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Select-based random access to variable-byte encodings

Jussi Timonen

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FACULTY OF SCIENCE

UNIVERSITY OF HELSINKI

Supervisor(s)

Prof. D.U. Mind, Dr. O. Why

Examiner(s)

Prof. D.U. Mind, Dr. O. Why

Contact information

P. O. Box 68 (Pietari Kalmin katu 5)

00014 University of Helsinki,Finland

Email address: info@cs.helsinki.fi

URL: http://www.cs.helsinki.fi/

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Contents

1 Introduction

Enormous datasets are a common case in today's applications. Compressing the datasets is beneficial, because they naturally decrease memory requirements but also are faster when compressed data is read from disk (Zobel and Moffat, 1995).

One of the leading methods of data compression is variable-length coding (Salomon, 2007), where frequent sequences of data are represented with shorter codewords. Because the sequences of data have different lengths when compressed, it is not trivial to determine the exact location of a certain element in the compressed data. If this is required, the usual data compression algorithms are inefficient. Fortunately this is not a requirement compression algorithms usually need to fulfill. However, random access of compressed data is useful in compressed data structures. It saves storage space, bandwidth and increases the likelihood of data already being in cache (Scholer et al., 2002). In most compression methods, the only way to do this is to decompress data from the beginning.

A variable-byte encoding based integer compression method with constant time random access was first introduced by (Brisaboa et al., 2009). They used clever block reorganizing and *rank* data structure to achieve random access. Their solution is currently the only published solution for the problem and it has been widely adopted.

An alternative solution with *select* data structure is proposed and explained in detail later in this thesis. Comparison to *rank* implementation by Brisaboa et al is shown with different implementations of *rank* and *select* and several different data sets. Proposed method does not use data reorganizing, but rather capitalizes on the assumption that data is encoded the same way it is in the source. Because variable-byte encoding does not assign new codewords to data when encoding, data can be read straight from the memory and reassembling the integer from blocks is not needed.

Rank method is superior when dataset contains mostly small integers. With larger integers, multiple *rank* calls are needed and *select* method performs better. Additionally, the proposed *select* method offers quick access to next or previous element.

2 Variable-bytes

Variable-byte (VB) encoding (Williams and Zobel, 1999) is a method for compressing unsigned integers via omitting leading zero bits that would be present in a longer fixed width word. In normal data sets, VB encoding loses in compression performance to generic algorithms like Huffman encoding or Lempel-Ziv encoding, but is generally faster to decode (Brisaboa et al., 2009) and sometimes preferred due to its simplicity.

A good data set for VB encoding is a list of mostly small integers with a need to support larger ones. A search engine may use an inverted index of words in documents. For each word, a list of document IDs where the word appears is stored. It may also store locations of the word in document for advanced search purposes. Usually these lists are preprocessed and stored as an inverted index or gaps, storing the difference to previous number instead of the actual number (Manning et al., 2008). Common words have a lot of entries in these lists, but because of gap storing the integers are small. In contrast, rare words have only a few entries but the integers stored are larger. These lists are excellent data sets for VB encoding.

Variable-byte encoding originates from and is used in MIDI music file format (MIDI Manufacturers Association and others, 1996) and several applications have a similar implementation of VB. Apache Lucene has vInt datatype. Wireless Application Protocol has a variable length unsigned integer uintvar, Google Protocol Buffers has a Base 128 Varint (Google, 2019), Microsoft .Net framework offers "7BitEncodedInt" in BinaryReader and BinaryWriter classes and IBM DB2 has a variable byte (Bhattacharjee et al., 2009).

Later, VB encoding was to be found efficient in compressing integer lists. It was first experimented as a tool for compressing inverted index lists of word locations in documents (Scholer et al., 2002). That yielded excellent records, and since then many different approaches have been introduced.

