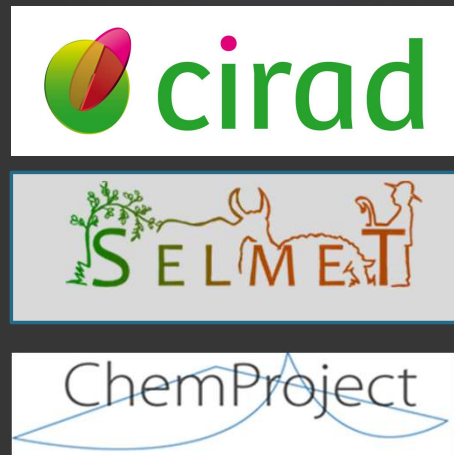


# Sparse PLSR by regularized SVD

matthieu.lesnoff@cirad.fr  
ChemHouse, Montpellier, 30 Sept 2025



*Statistical Applications in Genetics  
and Molecular Biology*

Volume 7, Issue 1

2008

Article 35

A Sparse PLS for Variable Selection when  
Integrating Omics Data

**Kim-Anh Lê Cao**, *INRA UR 631 and Université de Toulouse*

**Debra Rossouw**, *University of Stellenbosch*

**Christèle Robert-Granié**, *INRA UR 631*

**Philippe Besse**, *Université de Toulouse*

**Recommended Citation:**

Lê Cao, Kim-Anh; Rossouw, Debra; Robert-Granié, Christèle; and Besse, Philippe (2008) "A Sparse PLS for Variable Selection when Integrating Omics Data," *Statistical Applications in Genetics and Molecular Biology*: Vol. 7: Iss. 1, Article 35.

**DOI:** 10.2202/1544-6115.1390



**R function** `mixOmics::spl`

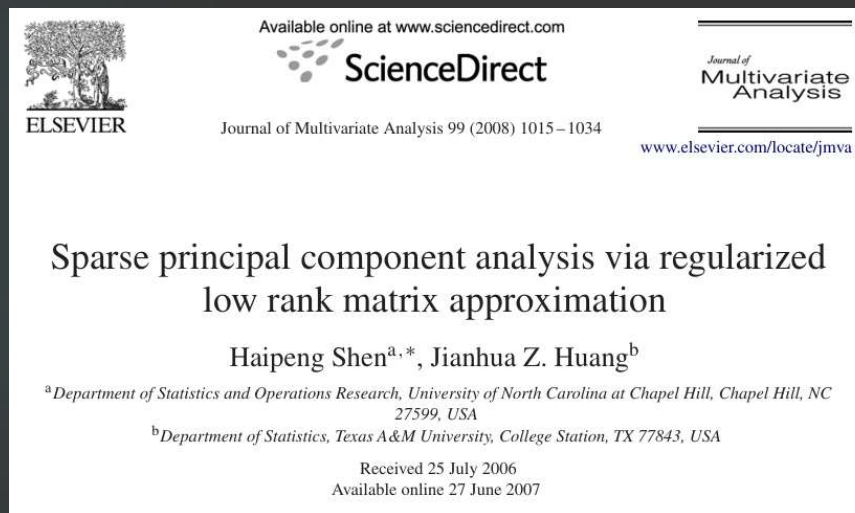
Lê Cao, K.-A., Rohart, F., Gonzalez, I., Dejean, S., Abadi, A.J., Gautier, B., Bartolo, F., Monget, P., Coquery, J., Yao, F., Liquet, B., 2022. mixOmics: Omics Data Integration Project.

<https://doi.org/10.18129/B9.bioc.mixOmics>

## In brief about the method

- Use of a **regularized** (instead of usual) SVD in the PLS algorithm

↖  
rSVD-sPCA



## PLS $X (n, p), Y (n, q)$

- Scores  $(n, 1)$   $t_X = X w_X$   $t_Y = Y w_Y$
- Loading weights  $w_X (p, 1), w_Y (q, 1)$

$$t_X = w_{X,1} x_1 + w_{X,2} x_2 + \dots + w_{X,p} x_p$$

$$t_Y = w_{Y,1} y_1 + w_{Y,2} y_2 + \dots + w_{Y,q} y_q$$

$w_X, w_Y$  such as

$$\max \text{cov}^2(t_X, t_Y) \quad \text{with} \quad \|w_X\| = \|w_Y\| = 1$$

## A usual PLS algorithm

Iterative NIPALS to get  $w_X$  and  $w_Y$ :

1. Set  $t_Y$
2. Repeat until convergence
  - a)  $w_X = X' t_Y$
  - b)  $w_X = w_X / \text{norm}(w_X)$
  - c)  $w_Y = Y' t_X / t_X' t_X$
  - d)  $w_Y = w_Y / \text{norm}(w_Y)$
  - e)  $t_Y = Y w_Y$
3.  $t_X = X w_X$

**But  $w_X$  and  $w_Y$  can be computed without iteration:**

- Let  $K = Y'X$  (could consider  $X'Y$ )
- SVD of  $K \Rightarrow U \Delta V'$
- $w_X = V[:, 1]$
- $w_Y = U[:, 1]$

e.g., Höskuldsson 1988 Journal of Chemometrics  
<https://doi.org/10.1002/cem.1180020306>

**(used in Jchemo: `plskern`, `plsipals`, `plscan`)**

## A simple approach to get sparse $w_x$

### Usual PLS

- $K = Y'X$
- SVD of  $K \Rightarrow U \Delta V'$
- $w_x = V[:, 1]$

### Sparse PLS

- $K = Y'X$
- **rSVD** (S&H 2008) of  $K \Rightarrow U \Delta V'$
- $w_x = V[:, 1]$



This is the idea used by Lê Cao et al.  
(authors also compute sparse  $w_y$ , not detailed in this presentation)

