Package 'r2redux'

August 9, 2023

C ,
Title R2 Statistic
Version 1.0.14
Description R2 statistic for significance test. Variance and covariance of R2 values used to assess the 95% CI and p-value of the R2 difference.
License GPL (>= 3)
<pre>URL https://github.com/mommy003/r2redux</pre>
Encoding UTF-8
RoxygenNote 7.1.2
NeedsCompilation no
Depends R (>= 2.10)
LazyData true
Suggests testthat (>= 3.0.0)
Config/testthat/edition 3
Author Hong Lee [aut, cph], Moksedul Momin [aut, cre, cph]
Maintainer Moksedul Momin < cvasu.momin@gmail.com>
Repository CRAN
Date/Publication 2023-08-09 08:50:02 UTC
Date/1 ubilcation 2025-00-07 00.50.02 01C
R topics documented:
cc_trf
dat1
dat2
olkin12_13
olkin12_3
olkin12_34
olkin1_2
olkin_beta1_2

cc_trf

	olkin_beta_inf .	 		 				 									8
	olkin_beta_ratio	 		 				 									9
	r2_beta_var	 		 				 									10
	$r2_diff \dots$	 		 				 									12
	r2_enrich_beta	 		 				 									15
	r2_var	 		 				 									18
	$r_diff . \ . \ . \ .$	 		 				 									20
Index																	23

cc_trf

 $cc_trffunction$

Description

This function transforms the predictive ability (R2) and its standard error (se) between the observed scale and liability scale

Usage

```
cc_trf(R2, se, K, P)
```

Arguments

R2	R2 or coefficient of determination on the observed or liability scale
se	Standard error of R2
K	Population prevalence
Р	The ratio of cases in the study samples

Value

This function will transform the R2 and its s.e between observed scale and liability scale.Output from the command is the lists of outcomes.

R21	Transformed R2 on the liability scale
sel	Transformed se on the liability scale
R20	Transformed R2 on the observed scale
se0	Transformed se on the observed scale

References

Lee, S. H., Goddard, M. E., Wray, N. R., and Visscher, P. M. A better coefficient of determination for genetic profile analysis. Genetic epidemiology, (2012). 36(3): p. 214-224.

dat1 3

Examples

```
#To get the transformed R2
output=cc_trf(0.06, 0.002, 0.05, 0.05)
output

#output$R21 (transformed R2 on the liability scale)
#0.2679337

#output$sel (transformed se on the liability scale)
#0.008931123

#output$R20 (transformed R2 on the observed scale)
#0.01343616

#output$se0 (transformed se on the observed scale)
#0.000447872
```

dat1

Phenotypes and 10 sets of PGSs

Description

A dataset containing phenotypes and multiple PGSs estimated from 10 sets of SNPs according to GWAS p-value thresholds

Usage

dat1

Format

A data frame with 1000 rows and 11 variables:

- V1 Phenotype, value
- **V2** PGS1, for p value threshold <=1
- **V3** PGS2, for p value threshold <=0.5
- V4 PGS3, for p value threshold <=0.4
- V5 PGS4, for p value threshold <=0.3
- **V6** PGS5, for p value threshold <=0.2
- V7 PGS6, for p value threshold <=0.1
- V8 PGS7, for p value threshold <=0.05
- **V9** PGS8, for p value threshold <=0.01
- V10 PGS9, for p value threshold <=0.001
- V11 PGS10, for p value threshold <=0.0001

0lkin12_1

dat2

Phenotypes and 2 sets of PGSs

Description

A dataset containing phenotypes and 2 sets of PGSs estimated from 2 sets of SNPs from regulatory and non-regulatory genomic regions

Usage

dat2

Format

A data frame with 1000 rows and 3 variables:

V1 Phenotype

V2 PGS1, regulatory region

V3 PGS2, non-regulatory region

olkin12_1

olkin12_1 function

Description

```
olkin12_1 function
```

Usage

```
olkin12_1(omat, nv)
```

Arguments

omat 3 by 3 matrix having the correlation coefficients between y, x1 and x2, i.e.

