### Exploring Social Metacognition: the role of confidence in updating estimates of advisor reliability with and without feedback.

Matt Jaquiery

Wolfson College University of Oxford

A thesis submitted for the degree of Doctor of Philosophy

Michaelmas 2021

### Abstract

This *R Markdown* template is for writing an Oxford University thesis. The template is built using Yihui Xie's bookdown package, with heavy inspiration from Chester Ismay's thesisdown, and the OxThesis LATEX template (most recently adapted by John McManigle).

This template's sample content include illustrations of how to do the various things you need to write a thesis in R Markdown, and largely follow the structure from this R Markdown workshop.

Congratulations for taking a step further into the lands of open, reproducible science, by writing your thesis using a tool that allows you to transparently include tables and dynamically generated plots directly from the underlying data. Hip hooray!

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Ulrik Lyngs Linacre College, Oxford 2 December 2018

### Abstract

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### List of Abbreviations

 ${f 1-D,\ 2-D}$  . . . One- or two-dimensional, referring in this thesis to spatial dimensions in an image.

Otter . . . . One of the finest of water mammals.

 $\bf Hedgehog \ . \ . \ . \ Quite a nice prickly friend.$ 

## Part I Introduction

This thesis attempts to determine whether individual psychological processes in the seeking and taking of advice are sufficient to produce entrenched biases at the network level. The work includes empirical investigation into the individual psychological processes underlying advice seeking and advice taking using behavioural experiments; computational modelling and behavioural experimentation exploring the effects of contextual factors on advice-taking; agent-based computational modelling of the effects interactions between agents with psychological advisor evaluation processes that produce biases in assimilation of information and source selection; and a comparison between the structures of networks produced in these models and those naturally occurring social networks. The organisation is as follows: this introduction establishes the core concepts invoked in this thesis, and describes their treatment in the literature; the following sections each include a short chapter on the specific question addressed and the techniques used, a detailed description of the work conducted, and a short discussion of the conclusions drawn from the work; and a final section offers broader conclusions arising as a consequence of the presented work, alongside some suggestions for related research.

#### Advice

Advice is broadly defined as information which comes from a social source. Advice is therefore different from other sources of information in that it is the result of (at least) mental processing of other information. In some cases, it may additionally include discussions among different group members (e.g. advice from the International Advisory Panel on Climate Change). Throughout this thesis, the focus is primarily on advice which comes from a single, stable source, as when we see a post by an acquaintance on social media, or when a stranger provides us with advice.

### Advice-taking

Advice occurs in the context of a decision, and forms a part of the information which is integrated during the decision-making process to produce a decision. To the extent that the decision reached differs from the decision that would have occurred had the advice not been presented, the advice has had an effect on the decision; to the extent that this difference changes the decision in a way consistent with the advice, the advice has been 'taken' (as opposed to 'rejected').

It is tacitly implied by many operationalizations of advice-taking that the informational content of the advice determines the extent to which it is taken or rejected citation needed. Insofar as the identity of the advisor matters, it matters because it functions as a cue to the informational content of the advice. This is likely a major oversimplification, however, because in many real-world contexts advice-giving and advice-taking form part of a developing social relationship: being consulted for advice and having one's advice followed are inherently rewarding (Hertz and Bahrami 2018; Hertz, Palminteri, et al. 2017); and taking advice can serve as a (sometimes costly) social signal of valuing a relationship with a person or group (Byrne et al. 2016). Furthermore, some authors have argued that people may perceive taking advice as sacrificing their independence or autonomy (CITATIONNEEDED). While this thesis follows previous literature in omitting to consider the wider social concerns influencing the taking of advice,

it is nevertheless important to remember that the processes investigated herein take place in a variety of social contexts where complex social agents attempt to optimise over numerous goals over numerous timescales.

### Three-factor model of trust

The degree to which advice is taken is proportional to the trust placed in the advisor by the decision-maker. Interpersonal trust, or the degree to which one is prepared to place one's fortune in the hands of another (e.g. by relying on their advice), is apportioned by Mayer et al. (1995) onto three properties of the advisor (as judged by the decision-maker): ability, benevolence, and integrity. To these three properties of the advisor we may add the decision-maker's general propensity to trust, as well as situational cues and task cues (e.g. the phenomenon that advice is more readily taken for hard tasks than easy ones, (Gino and Moore 2007)).

### Ability

Ability captures the expertise of an advisor: their raw ability to perform the task for which they are giving advice. In some cases this is relatively straightforward, as in the expertise of a General Practitioner in matters of health and disease, and in others more complex, as in the expertise of a hairdresser when deciding on a haircut (when matters of personal taste comingle with aesthetic considerations of facial structure, practical considerations of hair constitution, and social considerations of fashion). The greater the ability of an advisor, the greater the influence of their advice, as demonstrated by experiments showing that participants' decisions are more affected by the advice of advisors who are labelled as more expert in a relevant domain (Sah et al. 2013; Schultze et al. 2017; Sniezek, Schrah, et al. 2004; Sniezek and Van Swol 2001; Soll and Mannes 2011), or are shown to be more expert empirically (Pescetelli 2017; Sah et al. 2013; Ilan Yaniv and Kleinberger 2000).