## Summary of the rSVD of Shen & Huang 2008

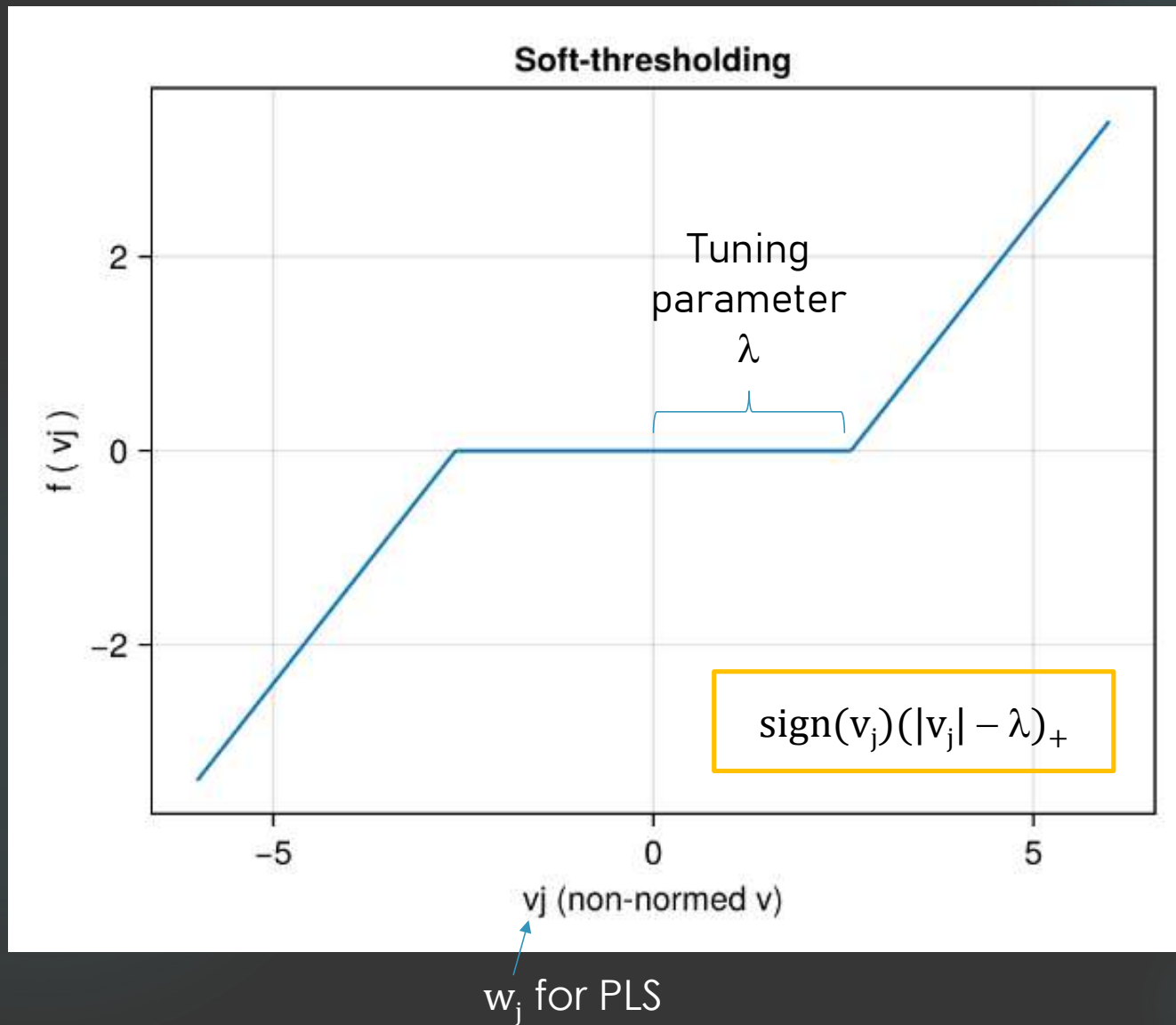
$$\hat{X} = u \delta v' \quad \|u\| = \|v\| = 1 \quad \text{1-rank SVD of a given matrix } X$$

### A usual iterative NIPALS algorithm

1. Set  $u$
2. Repeat until convergence
  - a)  $v = X' u$
  - b)  $u = X v / \text{norm}(X v)$
3.  $v = v / \text{norm}(v)$

### Regularization of Shen & Huang

1. Set  $u$
2. Repeat until convergence
  - a)  $v = f_{\lambda}(X' u)$  *soft thresholding*
  - b)  $u = X v / \text{norm}(X v)$
3.  $v = v / \text{norm}(v)$





# Illustration: MLNIR dataset

9

The screenshot shows the Zenodo dataset page for 'MLNIRdata: 208 near-infrared spectroscopic spectra and densities of hydrocarbon mixtures for chemometrics, data science, machine learning or signal processing'. The page is published on August 8, 2025, version 1.0.1. It is marked as a 'Dataset' and is 'Open'. The authors listed are Duval, Laurent (Data manager), Alsouki, Louna (Annotator), Laxalde, Jérémy (Data collector), and Caillol, Noémie (Data curator). A red circle highlights the text '1. IFP Energies nouvelles' in the 'About' section. The description states that the dataset has been used in chemometrics for property prediction of chemical mixtures with tools like 'Partial Least Squares' (PLS) or sparse PLS. Its publication as 'open data' is meant for further analyses and benchmarks in chemometrics, data science, machine learning, signal processing or artificial intelligence applications (prediction, regression, clustering, training, etc.). Its formats (including 'csv' files) can be imported into standard data processing frameworks (Matlab, Python, Julia, R). It is available at <https://doi.org/10.5281/zenodo.16781223>.

zenodo

Search records...

Communities My dashboard

Published August 8, 2025 | Version 1.0.1

Dataset Open

## MLNIRdata: 208 near-infrared spectroscopic spectra and densities of hydrocarbon mixtures for chemometrics, data science, machine learning or signal processing

Duval, Laurent (Data manager)<sup>1</sup> ; Alsouki, Louna (Annotator) ; Laxalde, Jérémy (Data collector) ; Caillol, Noémie (Data curator)

Hide affiliations

1. IFP Energies nouvelles

This note describes the content of the MLNIRdata dataset. It has already been used in chemometrics for property prediction of chemical mixtures with tools like "Partial Least Squares" (PLS) or sparse PLS.

Its publication as "open data" is meant for further analyses and benchmarks in chemometrics, data science, machine learning, signal processing or artificial intelligence applications (prediction, regression, clustering, training, etc.). Its formats (including "csv" files) can be imported into standard data processing frameworks (Matlab, Python, Julia, R). It is available at <https://doi.org/10.5281/zenodo.16781223>.

The screenshot shows the Elsevier journal page for 'Chemometrics and Intelligent Laboratory Systems'. The journal homepage is [www.elsevier.com/locate/chemometrics](http://www.elsevier.com/locate/chemometrics). The article title is 'Dual-sPLS: A family of Dual Sparse Partial Least Squares regressions for feature selection and prediction with tunable sparsity; evaluation on simulated and near-infrared (NIR) data'. The authors are Louna Alsouki<sup>a,c,\*</sup>, Laurent Duval<sup>b,1</sup>, Clément Marteau<sup>c,1</sup>, Rami El Haddad<sup>b,1</sup>, and François Wahl<sup>b,c,1</sup>. The footnotes provide the affiliations: <sup>a</sup> Laboratoire de Mathématiques et Applications, U.R. Mathématiques et modélisation, Faculté des sciences, Université Saint-Joseph, B.P. 7-5208, Mar Mikhaïl Beyrouth, 1104 2020, Liban; <sup>1</sup> IFP Energies nouvelles, 1-4 avenue du Bois-Préau, Rueil-Malmaison, 92852, France; <sup>c</sup> Institut Camille Jordan, Université Claude Bernard Lyon 1, 43 boulevard du 11 novembre 1918, Villeurbanne, 69100, France.

Contents lists available at ScienceDirect

Chemometrics and Intelligent Laboratory Systems

journal homepage: [www.elsevier.com/locate/chemometrics](http://www.elsevier.com/locate/chemometrics)

Dual-sPLS: A family of Dual Sparse Partial Least Squares regressions for feature selection and prediction with tunable sparsity; evaluation on simulated and near-infrared (NIR) data

Louna Alsouki<sup>a,c,\*</sup>, Laurent Duval<sup>b,1</sup>, Clément Marteau<sup>c,1</sup>, Rami El Haddad<sup>b,1</sup>, François Wahl<sup>b,c,1</sup>

<sup>a</sup> Laboratoire de Mathématiques et Applications, U.R. Mathématiques et modélisation, Faculté des sciences, Université Saint-Joseph, B.P. 7-5208, Mar Mikhaïl Beyrouth, 1104 2020, Liban

<sup>1</sup> IFP Energies nouvelles, 1-4 avenue du Bois-Préau, Rueil-Malmaison, 92852, France

<sup>c</sup> Institut Camille Jordan, Université Claude Bernard Lyon 1, 43 boulevard du 11 novembre 1918, Villeurbanne, 69100, France

All the analyses in this presentation: done with **Jchemo.jl**  
<https://github.com/mlesnoff/Jchemo.jl>

