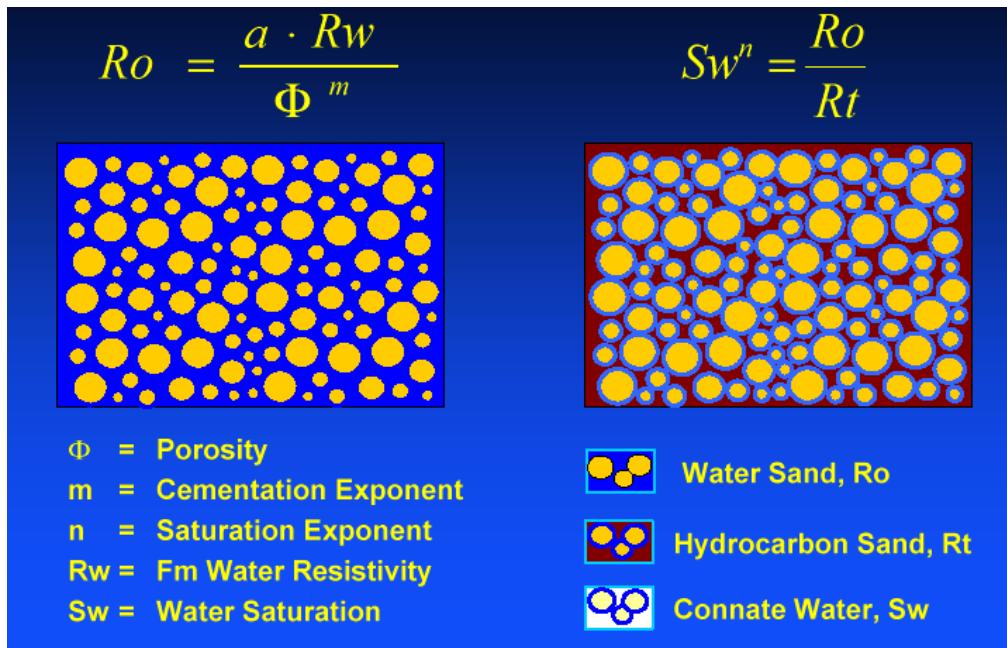
21

**DC ELECTRICAL CONDUCTION  
PHENOMENA IN POROUS MEDIA: Blockage  
of Conduction Paths by Hydrocarbons**



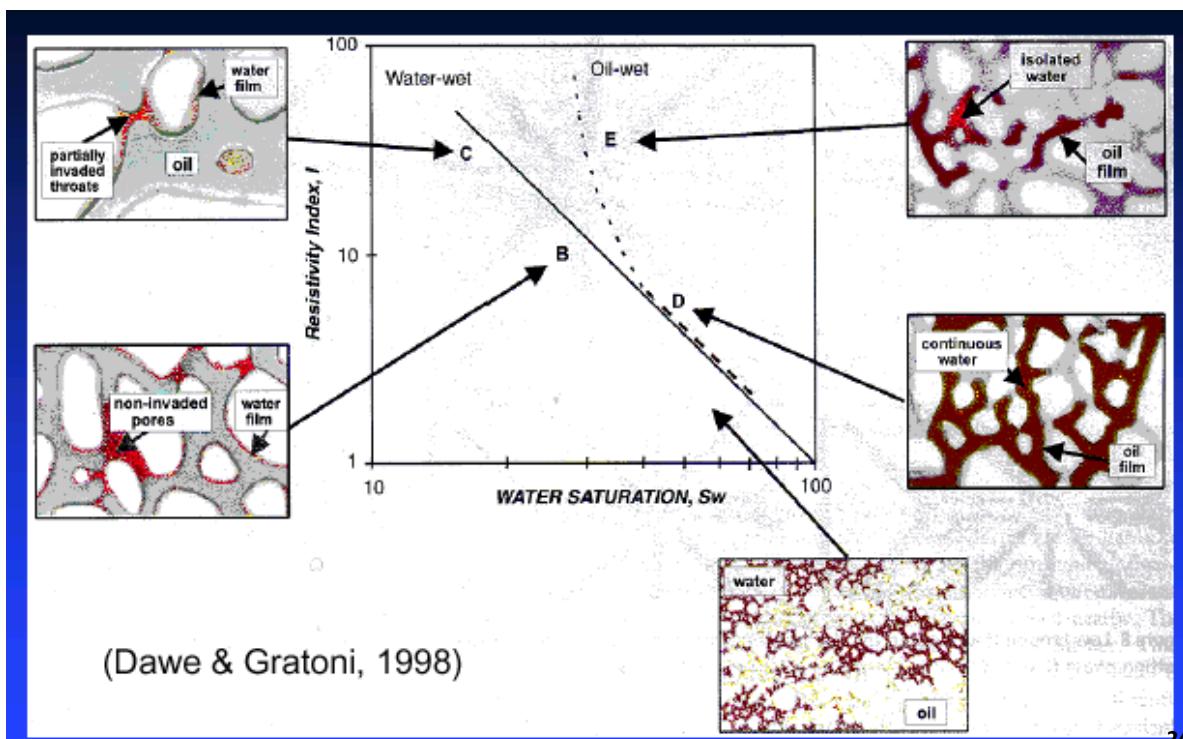
22

## ARCHIE'S "Clean Sand" Equation Effective DC Resistivity Response



23

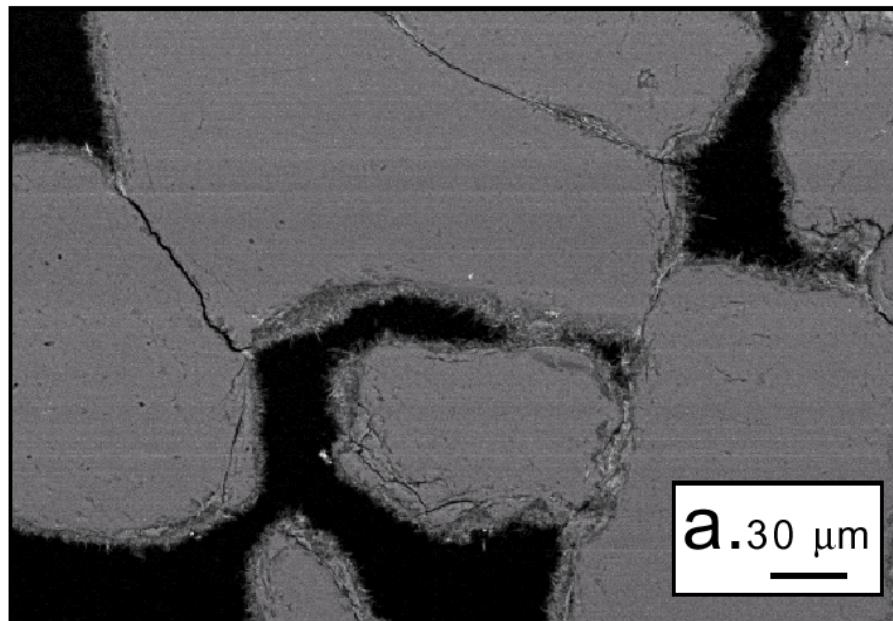
## Saturation Exponent: Water-Wet vs. Oil Wet



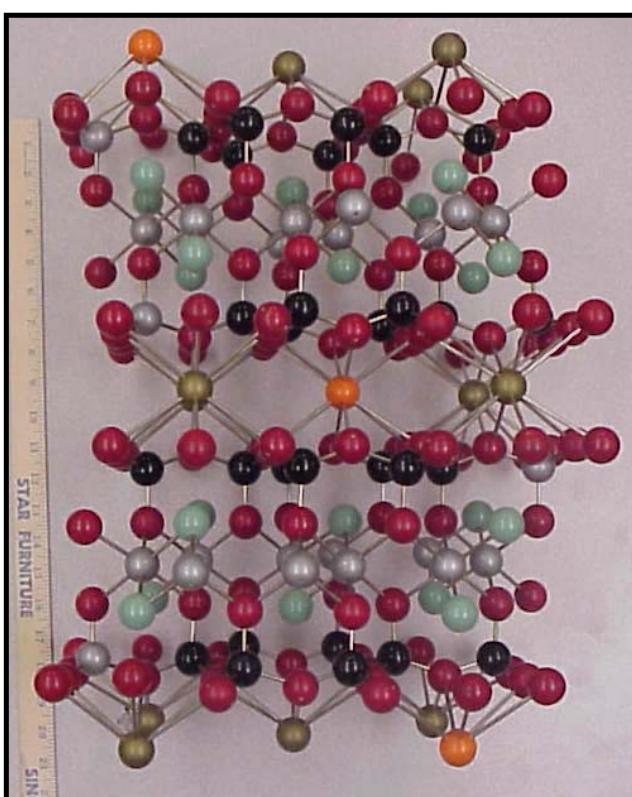
24

## What is a clay?

### Example of Clay-Coated Sand Grains



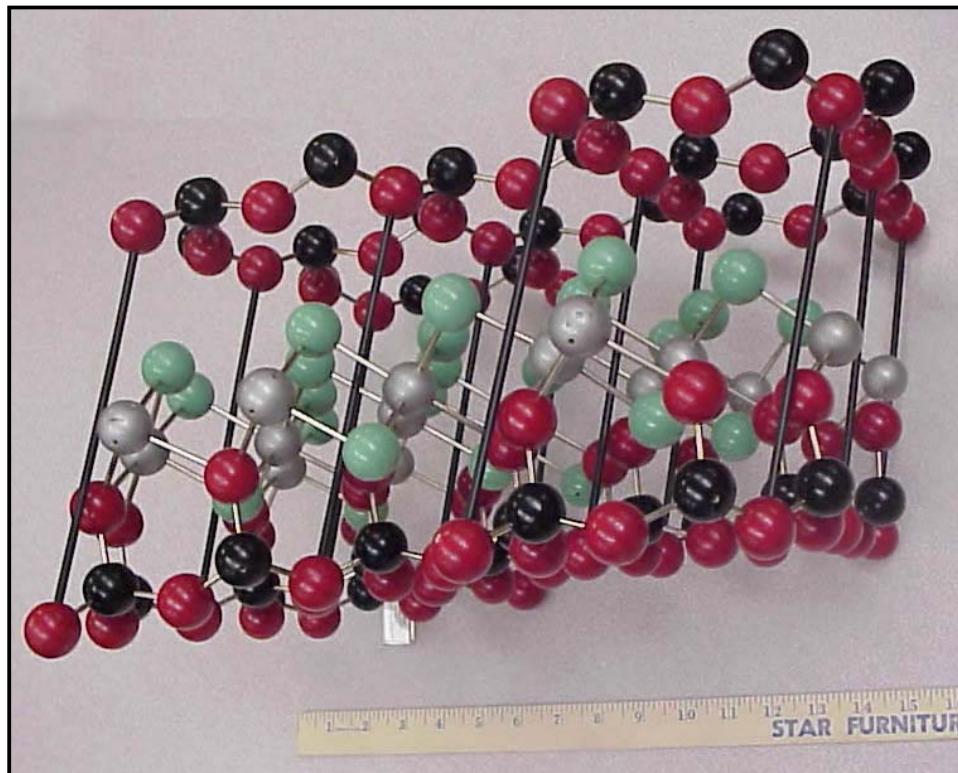
25



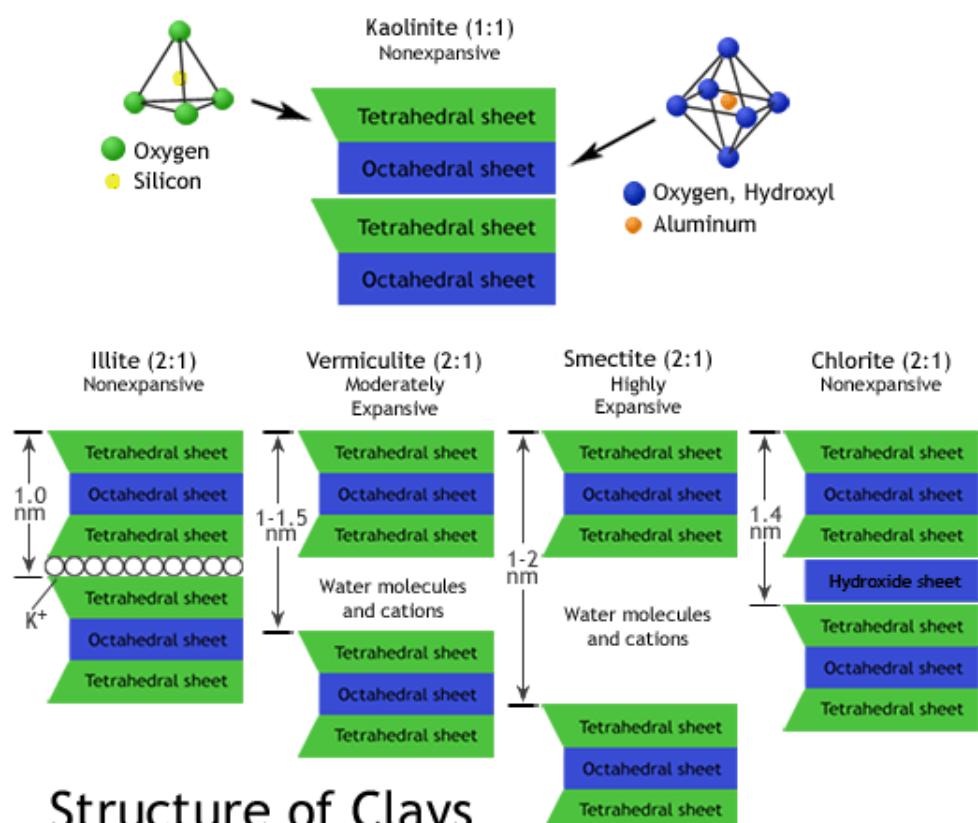
ILLITE:  
CRYSTALINE  
STRUCTURE

26

# KAOLINITE: CRYSTALINE STRUCTURE



27



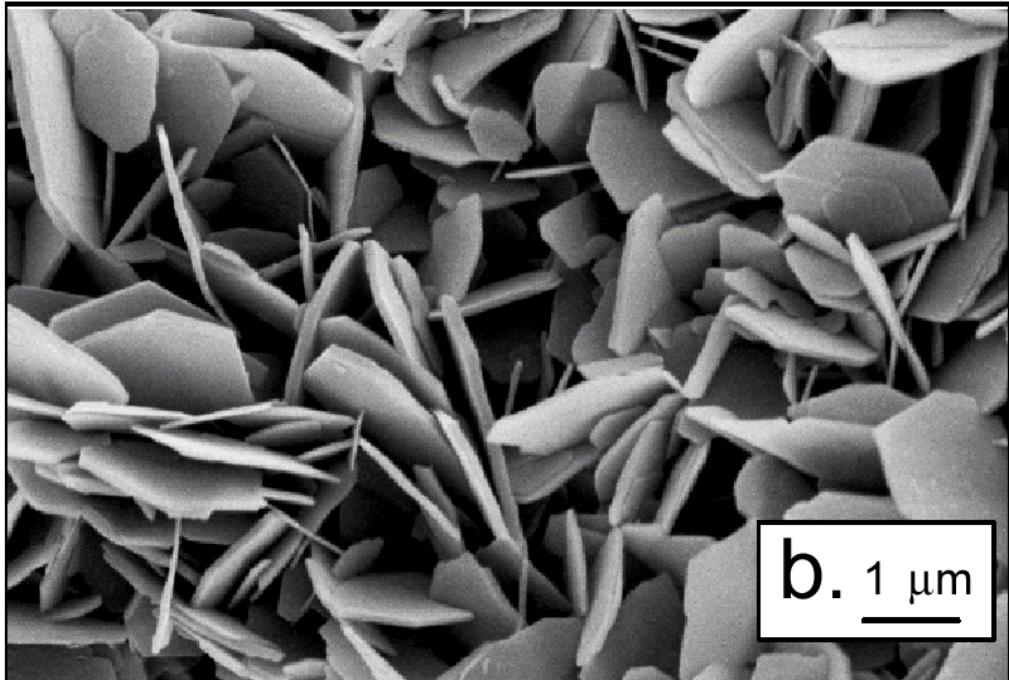
Structure of Clays

Created by Josh Lory for [www.soilsurvey.org](http://www.soilsurvey.org)

28

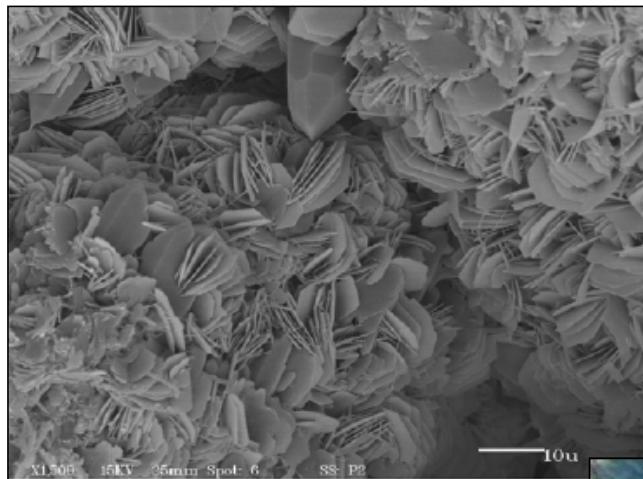
# What is a clay?

