

# Package ‘r2redux’

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**Type** Package

**Title** R2 statistic

**Version** 1.0.2

**Maintainer** Moksedul Momiin

**Description** R2 statistic for significance test.

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olkin_beta1_2	<i>olkin_beta1_2 function</i>
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## Description

This function derives Information matrix for  $\beta_1^2$  and  $\beta_2^2$  where  $\beta_1$  and  $\beta_2$  are regression coefficients from a multiple regression model, i.e.  $y = x_1 \cdot \beta_1 + x_2 \cdot \beta_2 + e$ , where  $y$ ,  $x_1$  and  $x_2$  are column-standardised, (i.e. in the context of correlation coefficients, see Olkin and Finn 1995).

## Usage

```
olkin_beta1_2(omat, nv)
```

**Arguments**

omat	3 by 3 matrix having the correlation coefficients between y, x1 and x2, i.e. $\text{omat} = \text{cor}(\text{dat})$ where dat is N by 3 matrix having variables in the order of cbind(y,x1,x2)
nv	sample size

**References**

Olkin, I. and J.D. Finn, Correlations redux. Psychological Bulletin, 1995. 118(1): p. 155.

**Examples**

To get information (variance-covariance) matrix of  $\beta_1^2$  and  $\beta_2^2$  where  $\beta_1$  and 2 are regression coefficients from a multiple regression model.

```
dat=read.table("test_ukbb_thresholds_scaled") (see example files)
omat=cor(dat)[1:3,1:3]
omat
1.0000000 0.1958636 0.1970060
0.1958636 1.0000000 0.9981003
0.1970060 0.9981003 1.0000000

nv=length(dat$V1)
output=olkin_beta1_2(omat,nv)
output

output$info (2x2 information (variance-covariance) matrix)
0.04146276 0.08158261
0.08158261 0.16111124

output$var1 (variance of  $\beta_1^2$ )
0.04146276

output$var2 (variance of  $\beta_2^2$ )
0.1611112

output$var1_2 (variance of difference between  $\beta_1^2$  and  $\beta_2^2$ )
0.03940878
```

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olkin_beta_inf	<i>olkin_beta_inf function</i>
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**Description**

This function derives Information matrix for  $\beta_1$  and  $\beta_2$  where  $\beta_1$  and 2 are regression coefficients from a multiple regression model, i.e.  $y = x_1 \cdot \beta_1 + x_2 \cdot \beta_2 + e$ , where y, x1 and x2 are column-standardised (see Olkin and Finn 1995).

**Usage**

```
olkin_beta_inf(omat, nv)
```

**Arguments**

omat	3 by 3 matrix having the correlation coefficients between y, x1 and x2, i.e. $\text{omat} = \text{cor}(\text{dat})$ where dat is N by 3 matrix having variables in the order of cbind(y,x1,x2)
nv	sample size

**References**

Olkin, I. and J.D. Finn, Correlations redux. Psychological Bulletin, 1995. 118(1): p. 155.

**Examples**

To get information (variance-covariance) matrix of  $\beta_1^2$  and  $\beta_2^2$  where  $\beta_1$  and 2 are regression coefficients from a multiple regression model.

```
dat=read.table("test_ukbb_thresholds_scaled") (see example files)
omat=cor(dat)[1:3,1:3]
omat
1.0000000 0.1958636 0.1970060
0.1958636 1.0000000 0.9981003
0.1970060 0.9981003 1.0000000
```

```
nv=length(dat$V1)
output=olkin_beta_inf(omat,nv)
output
```

```
output$info (2x2 information (variance-covariance) matrix)
0.2531406 -0.2526212
-0.2526212 0.2530269
```

```
output$var1 (variance of  $\beta_1^2$ )
0.2531406
```

```
output$var2 (variance of  $\beta_2^2$ )
0.2530269
```

```
output$var1_2 (variance of difference between  $\beta_1^2$  and  $\beta_2^2$ )
1.01141
```

