Package 'r2redux'

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Title R2 statistic
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Description R2 statistic for signficance test.
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olkin_beta1_2 olkin_beta1_2 function

Description

This function derives Information matrix for beta 1^2 and beta 2^2 where beta 1 and 2 are regression coefficients from a multiple regression model, i.e. $y = x1^{\circ}$ beta $1 + x2^{\circ}$ beta 2 + e, where y, x1 and x2 are column-standardised, (i.e. in the context of correlation coefficients, see Olkin and Finn 1995).

Usage

```
olkin_beta1_2(omat, nv)
```

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Arguments

omat 3 by 3 matrix having the correlation coefficients between y, x1 and x2, i.e.

omat=cor(dat) where dat is N by 3 matrix having variables in the order of cbind

(y,x1,x2)

nv sample size

References

Olkin, I. and J.D. Finn, Correlations redux. Psychological Bulletin, 1995. 118(1): p. 155.

Examples

```
olkin_beta1_2 (omat,nv) (see example file)
dat=read.table("test_ukbb_thresholds_scaled") (see example files)
omat=cor(dat)[1:3,1:3]
omat
1.0000000 0.1958636 0.1970060
0.1958636 1.0000000 0.9981003
0.1970060 0.9981003 1.0000000
```

olkin_beta_inf

olkin_beta_inf function

Description

This function derives Information matrix for beta1 and beta2 where beta1 and 2 are regression coefficients from a multiple regression model, i.e. $y = x1 \cdot beta1 + x2 \cdot beta2 + e$, where y, x1 and x2 are column-standardised (see Olkin and Finn 1995).

Usage

```
olkin_beta_inf(omat, nv)
```

Arguments

omat 3 by 3 matrix having the correlation coefficients between y, x1 and x2, i.e.

omat=cor(dat) where dat is N by 3 matrix having variables in the order of cbind

(y,x1,x2)

nv sample size

References

Olkin, I. and J.D. Finn, Correlations redux. Psychological Bulletin, 1995. 118(1): p. 155.

```
olkin_beta_inf (omat,nv) (see example file)
dat=read.table("test_ukbb_thresholds_scaled") (see example files)
omat=cor(dat)[1:3,1:3]
omat
1.0000000 0.1958636 0.1970060
0.1958636 1.0000000 0.9981003
0.1970060 0.9981003 1.0000000
```

 $r2_diff$ 3

r2_diff	r2_diff function		
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Description

This function estimates $var(R2(y\sim x[,v1]) - R2(y\sim x[,v2]))$ where R2 is the R squared value of the model, y is N by 1 matrix having the dependent variable, and x is N by M matrix having M explanatory variables. v1 or v2 indicates the ith column in the x matrix (v1 or v2 can be multiple values between 1 - M, see Arguments below)

Usage

```
r2_diff(dat, v1, v2, nv)
```

Arguments

dat	N by $(M+1)$ matrix having variables in the order of cbind (y,x)
v1	This can be set as $v1=c(1)$ or $v1=c(1,2)$
v2	This can be set as $v2=c(2)$, $v2=c(3)$, $v2=c(1,3)$ or $v2=c(3,4)$
nv	sample size

```
To get the test statistics for the difference between R2(y \sim x[,v1]) and R2(y \sim x[,v2]).
(here we define R2_1=R2(y \sim x[,v1])) and R2_2=R2(y \sim x[,v2])))
dat=read.table("test_ukbb_thresholds_scaled") (see example files)
nv=length(dat$V1)
v1=c(1)
v2=c(2)
output=r2_diff(dat,v1,v2,nv)
output
r2redux output
output$var1 (variance of R2_1)
0.0001437583
output$var2 (variance of R2_2)
0.0001452828
output$var_diff (variance of difference between R2_1 and R2_2)
5.678517e-07
\verb"output$r2\_based_p" (p-value for significant difference between R2\_1 and R2\_2)
0.5514562
outputmean\_diff (differences between R2_1 and R2_2)
-0.0004488044
output$upper_diff (upper limit of 95% CI for the difference)
0.001028172
```