#### Benevolence

Benevolence refers to the extent to which the advisor seeks to further the interests of the decision-maker. Where ability represents the absolute limit on the quality of advice, benevolence represents the extent to which the advice approaches this limit. The advice of even a renouned expert may be doubted if there is reason to believe their goal is to mislead, a vital lesson for medieval monarchs with their councils of politicking advisors. Experimental work has shown that psychology students relied more on the advice of their friends than on the advice of labelled experts (CITATIONNEEDED), and that participants are more inclined to reject advice when uncertainty is attributed to malice rather than ignorance (Schul and Peni 2015).

#### Integrity

Advisors with integrity exhibit adherence to principles which the decision-maker endorses. As with benevolence, integrity acts to determine the extent to which advice approaches the limit imposed by ability. While not mutually exclusive, integrity is typically important where relationships are less personal (e.g. we may place great trust in a General Practitioner because of their expertise in medical matters and their *integrity* in adhering to a set of professional ethical and conduct requirements). Some description of the research(CITATIONNEEDED)

### Normative models of advice-taking

Advice-taking can be evaluated formally with reference to a normative model. The simplest and most common of these views the decision-making task as an estimation problem (or combination of estimation problems), and provides an approximately Bayesian variance-weighted integration of independent estimates. To borrow from Galton (1907), consider the task of judging the weight of a bullock. We can model any single guess (e) as the true weight (v) plus some error (e):

$$e = v + \epsilon \tag{1.1}$$

The key insight is to observe that the error is drawn from a normal distribution  $(\mathcal{N}(\mu=0, \sigma^2))^1$ . As the number of samples from this distribution increases, the mean of those samples tends towards the mean of the distribution. Thus, the more estimates are taken, the closer on average the sum of errors will be to 0.

$$\frac{\sum_{i}^{N}(e_{i})}{N} = \frac{\sum_{i}^{N}(v + \mathcal{N}(\mu = 0, \sigma_{i}^{2}))}{N}$$
(1.2)

$$\frac{\sum_{i}^{N}(e_{i})}{N} = \frac{\sum_{i}^{N}(v)}{N} + \frac{\sum_{i}^{N}(\mathcal{N}(\mu = 0, \sigma_{i}^{2}))}{N}$$
(1.3)

$$\frac{\sum_{i}^{N}(e_i)}{N} = \frac{Nv}{N} + \hat{0} \tag{1.4}$$

$$\frac{\sum_{i}^{N}(e_{i})}{N} \approx v \tag{1.5}$$

Observe that this formulation is true no matter the value of N. On average, it is always better to have more estimates than fewer. This suggests that, even in the situation where there are only two estimates (the decision-maker's and the advisor's), the best policy will be to incorporate both estimates into the final decision.

The variance of the normal distribution from which errors are derived  $(\sigma_i^2)$  is, in the example above, drawn from a normal distribution itself  $(\sigma_i^2 \sim \mathcal{N}(\mu = 0, \text{sd}^2))$  meaning that it is also cancelled out on average over repeated samples). Where few estimates are taken, weighting those estimates by the variance of the error distributions will increase the accuracy of the estimates in proportion to the difference between the variances. Many experimental implementations of this model avoid weighting issues by calibrating decision-makers and advisors to be equally accurate on average  $(\sigma_{\text{decision-maker}}^2 = \sigma_{\text{advisor}}^2)$ . The result of this constraint is that the optimal policy is simply to average all estimates together.

### Egocentric-discounting

From the perspective of the normative model above, decision-makers should weigh their own estimate equally with each other estimate they receive in the process

 $<sup>^{1}</sup>$ The normal distribution is well-supported by empirical evidence, but note that any symmetrical distribution around 0 will lead to the same conclusion.

of coming to their decision. One of the most robust findings in the literature on advice-taking is that people routinely underweight advisory estimates relative to their own estimates, a phenomenon known as *egocentric discounting* (Dana and Cain 2015; Gino and Moore 2007; Hütter and Ache 2016; Liberman et al. 2012; Minson and Mueller 2012; Rader et al. 2017; Ronayne and Sgroi 2018; See et al. 2011; Soll and Mannes 2011; Trouche et al. 2018; Ilan Yaniv and Kleinberger 2000; Ilan Yaniv and Choshen-Hillel 2012; Ilan Yaniv and Milyavsky 2007). Egocentric discounting occurs in both feedback and no-feedback contexts (Ilan Yaniv and Kleinberger 2000).

