AMAT 503 – Assignment 1 - Lamoureux

Due Thursday, January 25, 2018

- 1. a) Download the "Discrete Wavelet Package" for MATLAB, from the website mentioned in the textbook. www.stthomas.edu/wavelets.
- b) Select 5 images and 5 sounds from the set in the package, and describe them briefly. (This is to show me you've figured out how to use the package.)
- c) Print out two of the images and include with your assignment.
- 2. a) Suppose U is an orthogonal matrix. Show that any eigenvalue λ of U has (complex) absolute value of one. i.e. $|\lambda| = 1$.
- b) Verify this result by finding the eigenvalues of the rotation matrix

$$U = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}.$$

Note the eigenvalues might be complex.

- 3. a) In MATLAB, Python, Julia or your favourite programming language, create a 10x10 matrix with random entries, compute the eigenvalues, and plot in the complex plane. Show me your code as well.
- b) Use Cholesky decomposition to convert this random matrix to an orthogonal matrix. Compute the eigenvalues and plot in the complex plane.

From the textbook:

3.5, 3.15 (images, colours)

3.22, 3.23 (energy)

4.24, 4.28 (Fourier series)