In particular,

function **splsr**

- Same results as **mixOmics::splsr** but
  - a) Sparsity only on  $w_x$  (predictive approach)
  - b) Nipals PLS algorithm replaced by the "**improved kernel algorithm #1**" of Dayal & McGegor 1997  $\Rightarrow$  faster



MLNIR dataset available at: <https://zenodo.org/records/16783068>

N = 208 hydrocarbon samples. For each sample, a near-infrared spectrum (intensities measured at given wavelengths in cm<sup>-1</sup>) and a density value are provided. The dataset contains:

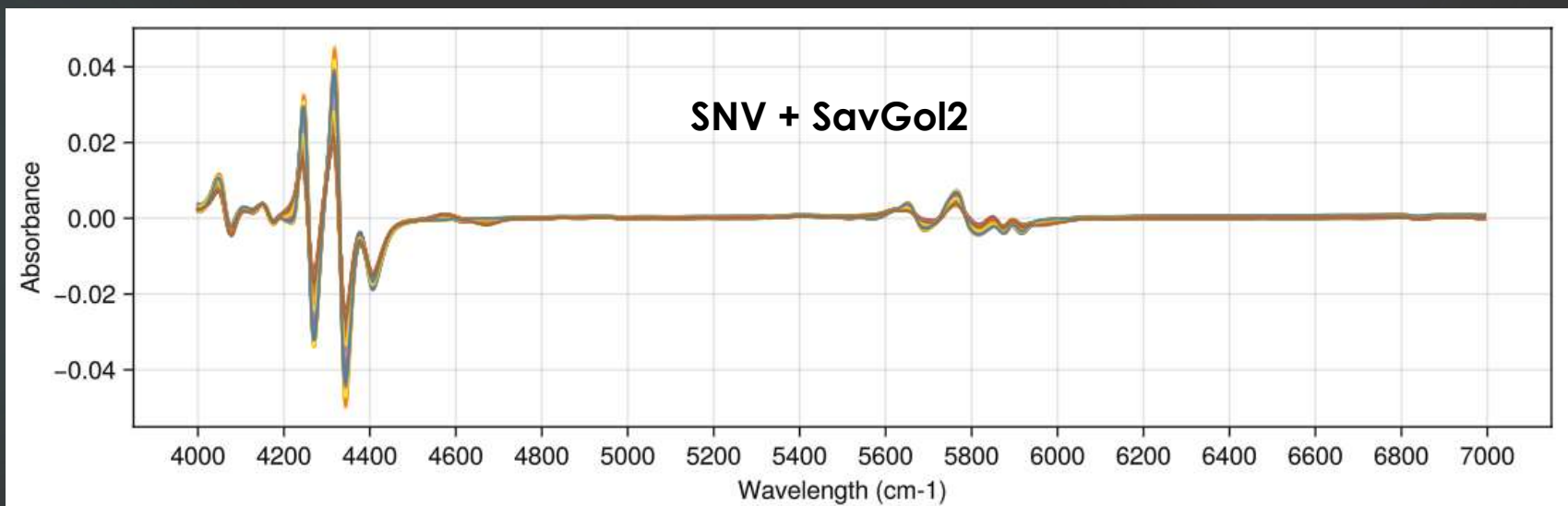
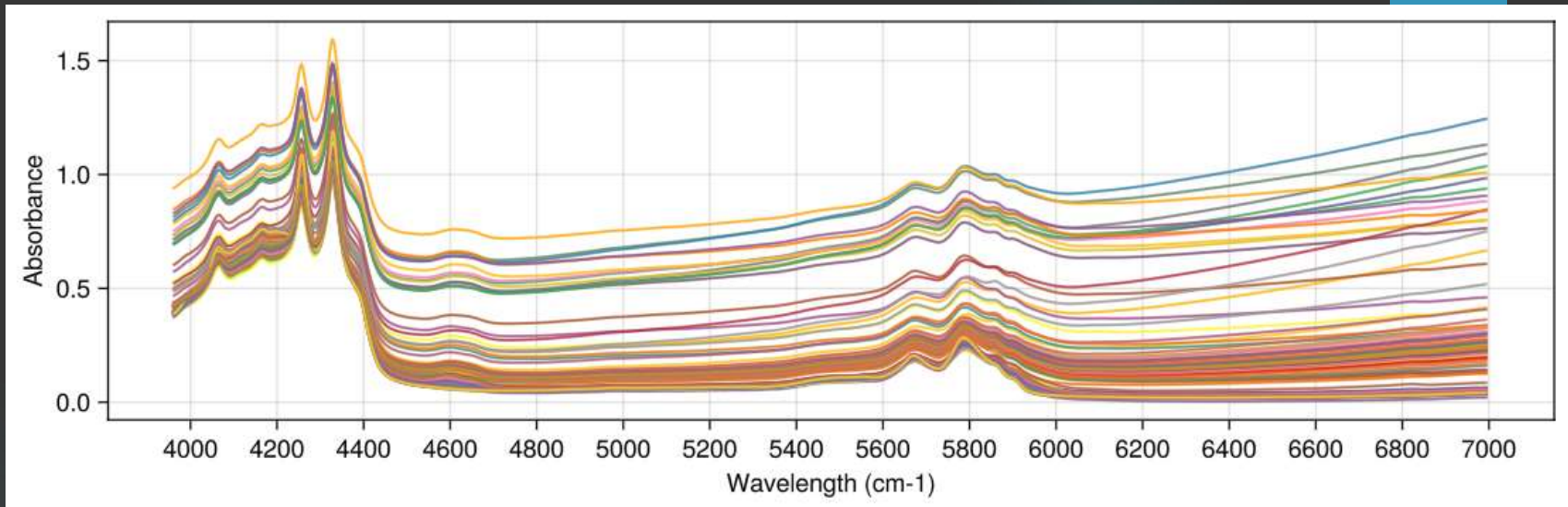
- X: Raw NIR data
- Xp: NIR data after preprocessing (SNV + 2nd derivative Savitzky-Golay)
- y: Density normalized to [0, 1] (response to predict)

Available (JLD2) at: <https://github.com/mlesnoff/JchemoData.jl?tab=readme-ov-file#mnist20pcts>