omat=cor(dat) where dat is N by 3 matrix having variables in the order of cbind

(y,x1,x2)

nv Sample size

Value

This function will be used as source code

olkin12_13 5

olkin12_13

 $olkin12_13$ function

Description

olkin12_13 function

Usage

```
olkin12_13(omat, nv)
```

Arguments

omat 3 by 3 matrix having the correlation coefficients between y, x1 and x2, i.e.

omat=cor(dat) where dat is N by 3 matrix having variables in the order of cbind

(y,x1,x2)

nv Sample size

Value

This function will be used as source code

olkin12_3

olkin12_3 function

Description

olkin12_3 function

Usage

```
olkin12_3(omat, nv)
```

Arguments

omat 3 by 3 matrix having the correlation coefficients between y, x1 and x2, i.e.

omat=cor(dat) where dat is N by 3 matrix having variables in the order of cbind

(y,x1,x2)

nv Sample size

Value

This function will be used as source code

6 olkin1_2

olkin12_34

 $olkin12_34$ function

Description

olkin12_34 function

Usage

```
olkin12_34(omat, nv)
```

Arguments

omat 3 by 3 matrix having the correlation coefficients between y, x1 and x2, i.e.

omat=cor(dat) where dat is N by 3 matrix having variables in the order of cbind

(y,x1,x2)

nv Sample size

Value

This function will be used as source code

olkin1_2

 $olkin1_2$ function

Description

olkin1_2 function

Usage

```
olkin1_2(omat, nv)
```

Arguments

omat 3 by 3 matrix having the correlation coefficients between y, x1 and x2, i.e.

omat=cor(dat) where dat is N by 3 matrix having variables in the order of cbind

(y,x1,x2)

nv Sample size

Value

This function will be used as source code

olkin_beta1_2

OINIII DELAI Z OINIII DEIAI ZIANCIION	olkin_beta1_2	olkin_beta1_2 function
---------------------------------------	---------------	------------------------

Description

This function derives Information matrix for beta 1^2 and beta 2^2 where beta 1 and 2 are regression coefficients from a multiple regression model, i.e. y = x1 * beta 1 + x2 * beta 2 + e, where y, x1 and x2 are column-standardised, (i.e. in the context of correlation coefficients, see Olkin and Finn 1995).

Usage

```
olkin_beta1_2(omat, nv)
```

Arguments

omat 3 by 3 matrix having the correlation coefficients between y, x1 and x2, i.e.

omat=cor(dat) where dat is N by 3 matrix having variables in the order of cbind

(y,x1,x2)

nv Sample size

Value

This function will give information (variance-covariance) matrix of beta1^2 and beta2^2. To get information (variance-covariance) matrix of beta1^2 and beta2^2. Where beta1 and beta2 are regression coefficients from a multiple regression model. The outputs are listed as follows.

info 2x2 information (variance-covariance) matrix

var1 Variance of beta1_2 var2 Variance of beta2_2

var1_2 Variance of difference between beta1_2 and beta2_2

References

Olkin, I. and Finn, J.D. Correlations redux. Psychological Bulletin, 1995. 118(1): p. 155.

```
#To get information (variance-covariance) matrix of beta1_2 and beta2_2 where #beta1 and 2 are regression coefficients from a multiple regression model. dat=dat1 omat=cor(dat)[1:3,1:3] #omat #1.0000000 0.1958636 0.1970060 #0.1958636 1.0000000 0.9981003 #0.1970060 0.9981003 1.0000000
```

8 olkin_beta_inf

```
nv=length(dat$V1)
output=olkin_beta1_2(omat,nv)
output

#output$info (2x2 information (variance-covariance) matrix)
#0.04146276 0.08158261
#0.08158261 0.16111124

#output$var1 (variance of beta1_2)
#0.04146276

#output$var2 (variance of beta2_2)
#0.1611112

#output$var1_2 (variance of difference between beta1_2 and beta2_2)
#0.03940878
```

olkin_beta_inf

olkin_beta_inf function

Description

This function derives Information matrix for beta1 and beta2 where beta1 and 2 are regression coefficients from a multiple regression model, i.e. y = x1 * beta1 + x2 * beta2 + e, where y, x1 and x2 are column-standardised (see Olkin and Finn 1995).