More recent studies have taken a look into the machine code level for VB and applied SIMD (Single instruction, multiple data) instructions to VB (Lemire et al., 2018; Plaisance et al., 2015). The bit operations in VB are simple and therefore modifying the code to use SIMD instructions is straightforward and the speed improvements are significant.

Elias Delta and Gamma codes (Elias, 1975) are popular encoding methods for foremen-

Original number	first block	second block	third block	fourth block
4	<u>1</u>0100			
17	<u>0</u>0001	<u>1</u>0001		
620	<u>0</u>1100	<u>0</u>0110	<u>1</u>0010	
60201	<u>1</u>1001	<u>0</u>0010	<u>0</u>1011	<u>1</u>1110

Table 2.1: VByte encoded integers, block size 4. Continuation bit underlined.

tioned data sets. Their encoding process assigns short bit array codes to small integers, which is why they outperform VB encoding on datasets with a lot of small integers (Williams and Zobel, 1999), such as inverted indexes (Anh and Moffat, 2005; Pibiri and Venturini, 2019). In this thesis, the compressable data sets will have the focus on slightly larger, unordered numbers.

2.1 VB encoding

VB encoding splits each integer into blocks of b bits and adds a continuation bit to the block to form chunks of length $1 + b$. The continuation bit is set to 1 only on the block containing the least significant bits of the integer. This information is used in decoding to signal if the current integer continues in the next chunk.

For example, the standard bit representation of an unsigned integer 42 is `00000000 00101010`. When split to blocks of length 4, it becomes `0000 0000 0010 1010`. The empty blocks are removed and then continuation bits are added. 1 is added to the least significant block and 0 to the other block, resulting in `00010 11010`. A pseudo code with block length 4 is shown in Figure 2.1. Prepend adds an element to the beginning of the list and extend adds all the elements of the second list to the end of the first list.

Smaller block length can yield a better compression rate at the cost of more bit manipulation, while bigger block lenghts need less bit manipulation and offer less effective compression. On the other hand, bigger block length means a smaller percentage of added continuation bits. Generally block length of 7 has been used because it tends to perform well on average and handling chunks as bytes is convenient (Manning et al., 2008).

```
function VBEncodeNumber(n)
    bytes ← list
    while true do
        prepend(bytes,n mod 128)
        if n < 128 then
            break
        n ← n div 128
    bytes[len(bytes)-1] += 128
    return bytes

function VBEncode(numbers)
    bytestream ← list
    for each n ∈ numbers do
        bytes ← VBEncodeNumber(n)
        extend(bytestream,bytes)
    return bytestream
```

Figure 2.1: VByte encoding

2.2 VB decoding

VB decoding reverses the encoding steps: encoded chunks are read until a chunk with 1 as continuation bit is found. Continuation bits are removed from all the chunks and the blocks are concatenated to form the original integer. A pseudo code implementation of VB decoding with block length of 7 is shown in Figure 2.2. Append adds an element to the end of the list. If block length is changed, additional bit operation steps when reading the data may be needed.

As how the encoding example ended, the encoded message was `00010` `11010` with block length of 4 and the goal is to decode a 16 bit unsigned integer. The block from the first chunk is extracted and added to n, making $n =$`10` (bit representation of 2). The continuation bit was 0 in this chunk, which means the encoded integer continues to the next block. A bitwise shift to the left equal to block length is applied to n, changing $n =$`100000` (bit representation of 32). Then the chunk reading process is repeated. The block of the next chunk is added to n, making $n =$`101010` (bit representation of 42). The continuation bit of this chunk is 1, which means the decoding for this number is complete.

function VBDECODE(*bytestream*)

    numbers ← list

    $n \leftarrow 0$

    for each $b \in bytestream$ **do**

        if $b < 128$ **then**

            $n \leftarrow 128 \times n + b$

        else

            $n \leftarrow 128 \times n + b$ - 128

            APPEND(numbers,n)

            $n \leftarrow 0$

    return numbers

Figure 2.2: VByte decoding

3 Directly addressable codes

The ability to handle large amounts of data fast is one of the key challenges in the field of search engines. Compressed data structures are applied to fit the data into cache, memory or even hard drive. Direct access to any element in a compressed list or array is one of the usual requirements in compressed data structures. It is not natively possible to decode the i-th element in variable-byte compression algorithms, because the position of the element in the compressed list depends on the length of the preceding compressed data. Direct access is achievable with supporting data structures. A naive solution is to store the location of each element to an array, but it adds a very large overhead which removes the benefit of compression.