## Example: Chlorite

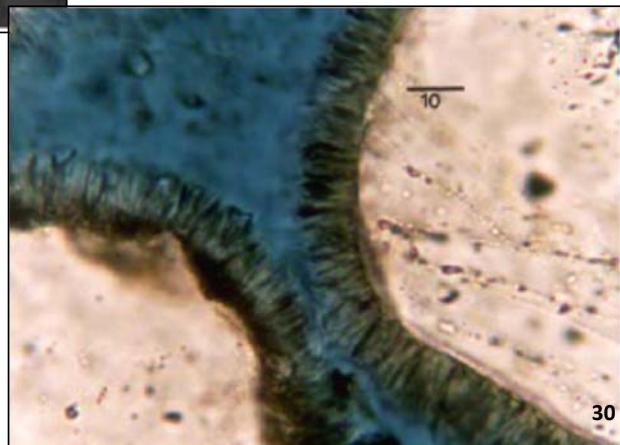


b.  $1 \mu\text{m}$

29

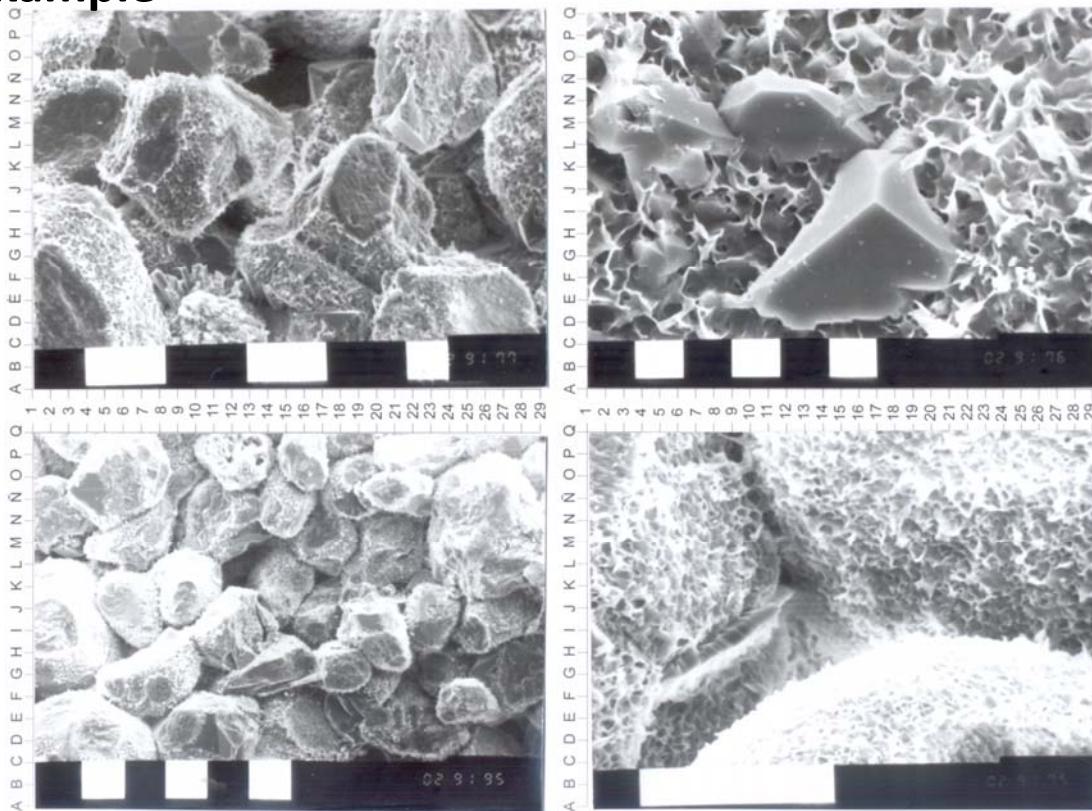


Examples of  
Grain-Coating  
Chlorite



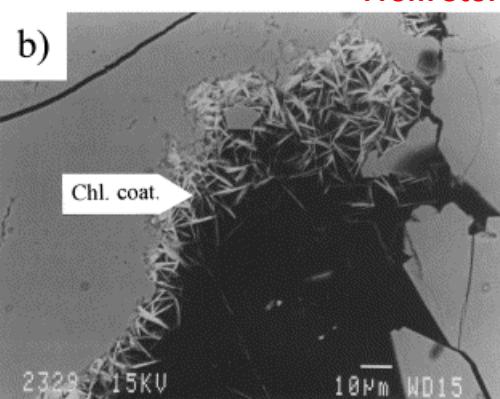
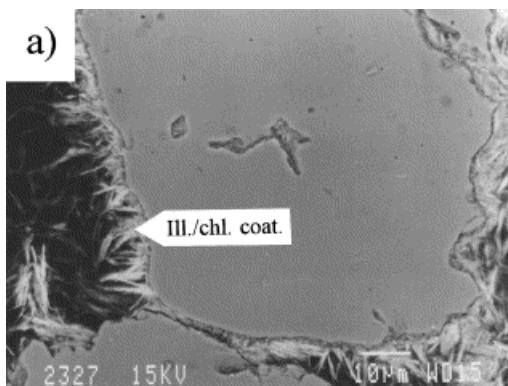
30

## Example



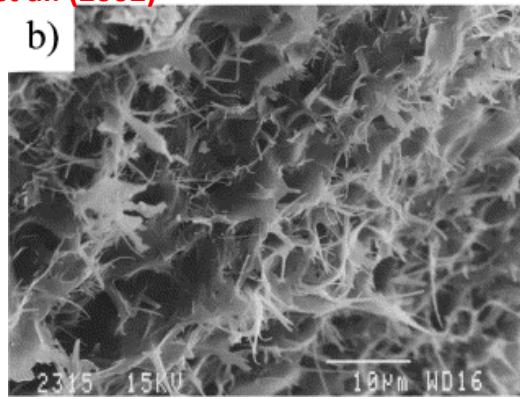
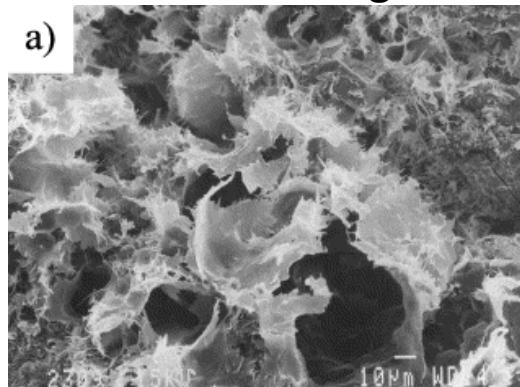
31

## Illite and Chlorite Coating



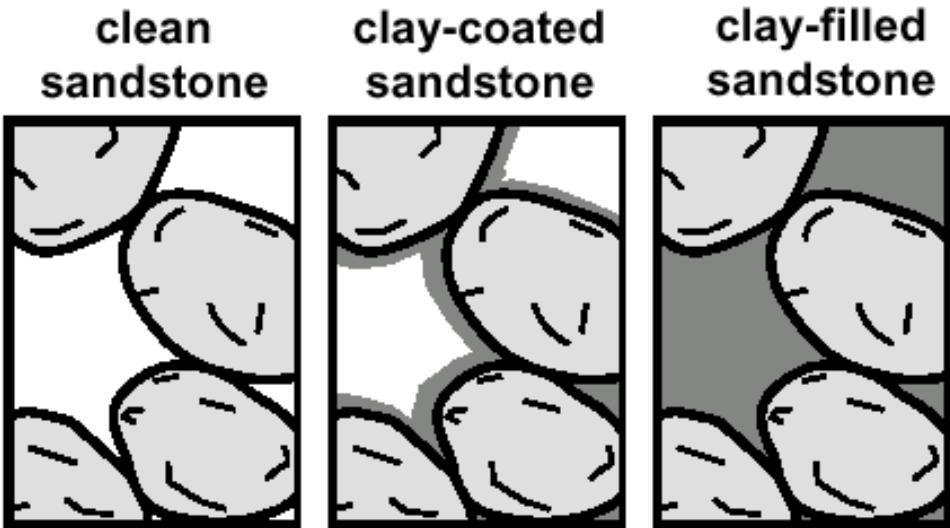
From Storvoll et al. (2002)

## Illite Coating



32

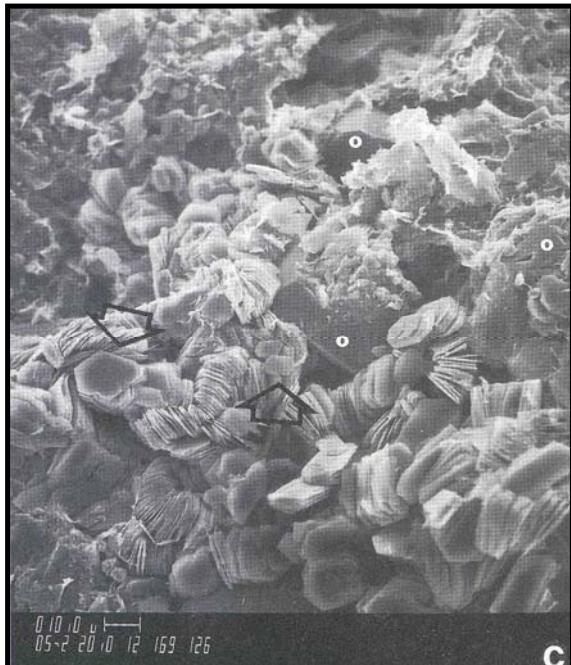
## Clay and Sandstone



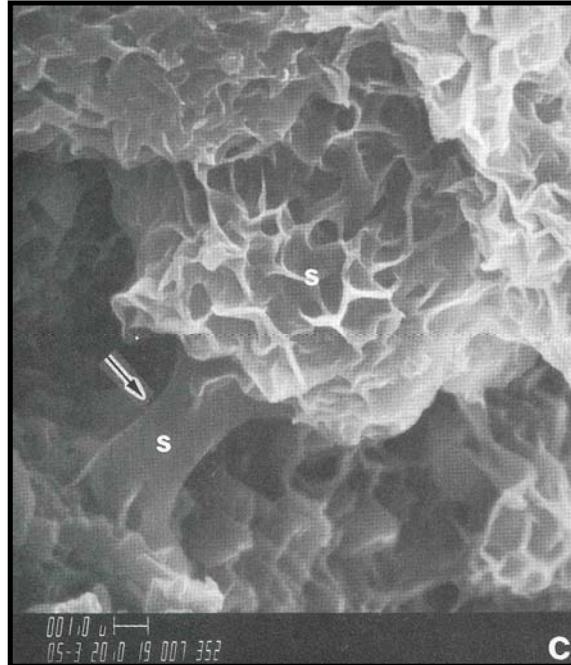
After Rabaute et al. (2003) 33

## SEM Images

Kaolinite

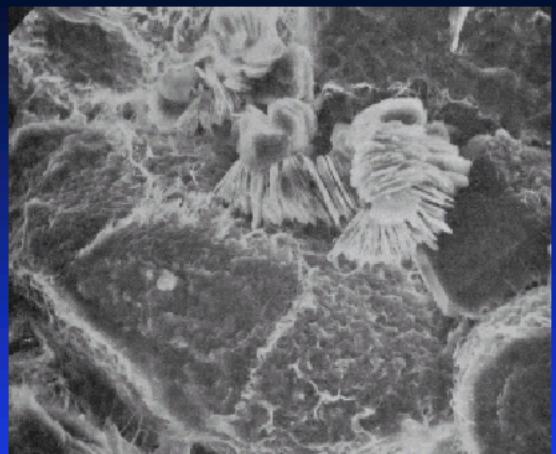
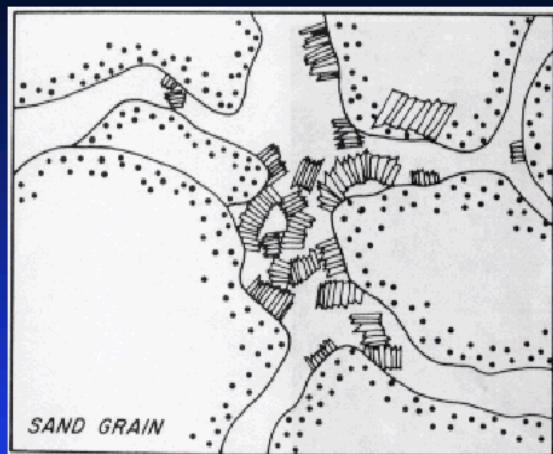


Smectite



## What is a clay?

### Example: Pore-Filling Kaolinite



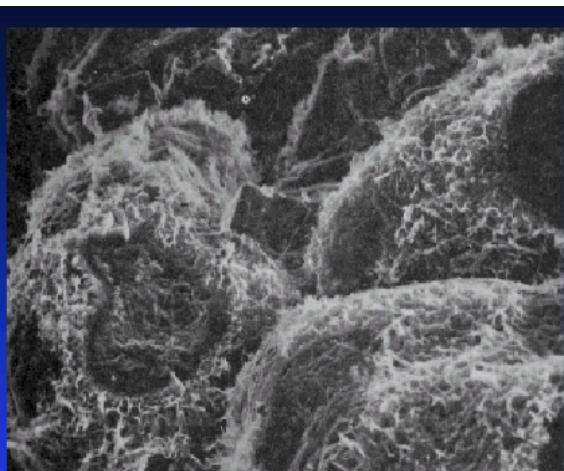
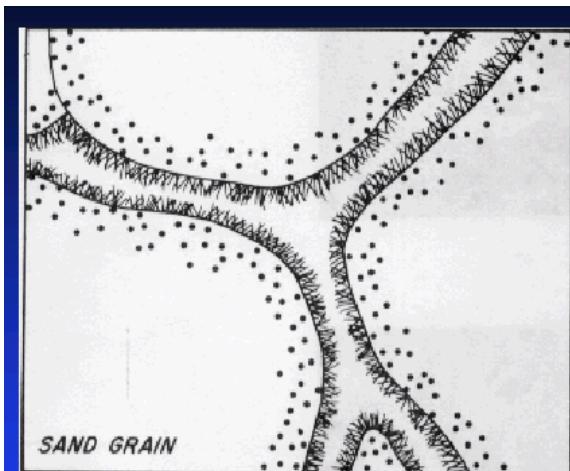
Classical Kaolinite “booklets” - potential for formation damage

From Neasham 1977, SPE 6858

35

## What is a clay?

### Example: Pore-Lining Chlorite



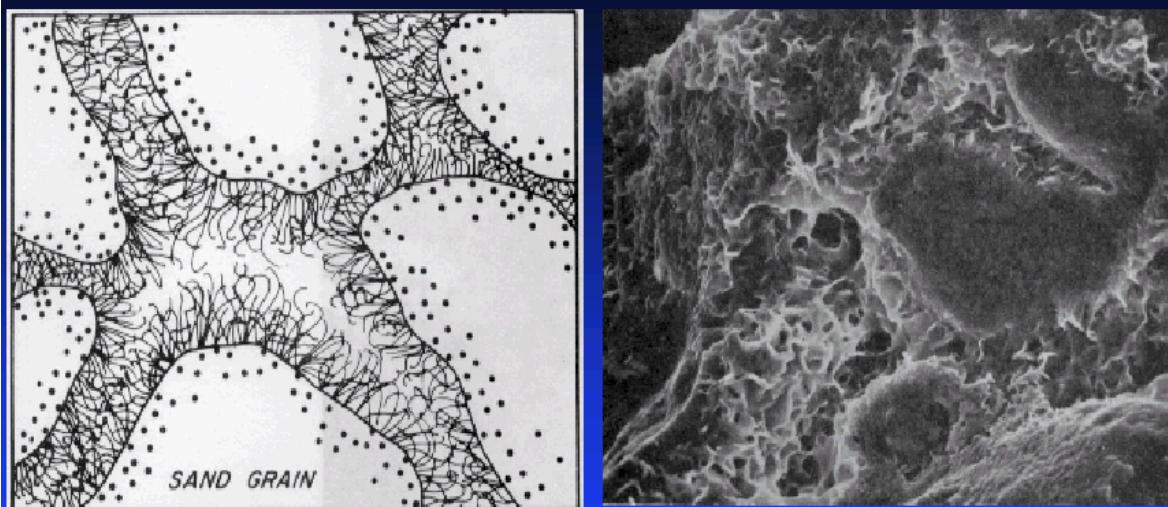
Cause of significant “Clay Bound Water” - detectable with  $\phi_n$

From Neasham 1977, SPE 6858

36

## What is a clay?

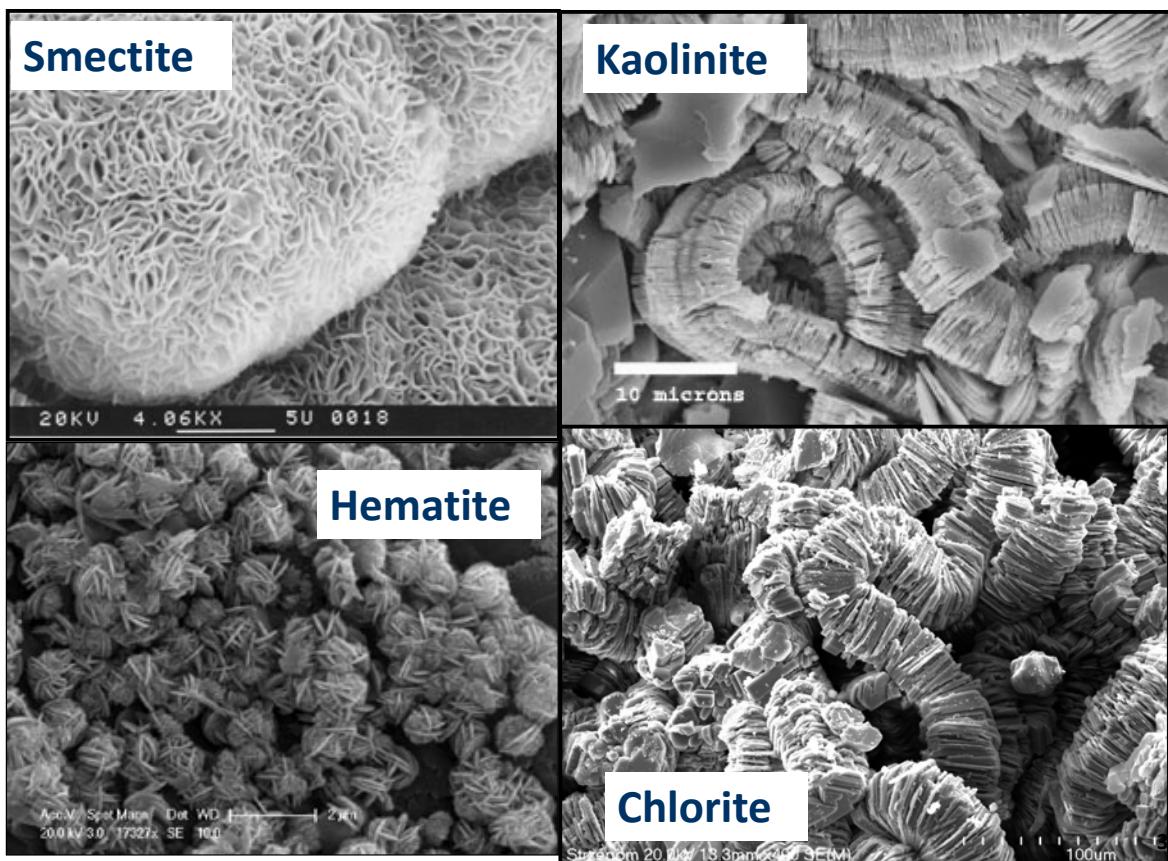
### Example: Pore-Bridging Illite



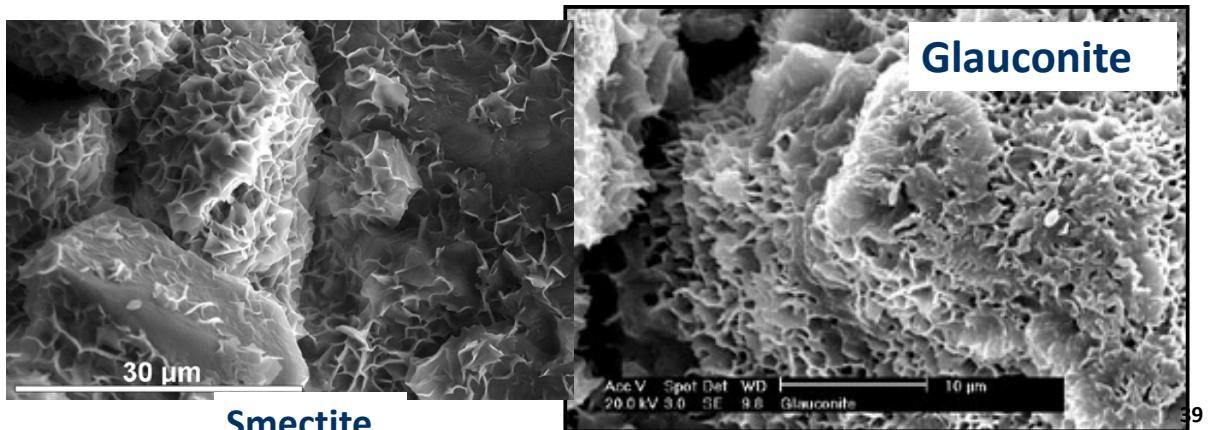
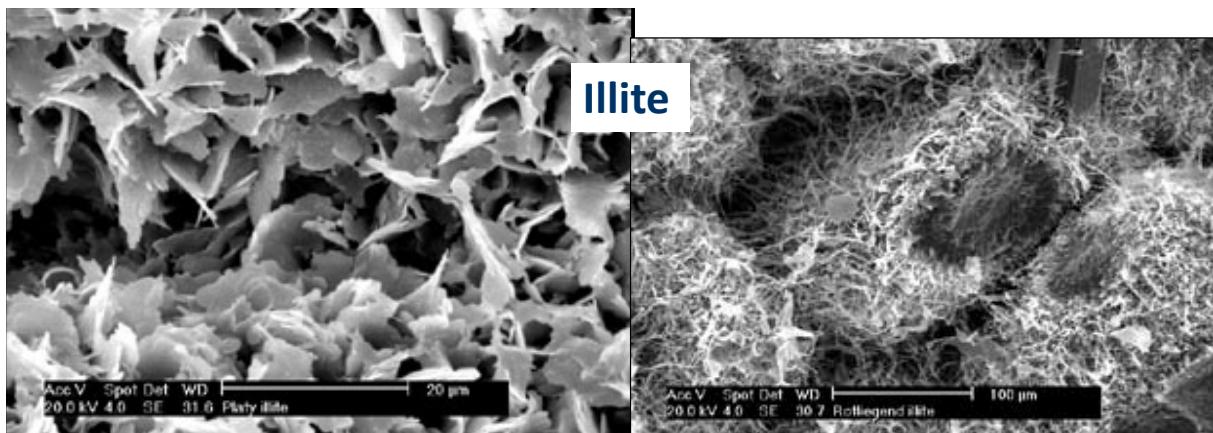
High surface area - high bound water - swelling clay