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r2\_diff

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*r2\_diff function*


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**Description**

This function estimates  $\text{var}(R^2(y \sim x[,v1]) - R^2(y \sim x[,v2]))$  where  $R^2$  is the R squared value of the model, y is N by 1 matrix having the dependent variable, and x is N by M matrix having M explanatory variables. v1 or v2 indicates the ith column in the x matrix (v1 or v2 can be multiple values between 1 - M, see Arguments below)

**Usage**

```
r2_diff(dat, v1, v2, nv)
```

**Arguments**

dat	N by (M+1) matrix having variables in the order of cbind(y,x)
v1	This can be set as v1=c(1) or v1=c(1,2)
v2	This can be set as v2=c(2), v2=c(3), v2=c(1,3) or v2=c(3,4)
nv	sample size

**Examples**

To get the test statistics for the difference between  $R2(y \sim x[,v1])$  and  $R2(y \sim x[,v2])$ . (here we define  $R2\_1 = R2(y \sim x[,v1])$  and  $R2\_2 = R2(y \sim x[,v2])$ )

```
dat=read.table("test_ukbb_thresholds_scaled") (see example files)
nv=length(dat$V1)
v1=c(1)
v2=c(2)
output=r2_diff(dat,v1,v2,nv)
output

r2redux output

output$var1 (variance of R2_1)
0.0001437583

output$var2 (variance of R2_2)
0.0001452828

output$var_diff (variance of difference between R2_1 and R2_2)
5.678517e-07

output$r2_based_p (p-value for significant difference between R2_1 and R2_2)
0.5514562

output$mean_diff (differences between R2_1 and R2_2)
-0.0004488044

output$upper_diff (upper limit of 95% CI for the difference)
0.001028172

output$lower_diff (lower limit of 95% CI for the difference)
-0.001925781
```

To get the test statistics for the difference between  $R2(y \sim x[,v1] + x[,v2])$  and  $R2(y \sim x[,v2])$ . (here  $R2\_1 = R2(y \sim x[,v1] + x[,v2])$  and  $R2\_2 = R2(y \sim x[,v1])$ )

```
dat=read.table("test_ukbb_thresholds_scaled") (see example files)
nv=length(dat$V1)
v1=c(1,2)
v2=c(1)
output=r2_diff(dat,v1,v2,nv)
output

r2redux output
```

```

output$var1 (variance of R2_1)
0.0001475195

output$var2 (variance of R2_2)
0.0001437583

output$var_diff (variance of difference between R2_1 and R2_2)
2.321425e-06

output$r2_based_p (p-value for significant difference between R2_1 and R2_2)
0.4369177

output$mean_diff (differences between R2_1 and R2_2)
0.0006042383

output$upper_diff (upper limit of 95% CI for the difference)
0.004887989

output$lower_diff (lower limit of 95% CI for the difference)
-0.0005574975

```

---

r2\_enrich

r2\_enrich

---

## Description

This function estimates  $\text{var}(t1/(t1+t2))$  where  $t1 = R2(y \sim x[,v1] + x[,v2]) - R2(y \sim x[,v1])$  and  $t2 = R2(y \sim x[,v1] + x[,v2]) - R2(y \sim x[,v2])$  where  $R2$  is the R squared value of the model,  $y$  is  $N$  by  $1$  matrix having the dependent variable, and  $x$  is  $N$  by  $M$  matrix having  $M$  explanatory variables.  $v1$  or  $v2$  indicates the  $i$ th column in the  $x$  matrix ( $v1$  or  $v2$  should be a single interger between  $1 - M$ , see Arguments below)

## Usage

```
r2_enrich(dat, v1, v2, nv, expl)
```

## Arguments

dat	$N$ by $(M+1)$ matrix having variables in the order of <code>cbind(y,x)</code>
nv	sample size
expl	The expectation of the ratio (e.g. # SNPs for the genomic region of interest / total # SNPs in genomic partitioning)
v1/v2	These can be set as $v1=1$ and $v2=2$ , $v1=2$ and $v2=1$ , $v1=3$ and $v2=2$ , or any combination as long as the value is between $1 - M$