3.1 Rank and Select

Rank and select are two succinct data structure operations which operate on a bit array B. $Rank_1$(B, i) gives the sum of 1 bits between B[0] and B[i] and $select_1$(B, i) gives the index of i-th 1 bit in B. Both operations can be implemented to work in constant time (Gog et al., 2014). To use rank or select in indexing, the set 1 bits in B should reflect to the element locations in the encoded data.

For most compression algorithms, this requires B to be created in addition to the existing data and the length of B usually has to be close to the length of the data, because encoded element lenghts vary. VB encoding has several advantages with search and rank: the data is compressed in blocks of equal length which significantly shrinks the length of B. Moreover the bit array C formed from the continuation bits already stores the locations of items and works as the needed indexing array. In this case, $rank_1$(C, i) would give the sum of end blocks up to i-th index and $select_1$(C, i) would give the location of the ending block of i-th compressed element.

Table 3.1: Memory requirements of SDSL rank and select data structures

Structure	Extra size taken
Rank	25% of bit array
Rankv5	6.25% of bit array
Select	8-12% of bit array

3.2   Rank and Select implementation

The rank and select implementations used in this thesis are from C++ library 'SDSL-lite' by (Gog et al., 2014). The library has an implementation of a bit array and several implementations of both rank and select to support the bit array. Also a few useful functions were used during the implementation phase. Table 3.1 has *rank* and *select* size requirements of implementations used in this experiment. Both rank implementations have a constant space requirement over the bit array, while select's needed size depends on the number of 1's in the data.

The data structure of rank has two layers. First layer is the superblock array. For every 512th bit, the number of 1's from the beginning of the array is stored to the superblock array. The second layer is the relative count block. It stores a relative count of 1's for every 64th bit. To calculate rank(i), the superblock index is s = i/512 and relative count block index is r = i-s / 64, both being integer divisions. Then number of 1 bits from index r to i are calculated. All three values added together add up to rank(i). Rankv5 is a lighter structure: it's superblock size is 2048 and relative counts are taken for every 384th bit. This causes the final bit calculation to be more costly, but reduces memory requirement to a quarter.

Select data structure works similarly to rank. The index location of every 4096th set bit is stored in the superblock and location of every 64th set bit is stored relative to the superblock. With similar calculations, the location of closest 64th set bit is calculated and then bit array is iterated until required amount of bits is reached.

In both cases, one function call always gets a value from the superblock and then from the superblock's relative block. The only differiating factor is the manual bit count from relative block's index to wanted index. This is at most the size of one relative block and thus both of the functions work in constant time (González et al., 2005).

3.3   DAC via rank

Directly addressable codes in VB was first introduced by (Brisaboa et al., 2009). In their solution, the chunks are sorted in separate arrays by their significance. For each integer, the block of the least significant chunk is stored in the first array A_1, and its bit to the first bit array B_1. Then if the number was stored in multiple chunks, the block of the next chunk is stored to A_2 and the bit to B_2 and so on. After the data is set, rank data structure is built for each bit array. The data structure is implicit and does not require additional space apart from the *rank* structure. Figure 3.1 contains a visualization of the data structure.

The chunk array. $C_{i,j} = B_{i,j} : A_{i,j}$

$\mathbf{C} =$	$C_{1,2}C_{1,1}$	$C_{2,1}$	$C_{3,3}C_{3,2}C_{3,1}$	$C_{4,2}C_{4,1}$	$C_{5,1}...$

$A_1 =$	$A_{1,1}$	$A_{2,1}$	$A_{3,1}$	$A_{4,1}$	$A_{5,1}$	...
$B_1 =$	0	1	0	0	1	...