Usage

```
olkin_beta_inf(omat, nv)
```

Arguments

omat 3 by 3 matrix having the correlation coefficients between y, x1 and x2, i.e.

omat=cor(dat) where dat is N by 3 matrix having variables in the order of cbind

(y,x1,x2)

nv Sample size

Value

This function will generate information (variance-covariance) matrix of beta1 and beta2. The outputs are listed as follows.

info 2x2 information (variance-covariance) matrix

var1 Variance of beta1 var2 Variance of beta2

var1_2 Variance of difference between beta1 and beta2

olkin_beta_ratio 9

References

Olkin, I. and Finn, J.D. Correlations redux. Psychological Bulletin, 1995. 118(1): p. 155.

Examples

```
\mbox{\#To get information (variance-covariance) matrix of beta1 and beta2 where}
#beta1 and 2 are regression coefficients from a multiple regression model.
omat=cor(dat)[1:3,1:3]
#omat
#1.0000000 0.1958636 0.1970060
#0.1958636 1.0000000 0.9981003
#0.1970060 0.9981003 1.0000000
nv=length(dat$V1)
output=olkin_beta_inf(omat,nv)
output
#output$info (2x2 information (variance-covariance) matrix)
#0.2531406 -0.2526212
#-0.2526212 0.2530269
#output$var1 (variance of beta1)
#0.2531406
#output$var2 (variance of beta2)
#0.2530269
#output$var1_2 (variance of difference between beta1 and beta2)
#1.01141
```

olkin_beta_ratio

olkin_beta_ratio function

Description

This function derives variance of beta $1^2 / R^2$ where beta 1 and 2 are regression coefficients from a multiple regression model, i.e. y = x1 * beta 1 + x2 * beta 2 + e, where y, x1 and x2 are column-standardised (see Olkin and Finn 1995).

Usage

```
olkin_beta_ratio(omat, nv)
```

Arguments

omat 3 by 3 matrix having the correlation coefficients between y, x1 and x2, i.e.

omat=cor(dat) where dat is N by 3 matrix having variables in the order of cbind

(y,x1,x2)

nv sampel size

10 r2_beta_var

Value

This function will generate the variance of the proportion, i.e. beta1_2/R^2. The outputs are listed as follows.

```
ratio_var Variance of ratio
```

References

Olkin, I. and Finn, J.D. Correlations redux. Psychological Bulletin, 1995. 118(1): p. 155.

Examples

```
#To get information (variance-covariance) matrix of beta1 and beta2 where
#beta1 and 2 are regression coefficients from a multiple regression model.
dat=dat2
omat=cor(dat)[1:3,1:3]
#omat
#1.0000000 0.1497007 0.136431
#0.1497007 1.00000000 0.622790
#0.1364310 0.6227900 1.0000000

nv=length(dat$V1)
output=olkin_beta_ratio(omat,nv)
output

#r2redux output

#output$ratio_var (Variance of ratio)
#0.08042288
```

r2_beta_var

r2_beta_var

Description

This function estimates $var(beta1^2)$ and $(beta2^2)$, and beta1 and 2 are regression coefficients from a multiple regression model, i.e. y = x1 * beta1 + x2 * beta2 + e, y, x1 and x2 are column-standardised (see Olkin and Finn 1995). y is y is y 1 matrix having the dependent variable, y 1 is y 1 matrix having the ith explanatory variable. y 2 is y 3 having the jth explanatory variable. y 3 and y 2 indicates the ith and jth column in the data (y 1 or y 2 should be a single interger between 1 - y 4, see Arguments below).

Usage

```
r2_beta_var(dat, v1, v2, nv)
```

r2_beta_var

Arguments

dat	N by $(M+1)$ matrix having variables in the order of $cbind(y,x)$
v1	This can be set as $v1=1,\ v1=2,\ v1=3$ or any value between 1 - M based on combination
v2	This can be set as $v2=1$, $v2=2$, $v2=3$, or any value between 1 - M based on combination
nv	Sample size

Value

This function will estiamte the variance of beta 1^2 and beta 2^2 , and the covariance between beta 1^2 and beta 2^2 , i.e. the information matrix of squared regression coefficients. beta 1 and beta 2 are regression coefficients from a multiple regression model, i.e. y = x1 * beta 1 + x2 * beta 2 + e, where y, x1 and x2 are column-standardised. The outputs are listed as follows.