From Neasham, 1977, SPE 6858

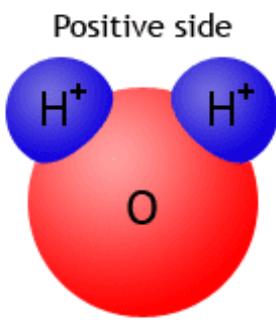
37



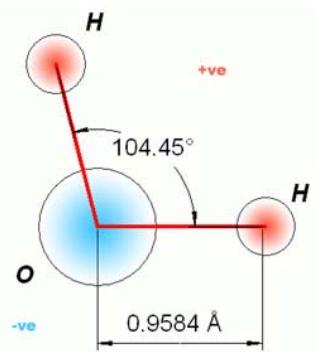
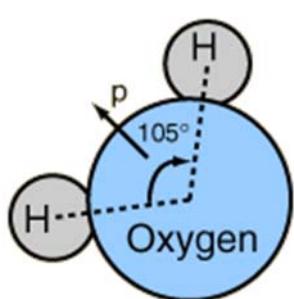
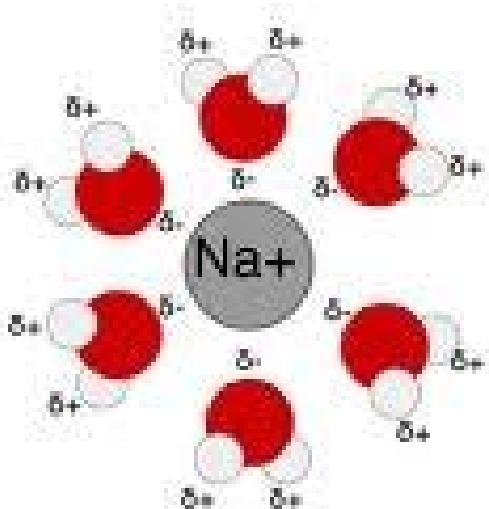
38



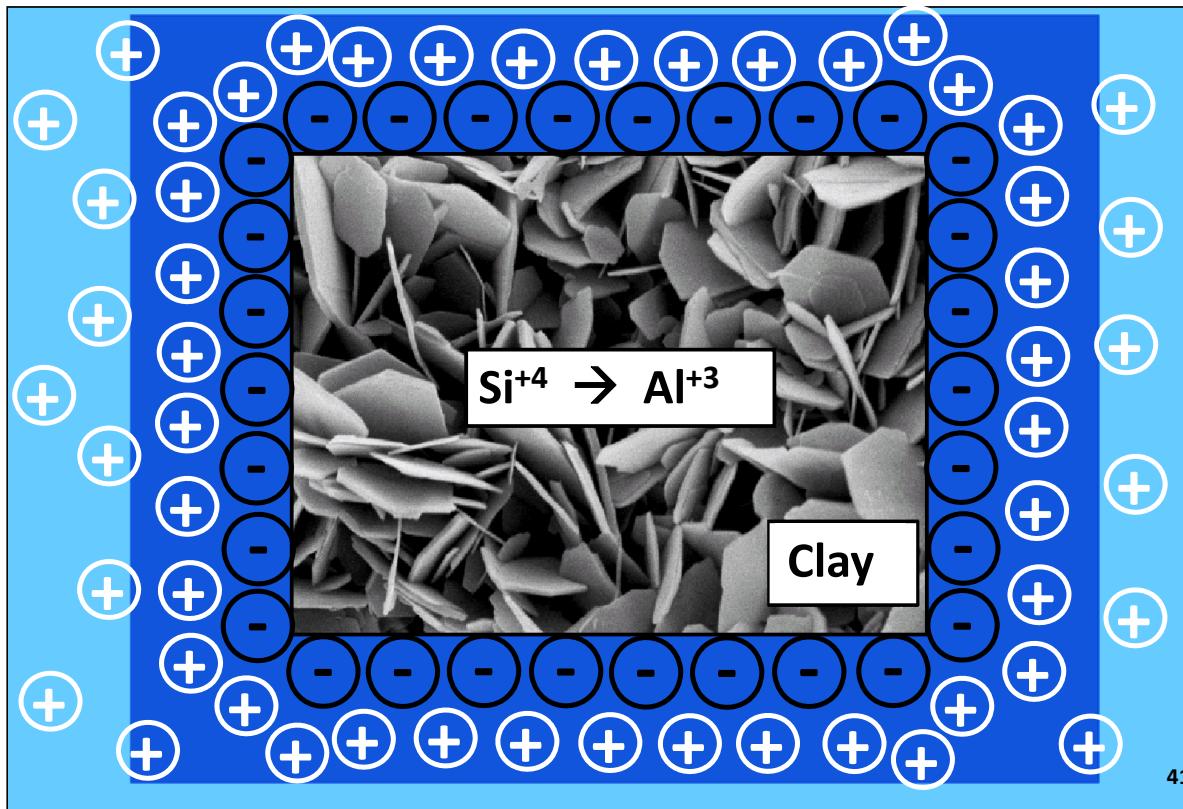
## Water Molecule



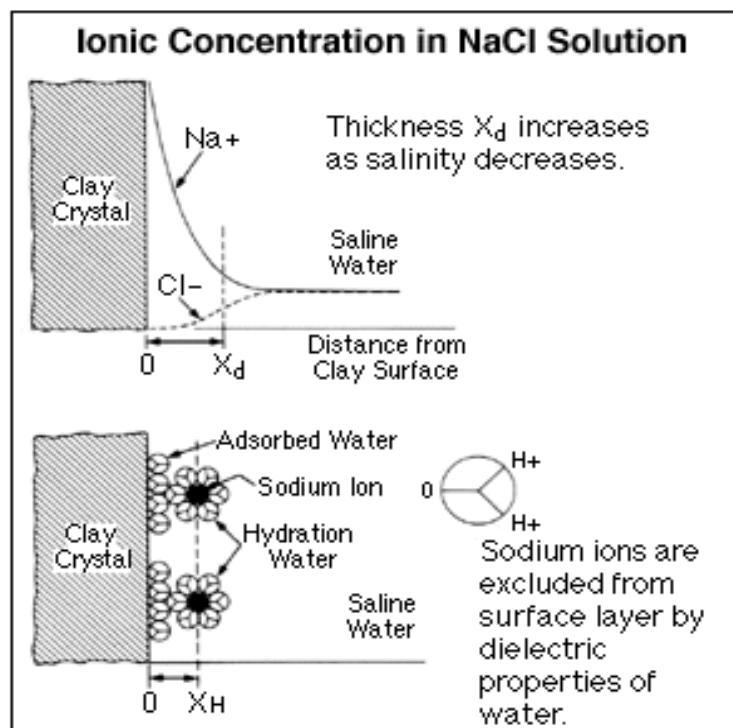
Josh Lory  
www.soilsurvey.org

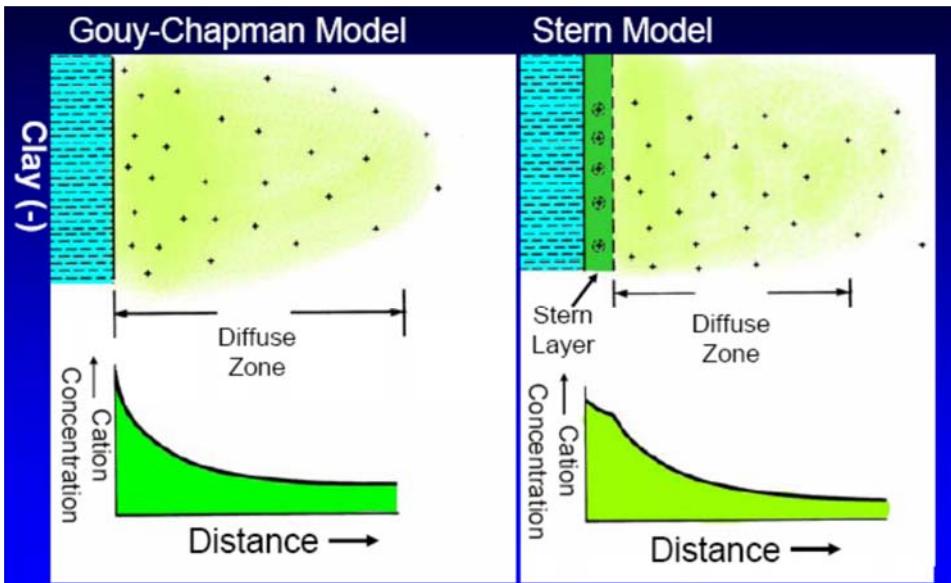


## ELECTRICAL DOUBLE LAYER OF CLAYS

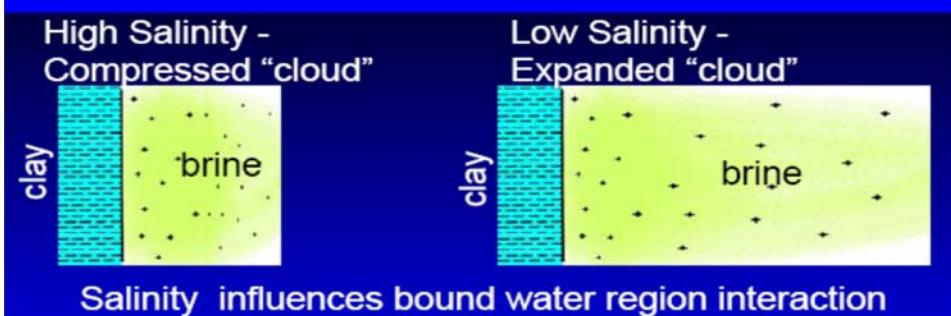


## Water Adsorption by Clays [Cation-Exchange-Capacity (CEC) Mechanism]





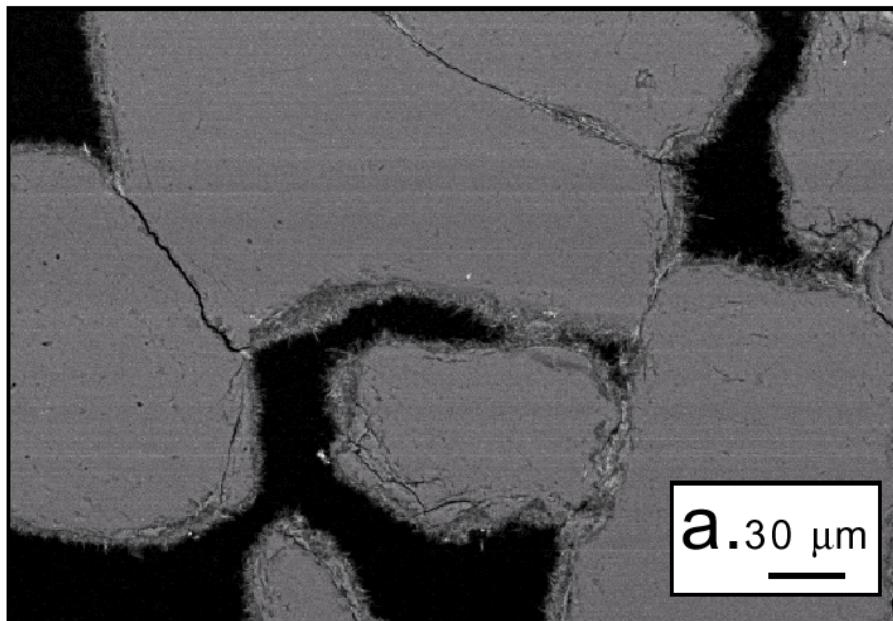
**MODELS**



43

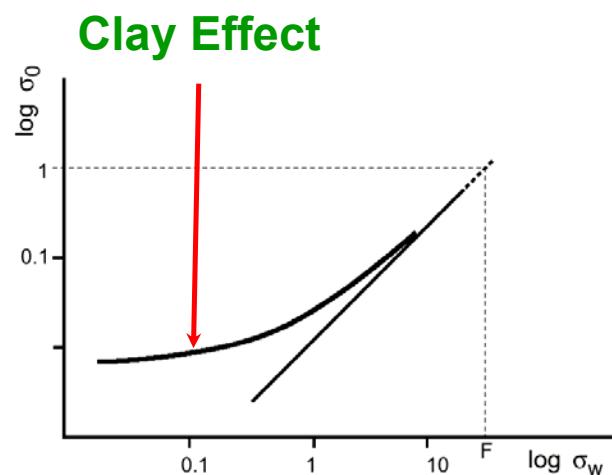
**What is a clay?**

**Example of Clay-Coated Sand Grains**



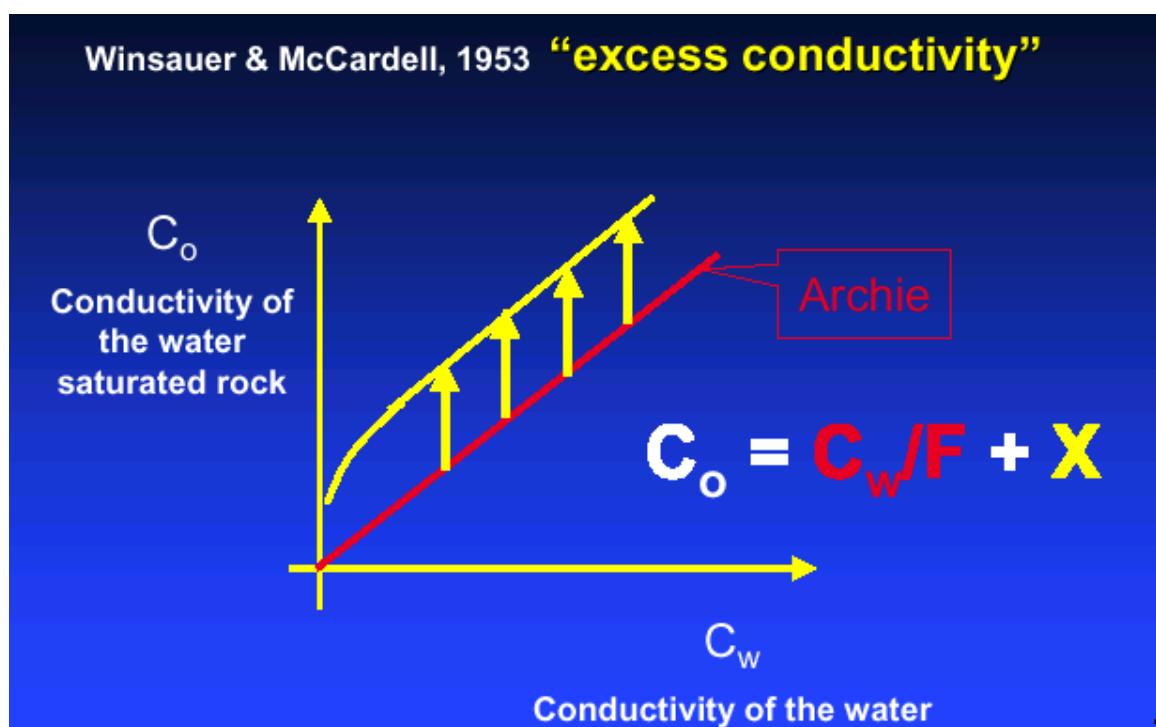
44

- Archie valid at high salinities > 100ppk at 200°F
- Archie also valid if there are no conductive materials (clays).
- In very fresh water surface conductance of ordinary grains can also be a problem



45

## ELECTRICAL PROPERTIES OF SHALY SANDS

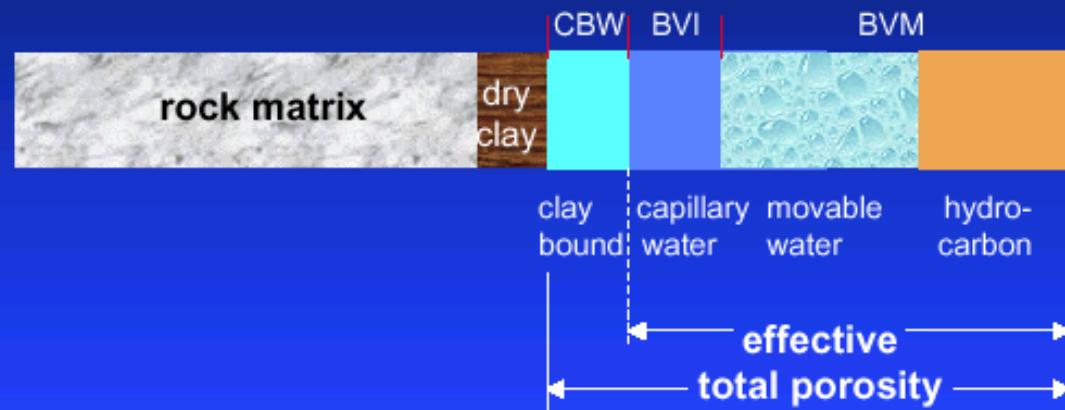


46

# Fluids in the Pore Space

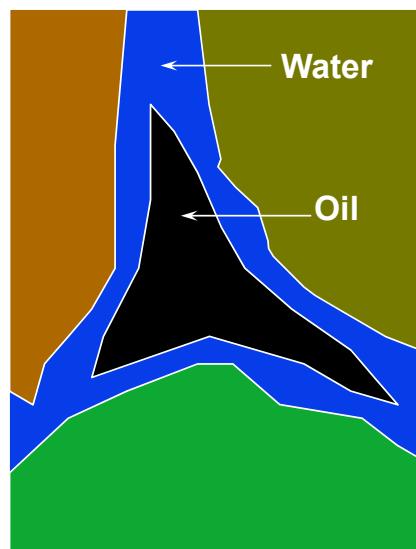
$$\text{saturation}_i = \frac{\text{volume fluid } i}{\text{pore volume}}$$

volumetric model



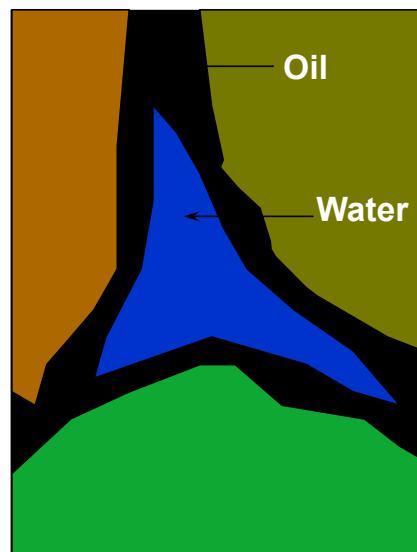
47

## Water-Wet Hydrocarbon-Bearing Rock Formation



48

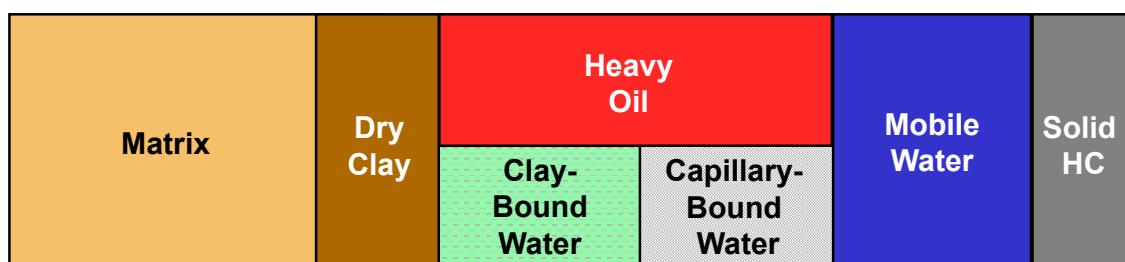
# **Oil-Wet Hydrocarbon-Bearing Rock Formation**



