

The Fundamental Theorem of Calculus

$$\underbrace{\quad}_{\hookrightarrow m_i \leq f(c_i) \leq M_i}$$

$$\hookrightarrow = (F(t_1) - F(a)) + (F(t_2) - F(t_1)) + \dots + (F(t_{n-1}) - F(t_{n-2})) + (F(b) - F(t_{n-1})) = F(b) - F(a)$$

Corollary: If g is continuous on $[a, b]$, then G is differentiable on $[a, b]$ and G is an antiderivative for g

Apply Thm B to a, x, y

?

$$0 \leq M = \sup |g|$$

Apply Thm B to a, x, c

$$\int_c^x g(t) dt$$

t can only take values in the interval with
end points c & x . Then $|t - c| \leq |x - c| < \delta$
Then, $|g(t) - g(c)| < \varepsilon/2$