## Examples

```

To get test statistics for the ratio, i.e.  $t1/(t1+t2)$ .
t1 = R2(y~x[,v1]+x[,v2]) - R2(y~x[,v1]) and
t2 = R2(y~x[,v1]+x[,v2]) - R2(y~x[,v2])
(here we define R2_1=R2(y~x[,v1]), R2_2=R2(y~x[,v2]), R2_12=R2(y~x[,v1]+x[,v2])

```

```

dat=read.table("test_ukbb_enrichment_choles") (see example file)
nv=length(dat$V1)
v1=c(1)
v2=c(2)
expected_ratio=0.04 (# SNPs for the regulatory/total # SNPs)
output=r2_enrich(dat,v1,v2,nv,expected_ratio)
output

r2redux output

output$var1 (variance of R2_1)
8.758455e-05

output$var2 (variance of R2_2)
7.36385e-05

output$var12 (variance of R2_12)
0.000102236

output$var_diff1_2 (var of difference of R2(y~x[,v1]) - R2(y~x[,v2]))
6.074567e-05

output$var_diff12_1 (var of difference of R2(y~x[,v1]+x[,v2]) - R2(y~x[,v1]))
1.184853e-05

output$var_diff12_2 (var of difference of R2(y~x[,v1]+x[,v2]) - R2(y~x[,v2]))
2.650564e-05

output$mean_diff12_1 (difference of R2(y~x[,v1]+x[,v2]) - R2(y~x[,v1]))
0.003048595

output$mean_diff12_2 (difference of R2(y~x[,v1]+x[,v2]) - R2(y~x[,v2]))
0.006845484

output$ratio (ratio = t1/(t1+t2))
0.6918768

output$ratio_var (variance of ratio, var(t1/(t1+t2))
0.1324076

output$enrich_p (p-value for testing the ratio significantly different
from the expectation (expl))
0.07321821

output$upper_ratio (upper limit of 95% CI for the ratio)
1.405079

output$lower_ratio (lower limit of 95% CI for the ratio)
-0.02132515

```

## Description

This function estimates  $\text{var}(t1/(t1+t2))$  where  $t1 = \text{beta1}^2$  and  $t2 = \text{beta2}^2$ , and  $\text{beta1}$  and  $\text{beta2}$  are regression coefficients from a multiple regression model, i.e.  $y = x1 \cdot \text{beta1} + x2 \cdot \text{beta2} + e$ , where  $y$ ,  $x1$  and  $x2$  are column-standardised (see Olkin and Finn 1995).  $y$  is  $N$  by  $1$  matrix having the dependent variable, and  $x1$  is  $N$  by  $1$  matrix having the  $i$ th explanatory variables.  $x2$  is  $N$  by  $1$  matrix having the  $j$ th explanatory variables.  $v1$  and  $v2$  indicates the  $i$ th and  $j$ th column in the data ( $v1$  or  $v2$  should be a single interger between  $1 - M$ , see Arguments below). Note that `r2_enrich` (above) and `r2_enrich_beta` is equivalent (identical p-value derived).

## Usage

```
r2_enrich_beta(dat, v1, v2, nv, expl)
```

## Arguments

<code>dat</code>	$N$ by $(M+1)$ matrix having variables in the order of <code>cbind(y,x)</code>
<code>nv</code>	sample size
<code>expl</code>	The expectation of the ratio (e.g. ratio of # SNPs in genomic partitioning)
<code>v1/v2</code>	These can be set as $v1=1$ and $v2=2$ , $v1=2$ and $v2=1$ , $v1=3$ and $v2=2$ , or any combination as long as the value is between $1 - M$

## References

Olkin, I. and J.D. Finn, Correlations redux. Psychological Bulletin, 1995. 118(1): p. 155.