Explanations for egocentric discounting are usually framed in terms of personal-level psychology: decision-makers have better access to reasons for their decision (Ilan Yaniv and Kleinberger 2000); overrate their own competence (Sniezek, Schrah, et al. 2004); may have a desire to appear consistent (Ilan Yaniv and Milyavsky 2007); may see opinions as possessions (Soll and Mannes 2011); may be loss-averse to providing a worse final estimate due to advice-taking (Soll and Mannes 2011); or have difficulty avoiding anchoring (Schultze et al. 2017) or repetition bias effects (Trouche et al. 2018). None of these explanations has survived rigorous empirical testing, however, and recently suggestions have widened to include consideration of aggregate-level rather than personal-level causes, with Trouche et al. (2018) arguing that the potential for misaligned incentives between decision-maker and advisor motivate discounting of advice.

In the course of this thesis crossref needed, I demonstrate that egocentric discounting may be a stable metastrategy which protects against exploitation, carelessness, incompetence, and miscommunication. From this perspective, the normative model pertains to a particular instantiation of a problem with questionable ecological validity given the typical ethology of advice-taking in humans. While such considerations affect the conclusions one draws from egocentric discounting relative to the normative model, they do not detract substantially from the practice of using the normative model as an optimum 'set point' from which to evaluate advice-taking behaviour.

### Evaluation of advice

The value of advice, in informational terms, is measured in relation to the optimal decision. It is necessary to distinguish two perspectives on the value of advice: the optimality of the decision recommended by the advice itself; and the optimality of the decision based on advice relative to the decision which would have been made had the advice not been received. This distinction is necessary because people alter their advice-giving behaviour in anticipation of discounting on the part of the decision-maker (CITATIONNEEDED; for a case in human-machine teaming see Azaria et al. 2016), somewhat akin to starting negotiations with a higher demand than one is hoping to settle for.

A single piece of advice can be evaluated using its own properties and the properties of the advisor giving the advice. Furthermore, that evaluation can serve to update the properties of the advisor. A piece of advice's own properties will include its plausibility (e.g. participants in estimation tasks discount advice which is distant from their own initial estimates more heavily (I. Yaniv 2004)), while the properties of the advisor will include the advisor's trustworthiness (see above). The updating of trust following experience of advice is likely to be largely in the domain of ability, although other domains may be affected where the advice is particularly egregious.

### Updating advisor evaluations

While a single piece of advice must be taken on its own terms, people can construct relatively accurate estimates of advisors' advice when provided with feedback on the decisions they use the advice to make (Pescetelli 2017; Sah et al. 2013; Ilan Yaniv and Kleinberger 2000). This likely happens as an analogue of reinforcement learning, where feedback allows an error signal to be used to update the estimate of the advisor's ability ( $\hat{s}^a$ ) rather than one's own beliefs about the world, according to some learning rate ( $\lambda$ ).

$$\hat{s}_{t+1} = \hat{s}_t + |e_t^a - v| \cdot \lambda \tag{1.7}$$

### Advisor evaluation without feedback

Where feedback is not available, participants in experiments continue to demonstrate an ability to respond rationally to differences in advisor quality (Pescetelli 2017). This is evidently not done through access to the correct real-world values, because feedback providing those values is unavailable, and, were participants aware of those values themselves, it stands to reason they would have provided those values (and thus not require advice!). Pescetelli and Yeung (2017) suggest the mechanism for this ability to discriminate between advisors in the absence of feedback is performing updates based on confidence-weighted agreement.

### Agreement

Consider first the non-weighted agreement case, where the advisor's estimate at time t ( $e_t^a$ ) and the decision-maker's estimate at time t ( $e_t^d$ ) are binary ( $\in 0, 1$ ). The estimate of the advisor's ability ( $\hat{s}^a$ ) is updated positively if the advisor and decision-maker agree, and negatively otherwise, according to the learning rate  $\lambda$ .

$$\hat{s}_{t+1} = \hat{s}_t + (-2|e_t^d - e_t^a| + 1)\dot{\lambda}$$
(1.8)

Confidence-weighted agreement

Continuous estimate case

Homophily and echo-chambers

Source selection and information weighting

Context-dependency of epistemic processes

## Part II Psychology of advice

Neque porro quisquam est qui dolorem ipsum quia dolor sit amet, consectetur, adipisci velit...

There is no one who loves pain itself, who seeks after it and wants to have it, simply because it is pain...

— Cicero's de Finibus Bonorum et Malorum.

2

### Psychological mechanisms of advisor evaluation

We're going to include footnotes  $^{1}$ .

<sup>&</sup>lt;sup>1</sup>and not only because Nick hates them...

### Psychology of advice-taking

Something something feedback.

### Psychology of source selection

Something something feedback.

## Part III Context of advice

# Context of Advice

Optimal advice policy differs by context.

### Sensitivity of advice-taking to context

Actual advice-taking behaviour differs by context.