beta1_sq	beta1_sq
beta2_sq	beta2_sq
var1	Variance of beta1_sq
var2	Variance of beta2_sq
var1_2	Variance of difference between beta1_sq and beta2_sq
cov	Covariance between beta1_sq and beta2_sq
upper_beta1_sq	upper limit of 95% CI for beta1_sq
<pre>lower_beta1_sq</pre>	lower limit of 95% CI for beta1_sq
upper_beta2_sq	upper limit of 95% CI for beta2_sq
lower_beta2_sq	lower limit of 95% CI for beta2 sq

References

Olkin, I. and Finn, J.D. Correlations redux. Psychological Bulletin, 1995. 118(1): p. 155.

```
#To get the 95% CI of beta1_sq and beta2_sq
#beta1 and beta2 are regression coefficients from a multiple regression model,
#i.e. y = x1 * beta1 + x2 * beta2 +e, where y, x1 and x2 are column-standardised.

dat=dat2
nv=length(dat$V1)
v1=c(1)
v2=c(2)
output=r2_beta_var(dat,v1,v2,nv)
output
#r2redux output
#output$beta1_sq (beta1_sq)
#0.01118301
```

r2_diff

```
#output$beta2_sq (beta2_sq)
#0.004980285
#output$var1 (variance of beta1_sq)
#7.072931e-05
#output$var2 (variance of beta2_sq)
#3.161929e-05
#output$var1_2 (variance of difference between beta1_sq and beta2_sq)
#0.000162113
#output$cov (covariance between beta1_sq and beta2_sq)
#-2.988221e-05
#output$upper_beta1_sq (upper limit of 95% CI for beta1_sq)
#0.03037793
#output$lower_beta1_sq (lower limit of 95% CI for beta1_sq)
#-0.00123582
#output$upper_beta2_sq (upper limit of 95% CI for beta2_sq)
#0.02490076
#output$lower_beta2_sq (lower limit of 95% CI for beta2_sq)
#-0.005127546
```

r2_diff

r2_diff function

Description

This function estimates $var(R2(y\sim x[,v1]) - R2(y\sim x[,v2]))$ where R2 is the R squared value of the model, y is N by 1 matrix having the dependent variable, and x is N by M matrix having M explanatory variables. v1 or v2 indicates the ith column in the x matrix (v1 or v2 can be multiple values between 1 - M, see Arguments below)

Usage

```
r2_diff(dat, v1, v2, nv)
```

Arguments

dat	N by $(M+1)$ matrix having variables in the order of cbind (y,x)
v1	This can be set as $v1=c(1)$ or $v1=c(1,2)$
v2	This can be set as $v2=c(2)$, $v2=c(3)$, $v2=c(1,3)$ or $v2=c(3,4)$
nv	Sample size

 $r2_diff$

Value

This function will estimate significant difference between two PGS (either dependent or independent and joint or single). To get the test statistics for the difference between $R2(y\sim x[,v1])$ and $R2(y\sim x[,v2])$. (here we define $R2_1=R2(y\sim x[,v1])$) and $R2_2=R2(y\sim x[,v2])$). The outputs are listed as follows.

```
rsq1
                 R2_1
                 R2 2
rsq2
                  Variance of R2_1
var1
                  variance of R2_2
var2
                  Variance of difference between R2_1 and R2_2
var_diff
r2_based_p
                  two tailed P-value for significant difference between R2_1 and R2_2
r2_based_p_one_tail
                  one tailed P-value for significant difference
mean_diff
                 Differences between R2_1 and R2_2
                  Upper limit of 95% CI for the difference
upper_diff
                 Lower limit of 95% CI for the difference
lower_diff
```

```
#To get the test statistics for the difference between R2(y^{x}[,1]) and
\#R2(y^x[,2]). (here we define R2_1=R2(y^x[,1])) and R2_2=R2(y^x[,2]))
dat=dat1
nv=length(dat$V1)
v1=c(1)
v2=c(2)
output=r2_diff(dat,v1,v2,nv)
output
#r2redux output
#output$rsq1 (R2_1)
#0.03836254
#output$rsq2 (R2_2)
#0.03881135
#output$var1 (variance of R2_1)
#0.0001436128
#output$var2 (variance of R2_2)
#0.0001451358
#output$var_diff (variance of difference between R2_1 and R2_2)
#5.678517e-07
#output$r2_based_p (two tailed p-value for significant difference)
```