r2_enrich

```
output$lower_diff (lower limit of 95% CI for the difference)
-0.001925781
To get the test statistics for the difference between R2(y \sim x[,v1]+x[,v2]) and R2(y \sim x[,v2]
(here R2_1=R2(y\sim x[,v1]+x[,v2]) and R2_2=R2(y\sim x[,v1]))
dat=read.table("test_ukbb_thresholds_scaled") (see example files)
nv=length(dat$V1)
v1=c(1,2)
v2=c(1)
output=r2_diff(dat,v1,v2,nv)
output
r2redux output
output$var1 (variance of R2_1)
0.0001475195
output$var2 (variance of R2_2)
0.0001437583
output$var_diff (variance of difference between R2_1 and R2_2)
2.321425e-06
output$r2_based_p (p-value for significant difference between R2_1 and R2_2)
0.4369177
output$mean_diff (differences between R2_1 and R2_2)
0.0006042383
output$upper_diff (upper limit of 95% CI for the difference)
0.004887989
output$lower_diff (lower limit of 95% CI for the difference)
-0.0005574975
```

r2_enrich

r2_enrich

Description

This function estimates var(t1/(t1+t2)) where $t1 = R2(y\sim x[,v1]+x[,v2]) - R2(y\sim x[,v1])$ and $t2 = R2(y\sim x[,v1]+x[,v2]) - R2(y\sim x[,v2])$ where R2 is the R squared value of the model, y is N by 1 matrix having the dependent variable, and x is N by M matrix having M explanatory variables. v1 or v2 indicates the ith column in the x matrix (v1 or v2 should be a single interger between 1 - M, see Arguments below)

Usage

```
r2_enrich(dat, v1, v2, nv, exp1)
```

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Arguments

N by (M+1) matrix having variables in the order of cbind(y,x)

nv sample size

exp1 The expectation of the ratio (e.g. # SNPs for the genomic region of interest/total # SNPs in genomic partitioning)

v1/v2 These can be set as v1=1 and v2=2, v1=2 and v2=1, v1=3 and v2=2, or any combination as long as the value is between 1 - M

Examples

0.1324076

```
To get test statistics for the ratio, i.e. t1/(t1+t2).
t1 = R2(y \sim x[,v1] + x[,v2]) - R2(y \sim x[,v1])) and
t2 = R2(y \sim x[, v1] + x[, v2]) - R2(y \sim x[, v2]))
(here we define R2_1=R2(y \sim x[,v1]), R2_2=R2(y \sim x[,v2]), R2_12=R2(y \sim x[,v1]+x[,v2])
dat=read.table("test_ukbb_enrichment_choles") (see example file)
nv=length(dat$V1)
v1=c(1)
v2=c(2)
expected_ratio=0.04 (# SNPs for the regulatory/total # SNPs)
output=r2_enrich(dat,v1,v2,nv,expected_ratio)
output
r2redux output
output$var1 (variance of R2_1)
8.758455e-05
output$var2 (variance of R2_2)
7.36385e-05
output$var12 (variance of R2_12)
0.000102236
\verb"output$var\_diff1\_2" (var of difference of R2(y~x[,v1]) - R2(y~x[,v2])))" \\
6.074567e-05
\texttt{output\$var\_diff12\_1} \ (\texttt{var} \ \texttt{of} \ \texttt{difference} \ \texttt{of} \ \texttt{R2}(\texttt{y} \sim \texttt{x}[\texttt{,v1}] + \texttt{x}[\texttt{,v2}]) \ - \ \texttt{R2}(\texttt{y} \sim \texttt{x}[\texttt{,v1}]))))
1.184853e-05
2.650564e-05
output\mbox{mean\_diff}12_1 (difference of R2(y \sim x[,v1] + x[,v2]) - R2(y \sim x[,v1])))
0.003048595
0.006845484
output$ratio (ratio = t1/(t1+t2))
0.6918768
output$ratio_var (variance of ratio, var(t1/(t1+t2))
```

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```
output$enrich_p (p-value for testing the ratio significantly different from the expectation (exp1))
0.07321821

output$upper_ratio (upper limit of 95% CI for the ratio)
1.405079

output$lower_ratio (lower limit of 95% CI for the ratio)
-0.02132515
```

```
r2_enrich_beta r2_enrich_beta
```

Description

This function estimates var(t1/(t1+t2)) where $t1 = beta1^2$ and $t2 = beta2^2$, and beta1 and 2 are regression coefficients from a multiple regression model, i.e. $y = x1 \cdot beta1 + x2 \cdot beta2 + e$, where y, x1 and x2 are column-standardised (see Olkin and Finn 1995). y is N by 1 matrix having the dependent variable, and x1 is N by 1 matrix having the ith explanatory variables. x2 is N by 1 matrix having the jth explanatory variables. v1 and v2 indicates the ith and jth column in the data (v1 or v2 should be a single interger between 1 - M, see Arguments below). Note that r2_enrich (above) and r2_enrich_beta is equivalent (identical p-value derived).

Usage