49

## **The Case of Heavy Oil**

### **Matrix and Fluid Distributions**



50

# Water-Wet Hydrocarbon-Bearing Carbonates

## Matrix and Fluid Distributions



51

## Several Water Saturation Models

### Shale-Free Electrical Model

- Archie (1942)

### Laminated Shale Electrical Model

- Poupon-Leveaux (Indonesian)

### “Double-Layer” Dispersed Clay Electrical Models

- Waxman-Smits

- Dual-Water

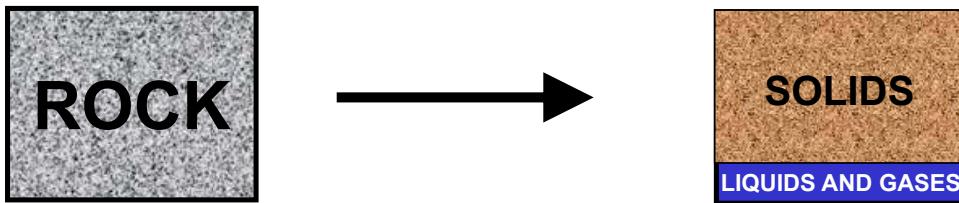
### Mixed Dispersed-Clay / Laminar-Shale Electrical Model

- Patchett-Herrick

52

## DEFINITION OF VOLUME OF SHALE

**Rock = Fluids + Solids (Matrix)**



**Shale**  
**Solid + Fluid Components**

$$\text{Volumetric Concentration of Shale} = \frac{\text{Volume of Shale}}{\text{Total Rock Volume}}$$

53

## SHALE AND ELECTRICAL RESISTIVITY

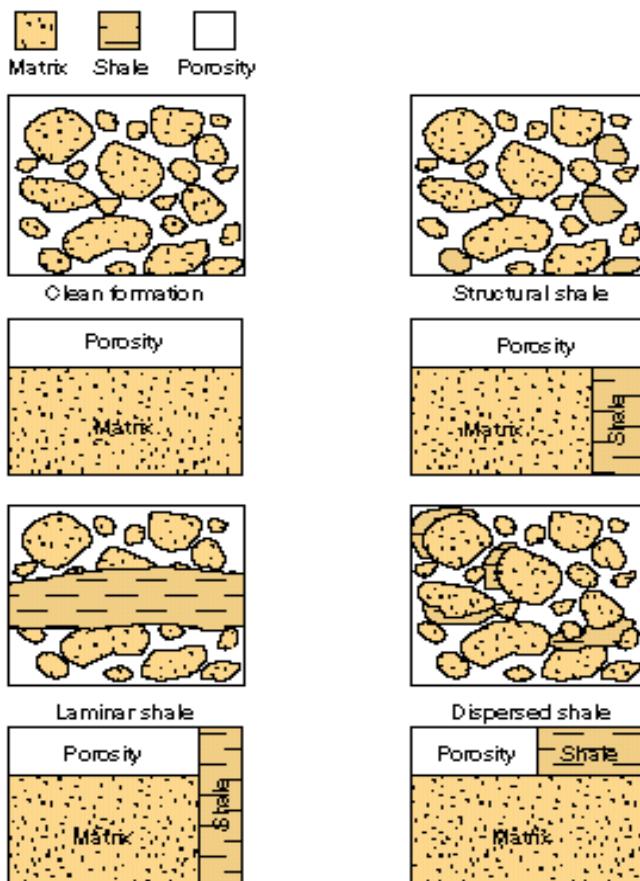
**Conductivity contribution of clay depends on**

- clay type (clay mineral)
- clay content (volume fraction)
- distribution of clay in the formation

**Clay distribution is described by 3 types of shale**  
**(Boyd et al. 1995, Doveton 1997) :**

- Laminar shale
- Dispersed shale
- Structural shale

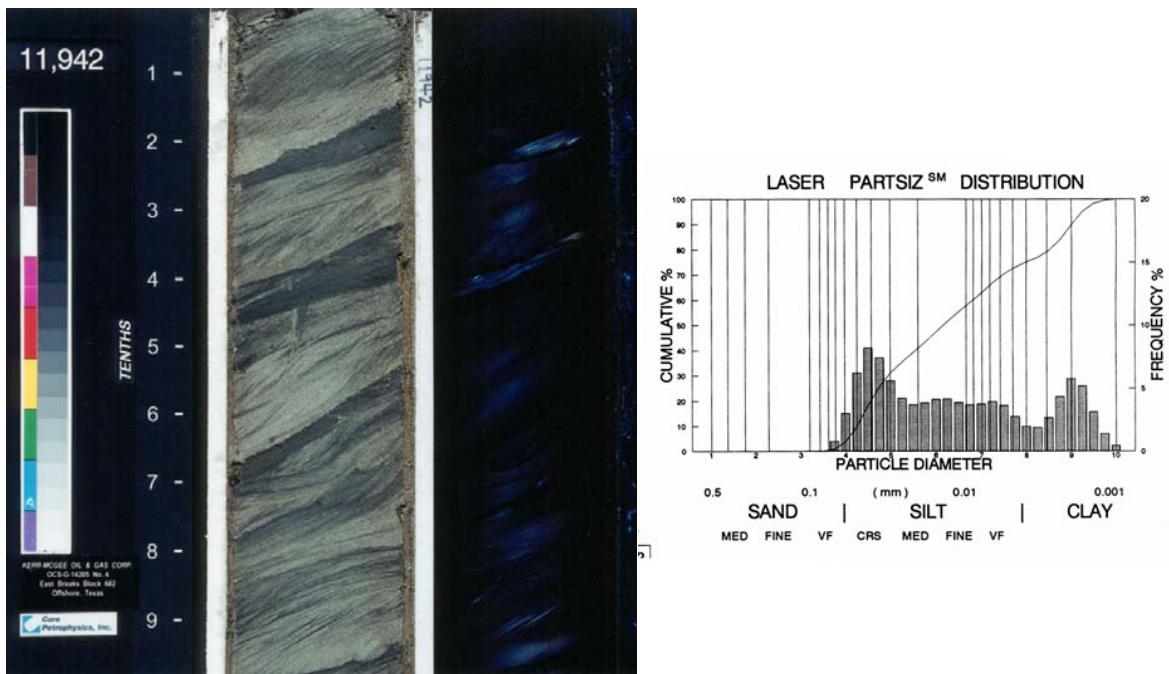
54



## Shale Distribution

55

## Core Vshale: Example



56

# Definitions

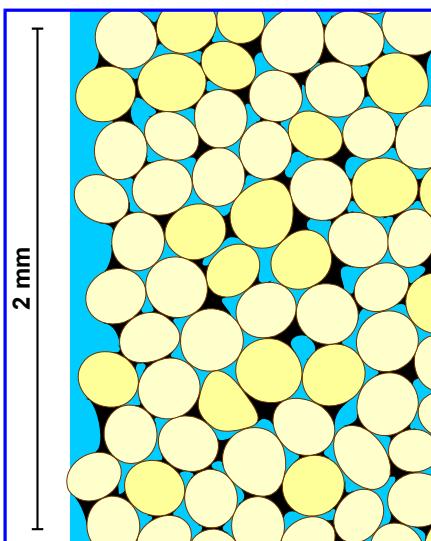
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- Shale can be dispersed, laminated or structural
- Shale structure is not critical in computing hydrocarbons-in-place. It is important in determining producibility.
- Shale structure can only be determined from core or with image logs, like the FMI.

57

## Dispersed Shale

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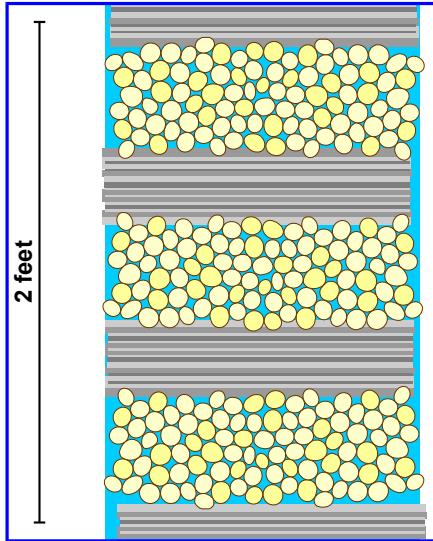
- Dispersed shale occupies only pore space
- $\phi_e = \phi_{ss} - Vsh_D$
- $\phi_{ss}$  or PHIMAX is the maximum clean sandstone  $\phi$

58

# Laminated Shale

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- Shale laminae occupy both pore space and grain space



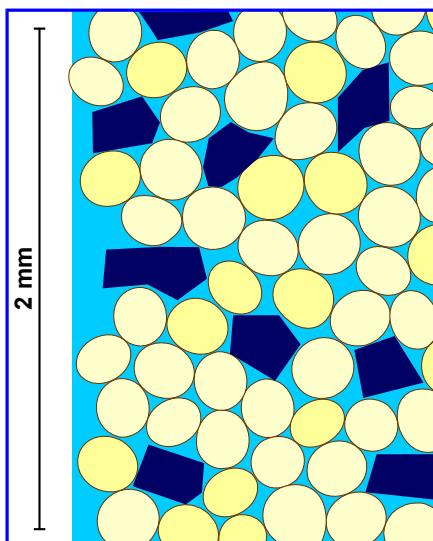
- $\phi_e = \phi_{ss} - V_{shL} \phi_{ss}$
- These laminae are at the density resolution limit. (sand grains not to scale)

59

# Structural Shale

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- Structural shale occupies grain space



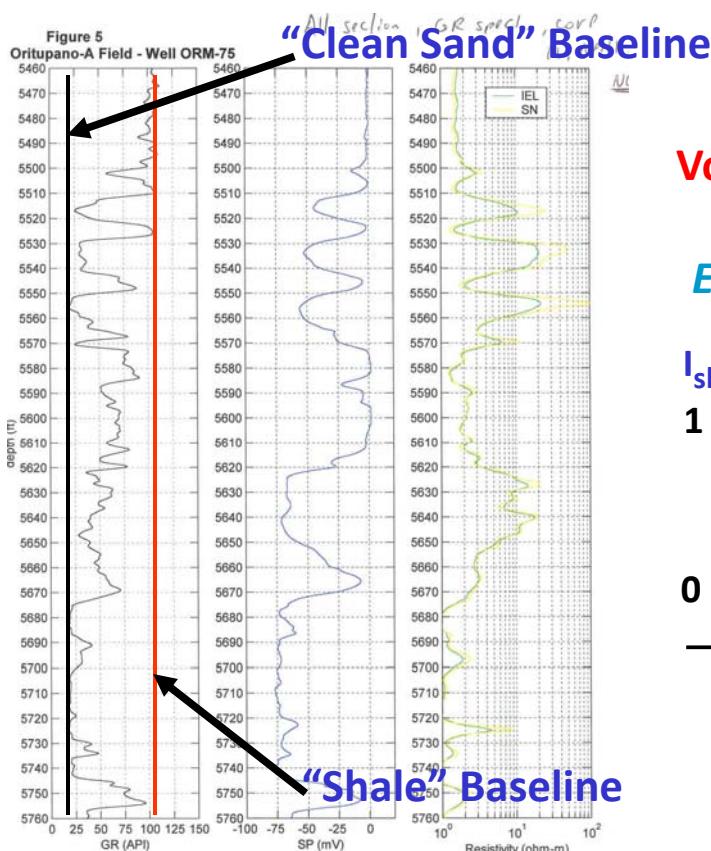
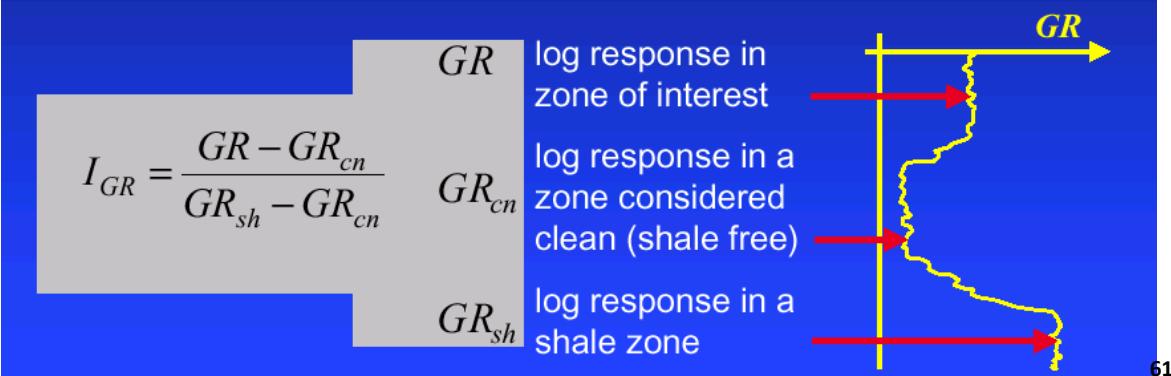
- $\phi_e = \phi_{ss}$

60

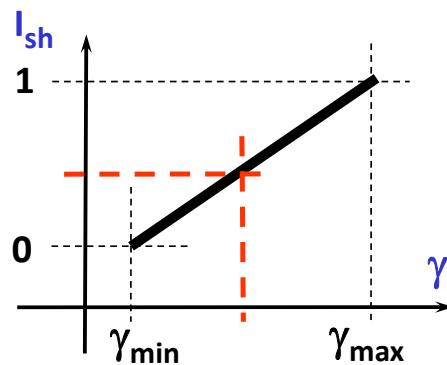
# ESTIMATION OF SHALE CONTENT

- Basis: correlation between shale content and gamma activity
- Assumption: only shale and clay are radioactive components in rock, no other radioactive minerals

## First step: Calculation of “gamma ray shale index”



Volume of Shale ( $V_{sh}$ )  
 Computation:  
*Empirical Technique*



# ESTIMATION OF SHALE CONTENT (I)

Second step: Select & apply a relationship  $I_{GR}$  vs. shaliness  $V_{sh}$

$$V_{sh} = I_{GR}$$

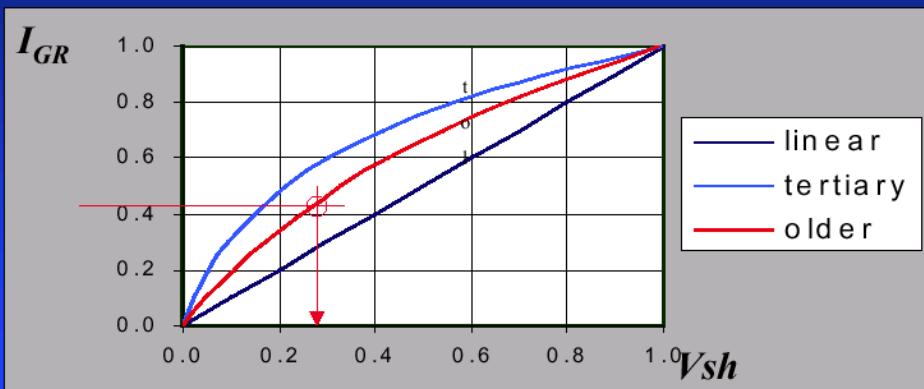
$$V_{sh} = 0.083 \cdot (2^{3.7 \cdot I_{GR}} - 1)$$

$$V_{sh} = 0.33 \cdot (2^{2 \cdot I_{GR}} - 1)$$

Linear relationship (upper limit)

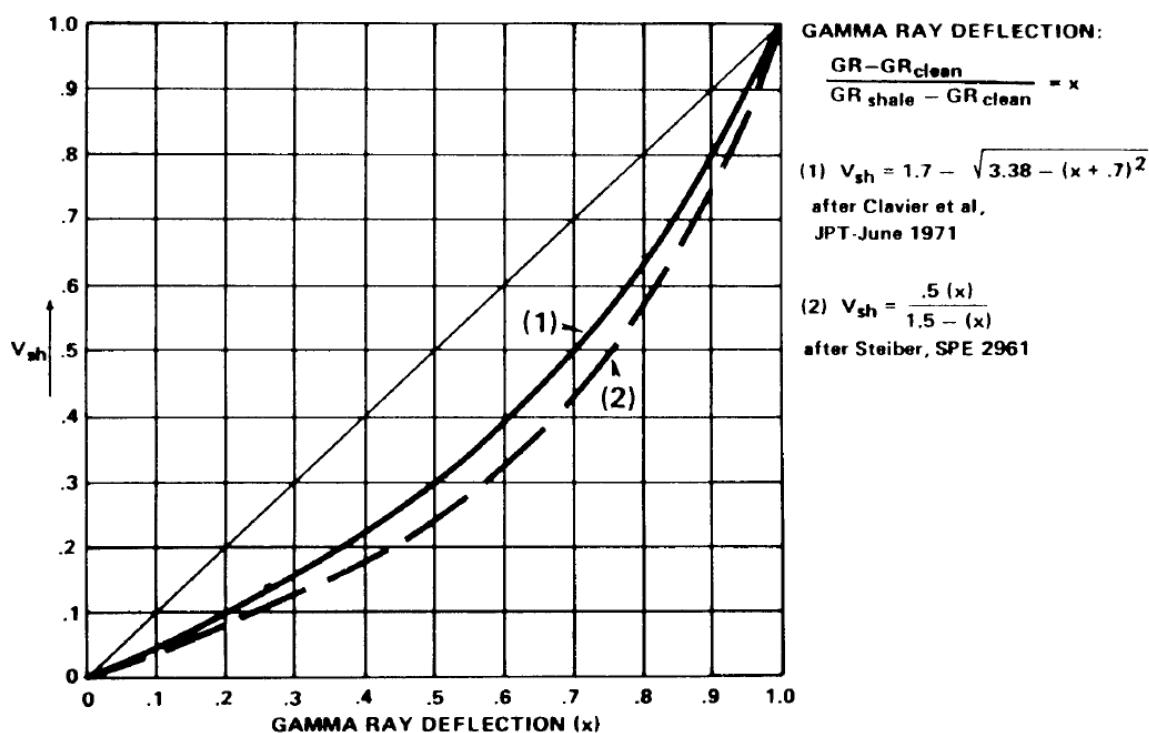
Tertiary clastics (Larionov 1969)

Mesozoic & older rocks (Larionov 1969)