## Part IV Interaction

### Interaction of psychological processes across minds

Models say this will go horribly wrong.

### Network effects of interaction

My models also suggest horrible things.

### Real-world network effects

My models may not be good models.

## Part V Conclusion

# 10 Conclusion

I haven't wasted 3 years of my life and Nick's time.

— Cicero's de Finibus Bonorum et Malorum. — Cicero's de Finibus Bonorum et Malorum.

### Part VI R Markdown demo

Neque porro quisquam est qui dolorem ipsum quia dolor sit amet, consectetur, adipisci velit...

There is no one who loves pain itself, who seeks after it and wants to have it, simply because it is pain...

— Cicero's de Finibus Bonorum et Malorum.

## 11

### R Markdown Basics: The Markdown syntax

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12.1.4 Including tables	12.1.2	Including images
12.1.5 A note on content positioning	12.1.3	Including plots
1 0	12.1.4	Including tables
2.2 Inline code	12.1.5	A note on content positioning
	2.2 Inlin	e code

Here is a brief introduction to using R Markdown. Markdown is a simple formatting syntax for authoring HTML, PDF, and MS Word documents and much, much more. R Markdown provides the flexibility of Markdown with the implementation of  $\mathbf{R}$  input and output. For more details on using R Markdown see http://rmarkdown.rstudio.com.

Be careful with your spacing in *Markdown* documents. While whitespace largely is ignored, it does at times give *Markdown* signals as to how to proceed. As a habit, try to keep everything left aligned whenever possible, especially as you type a new paragraph. In other words, there is no need to indent basic text in the Rmd

document (in fact, it might cause your text to do funny things if you do).

#### 11.1 Markdown basic syntax

#### 11.1.1 Italics and bold

- *Italics* are done like \*this\* or \_this\_
- Bold is done like \*\*this\*\* or \_\_\_this\_\_\_
- **Bold and italics** is done like \*\*\*this\*\*\*, \_\_\_\_this\_\_\_\_, or (the most transparent solution) \*\*\_this\_\*\*

#### 11.1.2 Inline code

• Inline code is created with backticks like `this`

#### 11.1.3 Sub and superscript

 $\operatorname{Sub}_2$  and  $\operatorname{super}^2$  script is created like this~2~ and this^2^

#### 11.1.4 Strikethrough

• Strikethrough is done ~~like this~~

#### 11.1.5 'Escaping' (aka "What if I need an actual asterisk?")

- To include an actual \*, \_ or \, add another \ in front of them: \\*, \\_, \\

#### 11.1.6 Endash (--), emdash (---)

• - and — with - -- and ---

#### 11.1.7 Blockquotes

Do like this:

Put a > in front of the line.

#### 11.1.8 Headings

- are done with #'s of increasing number, i.e.
  - # First-level heading
  - ## Second-level heading
  - ### Etc.

In PDF output, a level-five heading will turn into a paragraph heading, i.e. \paragraph{My level-five heading}, which will appears as bold text on the same line as the subsequent paragraph.

#### 11.1.9 Lists

Unordered list by starting a line with an \* or a -:

- Item 1
- Item 2

Ordered lists by starting a line with a number:

- 1. Item 1
- 2. Item 2

Notice that you rcan mislabel the numbers and *Markdown* will still make the order right in the output.

To create a sublist, indent the values a bit (at least four spaces or a tab):

- 1. Item 1
- 2. Item 2
- 3. Item 3
  - Item 3a
  - Item 3b

27

#### 11.1.10 Line breaks

The official *Markdown* way to create line breaks is by ending a line with more than two spaces.

Roses are red. Violets are blue.

This appears on the same line in the output, because we didn't add spaces after red.

Roses are red.

Violets are blue.

This appears with a line break because I added spaces after red.

I find this is confusing, so I recommend the alternative way: Ending a line with a backslash will also create a linebreak:

Roses are red.

Violets are blue.

To create a new paragraph, you put a blank line.

Therefore, this line starts its own paragraph.

#### 11.1.11 Hyperlinks

• This is a hyperlink created by writing the text you want turned into a clickable link in [square brackets followed by a](https://hyperlink-in-parentheses)

#### 11.1.12 Footnotes

• Are created<sup>1</sup> by writing either ^[my footnote text] for supplying the footnote content inline, or something like [^a-random-footnote-label] and supplying the text elsewhere in the format shown below <sup>2</sup>:

[^a-random-footnote-label]: This is a random test.

<sup>&</sup>lt;sup>1</sup>my footnote text

<sup>&</sup>lt;sup>2</sup>This is a random test.

#### 11.1.13 Comments

To write comments within your text that won't actually be included in the output, you use the same syntax as for writing comments in HTML. That is, <!-- this will not be included in the output -->.