$A_1 =$	$A_{1,2}$	$A_{3,2}$	$A_{4,2}$	...
$B_2 =$	1	0	1	...

$A_3 =$	$A_{3,3}$	...
$B_3 =$	1	...

Figure 3.1: Data structure by Brisaboa et al., visualized

To decode an element from index i, first block is fetched from $A_1[\text{i}]$. Because each encoded element is composed of at least one block, the first block is obtainable via straight indexing. With small integers, this is all that is required. If the data has a lot of small integers, the *rank* method has a huge advantage. In addition, the block length of this method can change within different array levels. This opens a possibility for further optimization.

However if the element was stored in multiple blocks, the index of the next block in A_2 is obtained from $i \leftarrow rank_0(A_1, \text{i})$. $Rank_0$ returns the number of zeros in the bit array preceding index i. In other words, the number of elements before i that continue to the next array. This in turn means that i now has the index of the element's next block in

array A_2. This process is repeated until the i-th bit of the bit array of current level is set. The resulting integer is constructed from the blocks of the fetched chunks. A pseudo code example of DAC with *rank* is shown in Figure 3.2 with block length of 8.

$index \leftarrow$ wanted index
$A \leftarrow$ block arrays
$B \leftarrow$ continuation bit arrays
$level \leftarrow 0$
$number \leftarrow 0$
while $B[level][index] = 0$ **do**
    $block \leftarrow A[level][index]$
    $number \leftarrow number \ll 8$
    $number \leftarrow number + block$
    $index \leftarrow \text{RANK}(B[level], index)$
    $level \leftarrow level + 1$
$block \leftarrow A[level][index]$
$number \leftarrow number \ll 8$
$number \leftarrow number + block$

Figure 3.2: Example pseudo code of DAC with rank by Brisaboa et al.

4 DAC with select query

Using $select_1$ on the continuation bit array to achieve direct access is more intuitive than using $rank_1$. The element locations are already marked with 1's in B and a single $select_1$ query gets the desired starting point, while the forementioned version (Brisaboa et al., 2009) used one $rank$ query for each chunk beyond the first. Minimizing the amount of $select$ and $rank$ queries is important. They run in constant time but their impact is huge, because rest of the VB decoding consists of a few bit operations.

To use $select_1$ with VB, continuation bits need to be separated from chunks to their own bit array and a $select_1$ structure built over it. Because every compressed element has 1 only on it's last block, $Select_1$(i) returns the location of the end byte of i-th element. Therefore the start of j-th element in the block array is at block $b_s = select_1$(j-1) + 1. Implementation was simplified by using only block sizes 4 and 8 to prevent block splitting between bytes.

Unlike the standard VB encoding, the continuation bits are removed from the chunks and stored in their own array, which leaves the blocks in their own array. This allows the compressed number to be read from the memory block and removes the need of block concatenation. The data in blocks is written into memory as they appear in the original integer, so that when reading a word from the block byte array, the bits and bytes are already in correct order.

For example, let the integer bit length be 32 and the original data be compressed to 5 blocks of 4 bits. First, the byte location of the first block is needed. $Select_1$(i) gets the index location of needed block. Because the block length differs from byte length, the the two values need to be calculated. First, the starting byte location s needs to be calculated $(s = select_1(i) \times 4) \div 8$, the latter operand being the integer division. Second, the first block might not be at the start of the byte s. This is why offset $o = (select_1(i) \times 4) \bmod 8$ is needed (in the example case, o equals to either 0 or 4). Then a 32-bit word w is read from memory from byte location s.