## Examples

To get the test statistic for the ratio which is significantly different from the expectation.  
 $\text{var}(t1/(t1+t2))$ , where  $t1 = \text{beta1}^2$  and  $t2 = \text{beta2}^2$ .  
 $\text{beta1}$  and  $\text{beta2}$  are regression coefficients from a multiple regression model, i.e.  $y = x1 \cdot \text{beta1} + x2 \cdot \text{beta2} + e$ , where  $y$ ,  $x1$  and  $x2$  are column-standardised

```
dat=read.table("test_ukbb_enrichment_choles") (see example file)
nv=length(dat$V1)
v1=c(1)
v2=c(2)
expected_ratio=0.04
output=r2_enrich_beta(dat,v1,v2,nv,expected_ratio)
output
```

```
r2redux output
```

```
output$var1 (variance of t1)
7.072931e-05
```

```
output$var2 (variance of t2)
3.161929e-05
```

```
output$var1_2 (difference between t1 and t2)
0.000162113
```

```
output$beta1_sq (t1)
0.01118301
```

```

output$beta2_sq (t2)
0.004980285

output$cov (covariance between t1 and t2)
-2.988221e-05

output$ratio (ratio = t1/(t1+t2))
0.6918768

output$ratio_var (variance of ratio, var(t1/(t1+t2))
0.1324076

output$enrich_p (p-value for testing the ratio significantly different from
the expectation (exp1))
0.07321821

output$upper_ratio (upper limit of 95% CI for the ratio)
1.405079

output$lower_ratio (lower limit of 95% CI for the ratio)
-0.02132515

output$enrich_p2 (p-value for testing the difference between t1/exp and t2/exp)
0.1997805

output$mean_diff (difference between t1/exp and t2/exp)
0.2743874

output$var_diff (variance of difference, t1/exp - t2/exp)
0.04579649

output$upper_diff (upper limit of 95% CI for the mean difference)
0.6938296

output$lower_diff (lower limit of 95% CI for the mean difference)
-0.1450549

```

---

r2\_var

r2\_var function

---

## Description

This function estimates  $\text{var}(R^2(y \sim x[,v1]))$  where  $R^2$  is the R squared value of the model, where  $R^2$  is the R squared value of the model,  $y$  is  $N$  by  $1$  matrix having the dependent variable, and  $x$  is  $N$  by  $M$  matrix having  $M$  explanatory variables.  $v1$  indicates the  $i$ th column in the  $x$  matrix ( $v1$  can be multiple values between  $1 - M$ , see Arguments below)

## Usage

```
r2_var(dat, v1, nv)
```



**Arguments**

dat	N by (M+1) matrix having variables in the order of cbind(y,x)
v1	This can be set as v1=c(1), v1=c(1,2) or possibly with more values
nv	sample size

**Examples**

To get the test statistics for  $R^2(y \sim x[,v1])$

```
dat=read.table("test_ukbb_thresholds_scaled") (see example file)
nv=length(dat$V1)
v1=c(1)
output=r2_var(dat,v1,nv)
```

r2redux output

```
output$var (variance of R2)
0.0001437583
```

```
output$r2_based_p (P-value under the null hypothesis, i.e. R2=0)
1.213645e-10
```

```
output$mean_r2 (R2)
0.03836254
```

```
output$upper_r2 (upper limit of 95% CI for R2)
0.06435214
```

```
output$lower_r2 (lower limit of 95% CI for R2)
0.01763347
```

To get the test statistic for  $R^2(y \sim x[,v1]+x[,v2]+x[,v3])$

```
dat=read.table("test_ukbb_thresholds_scaled") (see example file)
nv=length(dat$V1)
v1=c(1,2,3)
outout=r2_var(dat,v1,nv)
output
```

r2redux output

```
output$var (variance of R2)
0.0001499374
```

```
output$r2_based_p (R2 based P-value)
7.461267e-11
```

```
output$mean_r2 (R2)
0.03917668
```

```
output$upper_r2 (upper limit of 95% CI for R2)
0.06538839
```

```
output$lower_r2 (lower limit of 95% CI for R2)
```

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*r2\_var*

0.01821657

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