#### 11.1.14 Math

The syntax for writing math is stolen from LaTeX. To write a math expression that will be shown **inline**, enclose it in dollar signs. - This:  $A = \pi^* r^2$  Becomes:  $A = \pi * r^2$ 

To write a math expression that will be shown in a block, enclose it in two dollar signs.

This:  $\$A = \pi^{r}\{2\}$ \$\$

Becomes:

$$A = \pi * r^2$$

To create numbered equations, put them in an 'equation' environment and give them a label with the syntax (\#eq:label), like this:

```
\begin{equation}
f\left(k\right) = \binom{n}{k} p^k\left(1-p\right)^{n-k}
  (\#eq:binom)
\end{equation}
```

Becomes:

$$f(k) = \binom{n}{k} p^k (1-p)^{n-k}$$
 (11.1)

For more (e.g. how to theorems), see e.g. the documentation on bookdown.org

#### 11.2 Additional resources

- R Markdown: The Definitive Guide https://bookdown.org/yihui/rmarkdown/
- R for Data Science https://r4ds.had.co.nz

#### Contents

PDF output
Gitbook output
Insert references easily with the citr add-in
s-referencing $\dots$
Section references
Figure (image and plot) references
Table references
Including page numbers

The magic of R Markdown is that we can add code within our document to make it dynamic.

We do this either as *code chunks* (generally used for loading libraries and data, performing calculations, and adding images, plots, and tables), or *inline code* (generally used for dynamically reporting results within our text).

#### 12.1 Code chunks

The syntax of a code chunk is shown in Figure 12.1.

## Warning: package 'ggplot2' was built under R version 3.5.2

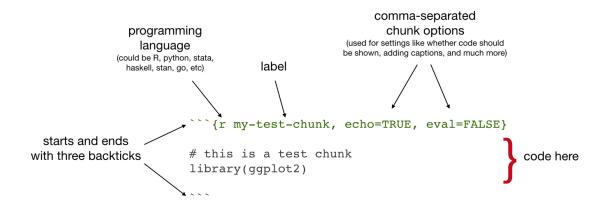


Figure 12.1: Code chunk syntax

## Warning: package 'dplyr' was built under R version 3.5.2
## Warning: package 'stringr' was built under R version 3.5.3
Common chunk options include (see e.g. bookdown.org):

- echo: whether or not to display code in knitted output
- eval: whether or to to run the code in the chunk when knitting
- include: wheter to include anything from the from a code chunk in the output document
- fig.cap: figure caption

**IMPORTANT**: Do *not* use underscoores in your chunk labels - if you do, you are likely to get an error in PDF output saying something like "! Package caption Error: \caption outside float".

#### 12.1.1 Setup chunks

An R Markdown document usually begins with a chunk that is used to load libraries, and to set default chunk options with knitr::opts\_chunk\$set.

In your thesis, this will probably happen in **index.Rmd** and/or as opening chunks in each of your chapters.

```
"" {r setup, include=FALSE}

# don't show code unless we explicitly set echo = TRUE
```



Figure 12.2: Oxford logo

```
knitr::opts_chunk$set(echo = FALSE)

library(tidyverse)
...
```

#### 12.1.2 Including images

Code chunks are also used for including images, with include\_graphics from the knitr package, as in Figure 12.2

```
knitr::include_graphics("figures/beltcrest.png")
```

Useful chunk options for figures include: - out.width (use with a percentage) for setting the image size - if you've got an image that gets waaay to big in your output, it will be constrained to the page width by setting out.width = "100%"

#### Figure rotation

You can use the chunk option out.extra to rotate images.

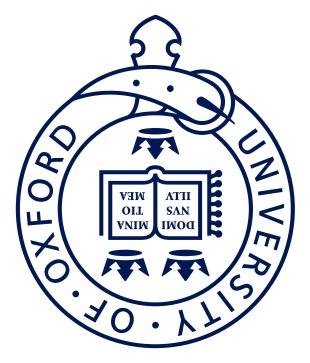


Figure 12.3: Oxford logo, rotated

The syntax is different for LaTeX and HTML, so for ease we might start by assigning the right string to a variable that depends on the format you're outputting to:

```
if (knitr::opts_knit$get('rmarkdown.pandoc.to') == 'latex'){
  rotate180 <- "angle=180"
} else {
  rotate180 <- "style='transform:rotate(180deg);'"
}</pre>
```

Then you can reference that variable as the value of out.extra to rotate images, as in Figure 12.3.