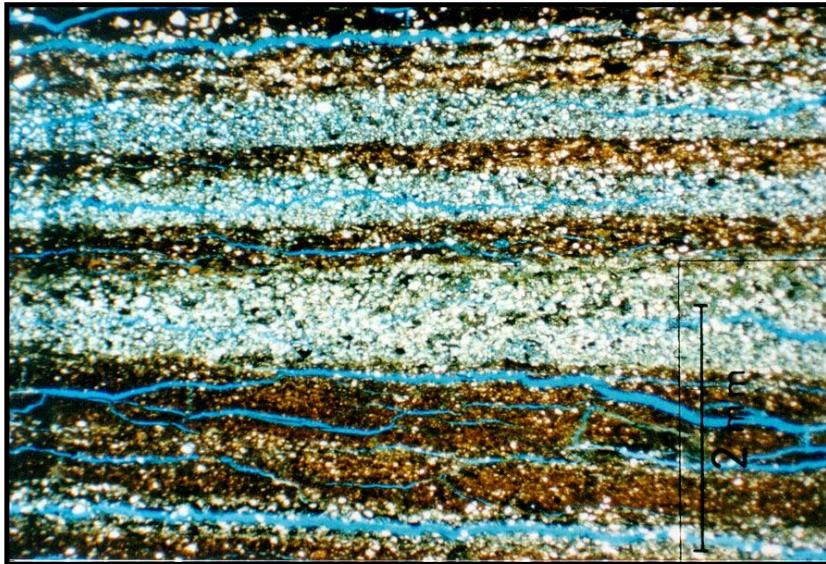
63

# ESTIMATION OF SHALE CONTENT (II)



64

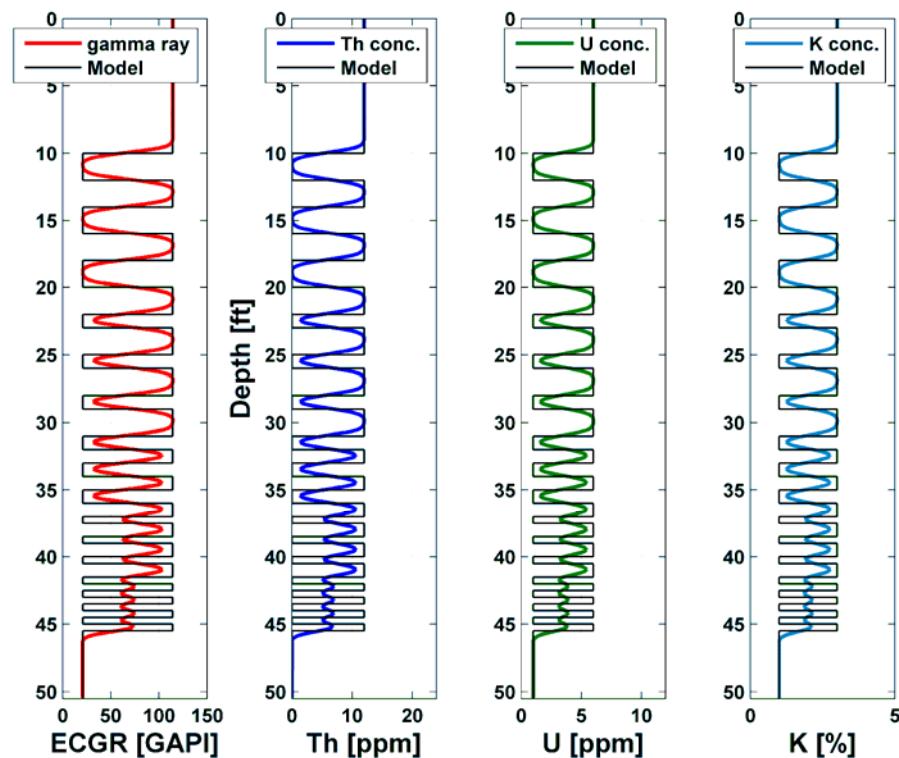
# Issue: Laminated Sandstones



- Laminae can be very thin as in this thin section
- The laminae are about 1 mm thick.

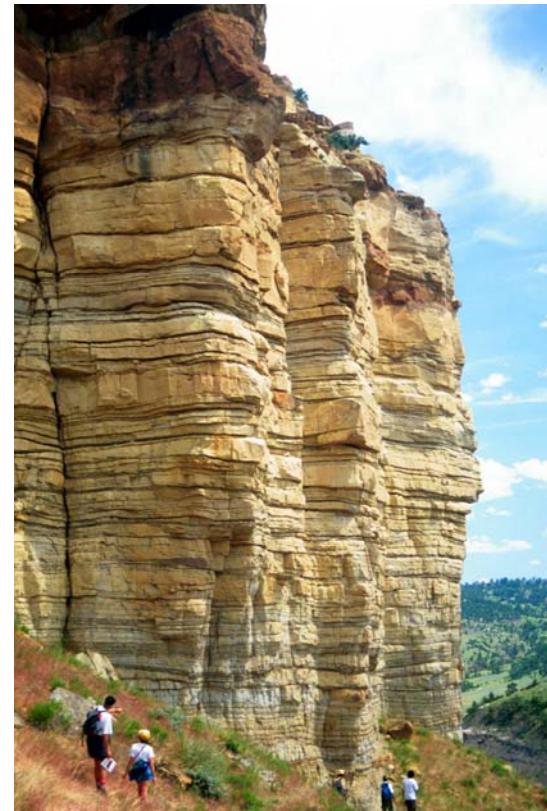
65

## EXAMPLE: Synthetic gamma-ray logs



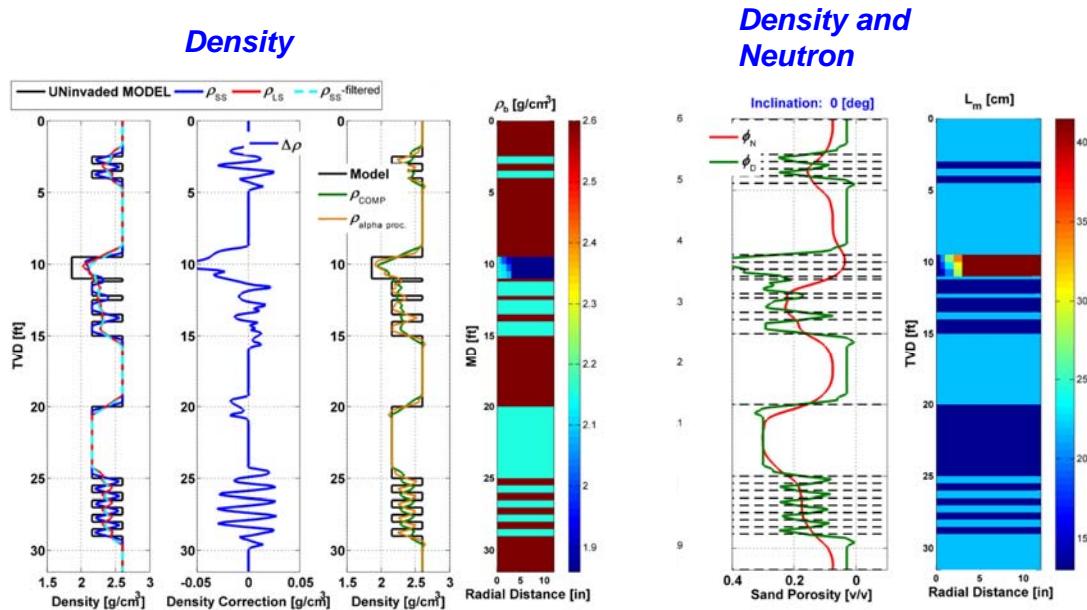
66

**Tide Influenced Delta**  
**Frewins Castle Sandstone**  
**Belle Fourche Member**  
**Frontier Formation**  
**Cretaceous (Cenomanian)**  
**Tisdale Mountain Anticline, Wyoming**

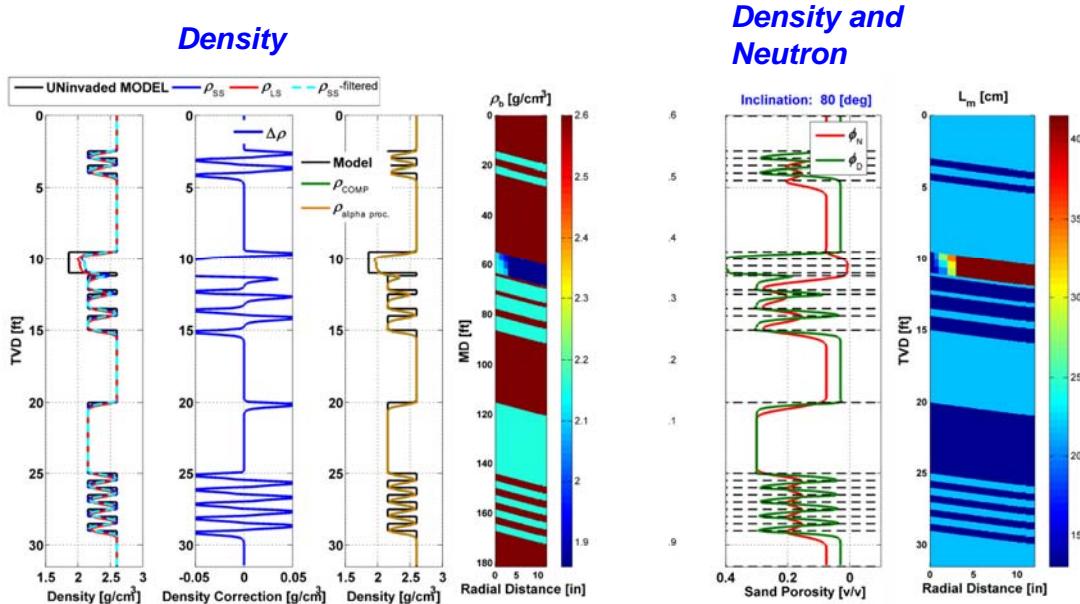


67  
Photo by Rob Wellner

## EXAMPLE: Synthetic density and neutron logs

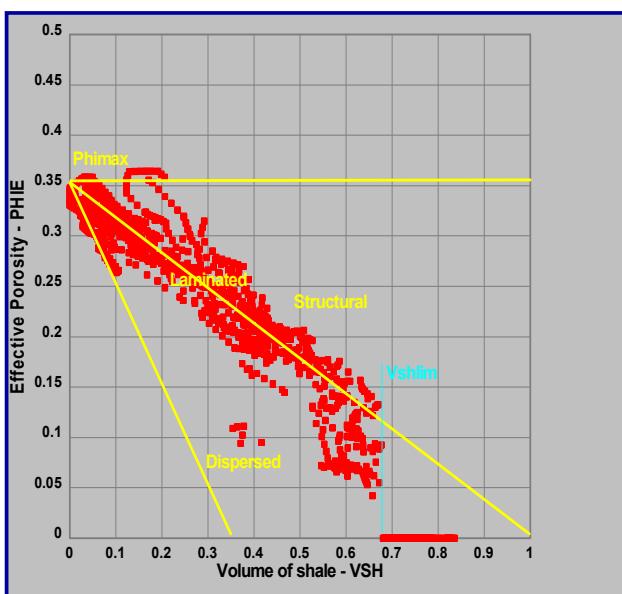


## EXAMPLE: Synthetic density and neutron logs in dipping beds



69

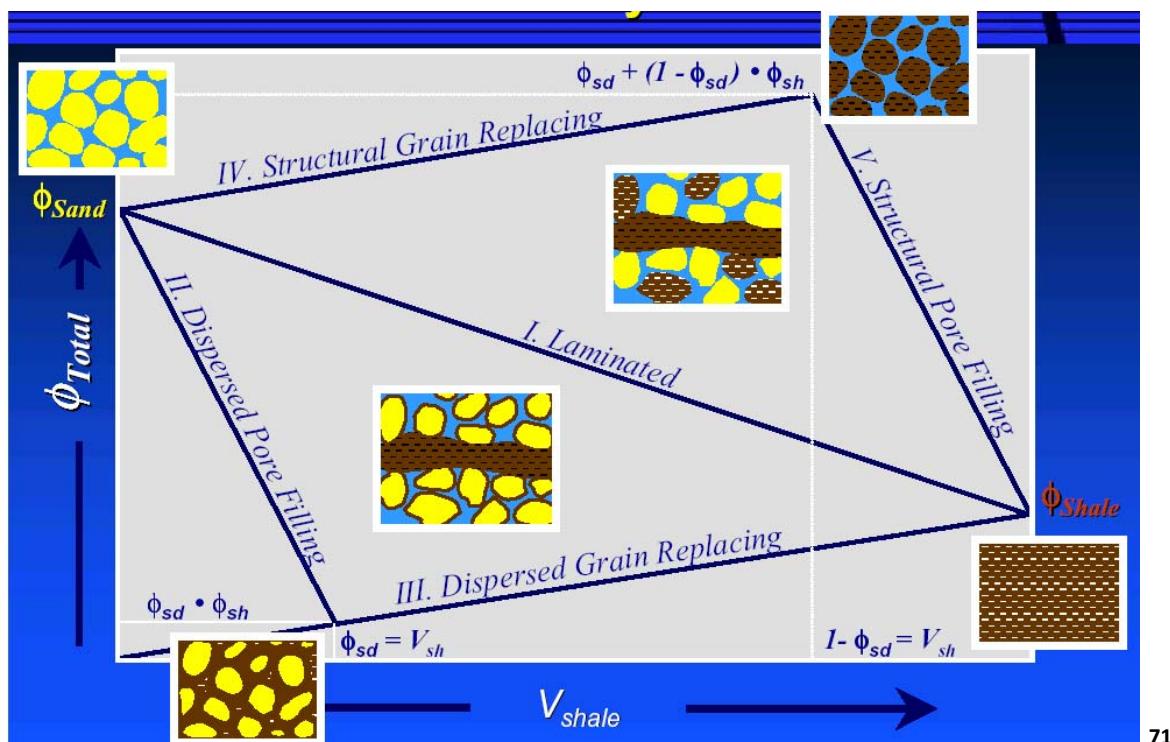
## Determining Shale Structure: Thomas-Steiber Plot



- Points on the Phimax to PHISH ( $\text{PHIE}=0$ ) line are 100% laminated SS
- Points above the line have laminated shale and structural shale
- Points below have dispersed shale and laminated shale

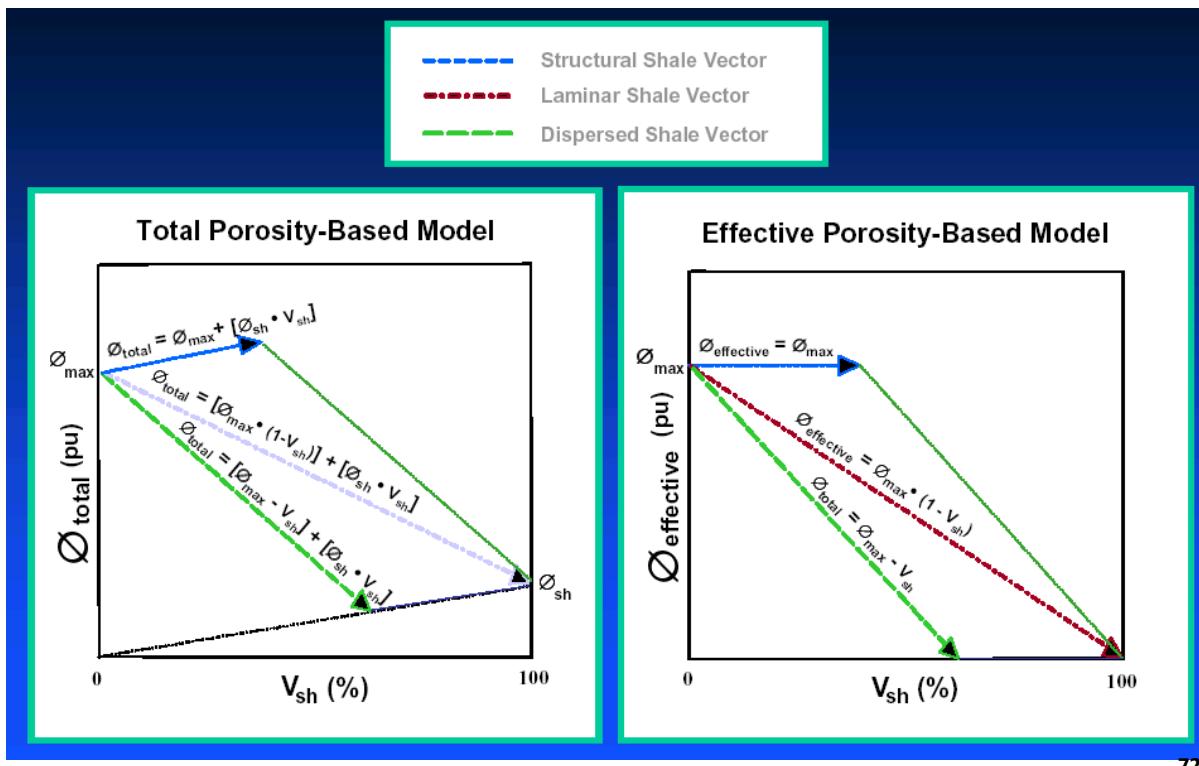
70

# THOMAS-STEIBER PLOT



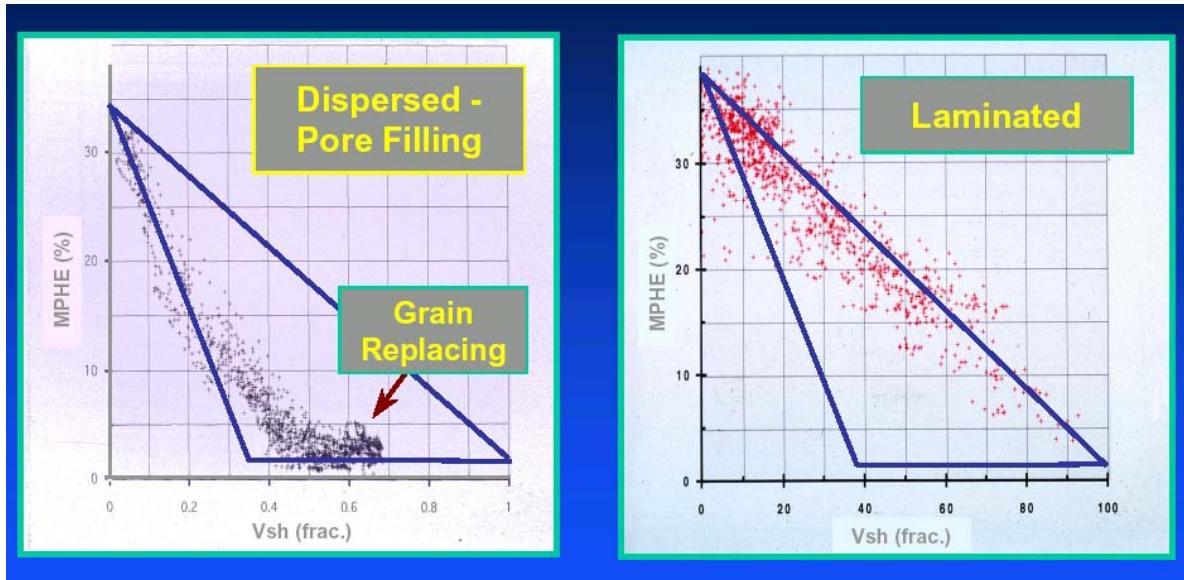
71

## POROSITY vs. SHALE MODEL



72

## POROSITY vs. SHALE MODEL: Examples



73

## THOMAS-STEIBER POROSITY MODEL

### I. Laminated

$$\phi_T = \phi_{Sd} - V_{Sh} \cdot (\phi_{Sd} - \phi_{Sh})$$

### II. Dispersed Pore Filling

$$\phi_T = \phi_{Sd} - V_{Sh} \cdot (1 - \phi_{Sh}) \quad V_{Sh} \leq \phi_{Sd}$$