At this point, w contains the wanted bits, but also has extra bits from the previous and next compressed integers. If offset was not zero, there are trailing o bits in w from the previous integer. These can be conveniently removed by bit-shifting w right for o bits. Then a pre-calculated bitmask (0xFFFFF in this case) is applied and w contains the

requested value. Because most systems are able to read memory only from byte addresses, there is a corner case where the value is stored in too many bytes for a word. In this setup, this happens if compressed length was 8 blocks and offset was 4. Then another step of reading another byte and storing the remaining bits to w is required. This is entirely avoidable if integer length is constrained. In this case maximum integer length would be 28 bits.

The most intuitive way to calculate block length of i-th element is from $select_1(i+1)$ and subtract the previously calculated start block index. This however causes a second $select_1$ query, which is costly. A much faster option is to iterate forward in bit array until the next 1. Alternatively, the block length can be calculated by reading an integer from the bit array, aligning it's offset and counting the trailing zeros. Figure 4.1 contains an example of VB decoding with DAC with *select* and block size 8. Different block sizes need extra calculation to get the block location from the byte array. In the example, *CalculateLength* returns the length of the number in blocks and $ByteMask(k)$ returns a bit mask for k bytes.

$i \leftarrow$ wanted index
$A \leftarrow$ block byte array
$B \leftarrow$ continuation bit array
$begin \leftarrow \textsc{Select}(index)$
$len \leftarrow \textsc{CalculateLength}(begin)$
$mask \leftarrow \textsc{ByteMask}(len)$
$word \leftarrow A[begin]$ ▷ read a word from the byte array
$word \leftarrow word \,\&\, mask$

Figure 4.1: Pseudo code of DAC with select with block length 8

Figure 4.2 portrays an example of the bit array and the block array. $Select_1(k-1)+1$ returns the index of the starting byte of ith compressed element. Length of the compressed element is obtainable e.g. via $select_1(k)$. Then a word is read from the block array, starting from block A_i. Because element length in this case is 3, blocks not belonging to the element are removed either with a bitmask or by double bit shifting, resulting in decoded k-th element.
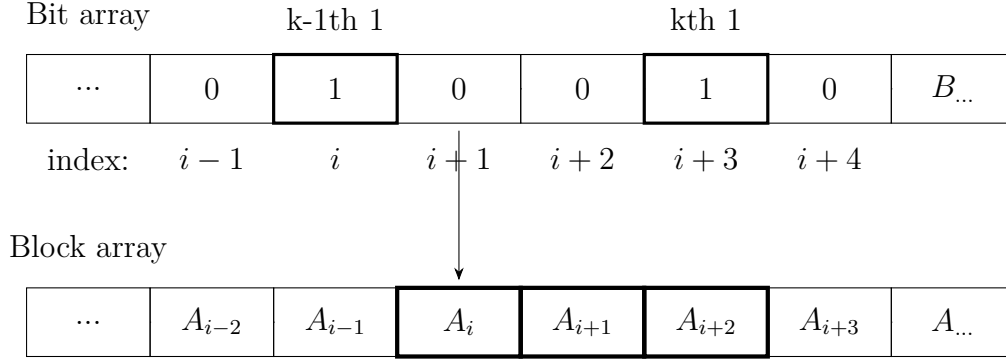
Figure 4.2: Data

4.1   Elias-Fano encoding

Direct access via select can also be implemented with Elias-Fano (TODO citation to Elias-Fano?), but the data has to be sorted. In Elias-Fano encoding, the data is at first split into low and high bits. Low bits, the k least significant bits, are stored to their own array. Direct access to the lower bits is trivial. The higher bits are gap-encoded and then encoded in unary. For example, [1,3,5,8,11] becomes [1,2,2,3,3] and then is encoded as unary bit array B = 0100100100010001. $Select_1$ has an interesting interaction with gap encoded unary arrays. $k = Select_1(B, i)$ returns the location of i-th 1 in B. Up to index k, the bit array has had i ones and $i - k$ zeros. The i corresponds to the number of compressed integers in B and every zero in the array means an increment of 1 in the numbers. In other words, $i - k$ equals to the integer at position i before gap-encoding. Therefore $select_1(i)$ - i returns the original higher bit number. The split between bits is made to reduce the gap sizes. This approach can be further optimized by finding clusters in the integers and partitioning the indexes (Ottaviano and Venturini, 2014).