#### 12.1.3 Including plots

Similarly, code chunks are used for including dynamically generated plots. You use ordinary code in R or other languages - Figure 12.4 shows a plot of the cars dataset of stopping distances for cars at various speeds (this dataset is built in to R).

```
cars %>%
ggplot() +
```

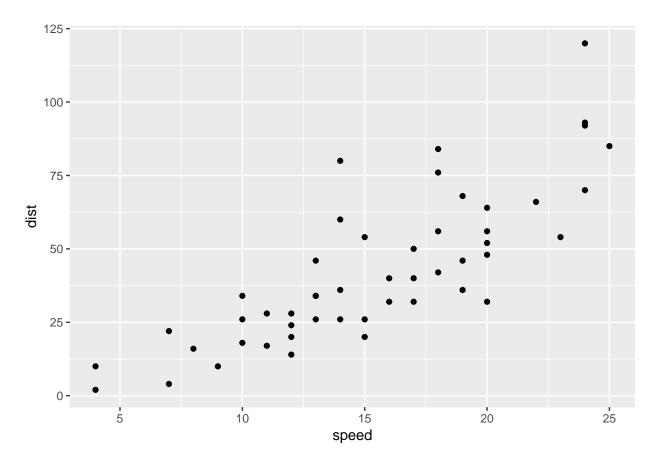


Figure 12.4: A ggplot of car stuff

```
aes(x = speed, y = dist) +
geom_point()
```

Under the hood, plots are included in your document in the same way as images
- when you build the book or knit a chapter, the plot is automatically generated
from your code, saved as an image, then included into the output document.

#### 12.1.4 Including tables

Tables are usually included with the kable function from the knitr package.

Table 12.1 shows the first rows of that cars data - read in your own data, then use this approach to automatically generate tables.

```
cars %>%
head() %>%
knitr::kable(caption = "A knitr kable table")
```

speed	dist
4	2
4	10
7	4
7	22
8	16

10

Table 12.1: A knitr kable table

- Gotcha: when using kable, captions are set inside the kable function
- The kable package is often used with the kableExtra package

#### 12.1.5 A note on content positioning

One thing that may be annoying is the way R Markdown handles "floats" like tables and figures.

In your PDF output, LaTeX will try to find the best place to put your object based on the text around it and until you're really, truly done writing you should just leave it where it lies.

When the time comes for you to make final tweaks to content positioning, read the relevant R Markdown documentation to see if there are easy ways to do what you want.

If you have very specific needs, you might have to read up on LaTeX (https://en.wikibooks.org/wiki/LaTeX/Floats,\_Figures\_and\_Captions) for your PDF output and/or on how to style HTML documents with CSS for your gitbook output.

#### 12.2 Inline code

'Inline code' simply means inclusion of code inside text.

The syntax for doing this is `r R CODE`

For example, `r 4 + 4` would output 8 in your text.

You will usually use this in parts of your thesis where you report results - read in data or results in a code chunk, store things you want to report in a variable,

then insert the value of that variable in your text.

For example, we might assign the number of rows in the cars dataset to a variable:

```
num_car_observations <- nrow(cars)</pre>
```

We might then write:

"In the cars dataset, we have `r num car observations` observations."

Which would output:

"In the cars dataset, we have 50 observations."

### 12.2.1 Referring to results computed in other languages than R

At the moment, inline code only works with R, so syntax such as `python code here` is not valid. However, you can use the reticulate package to access variables from python chunks. Here's a Python code chunk:

```
my_number = 4 + 8
print(my_number)
```

## 12

The reticulate package allows  ${\bf R}$  to access variables defined in python environments with the syntax pyvariable:

```
library(reticulate)
## Warning: package 'reticulate' was built under R version 3.5.3
py$my_number
## [1] 12
```

This means that inline, we can include results from python chunks with `r py\$variable`. For example, we can state that the value of my\_number defined in the python chunk, is 12.

# 13

#### Citations and cross-references

#### Contents

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#### 13.1 Citations

The usual way to include citations in an *R Markdown* document is to put references in a plain text file with the extension .bib, in **BibTex** format.<sup>1</sup> Then reference the path to this file in **index.Rmd**'s YAML header with bibliography: example.bib.

Most reference managers can create a .bib file with you references automatically. However, the **by far** best reference manager to use with *R Markdown* is Zotero with the Better BibTex plug-in, because the citr plugin for RStudio (see below) can read references directly from your Zotero library!

 $<sup>^1{\</sup>rm The~bibliography~can~be~in~other~formats~as~well,~including~EndNote~(.enl)~and~RIS~(.ris), see rmarkdown.rstudio.com/authoring_bibliographies_and_citations.$ 

Here is an example of an entry in a .bib file:

```
@article{Shea2014,
                   {Shea, Nicholas and Boldt, Annika},
  author =
  journal =
                   {Trends in Cognitive Sciences},
                   \{186 - -193\},
  pages =
  title =
                   {{Supra-personal cognitive control}},
  volume =
                   {18},
  year =
                   {2014},
  doi =
                   {10.1016/j.tics.2014.01.006},
}
```

In this entry highlighed section, 'Shea2014' is the **citation identifier**. To default way to cite an entry in your text is with this syntax: [@citation-identifier].

So I might cite some things (Shea2014; Lottridge2012).