## MLNIR data

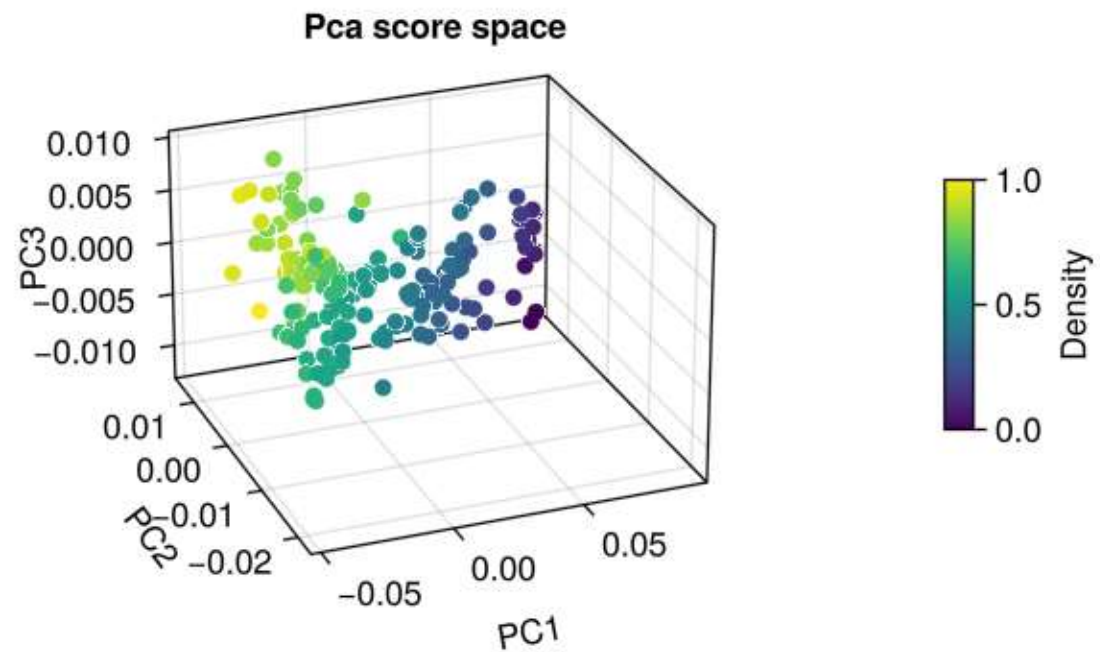
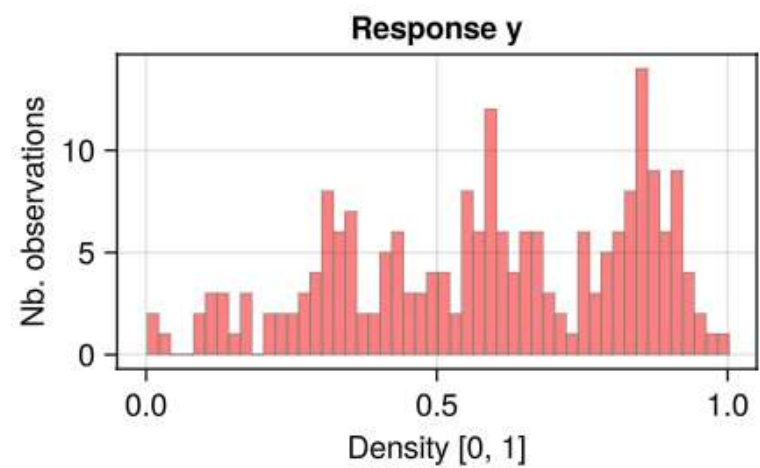
with pre-selection  
of range  
4000-7000  $\text{cm}^{-1}$

1556 variables  
(wavelengths)



## Response y Hydrocarbon density

13



## Model calibration and validation

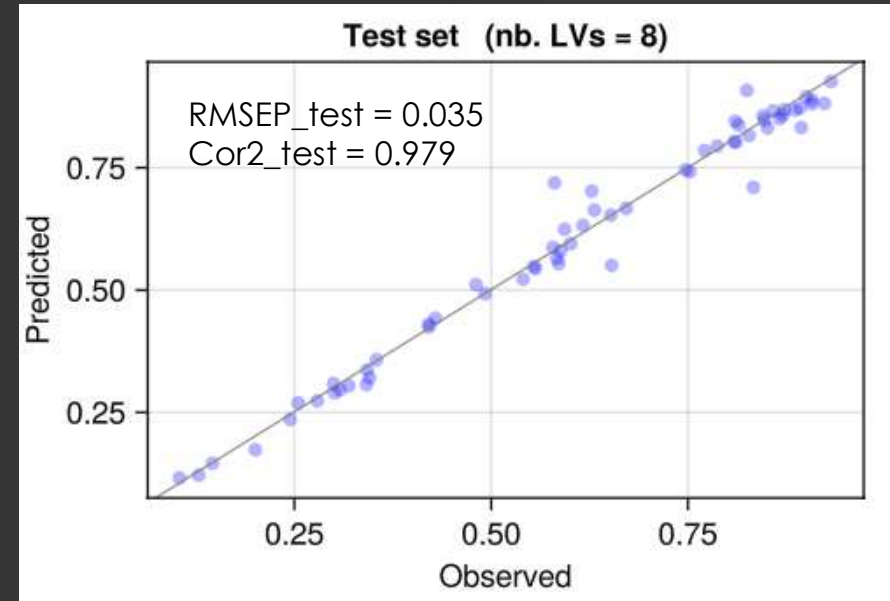
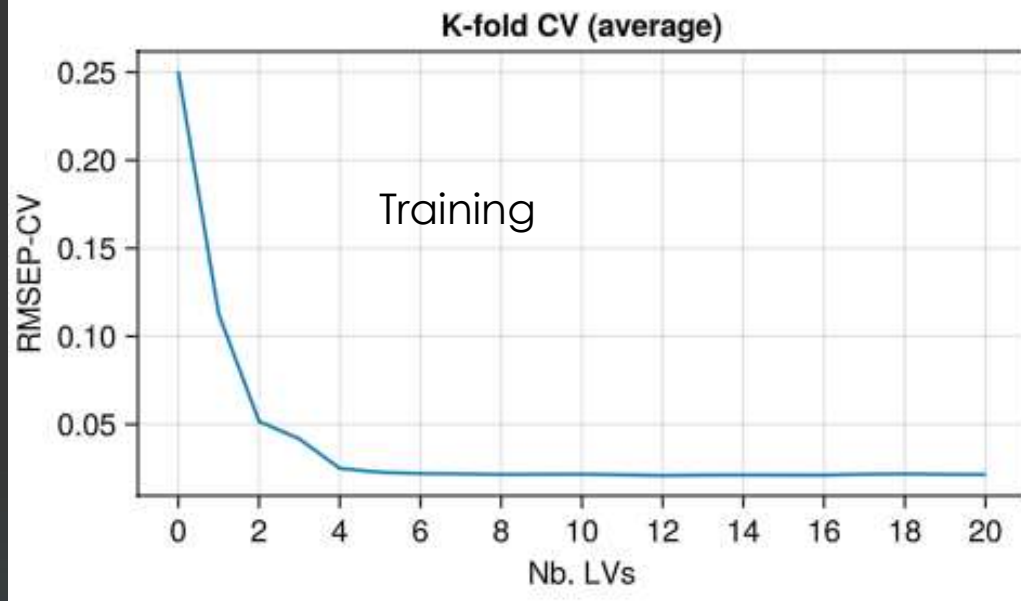
Total  $n = 208$  obs.