r2_diff

```
#0.5514562
#output$r2_based_p_one_tail(one tailed p-value for significant difference)
#output$mean_diff (differences between R2_1 and R2_2)
#-0.0004488044
#output$upper_diff (upper limit of 95% CI for the difference)
#0.001028172
#output$lower_diff (lower limit of 95% CI for the difference)
#-0.001925781
#To get the test statistics for the difference between R2(y^x[,1]+x[,2]) and
\#R2(y^x[,2]). (here R2_1=R2(y^x[,1]+x[,2]) and R2_2=R2(y^x[,1]))
dat=dat1
nv=length(dat$V1)
v1=c(1,2)
v2=c(1)
output=r2_diff(dat,v1,v2,nv)
#r2redux output
#output$rsq1 (R2_1)
#0.03896678
#output$rsq2 (R2_2)
#0.03836254
#output$var1 (variance of R2_1)
#0.0001473686
#output$var2 (variance of R2_2)
#0.0001436128
#output$var_diff (variance of difference between R2_1 and R2_2)
#2.321425e-06
#output$r2_based_p (p-value for significant difference between R2_1 and R2_2)
#0.4366883
#output$mean_diff (differences between R2_1 and R2_2)
#0.0006042383
#output$upper_diff (upper limit of 95% CI for the difference)
#0.00488788
#output$lower_diff (lower limit of 95% CI for the difference)
#-0.0005576171
```

r2_enrich_beta

```
##When faced with multiple predictors, exceeding two in number,
#as seen in the scenario:
y = PRS vs. y = PRS+any_cov1+any_cov2+...+any_covN
#A more streamlined approach can be adopted by consolidating the various
#predictors (any_cov1, any_cov2, ..., any_covN) into a single predictor,
#following this procedure in R:
#R
\#mod \leftarrow lm(y \sim PRS + any_cov1 + any_cov2 + ... + any_covN)
#merged_predictor <- cbind(any_cov1, any_cov2, ..., any_covN)</pre>
#%*% mod$coefficients[3:(2+N)]
#Subsequently, the comparison can be equivalently expressed as:
#y = PRS vs. y = PRS + merged_predictor
#This comparison can be simply achieved using the r2_diff function,
#as exemplified in the second example above.
##In another scenario:
#y = any_cov1 + any_cov2 + ... + any_covN vs.
y = PRS + any_cov1 + any_cov2 + ... + any_covN
#The same approach applies as
mod <- lm(y \sim PRS + any_cov1 + any_cov2 + ... + any_covN)
#merged_predictor <- cbind(any_cov1, any_cov2, ..., any_covN)</pre>
#%*% mod$coefficients[3:(2+N)]
#the comparison can be equivalently expressed as:
#y = merged_predictor vs. y = PRS + merged_predictor
##For this scenario, alternatively, the outcome variable (y) can be preadjusted
#with covariate(s), following the procedure in R:
\#mod <- lm(y \sim any\_cov1 + any\_cov2 + ... + any\_covN)
#y_adj=scale(mod$residuals)
#then, the comparative significance test can be approximated by using
#the following model y_adj = PRS
```

r2_enrich_beta

r2_enrich_beta

Description

This function estimates var(beta1 2 /R 2), beta1 and R 2 are regression coefficient and the coefficient of determination from a multiple regression model, i.e. y = x1 * beta1 + x2 * beta2 + e, where y, x1 and x2 are column-standardised (see Olkin and Finn 1995). y is N by 1 matrix having the

16 r2_enrich_beta

dependent variable, and x1 is N by 1 matrix having the ith explanatory variables. x2 is N by 1 matrix having the jth explanatory variables. v1 and v2 indicates the ith and jth column in the data (v1 or v2 should be a single interger between 1 - M, see Arguments below).