#### 13.1.1 PDF output

In PDF output, the bibliography is handled by the OxThesis LaTeX template. If you set bib-humanities: true in index.Rmd, then in-text references will be formatted as author-year; otherwise references will be shown as numbers.

If you choose author-year formatting, a number of variations on the citation syntax are useful to know:

- Put author names outside the parenthesis
  - This: @Shea2014 says blah.
  - Becomes: **Shea2014** says blah.
- Include only the citation-year (in parenthesis)
  - This: Shea et al. says blah [-@Shea2014]
  - Becomes: Shea et al. says blah (Shea2014)
- Add text and page or chapter references to the citation
  - This: [see @Shea2014, pp. 33-35; also @Wu2016, ch. 1]

- Becomes: Blah blah (Shea2014; Wu2016).

#### 13.1.2 Gitbook output

In gitbook output, citations are by default inserted in the Chicago author-date format.

To change the format, add csl: some-other-style.csl in index.Rmd's YAML header. You can browse through and download styles at zotero.org/styles.

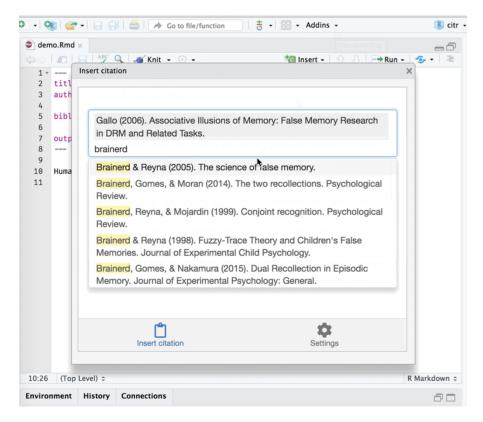


Figure 13.1: The 'citr' add-in

#### 13.1.3 Insert references easily with the citr add-in

For an easy way to insert citations, try the citr RStudio add-in (Figure 13.1). You can install this add-in by typing install.packages("citr") in the R Console.

#### 13.2 Cross-referencing

We can make cross-references to **sections** within our document, as well as to **figures** (images and plots) and **tables**.

The general cross-referencing syntax is \@ref(label)

#### 13.2.1 Section references

Headers are automatically assigned a reference label, which is the text in lower caps separated by dashes. For example, # My header is automatically given the label my-header. So # My header can be referenced with \@ref(my-section)

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Remember what we wrote in section 13.1?

We can also use **hyperlink syntax** and add # before the label, though this is only guaranteed to work properly in HTML output:

- So if we write Remember what we wrote up in [the previous section] (#citations)?
- It becomes Remember what we wrote up in the previous section?

#### Creating custom labels

It is a very good idea to create **custom labels** for our sections. This is because the automatically assigned labels will change when we change the titles of the sections - to avoid this, we can create the labels ourselves and leave them untouched if we change the section titles.

We create custom labels by adding {#label} after a header, e.g. # My section {#my-label}. See our chapter title for an example. That was section 13.

#### 13.2.2 Figure (image and plot) references

- To refer to figures (i.e. images and plots) use the syntax \Oref(fig:label)
- GOTCHA: Figures and tables must have captions if you wish to cross-reference them.

Let's add an image:

#### knitr::include\_graphics("figures/captain.jpeg")

We refer to this image with \@ref(fig:captain). So Figure 13.2 is this image. And in Figure 12.4 we saw a cars plot.

#### 13.2.3 Table references

• To refer to tables use the syntax \@ref(tab:label)

Let's include a table:



Figure 13.2: A marvel-lous meme

Table 13.1: Stopping cars

speed	dist
4	2
4	10
7	4
7	22
8	16

We refer to this table with \@ref(tab:cars-table2). So Table 13.1 is this table.

And in Table 12.1 we saw more or less the same cars table.

#### 13.2.4 Including page numbers

Finally, in the PDF output we might also want to include the page number of a reference, so that it's easy to find in physical printed output. LaTeX has a command for this, which looks like this: \pageref{fig/tab:label} (note: curly

braces, not parentheses)

When we output to PDF, we can use raw LaTeX directly in our .Rmd files. So if we wanted to include the page of the cars plot we could write:

- This: Figure \@ref(fig:cars-plot) on page \pageref(fig:cars-plot)
- Becomes: Figure 12.4 on page 33

#### Include page numbers only in PDF output

A problem here is that LaTeX commands don't display in HTML output, so in the gitbook output we'd see simply "Figure 12.4 on page".

One way to get around this is to use inline R code to insert the text, and use an ifelse statement to check the output format and then insert the appropriate text.

- So this: `r ifelse(knitr::is\_latex\_output(), "Figure \\@ref(fig:cars-plot)
   on page \\pageref{fig:cars-plot}", "")`
- Inserts this (check this on both PDF and gitbook): Figure 12.4 on page 33

Note that we need to escape the backslash with another backslash here to get the correct output.