Train  $n = 146$   $\Rightarrow$  Replicated K-fold CV  $K = 3$ ,  $nrep = 30$

test  $n = 62$  30% by random sampling

# PLSR

15

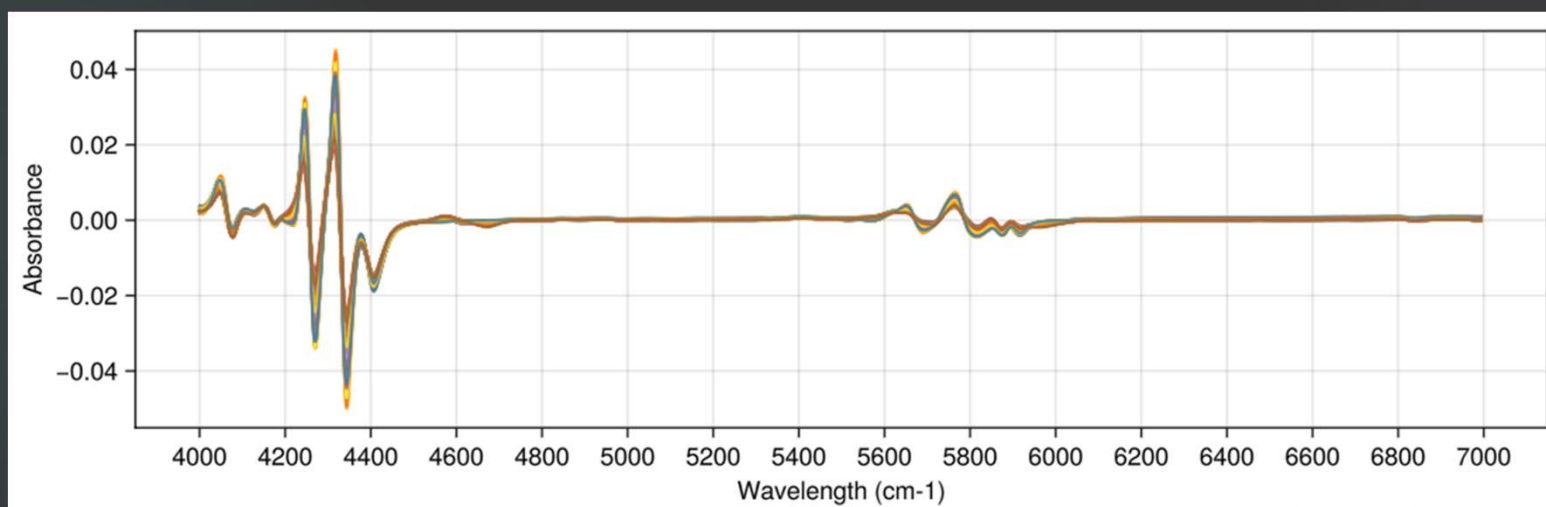
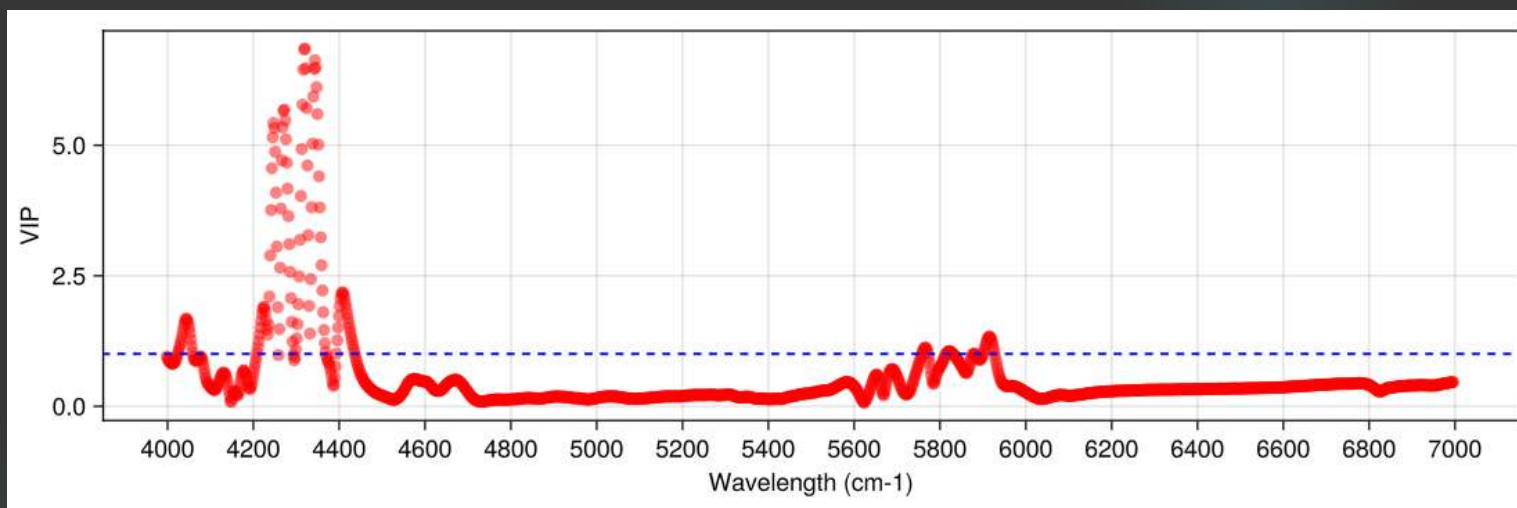