### III. Dispersed Grain Filling

$$\phi_T = V_{Sh} \cdot \phi_{Sh} \quad V_{Sh} > \phi_{Sd}$$

### IV. Structural Grain Replacing

$$\phi_T = \phi_{Sd} + V_{Sh} \cdot \phi_{Sh} \quad V_{Sh} \leq 1 - \phi_{Sd}$$

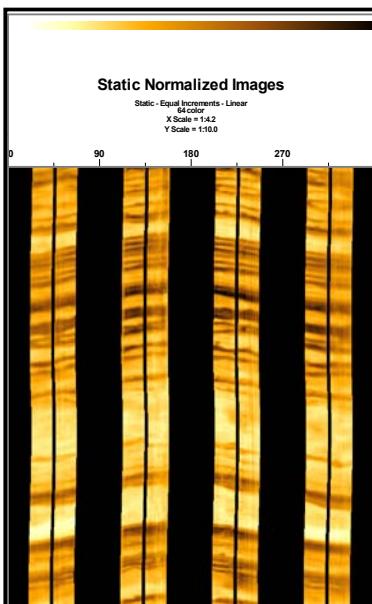
### V. Structural Pore Filling

$$\phi_T = 1 - V_{Sh} \cdot (1 - \phi_{Sh}) \quad V_{Sh} > 1 - \phi_{Sd}$$

74

## Example: Thin Bedded Pay

---



- Deep water facies thin bedded pays appear as organized bands and have moderate dips.
- This facies makes good reservoirs, even with a very high Vsh and low interval average PHIE.
- They are hard to detect due to low resistivity and high GR

75

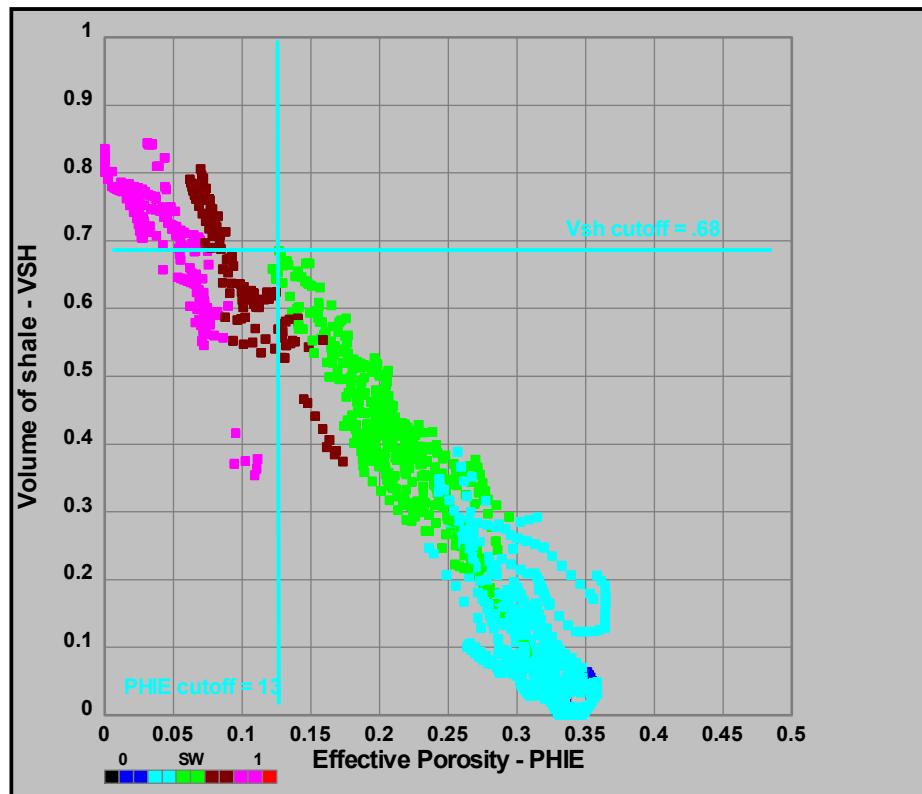
## Net Pay Cut-Offs

---

- How are they picked?
- “Typical Values” or “Rules of Thumb”
- Regional knowledge (what about rank wildcat?)
- How to verify?

76

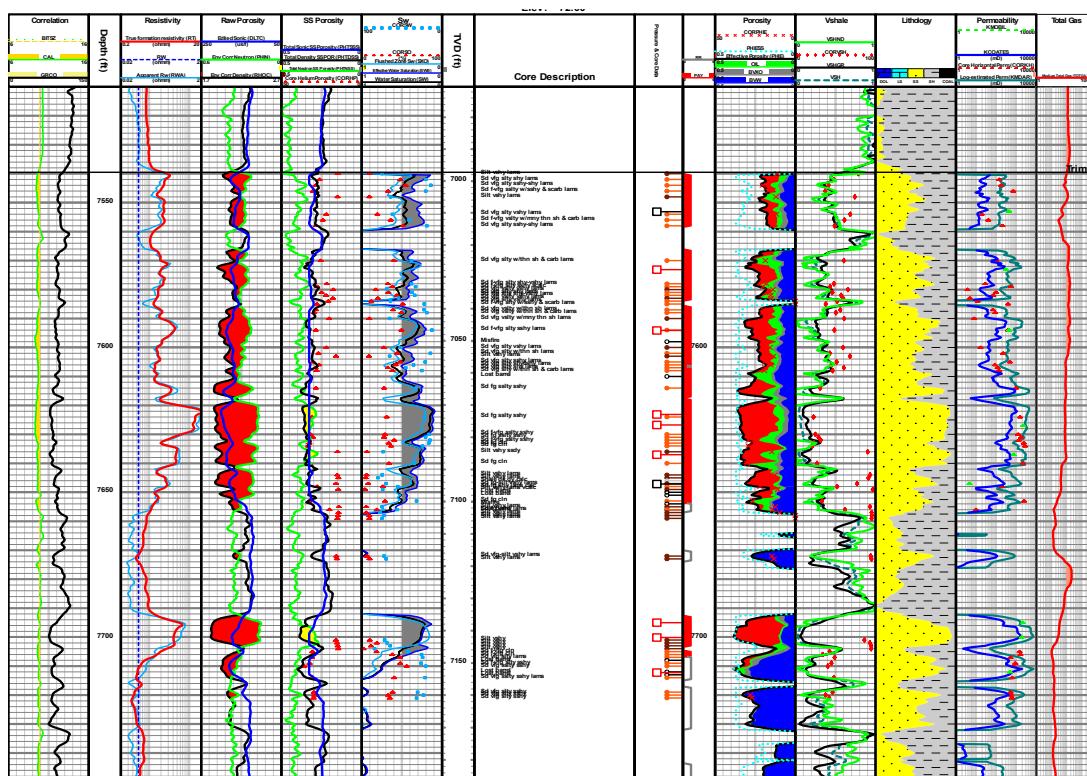
# Determine Cutoffs



77

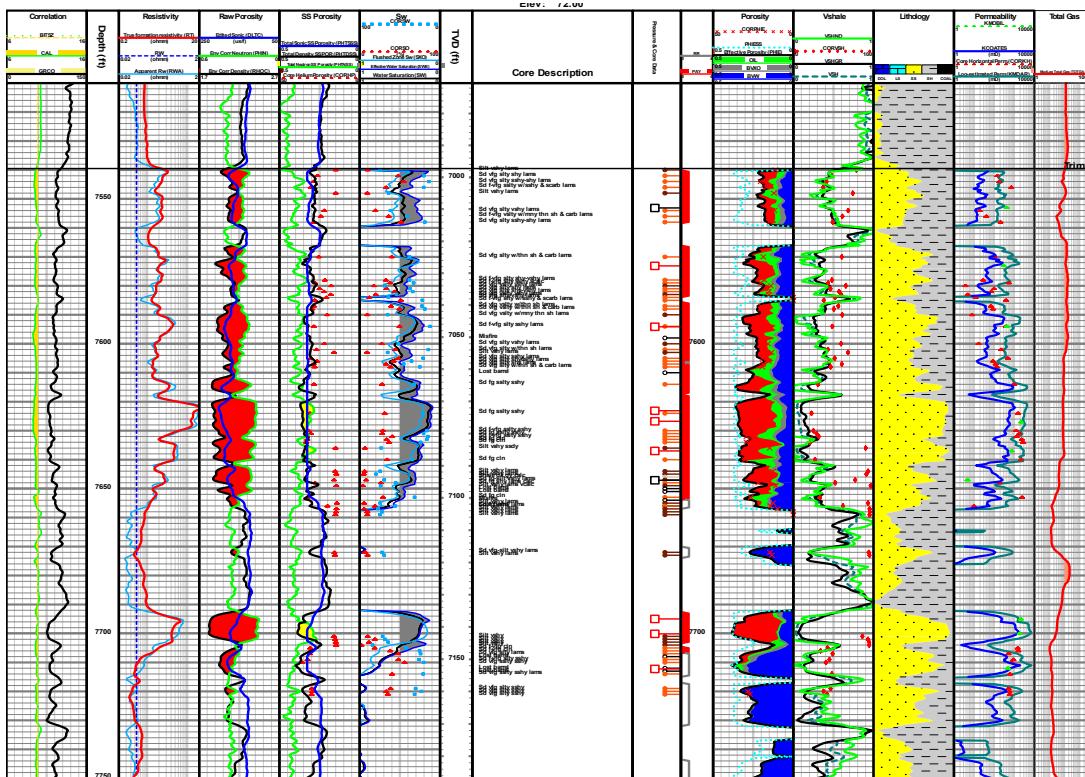
## EXAMPLE

VSH LIM = 0.63



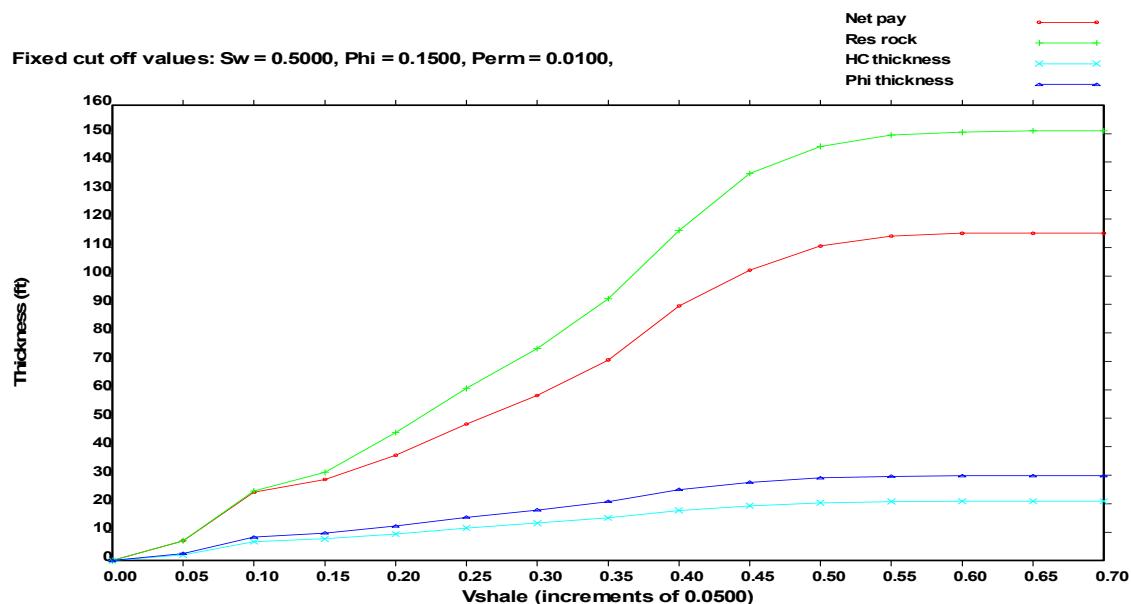
78

# EXAMPLE VSH LIM = 0.63



79

# EXAMPLE



$V_{shale}$	0.00	0.05	0.10	0.15	0.20	0.25	0.30	0.35	0.40	0.45	0.50	0.55	0.60	0.65	0.70
Net pay	0.0	7.0	24.0	28.5	37.0	48.0	58.0	70.5	89.5	102.0	110.5	114.0	115.0	115.0	115.0
Res rock	0.0	7.0	24.5	31.0	45.0	60.5	74.5	92.0	116.0	136.0	145.5	149.5	150.5	151.0	151.0
HC thickness	0.0	2.0	6.6	7.7	9.4	11.5	13.2	15.0	17.6	19.3	20.4	20.8	20.9	20.9	20.9
Phi thickness	0.0	2.5	8.2	9.7	12.1	15.2	17.7	20.8	25.0	27.5	29.0	29.6	29.8	29.8	29.8

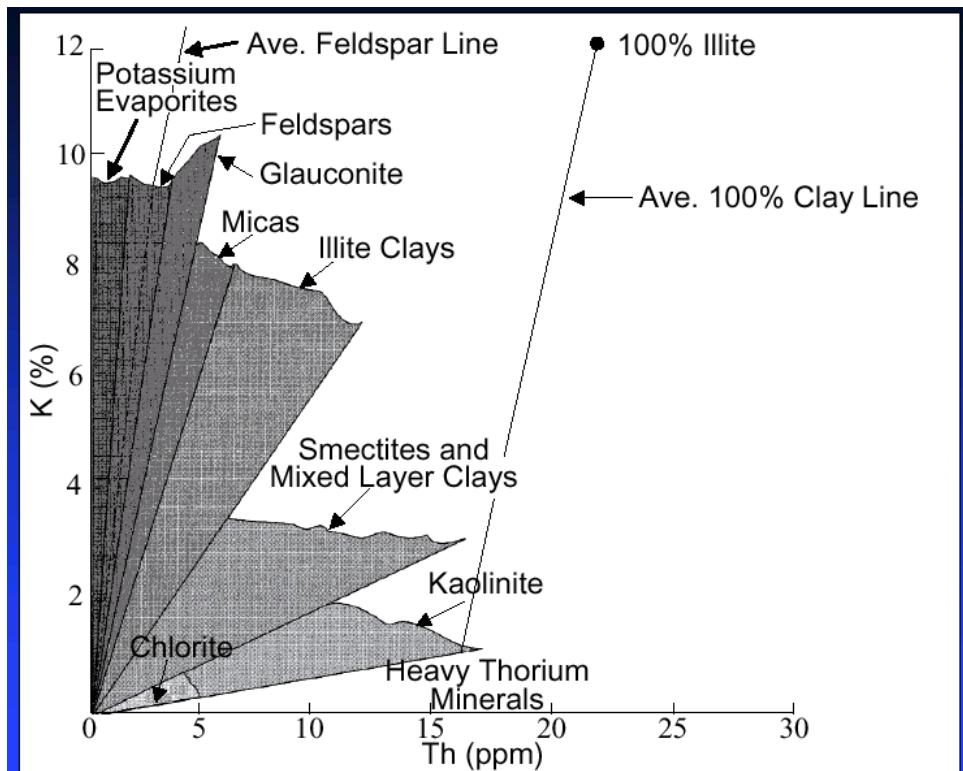
80

# CLAY MINERAL IDENTIFICATION

- Clay minerals show different Th/K ratios for different mineral composition
- Used for clay mineral identification
- Combination with other properties (Pe, neutron) recommended

81

# MINERAL IDENTIFICATION



82

# Several Water Saturation Models

Shale-Free Electrical Model

- Archie (1942)

Laminated Shale Electrical Model

- Poupon-Leveaux (Indonesian)

“Double-Layer” Dispersed Clay Electrical Models

- Waxman-Smits

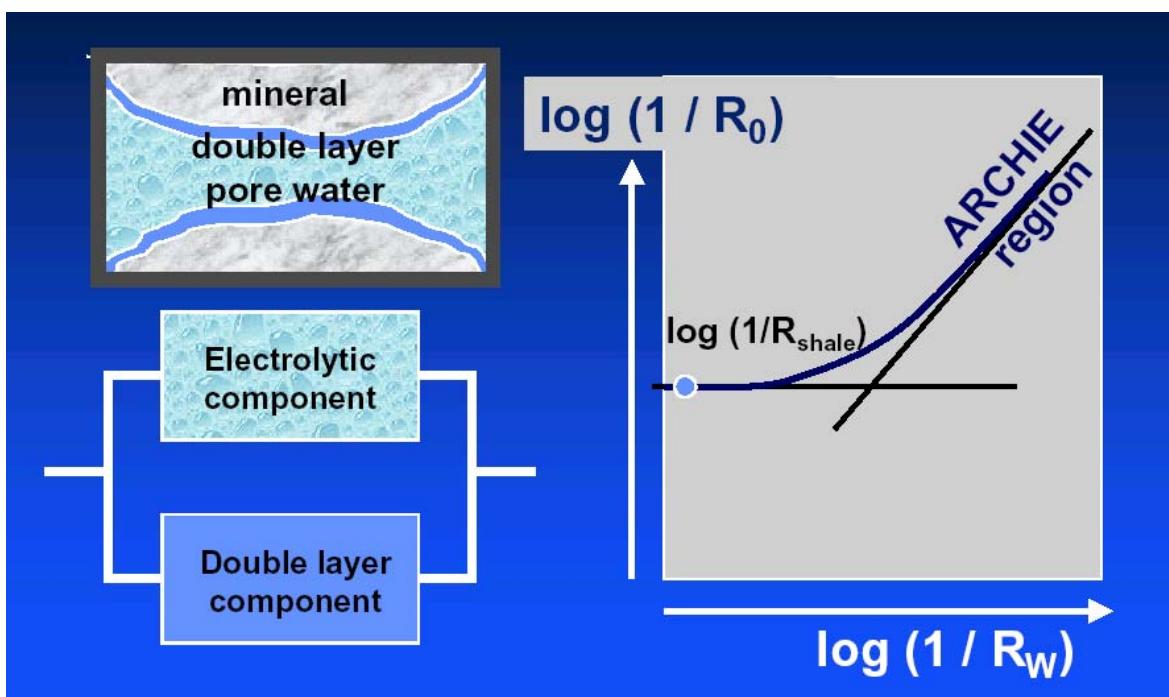
- Dual-Water

Mixed Dispersed-Clay / Laminar-Shale Electrical Model

- Patchett-Herrick

83

## PARALLEL CIRCUIT MODEL



84

# CATION EXCHANGE CAPACITY (CEC)

Physical origin of clay conductance can be described by cation exchange capacity (CEC) phenomenon;