There is grandeur in this view of life, with its several powers, having been originally breathed into a few forms or into one; and that, whilst this planet has gone cycling on according to the fixed law of gravity, from so simple a beginning endless forms most beautiful and most wonderful have been, and are being, evolved.

— Charles Darwin (**Darwin1859**)

14

# Final Notes on The OxThesis template and on collaboration

#### 14.1 Beginning chapters with quotes

The OxThesis LaTeX template lets you inject some wittiness into your thesis by including a block of type savequote at the beginning of chapters. To do this, use the syntax ```{block type='savequote'}.¹

Add the reference for the quote with the chunk option quote\_author="my author name". You will also want to add the chunk option include=knitr::is\_latex\_output() so that quotes are only included in PDF output.

It's not possible to use markdown syntax inside chunk options, so if you want to e.g. italicise a book name in the reference use a 'text reference': Create a named piece of text with '(ref:label-name) My text', then point to this in the chunk option with quote author='(ref:label-name)'.

#### 14.2 Highlighting corrections

For when it comes time to do corrections, you may want to highlight changes made when you submit a post-viva, corrected copy to your examiners so they can quickly

<sup>&</sup>lt;sup>1</sup>For more on custom block types, see the relevant section in Authoring Books with R Markdown.

verify you've completed the task. You can do so like this:

#### 14.2.1 Short, inline corrections

Highlight short, inline corrections by wrapping them in a <span> tag with the class 'correction'. In other words, if you do <span class="correction">like this</span>, the text between the span tags will be highlighted in blue in the output.

#### 14.2.2 Blocks of added or changed material

Highlight entire blocks of added or changed material by putting them in a block of type correction, using the syntax ```{block type='correction'}.2 Like so:

For larger chunks, like this paragraph or indeed entire figures, you can use the correction block type. This environment **highlights paragraph-sized and** larger blocks with the same blue colour.

## 14.2.3 Stopping corrections from being highlighted in the output

For **PDF** output, go to **index.Rmd** and (i) set corrections: false under params in the YAML header (stops block of corrections from being highlighted), (ii) comment out pandoc\_args: ["--lua-filter=scripts\_and\_filters/correction\_filter.lua"] (stops inline corrections from being highlighted).

For **gitbook** output, go to **style.css** and comment out the styling for .correction.

#### 14.3 Diving in to the OxThesis LaTeX template

For LaTeX minded people, you can read through **templates/template.tex** to see which additional customisation options are available as well as **templates/ociamthesis.cls** which supplies the base class. For example, **template.tex** provides an option for

<sup>&</sup>lt;sup>2</sup>In the .tex file for PDF output, this will put the content between \begin{correction} and \end{correction}; in gitbook output it will be put between <div class="correction"> and </div>.

master's degree submissions, which changes identifying information to candidate number and includes a word count. At the time of writing, you must set this directly in **template.tex** rather than from the YAML header in **index.Rmd**.

#### 14.4 Collaborative writing

Best practices for collaboration and change tracking when using R Markdown are still an open question. In the blog post **One year to dissertate** by Lucy D'Agostino, which I highly recommend, the author notes that she knits .Rmd files to a word\_document, then uses the googledrive R package to send this to Google Drive for comments / revisions from co-authors, then incorporates Google Drive suggestions by hand into the .Rmd source files. This is a bit clunky, and there are ongoing discussions among the R Markdown developers about what the best way is to handle collaborative writing (see issue #1463 on GitHub, where CriticMarkup is among the suggestions).

For now, this is an open question in the community of R Markdown users. I often knit to a format that can easily be imported to Google Docs for comments, then go over suggested revisions and manually incorporate them back in to the .Rmd source files. For articles, I sometimes upload a near-final draft to Overleaf, then collaboratively make final edits to the LATEX file there. I suspect some great solution will be developed in the not-to-distant future, probably by the RStudio team.

Alles Gescheite ist schon gedacht worden. Man muss nur versuchen, es noch einmal zu denken.

All intelligent thoughts have already been thought; what is necessary is only to try to think them again.

— Johann Wolfgang von Goethe (von\_goethe\_wilhelm\_1829)

#### Conclusion

If we don't want Conclusion to have a chapter number next to it, we can add the {-} attribute.

#### More info

And here's some other random info: the first paragraph after a chapter title or section head *shouldn't be* indented, because indents are to tell the reader that you're starting a new paragraph. Since that's obvious after a chapter or section title, proper typesetting doesn't add an indent there.

Appendices



### The First Appendix

This first appendix includes an R chunk that was hidden in the document (using echo = FALSE) to help with readibility:

In 02-rmd-basics-code.Rmd

```
library(tidyverse)
knitr::include_graphics("figures/chunk-parts.png")
```

And here's another one from the same chapter, i.e. Chapter 12:

knitr::include\_graphics("figures/beltcrest.png")

# B

The Second Appendix, for Fun

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