VIPs

PLS 8 LVs

16



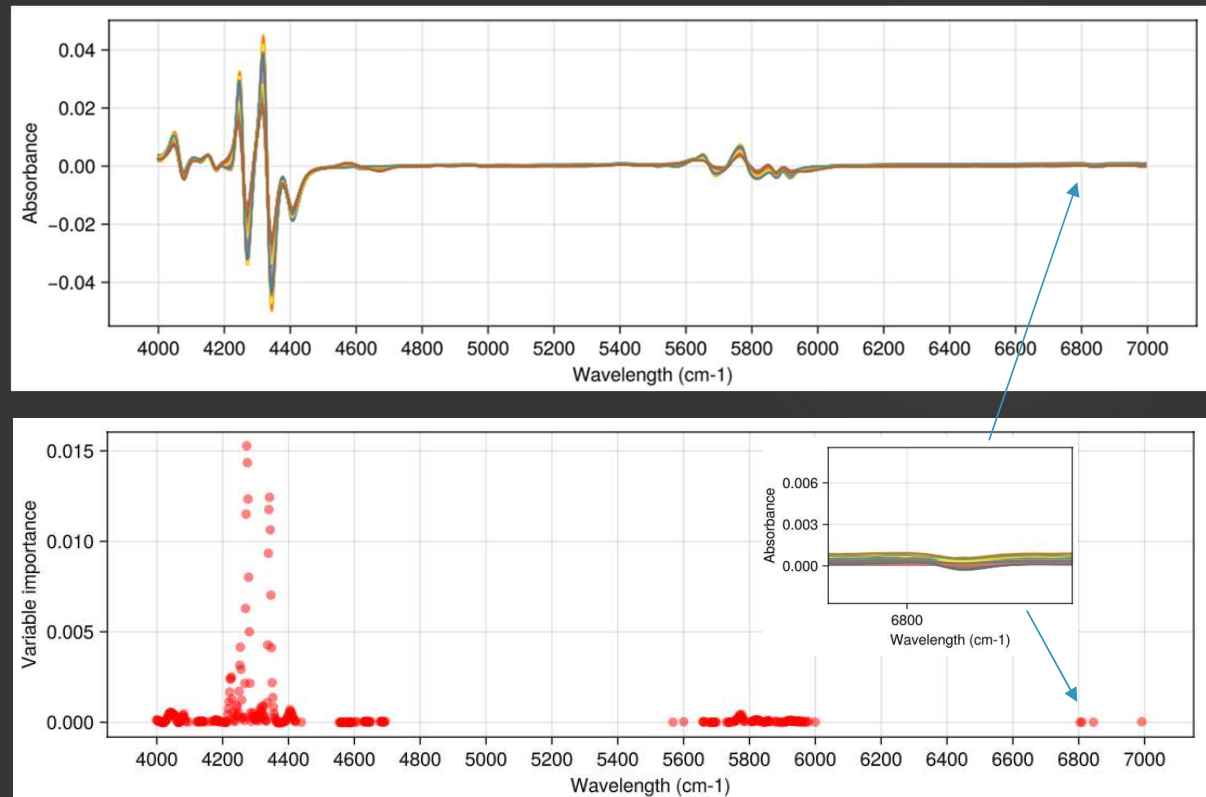


## Alternative to VIPs (very simple and efficient):

## Variable importance by permutation

17

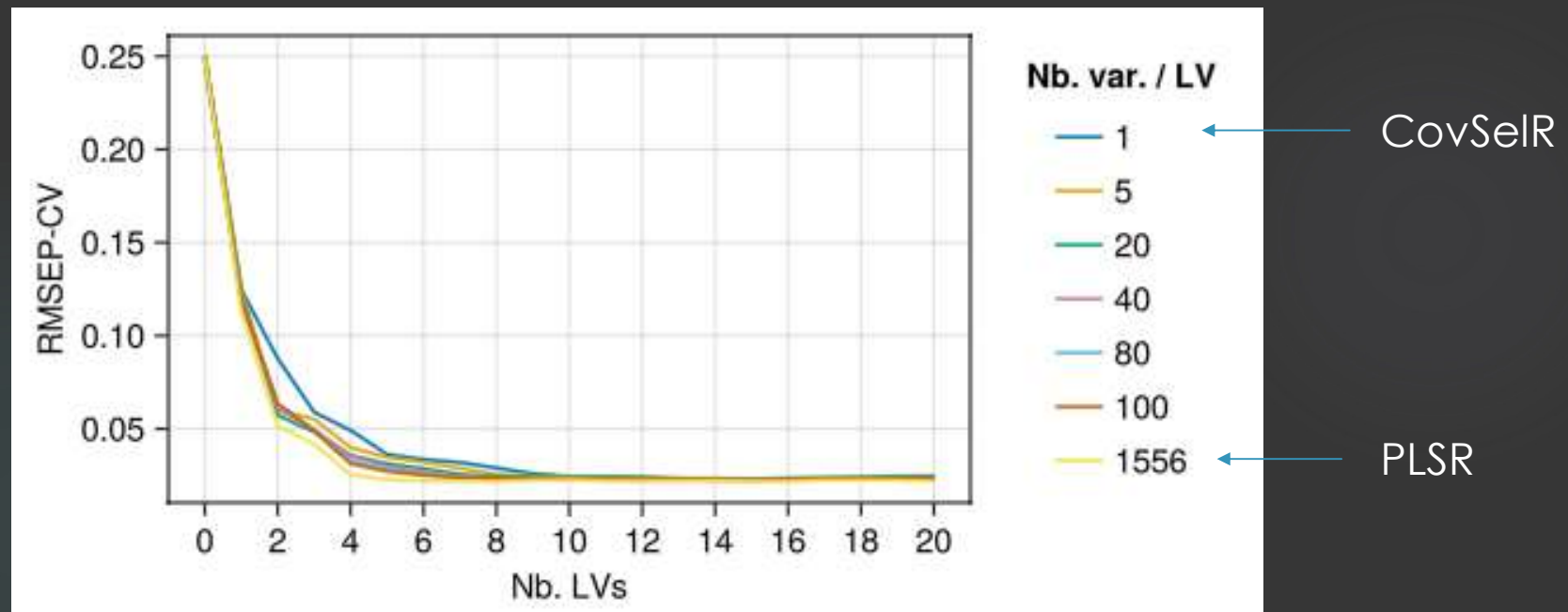
- Successively for each variable:
  - a) Obs. are **randomly permuted**
  - b) The model (here PLSR 8 LVs) is fitted on Xtrain and used to predict Xtest
  - c) Rmsep\_test (or other indicator) is computed and compared to the original without permutation
- Grouped-approaches are very easy to implement (simultaneous permutation of sets of variables)
- Better than Interval-PLS