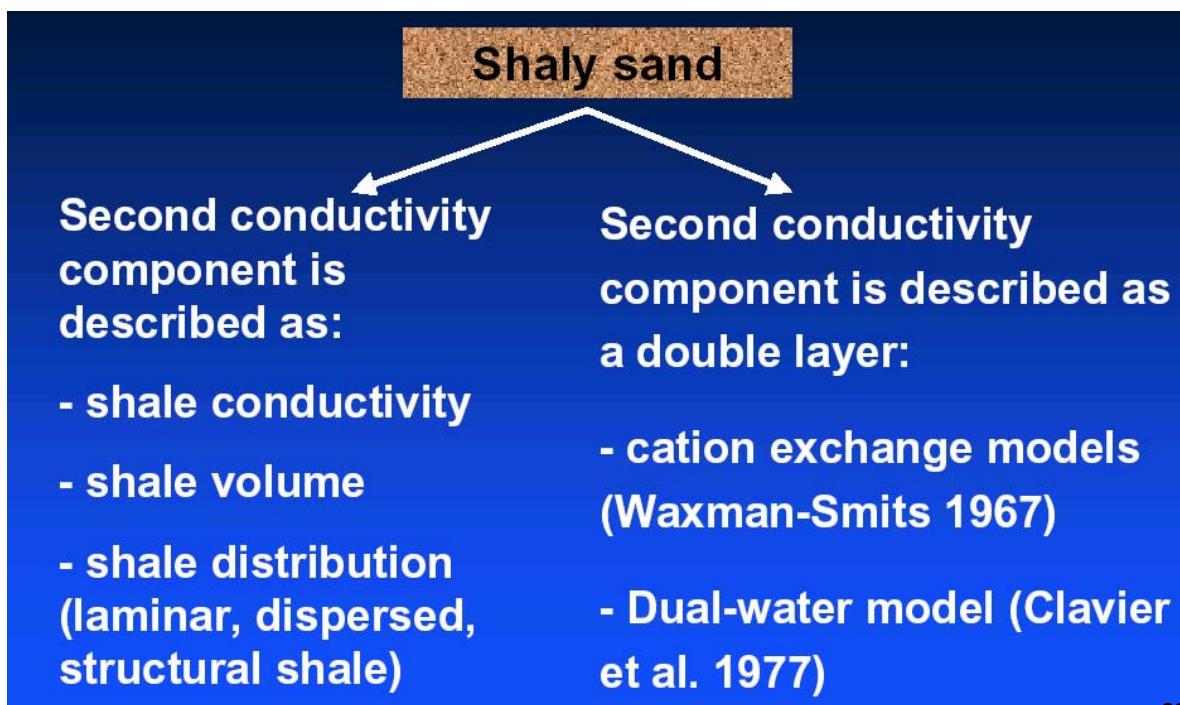
Unit: milliequivalent per 100 grams of dry clay;

CEC & specific surface for minerals (Olhoeft 1981, Keller & Frischknecht 1966, Boyd et al. 1995, Schön 1996)

Mineral	CEC (mequiv/100 g)	Surface area ( $\text{m}^2/\text{g}$ )
montmorillonite	80 ... 150	82 ... 767
chlorite	4 ... 40	42
illite	10 ... 40	97 ... 113
glauconite	11 ... 20	
kaolinite	3 ... 15	15 ... 23

85

## Conceptual Models for Shaly Sand



86

## Laminar Shaly Sand Model

(Poupon et al. 1954)



**Parallel conductor model:**

$$\frac{1}{R_t} = \frac{V_{sh-lam}}{R_{sh}} + \frac{1 - V_{sh-lam}}{R_{sd}}$$

$R_{sh}$  shale resistivity  
 $R_{sd}$  sand resistivity  
 $R_{sd} = R_w \cdot F \cdot S_w^{-n}$

87

## Calculation of Water Saturation

**$S_w = ?$**

$$\frac{1}{R_t} = \frac{V_{sh-lam}}{R_{sh}} + \frac{1 - V_{sh-lam}}{R_{sd}}$$

$$R_{sd} = (1 - V_{sh-lam}) \cdot \left( \frac{1}{R_t} - \frac{V_{sh-lam}}{R_{sh}} \right)^{-1}$$

$$R_{sd} = R_w \cdot F \cdot S_w^{-n} = R_w \cdot \frac{a}{\phi^m} \cdot S_w^{-n}$$

$$R_t = R_w \cdot F \cdot S_w^{-n} = R_w \cdot \frac{a}{\phi^m} \cdot S_w^{-n}$$

$$S_w = \left( \frac{R_w}{R_t} \cdot \frac{a}{\phi^m} \right)^{\frac{1}{n}}$$

*perfect world  
Archie is valid*

*shaly sand  
simplest  
model*

$$S_w = \left[ R_w \cdot \left( \frac{1}{R_t} - \frac{V_{sh-lam}}{R_{sh}} \right) \cdot \frac{a}{\phi^m} \cdot \frac{1}{1 - V_{sh-lam}} \right]^{\frac{1}{n}}$$

88

## Waxman-Smits Model

### Terminology:

$C_t$  conductivity of the shaly-sand

$C_W$  conductivity of the formation-water

$\Phi$  porosity

$S_w$  water-saturation

$F^*$  formation factor for shaly sand

$a, m, n$  Archie parameters

$Q_v$  shaliness factor, cation exchange capacity per unit volume ( $\text{meq cm}^{-3}$ )

$B$  equivalent conductivity of sodium clay-exchange cations

### Water-saturated shaly sand

$$\frac{1}{R_0} = C_0 = \frac{1}{F^*} \cdot (C_W + B \cdot Q_v)$$

89

## Waxman-Smits Model

$S_w = 1$

$$\frac{1}{R_0} = C_0 = \frac{1}{F^*} \cdot (C_W + B \cdot Q_v)$$

$$R_0 = F^* \cdot (R_w^{-1} + B \cdot Q_v)^{-1}$$

mobility  
of the  
ions

$$B = \frac{-5.41 + 0.133 \cdot T - 1.253 \cdot 10^{-4} \cdot T^{-2}}{1 + R_w^{1.23} \cdot (0.025 \cdot T - 1.07)}$$

Juhasz (1981)

T in Fahrenheit

$$B = \frac{-1.28 + 0.255 \cdot T - 4.059 \cdot 10^{-4} \cdot T^{-2}}{1 + R_w^{1.23} \cdot (0.045 \cdot T - 0.27)}$$

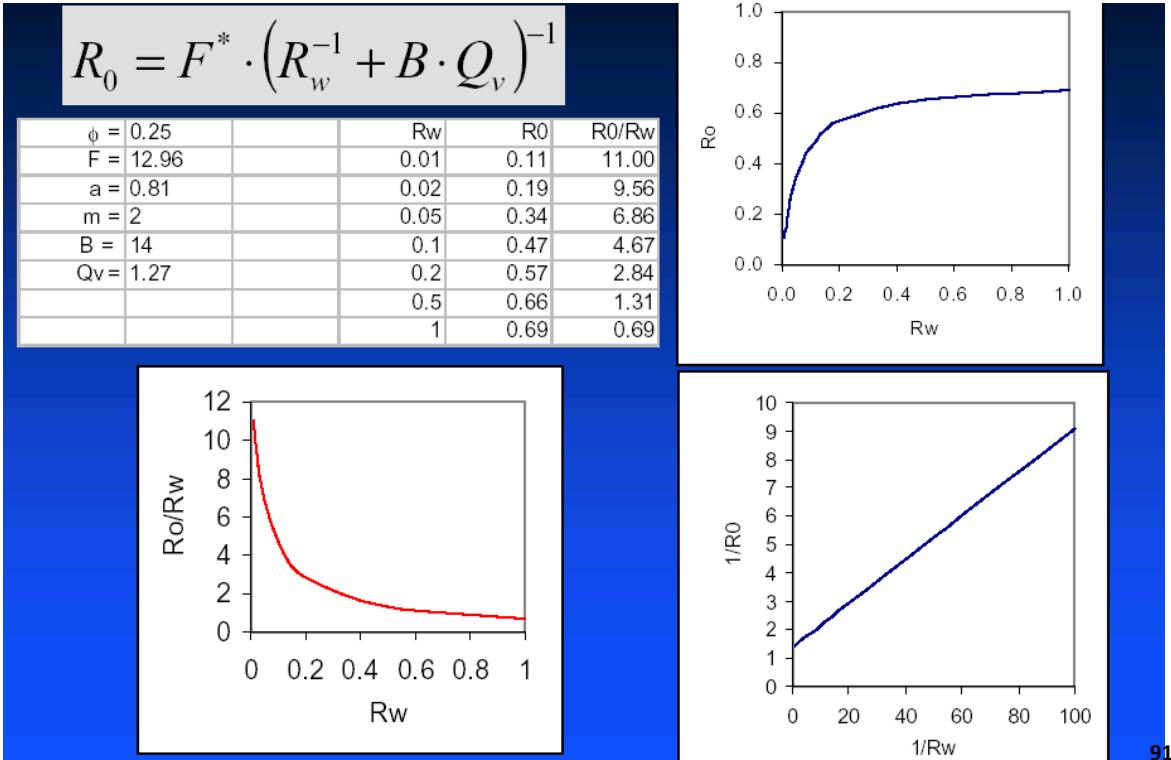
T in Celsius

charge per unit  
pore volume

$$Q_v = CEC \cdot \frac{1-\phi}{\phi} \cdot \rho_{\text{mineral}}$$

90

## Example: Waxman-Smits Model, $Sw = 1$



## Example: Waxman-Smits Model, $Sw = ?$

**$Sw = ?$**

$$\frac{1}{R_t} = \frac{S_w^n}{F^*} \cdot \left( \frac{1}{R_w} + \frac{B \cdot Q_v}{S_w} \right)$$

assume  $n = 2$ :



explicit  
solution

$$\frac{1}{R_t} = \frac{S_w^2}{F^*} \cdot \left( \frac{1}{R_w} + \frac{B \cdot Q_v}{S_w} \right) = \frac{1}{F^*} \cdot \left( \frac{S_w^2}{R_w} + B \cdot Q_v \cdot S_w \right)$$

$$S_w = \left( \frac{F^* \cdot R_w}{R_t} + \left( \frac{B \cdot Q_v \cdot R_w}{2} \right)^2 \right)^{\frac{1}{2}} - \left( \frac{B \cdot Q_v \cdot R_w}{2} \right)$$

## Example: Waxman-Smits Model, $S_w = ?$

**$S_w = ?$**

$$\frac{1}{R_t} = \frac{S_w^n}{F^*} \cdot \left( \frac{1}{R_w} + \frac{B \cdot Q_v}{S_w} \right)$$

$n \neq 2$ : no explicit solution --> iteration

$$S_w = \left( \frac{F^* \cdot R_w}{R_t \cdot \left( 1 + \frac{B \cdot Q_v \cdot R_w}{S_w} \right)} \right)^{\frac{1}{n}}$$

start with assumption for  $S_w$  and calculate iteratively

93

## Example: Waxman-Smits Model, $S_w = ?$

**Example 1** (Introduction to Wireline Log Analysis/Baker Atlas, p. 260)

Given:

$$\begin{aligned} a &= 0.81 & m &= 2.0 & n &= 2.0 \\ R_w &= 0.05 \text{ ohm-m} & B \cdot Q_v &= 17 & \phi &= 25 \% & R_t &= 10 \text{ ohm-m} \end{aligned}$$

### 1. Calculation based on ARCHIE equation:

$$S_w = \left( \frac{R_w}{R_t} \cdot \frac{a}{\phi^m} \right)^{\frac{1}{n}} = \sqrt[2]{\frac{0.05}{10} \cdot \frac{0.81}{0.25^2}} = 0.254$$

$S_w = 25 \%$

### 2. Calculation based on Waxman-Smits equation:

$$\begin{aligned} S_w &= \left( \frac{F^* \cdot R_w}{R_t} + \left( \frac{B \cdot Q_v \cdot R_w}{2} \right)^2 \right)^{\frac{1}{2}} - \left( \frac{B \cdot Q_v \cdot R_w}{2} \right) \\ &= \left( \frac{0.81 \cdot 0.05}{0.25^2 \cdot 10} + \left( \frac{14 \cdot 1.27 \cdot 0.05}{2} \right)^2 \right)^{\frac{1}{2}} - \left( \frac{14 \cdot 1.27 \cdot 0.05}{2} \right) \\ &= (0.0648 + (0.4445)^2)^{\frac{1}{2}} - 0.4445 = 0.067 \end{aligned}$$

$S_w = 7 \%$

94

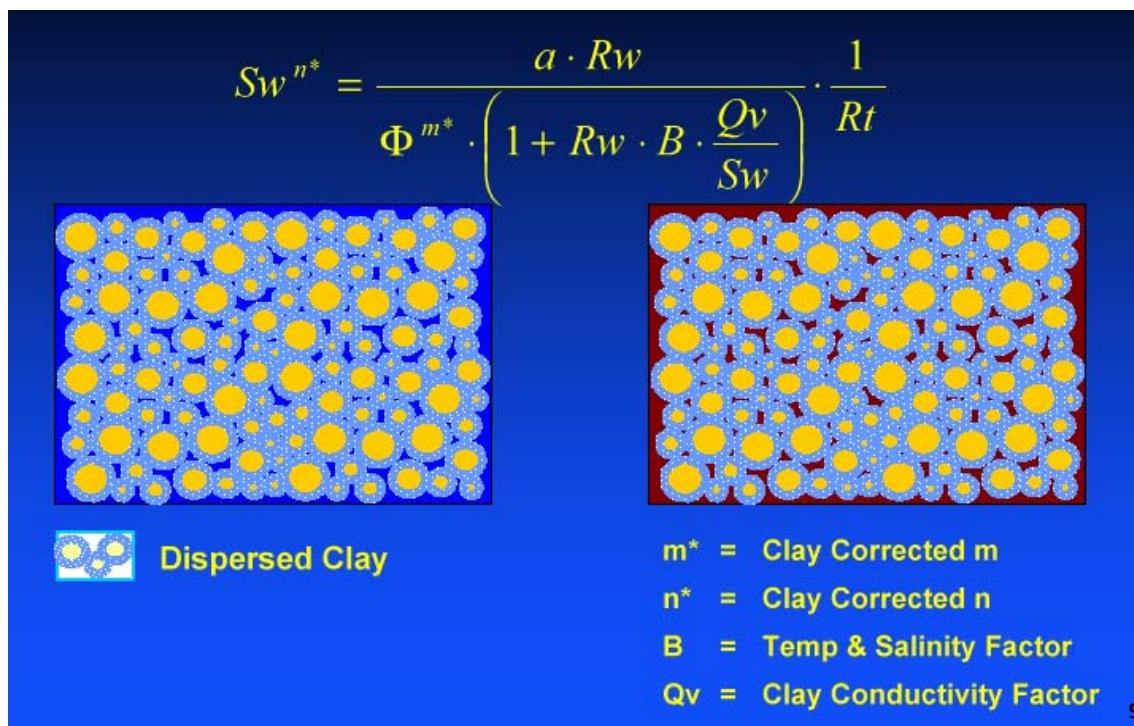
TABLE 6-1 – A Few of the Many Shaly Sand Saturation Equations

Simandoux	$C_t = \frac{C_w}{F} S_w^2 + \varepsilon V_{sh} C_{sh}$	1 $\varepsilon = 1$ for high $S_w$ ; $\varepsilon < 1$ for low $S_w$ .
Schlumberger	$C_t = \frac{C_w}{F(1 - V_{sh})} S_w^2 + V_{sh} C_{sh} S_w$	2 $F$ relates to the free fluid porosity of the total rock volume, inclusive of intraformational (laminated) shales.
Clavier <i>et al.</i>	$C_t = \frac{C_w}{F_o} S_w^2 + \frac{(C_{bw} - C_w V_{QV})}{F_o} S_w$	2 Dual-water model $F_o$ relates to total interconnected porosity. $S_w$ relates to the total interconnected pore space.
Waxman and Smits	$C_t = \frac{C_w}{F_*} S_w^2 + \frac{B Q_V}{F_*} S_w$	2 $F_*$ relates to total interconnected porosity. $S_w$ relates to total interconnected pore space.
Juhasz	$C_t = \frac{C_w}{F} S_w^2 + \left( \frac{C_{sh}}{F_{sh}} - C_w \right) \frac{V_{sh} \phi_{sh} S_w}{\phi}$	2 Normalized Waxman-Smits equation $F=1/\phi^m$ where $\phi$ is the porosity derived from the density log and corrected for hydrocarbon effects. $F_{sh} = \frac{1}{m}$ where $\phi_{sh}$ is the shale porosity derived from the density log. $S_w$ relates to total interconnected pore space.
Poupon and Leveaux	$C_t = \frac{C_w}{F} S_w^2 + 2 \sqrt{\frac{C_w V_{sh}^{2-V_{sh} C_{sh}}}{F}} S_w^2 + V_{sh}^{2-V_{sh} C_{sh} S_w} 2$	3 “Indonesia” formula
Poupon and Leveaux	$C_t = \frac{C_w}{F} S_w^2 + 2 \sqrt{\frac{C_w V_{sh} C_{sh}}{F}} S_w^2 + V_{sh}^2 C_{sh} S_w^2$	3 Simplified Indonesia formula for $V_{sh} \leq 0.5$

95

## WAXMAN-SMITS “Dispersed Clay” Equation

### Effective DC Resistivity Response



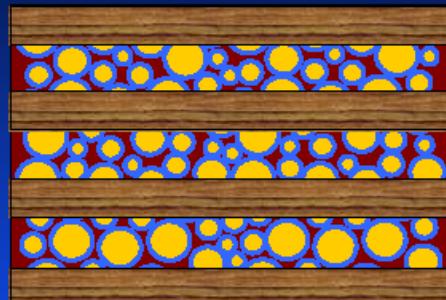
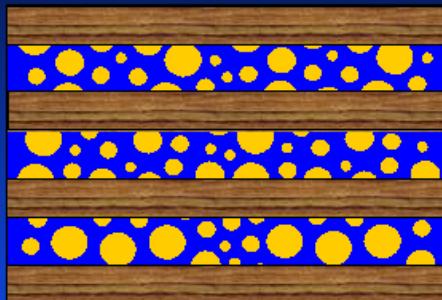
96

## POUPON “Laminar Sand-Shale” Equation

### Effective DC Resistivity Response

$$\frac{1}{Rt} = \frac{1}{Rsd} \cdot (1 - Vlam) + \frac{1}{Rsh} \cdot Vlam$$

$$Sw^n = \left[ \frac{1}{(1 - Vlam)} \cdot \frac{a \cdot Rw}{\Phi^m} \right] \cdot \left[ \frac{1}{Rt} - \frac{Vlam}{Rsh} \right]$$



Rt = Total Resistivity

Rsd = Sand Resistivity

Rsh = Laminar Shale Resistivity

Vlam = Laminar Shale Volume

Laminar Shale

Water Sand

Hydrocarbon Sand

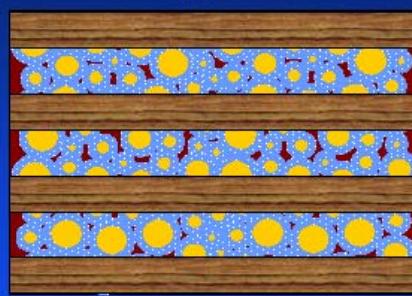
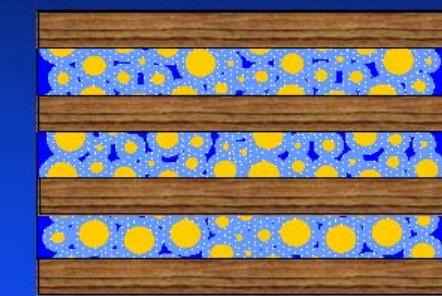
Connate Water

97

## PATCHETT-HERRICK (Poupon + Waxman-Smits) Equation

### Effective DC Resistivity Response

$$Sw^{n*} = \left[ \frac{1}{(1 - Vlam)} \cdot \frac{a \cdot Rw}{\Phi^{m*} \cdot \left( 1 + Rw \cdot B \cdot \frac{Qv}{Sw} \right)} \right] \cdot \left[ \frac{1}{Rt} - \frac{Vlam}{Rsh} \right]$$



Dispersed Clay

Laminar Shale

$m^*$  = Clay Corrected m

$n^*$  = Clay Corrected n

B = Temp & Salinity Factor

Qv = Clay Conductivity Factor

98

## Laminar Shaly Sand Model

(Poupon et al. 1954)



