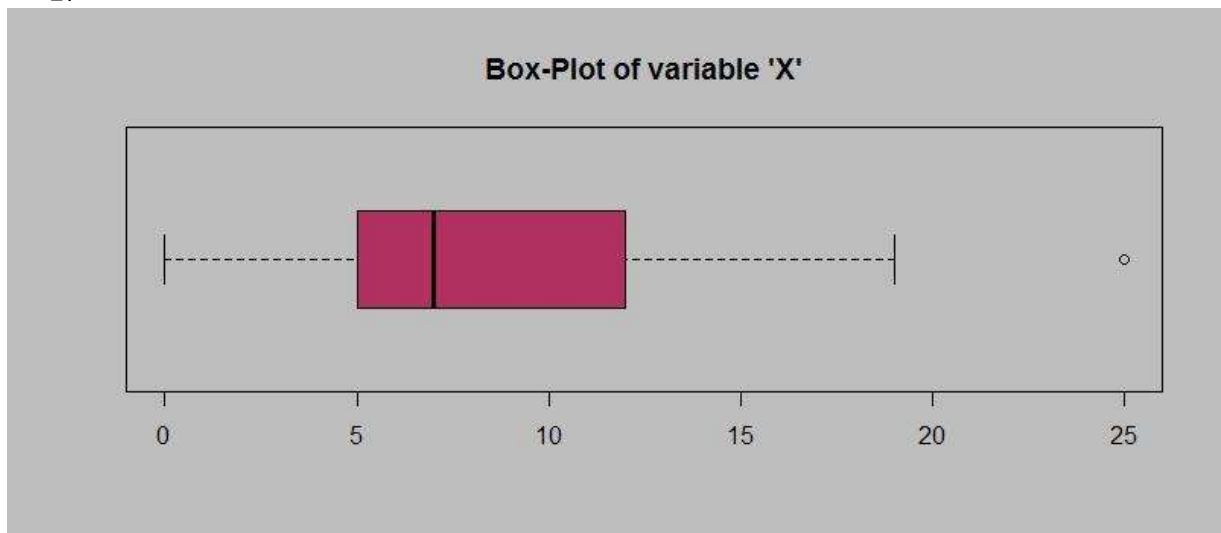


Topics: Descriptive Statistics and Probability

1. Look at the data given below. Plot the data, find the outliers and find out μ, σ, σ^2

Name of company	Measure X
Allied Signal	24.23%
Bankers Trust	25.53%
General Mills	25.41%
ITT Industries	24.14%
J.P.Morgan & Co.	29.62%
Lehman Brothers	28.25%
Marriott	25.81%
MCI	24.39%
Merrill Lynch	40.26%
Microsoft	32.95%
Morgan Stanley	91.36%
Sun Microsystems	25.99%
Travelers	39.42%
US Airways	26.71%
Warner-Lambert	35.00%

2.



Answer the following three questions based on the box-plot above.

- (i) What is inter-quartile range of this dataset? (please approximate the numbers) In one line, explain what this value implies .

ANS

Approximate inter quartile range is

The first quartile (Q1) = 5

The third quartile (Q3) = 12

INTER QUARTILE RANGE(IQR) = Q3 – Q1 = 12 – 5 = 7

Value implies

- (ii) What can we say about the skewness of this dataset?