Usage

```
r2_enrich_beta(dat, v1, v2, nv, exp1)
```

Arguments

dat	N by $(M+1)$ matrix having variables in the order of cbind (y,x)
v1	These can be set as $v1=1$, $v1=2$, $v1=3$ or any value between 1 - M based on combination
v2	These can be set as v2=1, v2=2, v2=3, or any value between 1 - M based on combination
nv	Sample size
exp1	The expectation of the ratio (e.g. ratio of # SNPs in genomic partitioning)

Value

This function will estimate var(beta1 2 /R 2), beta1 and R 2 are regression coefficient and the coefficient of determination from a multiple regression model, i.e. y = x1 * beta1 + x2 * beta2 + e, where y, x1 and x2 are column-standardised. The outputs are listed as follows.

```
beta1_sq
                  beta1_sq
beta2_sq
                  beta2_sq
ratio1
                  beta1_sq/R^2
                  beta2 sq/R^2
ratio2
ratio_var1
                  variance of ratio 1
ratio var2
                  variance of ratio 2
upper_ratio1
                  upper limit of 95% CI for ratio 1
lower_ratio1
                  lower limit of 95% CI for ratio 1
upper_ratio2
                  upper limit of 95% CI for ratio 2
lower_ratio2
                  lower limit of 95% CI for ratio 2
                  two tailed P-value for beta1_sq/R^2 is significantly different from exp1
enrich_p1
enrich_p1_one_tail
                  one tailed P-value for beta1_sq/R^2 is significantly different from exp1
enrich_p2
                  P-value for beta2_sq/R2 is significantly different from (1-exp1)
enrich_p2_one_tail
                  one tailed P-value for beta2_sq/R2 is significantly different from (1-exp1)
```

References

Olkin, I. and Finn, J.D. Correlations redux. Psychological Bulletin, 1995. 118(1): p. 155.

r2_enrich_beta

```
#To get the test statistic for the ratio which is significantly
#different from the expectation, this function estiamtes
#var (beta1^2/R^2), where
#beta1^2 and R^2 are regression coefficients and the
#coefficient of dterminationfrom a multiple regression model,
#i.e. y = x1 * beta1 + x2 * beta2 + e, where y, x1 and x2 are
#column-standardised.
dat=dat2
nv=length(dat$V1)
v1=c(1)
v2=c(2)
expected_ratio=0.04
output=r2_enrich_beta(dat,v1,v2,nv,expected_ratio)
output
#r2redux output
#output$beta1_sq (beta1_sq)
#0.01118301
#output$beta2_sq (beta2_sq)
#0.004980285
#output$ratio1 (beta1_sq/R^2)
#0.4392572
#output$ratio2 (beta2_sq/R^2)
#0.1956205
#output$ratio_var1 (variance of ratio 1)
#0.08042288
#output$ratio_var2 (variance of ratio 2)
#0.0431134
#output$upper_ratio1 (upper limit of 95% CI for ratio 1)
#0.9950922
#output$lower_ratio1 (lower limit of 95% CI for ratio 1)
#-0.1165778
#output$upper_ratio2 upper limit of 95% CI for ratio 2)
#0.6025904
#output$lower_ratio2 (lower limit of 95% CI for ratio 2)
#-0.2113493
#output$enrich_p1 (two tailed P-value for beta1_sq/R^2 is
#significantly different from exp1)
#0.1591692
```

18 r2_var

```
#output$enrich_p1_one_tail (one tailed P-value for beta1_sq/R^2
#is significantly different from exp1)
#0.07958459

#output$enrich_p2 (two tailed P-value for beta2_sq/R2 is
#significantly different from (1-exp1))
#0.000232035

#output$enrich_p2_one_tail (one tailed P-value for beta2_sq/R2
#is significantly different from (1-exp1))
#0.0001160175
```

r2_var

r2_var function

Description

This function estimates $var(R2(y\sim x[,v1]))$ where R2 is the R squared value of the model, where R2 is the R squared value of the model, y is N by 1 matrix having the dependent variable, and x is N by M matrix having M explanatory variables. v1 indicates the ith column in the x matrix (v1 can be multiple values between 1 - M, see Arguments below)

Usage

```
r2_var(dat, v1, nv)
```

Arguments

dat	N by $(M+1)$ matrix having variables in the order of cbind (y,x)
v1	This can be set as $v1=c(1)$, $v1=c(1,2)$ or possibly with more values
nv	Sample size