Parallel conductor  
model:

$$\frac{1}{R_t} = \frac{V_{sh-lam}}{R_{sh}} + \frac{1 - V_{sh-lam}}{R_{sd}}$$

$R_{sh}$  shale resistivity y

$R_{sd}$  sand resistivity y

$$R_{sd} = R_W \cdot F \cdot S_W^{-n}$$

99

## Anisotropic Sand-Shale Resistivity Model Case of Electrically Isotropic Shale

### Horizontal Resistivity

$$\frac{1}{R_H} = \frac{V_{sh-lam}}{R_{sh}} + \frac{1 - V_{sh-lam}}{R_{sand}}$$

### Vertical Resistivity

$$R_V = V_{sh-lam} R_{sh} + (1 - V_{sh-lam}) R_{sand}$$

Solve for  $R_{sand}$

100

# Anisotropic Sand-Shale Resistivity Model

## Case of Transversely-Isotropic (TI) Shale

### Horizontal Resistivity

$$\frac{1}{R_H} = \frac{V_{sh-lam}}{R_{H-sh}} + \frac{1 - V_{sh-lam}}{R_{sand}}$$

### Vertical Resistivity

$$R_V = V_{sh-lam} R_{V-sh} + (1 - V_{sh-lam}) R_{sand}$$

Solve for  $R_{sand}$

101

## Origin of Electrical Anisotropy



Laminated  
sand-shale sequences



Sands With  
Different Grain Size

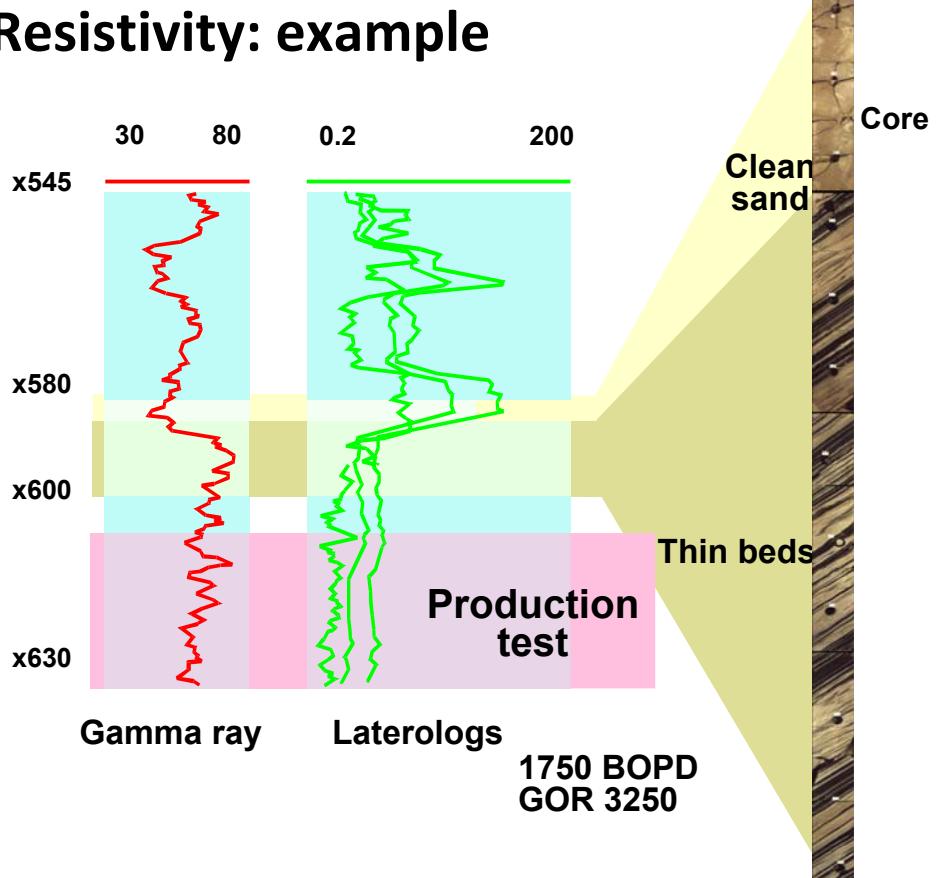


Thin resistive or  
conductive streaks

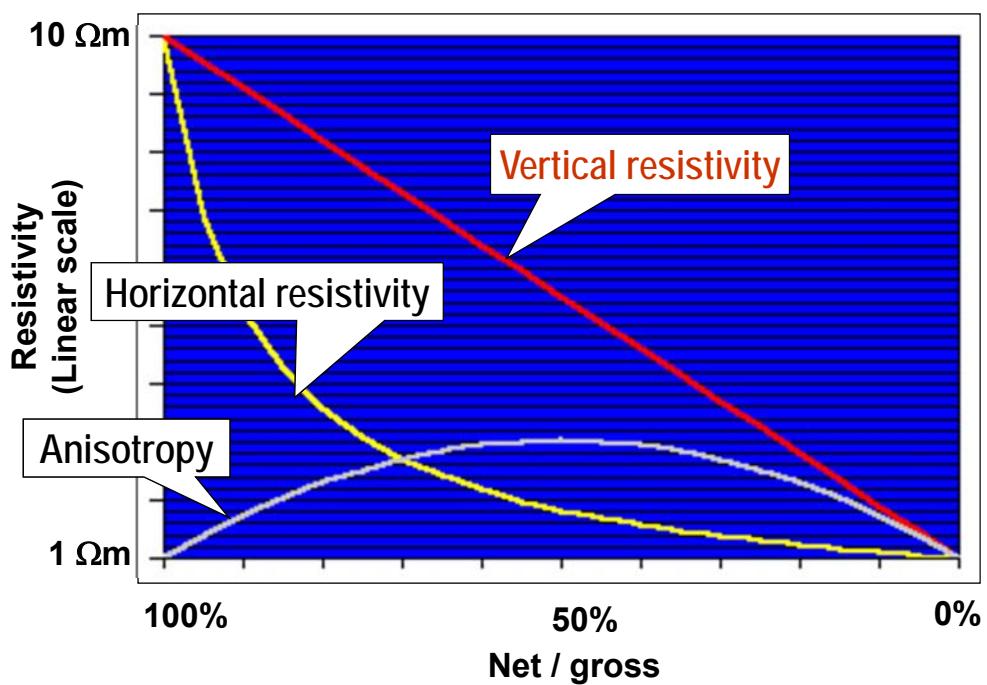
20-30% of global reserves in anisotropic reservoirs

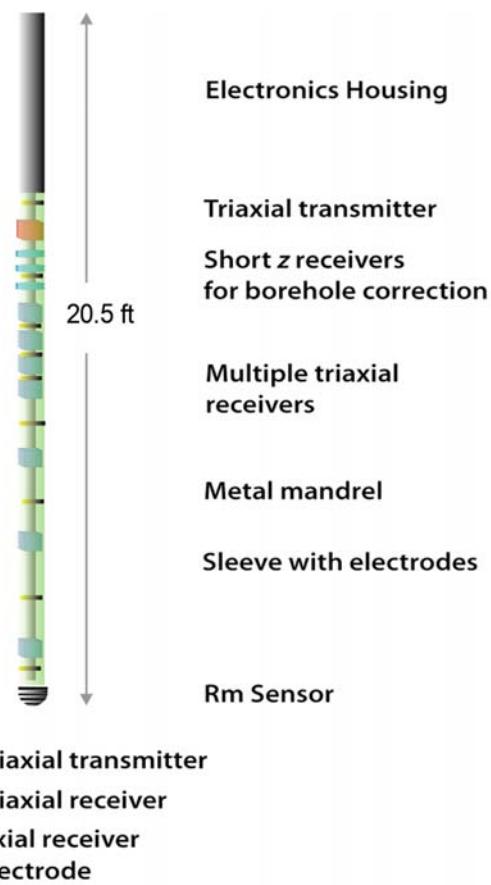
102

## Resistivity: example



## Resistivity Response in Laminar Sand/Shale Sequences





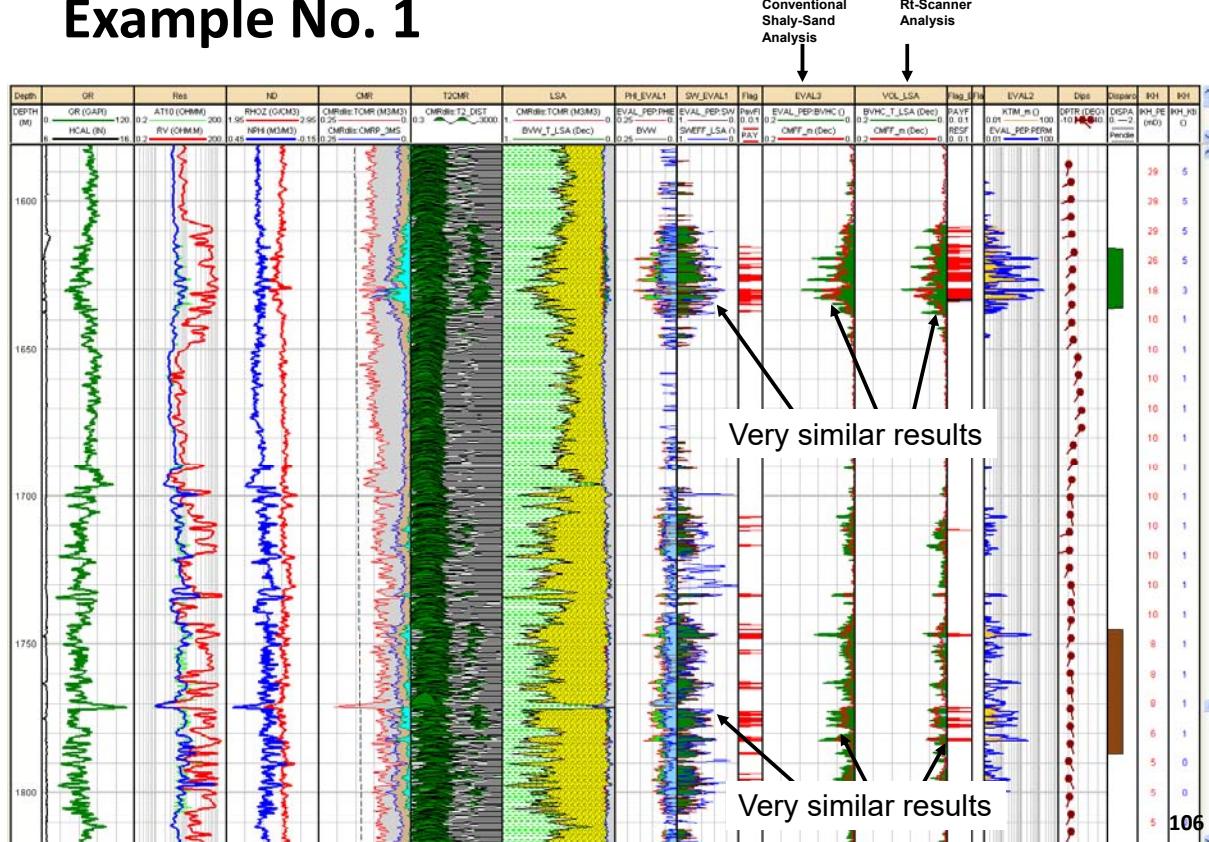
# Schlumberger's Rt-Scanner Tool

- Triaxial transmitter
- Triaxial receiver
- Axial receiver
- Electrode

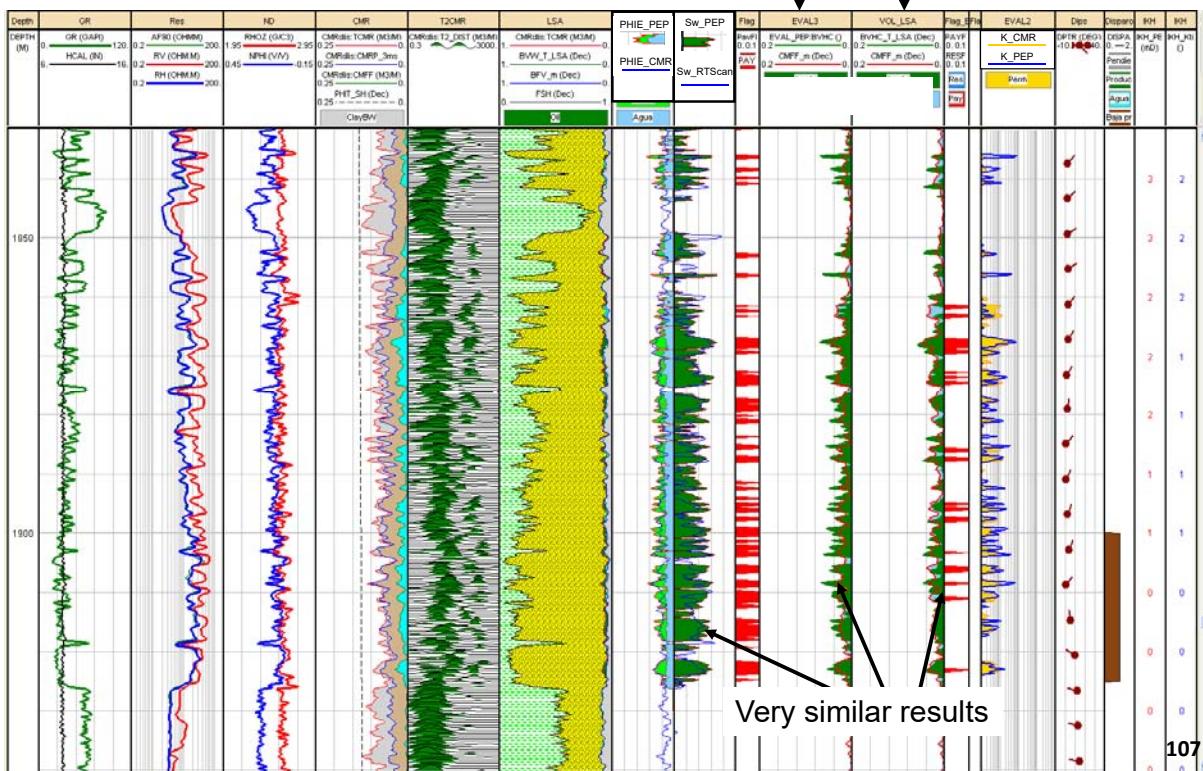
Schlumberger

105

## **Example No. 1**

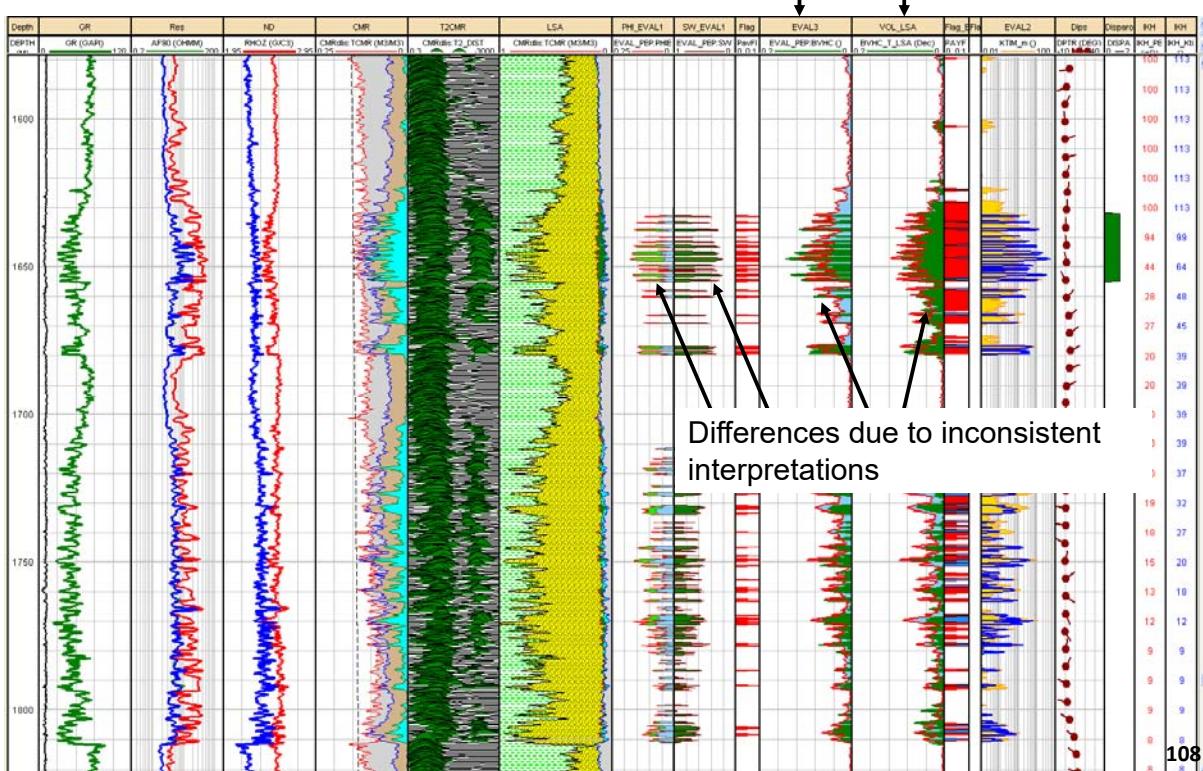


## **Example No. 2**

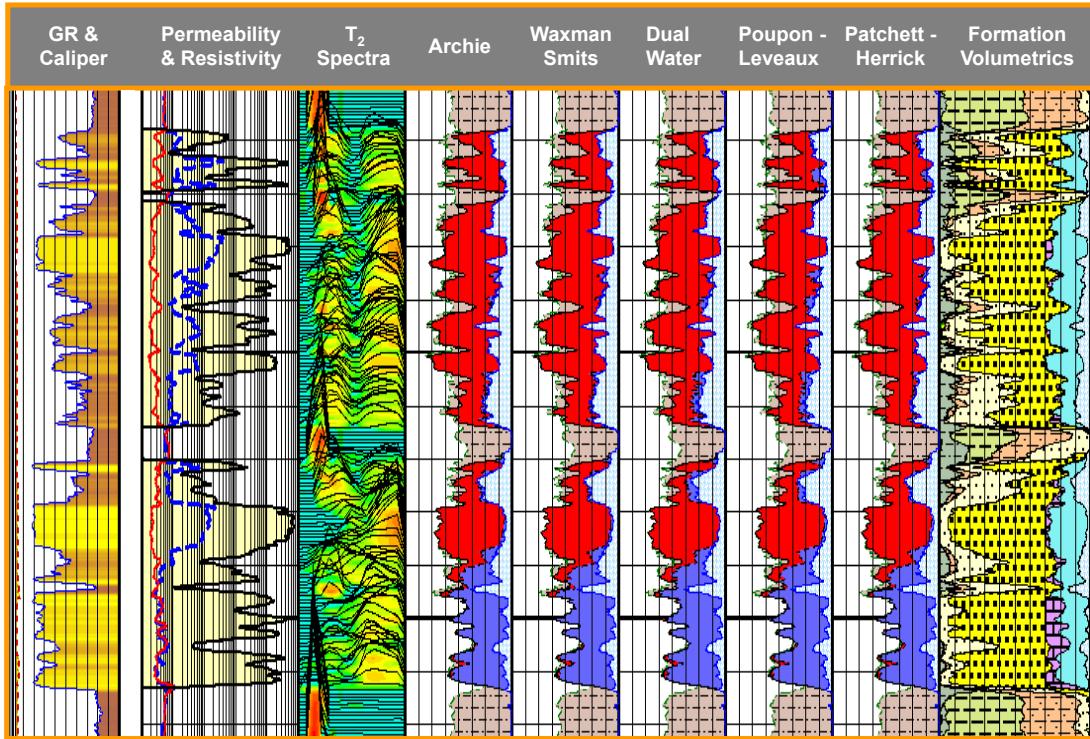


Very similar results

## **Example No. 4**



## MULTIPLE WATER SATURATION INTERPRETATIONS



## Acknowledgements:

- Baker Atlas
- Schlumberger