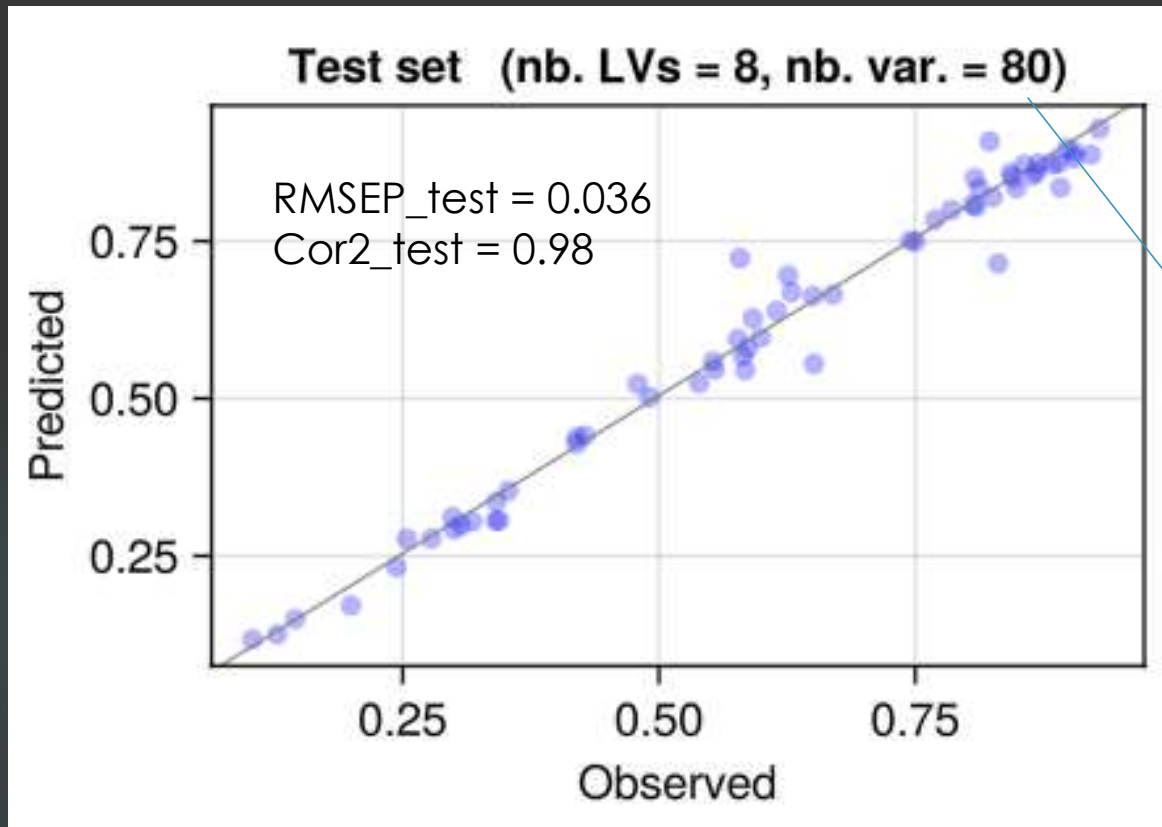
## Sparse PLSR

18

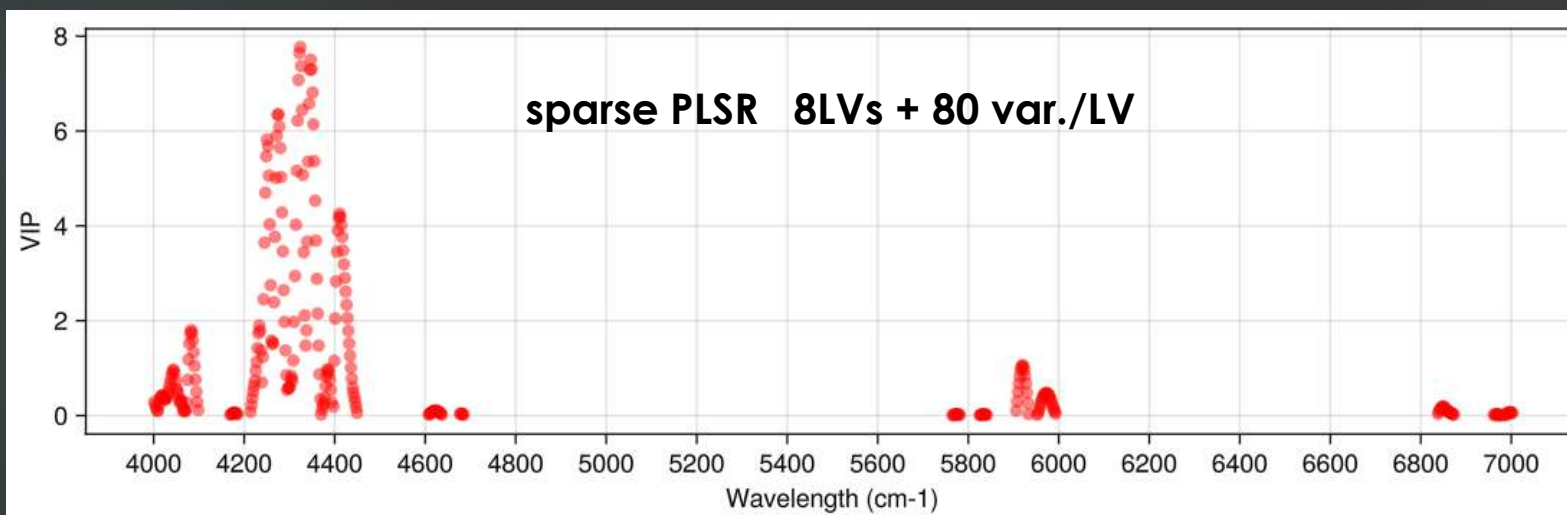
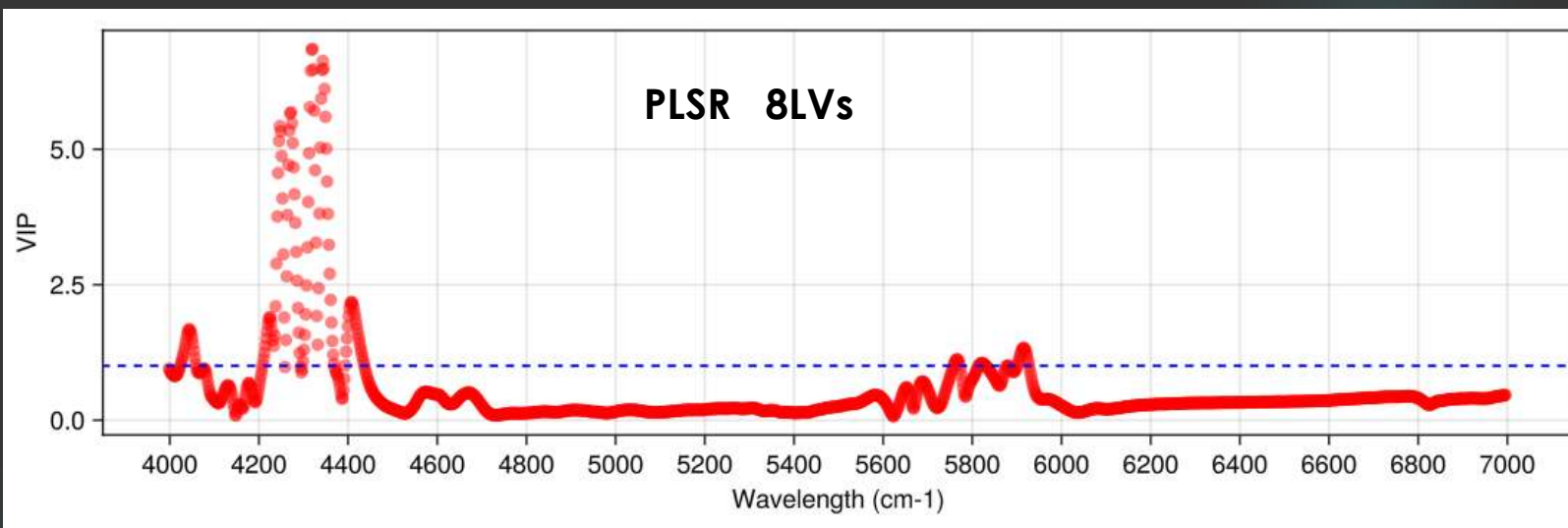
⇒ CV to tune the nb. LVs and the nb. variables that are selected for each LV



In this example, the same nb. variables are selected for all the LVs, but this can be relaxed

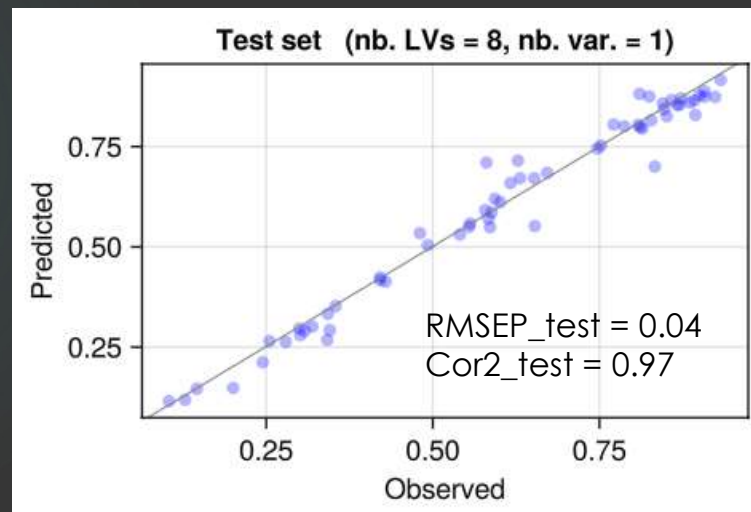
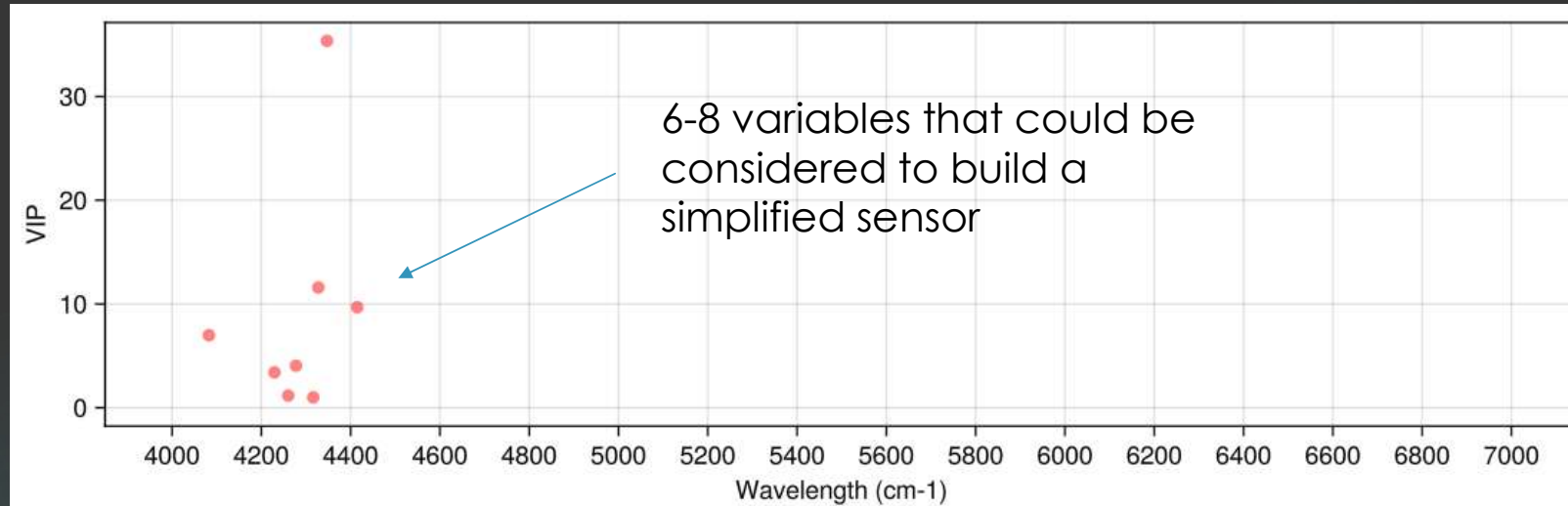