```
r2_enrich_beta(dat, v1, v2, nv, exp1)
```

Arguments

dat	N by (M+1) matrix having variables in the order of cbind(y,x)
nv	sample size
exp1	The expectation of the ratio (e.g. ratio of # SNPs in genomic partitioning)
v1/v2	These can be set as v1=1 and v2=2, v1=2 and v2=1, v1=3 and v2=2, or any combination as long as the value is between 1 - M

References

Olkin, I. and J.D. Finn, Correlations redux. Psychological Bulletin, 1995. 118(1): p. 155.

```
To get the test statistic for the ratio which is significantly different from the expectation. var(t1/(t1+t2)), \text{ where } t1 = beta1^2 \text{ and } t2 = beta2^2. beta1 and beta2 are regression coefficients from a multiple regression model, i.e. y = x1 \cdot beta1 + x2 \cdot beta2 + e, where y, x1 and x2 are column-standardised dat=read.table("test_ukbb_enrichment_choles") (see example file) v = c(1) v = c(1) v = c(2) expected_ratio=0.04
```

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```
output=r2_enrich_beta(dat,v1,v2,nv,expected_ratio)
output
r2redux output
output$var1 (variance of t1)
7.072931e-05
output$var2 (variance of t2)
3.161929e-05
output$var1_2 (difference between t1 and t2)
0.000162113
output$beta1_sq (t1)
0.01118301
output$beta2_sq (t2)
0.004980285
output$cov (covariance between t1 and t2)
-2.988221e-05
output$ratio (ratio = t1/(t1+t2_2))
0.6918768
output\rown var(t1/(t1+t2))
0.1324076
output$enrich_p (p-value for testing the ratio significantly different from
the expectation (expl))
0.07321821
output$upper_ratio (upper limit of 95% CI for the ratio)
output$lower_ratio (lower limit of 95% CI for the ratio)
-0.02132515
```

r2_var

*r*2_*var function*

Description

This function estimates $var(R2(y\sim x[,v1]))$ where R2 is the R squared value of the model, where R2 is the R squared value of the model, y is N by 1 matrix having the dependent variable, and x is N by M matrix having M explanatory variables. v1 indicates the ith column in the x matrix (v1 can be multiple values between 1 - M, see Arguments below)

Usage

```
r2_var(dat, v1, nv)
```

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Arguments

dat N by (M+1) matrix having variables in the order of cbind(y,x) v1 This can be set as v1=c(1), v1=c(1,2) or possibly with more values nv sample size

```
To get the test statistics for R2(y\sim x[,v1])
dat=read.table("test_ukbb_thresholds_scaled") (see example file)
nv=length(dat$V1)
v1=c(1)
output=r2_var(dat,v1,nv)
r2redux output
output$var (variance of R2)
0.0001437583
output$r2\_based\_p (P-value under the null hypothesis, i.e. R2=0)
1.213645e-10
output$mean_r2 (R2)
0.03836254
output$upper_r2 (upper limit of 95% CI for R2)
0.06435214
output$lower_r2 (lower limit of 95% CI for R2)
0.01763347
To get the test statistic for R2(y\sim x[,v1]+x[,v2]+x[,v3])
dat=read.table("test_ukbb_thresholds_scaled") (see example file)
nv=length(dat$V1)
v1=c(1,2,3) ##1=R2(y\sim x[,v1]+x[,v2]+x[,v3])
outout=r2_var(dat,v1,nv)
output
r2redux output
output$var (variance of R2)
0.0001499374
output$r2_based_p (R2 based P-value)
7.461267e-11
output$mean_r2 (R2)
0.03917668
output$upper_r2 (upper limit of 95% CI for R2)
0.06538839
output$lower_r2 (lower limit of 95% CI for R2)
```

r2_var

0.01821657

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