Value

This function will test the null hypothesis for R2. To get the test statistics for $R2(y\sim x[,v1])$. The outputs are listed as follows.

rsq	R2
var	Variance of R2
r2_based_p	P-value under the null hypothesis, i.e. R2=0
upper_r2	Upper limit of 95% CI for R2
lower_r2	Lower limit of 95% CI for R2

r2_var 19

```
#To get the test statistics for R2(y^x[,1])
dat=dat1
nv=length(dat$V1)
v1=c(1)
output=r2_var(dat,v1,nv)
output
#r2redux output
#output$rsq (R2)
#0.03836254
#output$var (variance of R2)
#0.0001436128
#output$r2_based_p (P-value under the null hypothesis, i.e. R2=0)
#1.188162e-10
#output$upper_r2 (upper limit of 95% CI for R2)
#0.06433782
#output$lower_r2 (lower limit of 95% CI for R2)
#0.01764252
#To get the test statistic for R2(y^x[,1]+x[,2]+x[,3])
dat=dat1
nv=length(dat$V1)
v1=c(1,2,3)
r2_var(dat,v1,nv)
#r2redux output
#output$rsq (R2)
#0.03836254
#output$var (variance of R2)
#0.0001436128
#output$r2_based_p (R2 based P-value)
#1.188162e-10
#output$upper_r2 (upper limit of 95% CI for R2)
#0.06433782
#output$lower_r2 (lower limit of 95% CI for R2)
#0.0176425
```

 r_{diff}

```
#When comparing two independent sets of PGSs
#Let's assume dat1$V1 and dat2$V2 are independent for this example
#(e.g. male PGS vs. female PGS)
nv=length(dat1$V1)
v1=c(1)
output1=r2_var(dat1,v1,nv)
nv=length(dat2$V1)
v1=c(1)
output2=r2_var(dat2,v1,nv)
#To get the difference between two independent sets of PGSs
r2_diff_independent=abs(output1$rsq-output2$rsq)
#To get the variance of the difference between two independent sets of PGSs
var_r2_diff_independent= output1$var+output2$var
sd_r2_diff_independent=sqrt(var_r2_diff_independent)
#To get p-value (following eq. 15 in the paper)
chi=r2_diff_independent^2/var_r2_diff_independent
p_value=pchisq(chi,1,lower.tail=FALSE)
#to get 95% CI (following eq. 15 in the paper)
uci = r2\_diff\_independent + 1.96*sd\_r2\_diff\_independent
lci=r2\_diff\_independent-1.96*sd\_r2\_diff\_independent
```

r_diff

r_diff function

Description

This function estimates $var(R(y\sim x[,v1]) - R(y\sim x[,v2]))$ where R is the correlation between y and x, y is N by 1 matrix having the dependent variable, and x is N by M matrix having M explanatory variables. v1 or v2 indicates the ith column in the x matrix (v1 or v2 can be multiple values between 1 - M, see Arguments below)

Usage

```
r_diff(dat, v1, v2, nv)
```

Arguments

dat	N by $(M+1)$ matrix having variables in the order of $cbind(y,x)$
v1	This can be set as $v1=c(1)$ or $v1=c(1,2)$
v2	This can be set as $v2=c(2)$, $v2=c(3)$, $v2=c(1,3)$ or $v2=c(3,4)$
nv	Sample size

r_diff 21

Value

This function will estimate significant difference between two PGS (either dependent or independent and joint or single). To get the test statistics for the difference between $R(y\sim x[,v1])$ and $R(y\sim x[,v2])$. (here we define $R_1=R(y\sim x[,v1])$) and $R_2=R(y\sim x[,v2])$). The outputs are listed as follows.