⇒ Total nb. selected  
variables = 256 (over 1556)



## With only 1 variable selected / LV (CovSelR)

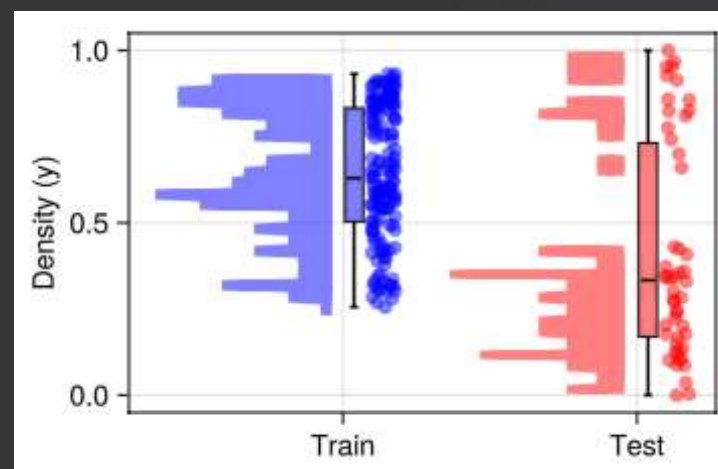
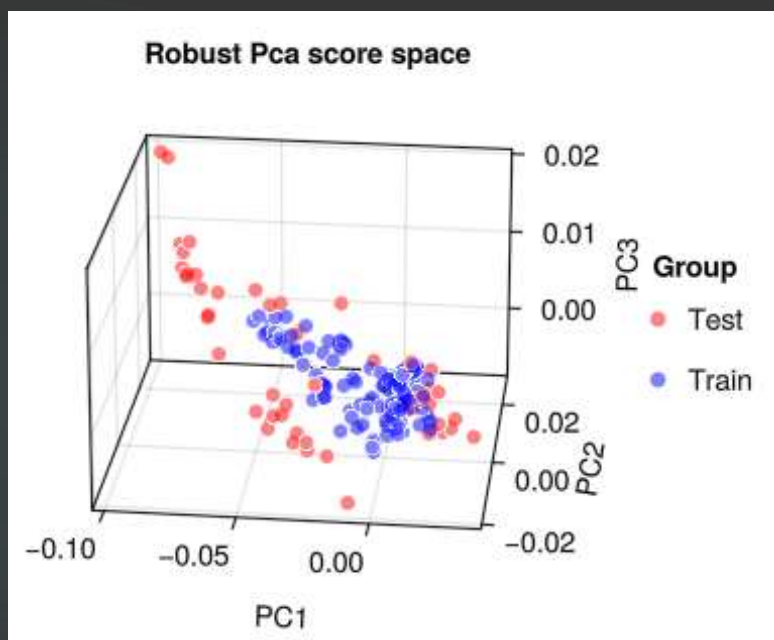
21

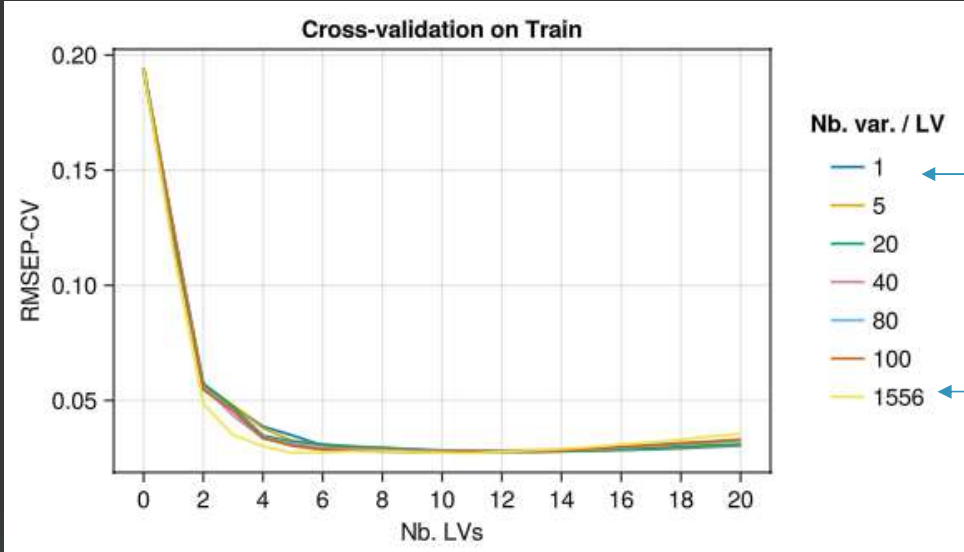


## And what about predictive robustness?

### New split Train/Test

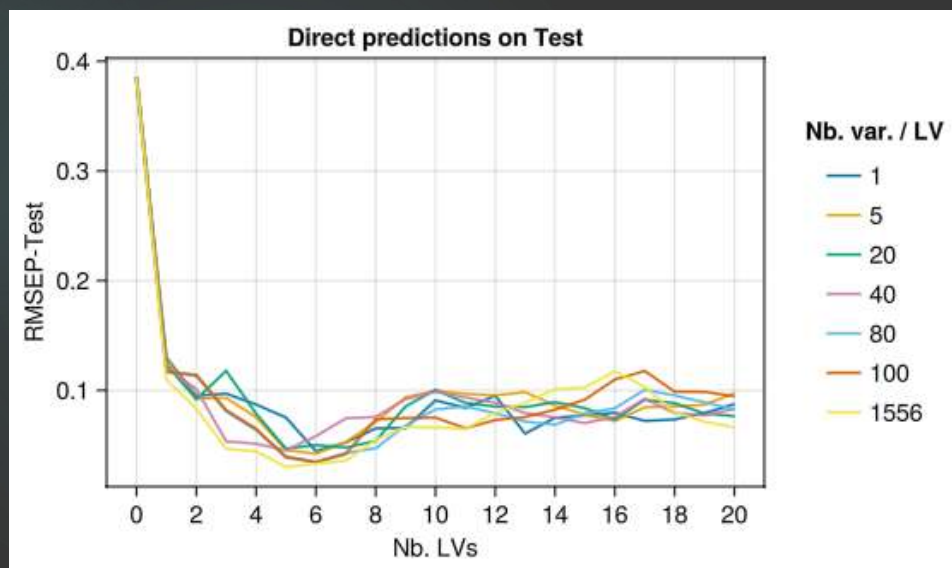
- Test ( $n = 50$ ): Mainly in extrapolation





CovSelR

PLSR



sparse PLSR 8LVs 80 var. / LV

