

# Zero and Category Theory

In category theory, a category  $C$  consists of:

Objects: which, in the context of "Zero," we could interpret as 'states' of existence.

Morphisms (arrows): which could be interpreted as 'transitions' between states. Each morphism has a domain (source) and codomain (target).

Composition: For any three objects

$A, B, C$ , if there is a morphism from

$A$  to  $B$  and a morphism from  $B$  to  $C$ , then there must be a composite morphism from  $A$  to  $C$ . This could correspond to the idea that one transition followed by another yields a resultant transition.

Associativity: If there are morphisms from  $A$  to  $B$ ,  $B$  to  $C$ , and  $C$  to  $D$ , then the composition of the morphisms is associative:

$(f \circ g) \circ h = f \circ (g \circ h)$ . In "Zero," this would require that the composition of transitions is associative.

Identity: For every object  $A$ , there is an identity morphism  $A$  that composes with any morphism

$f: A \rightarrow B$  or

$g: C \rightarrow A$  to give  $f$  or  $g$  respectively. This suggests that there must be a 'non-transition' or a 'null transition' for each state that essentially leaves the state unchanged.

Now, considering the axioms and definitions of "Zero," if we interpret states as objects and transitions as morphisms, we can make a correspondence to the first two requirements of a category. However, the axioms of "Zero" don't provide explicit structures for composition, associativity, and identity.

For the conjecture to be true, the following conditions must be met in "Zero":

Composition: There must be a well-defined rule for composing transitions, which would be our morphisms.

Associativity: The rule for composing transitions must be associative.

Identity: Each state must have an associated 'identity transition' that, when composed with any other transition, results in that original transition.

If "Zero" inherently supports these conditions, then the conjecture could be true. However, as "Zero" stands with the information given, we cannot confirm the conjecture without additional postulates that define composition, associativity, and identity in the context of transitions and states. Therefore, as it is currently presented, the conjecture is not necessarily true—it requires further elaboration of the theory to align with the structure of a category in category theory.