r1 R_1 R 2 r2 Variance of R_1 var1 variance of R 2 var2 Variance of difference between R_1 and R_2 var_diff r2_based_p P-value for significant difference between R_1 and R_2 for two tailed test r_based_p_one_tail P-value for significant difference between R 1 and R 2 for one tailed test mean_diff Differences between R_1 and R_2 Upper limit of 95% CI for the difference upper_diff Lower limit of 95% CI for the difference lower_diff

```
#To get the test statistics for the difference between R(y^x[,1]) and
\#R(y^x[,2]). (here we define R_1=R(y^x[,1])) and R_2=R(y^x[,2]))
dat=dat1
nv=length(dat$V1)
v1=c(1)
v2=c(2)
output=r_diff(dat,v1,v2,nv)
output
#r2redux output
#output$r1 (R_1)
#0.1958636
#output$r2 (R_2)
#0.197006
#output$var1 (variance of R_1)
#0.0009247466
#output$var2 (variance of R_1)
#0.0001451358
#output$var_diff (variance of difference between R_1 and R_2)
#3.65286e-06
#output$r_based_p (two tailed p-value for significant difference between R_1 and R_2)
```

 r_{diff}

```
#0.5500319
#output$r_based_p_one_tail (one tailed p-value
#0.2750159
#output$mean_diff
#-0.001142375 (differences between R2_1 and R2_2)
#output$upper_diff (upper limit of 95% CI for the difference)
#0.002603666
#output$lower_diff (lower limit of 95% CI for the difference)
#-0.004888417
#To get the test statistics for the difference between R(y^x[,1]+[,2]) and
\#R(y^x[,2]). (here R_1=R(y^x[,1]+x[,2]) and R_2=R(y^x[,1]))
nv=length(dat$V1)
v1=c(1,2)
v2=c(2)
output=r_diff(dat,v1,v2,nv)
output
#output$r1
#0.1974001
#output$r2
#0.197006
#output$var1
#0.0009235848
#output$var2
#0.0009238836
#output$var_diff
#3.837451e-06
#output$r2_based_p
#0.8405593
#output$mean_diff
#0.0003940961
#output$upper_diff
#0.004233621
#output$lower_diff
#-0.003445429
```

Index

* R2	* in
cc_trf, 2	olkin_beta1_2,7
r2_diff, 12	olkin_beta_inf, 8
r2_var, 18	olkin_beta_ratio,9
r_diff, 20	* liability
* Transformation	cc_trf, 2
cc_trf, 2	* matrix
* and	olkin_beta1_2,7
cc_trf,2	olkin_beta_inf, 8
* a	olkin_beta_ratio,9
r2_beta_var, 10	r2_diff, 12
r2_enrich_beta, 15	r2_var, 18
* beta^2	r_diff, 20
r2_beta_var, 10	* multiple
r2_enrich_beta, 15	r2_beta_var, 10
* between	r2_enrich_beta, 15
cc_trf, 2	* observed
r2_enrich_beta, 15	cc_trf, 2
* context	* of
olkin_beta1_2,7	cc_trf, 2
olkin_beta_inf, 8	olkin_beta1_2,7
olkin_beta_ratio, 9	olkin_beta_inf, 8
* correlation	olkin_beta_ratio, 9
olkin_beta1_2,7	r2_beta_var, 10
olkin_beta_inf, 8	r2_enrich_beta, 15
olkin_beta_ratio,9	* ratio
* datasets	r2_enrich_beta, 15
dat1,3	* regression
dat2,4	r2_beta_var, 10
* from	r2_enrich_beta, 15
r2_beta_var, 10	* scale
r2_enrich_beta, 15	cc_trf, 2
* information	* source
olkin_beta1_2,7	olkin12_1, 4
olkin_beta_inf, 8	olkin12_13,5
olkin_beta_ratio, 9	olkin12_13, 5
r2_diff, 12	olkin12_34, 6
r2_var, 18	olkin1_2, 6
r_diff, 20	* the
1_4111, 20	T LIIC

24 INDEX

```
olkin_beta1_2,7
    olkin_beta_inf, 8
    olkin_beta_ratio, 9
* variance
    r2_beta_var, 10
    r2_diff, 12
    r2_enrich_beta, 15
    r2_var, 18
    r_diff, 20
cc_trf, 2
dat1, 3
dat2, 4
olkin12_1, 4
olkin12_13, 5
olkin12_3, 5
olkin12_34,6
olkin1_2, 6
olkin_beta1_2, 7
olkin_beta_inf, 8
olkin_beta_ratio,9
r2_beta_var, 10
r2_diff, 12
r2_enrich_beta, 15
r2_var, 18
r_diff, 20
```