ANS

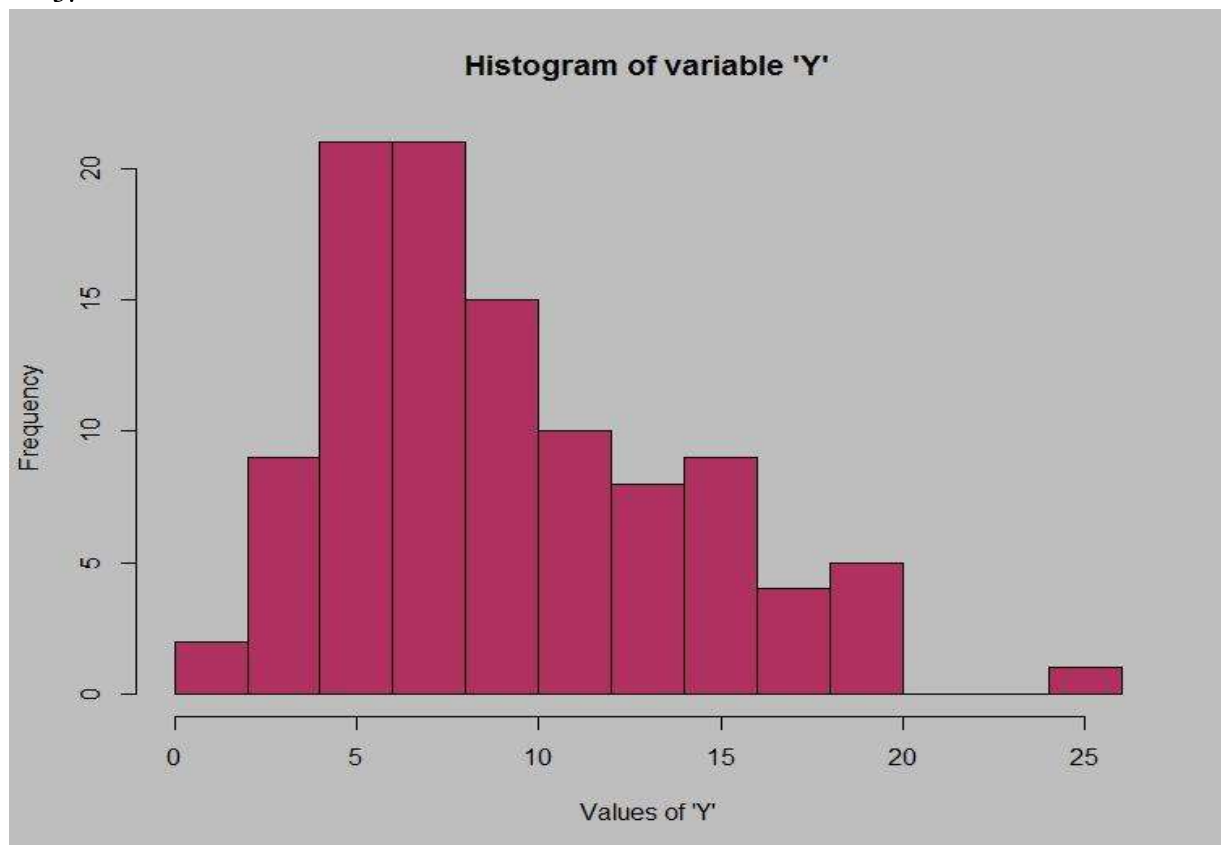
Positive skewness

- (iii) If it was found that the data point with the value 25 is actually 2.5, how would the new box-plot be affected?

ANS

There will not be any change in skewness; there may be a change in the box-plot but it will not affect the box plot

3.



Answer the following three questions based on the histogram above.

- (i) Where would the mode of this dataset lie?

ANS

Mode lies 4 to 10

- (ii) Comment on the skewness of the dataset.

ANS

Right skew because $\text{mode} > \text{median} > \text{mean}$

- (iii) Suppose that the above histogram and the box-plot in question 2 are plotted for the same dataset. Explain how these graphs complement each other in providing information about any dataset.

ANS

Both above graphs are a right skew

Both graphs' median will be the same

4. AT&T was running commercials in 1990 aimed at luring back customers who had switched to one of the other long-distance phone service providers. One such commercial shows a businessman trying to reach Phoenix and mistakenly getting Fiji, where a half-naked native on a beach responds incomprehensibly in Polynesian. When asked about this advertisement, AT&T admitted that the portrayed incident did not actually take place but added that this was an enactment of something that “could happen.” Suppose that one in 200 long-distance telephone calls is misdirected. What is the probability that at least one in five attempted telephone calls reaches the wrong number? (Assume independence of attempts.)

ANS

1 in 200 long distance is misdirected

Probability of success rate (= $199/200 = 0.995$

Probability of misdirected = $1/200 = 0.005$

Probability that at least one in five attempted

No of calls = 5

Probability = (Total no of probability of misdirected) / (Total no of probability)

Probability = $5 / 200 = 0.025$

5. Returns on a certain business venture, to the nearest \$1,000, are known to follow the following probability distribution

x	P(x)
-2,000	0.1
-1,000	0.1
0	0.2
1000	0.2
2000	0.3
3000	0.1

- (i) What is the most likely monetary outcome of the business venture?

ANS

The most monetary outcome of the business venture is 2000 and it have higher return ratio of 0.3

- (ii) Is the venture likely to be successful? Explain

ANS

Yes probability of $x > 0$ is higher than $x < 0$ so the venture will be having higher ratio of successful

- (iii) What is the long-term average earning of business ventures of this kind? Explain

ANS

The long-term average is Expected value = $\text{Sum}(X * P(X)) = 800\$$ which means on an average the returns will be + 800\$

- (iv) What is the good measure of the risk involved in a venture of this kind? Compute this measure

ANS

$$\begin{aligned}\text{Var}(X) &= E(X^2) - (E(X))^2 \\ &= 2800000 - 800^2 \\ &= 2160000\end{aligned}$$