5 Sub-array access

After locating and decompressing one value from a compressed data structure, compressing the subsequent items gets a lot easier. Because the next compressed value is usually located next to the fetched in memory, locating the data is not needed. This is especially beneficial to the VByte decoding with *select* method, where calculating the start byte location takes majority of he runtime. In addition to this, the length of the next compressed integer is faster to calculate because already manipulated data in memory.

The shown *rank* method by Brisaboa et al. can also effectively decompress the next value but some modifications are needed. When fetching a longer subarray, the goal becomes to minimize *rank* calls. If an additional pointer array is stored during subarray decompression, only one *rank* call for each accessed block level is needed. This can be observed from Figure 3.1; the blocks of a subarray are located next to each other in different block levels.

- examples / visualizaton?

- TODO get results from this

6 Experimental results

The following experiments were run on a AMD Phenom(tm) II X6 1055T Processor@2.8Ghz with 64kB+64kB L1 cache, 512kB L2 cache, 6144kB L3 cache and 32GB of DDR3 1333MHz. The computer runs Ubuntu 14.04.4 (3.13.0-91-generic x86_64). The codes were compiled with `g++-7 -std=c++11 -DNDEBUG` and with libraries `-lsdsl -ldivsufsort -ldivsufsort64`.

Five different VB decoding algorithms were compared. The Bris-algorithms are from (Brisaboa et al., 2009). All algorithms are implemented using data structures and functions from the SDSL library (Gog et al., 2014). Each implementation is compressing and decoding uint64_t type integers.

- Bris4v5 - Bris implementation with block size 4, using rank support v5

- Bris8 - Bris implementation with block size 8, using rank support v

- Bris8v5 - Bris implementation with block size 8, using rank support v5

- Select4 - Proposed implementation with block size 4, using select support mcl

- Select8 - Proposed implementation with block size 8, using select support mcl

Four differently constructed datasets were used and three different sizes of dataset were used (5M, 50M, 500M).

- all - all integers randomly 1-4 bytes long

- twolarge - one eighth of integers 4 bytes long, one eighth 2 bytes long, rest 1 byte

- onelarge - one eighth of integers 2 bytes long, rest 4 bits or less

- onlysmall - all integers 4 bits or less

All implementations read the data set from a file and compress it to memory, randomize one million indexes and stored to an array. The times shown in Table 6.1 are times taken from looping through the index array and VB decoding the number in the index. Additionally, each run is iterated multiple times and an average of the runtimes is taken.

Table 6.1: Results in milliseconds, smaller is better.

	bris8	bris4	bris8v5	bris4v5	select8	select4
all (5M)	191.80	471.50	234.00	569.40	149.20	175.90
all (50M)	269.20	573.80	323.00	785.00	245.40	275.00
all (500M)	298.50	677.80	368.20	941.80	355.90	382.20
twolarge (5M)	96.70	275.50	110.70	329.00	125.60	151.90
twolarge (50M)	140.40	379.70	159.80	456.80	227.70	242.20
twolarge (500M)	168.20	441.00	191.50	584.70	330.20	341.00
onelarge (5M)	25.80	40.10	28.30	49.20	95.90	100.40
onelarge (50M)	49.80	91.30	50.90	105.70	212.70	213.20
onelarge (500M)	55.00	100.00	58.50	124.00	315.80	307.70
onlysmall (5M)	16.50	20.20	16.50	23.80	84.70	88.40
onlysmall (50M)	31.20	51.80	32.10	57.00	201.20	198.80
onlysmall (500M)	34.10	56.00	35.00	63.10	297.90	293.80

The results show that the proposed *select* method outperforms *rank* when the data set contains several integers that are encoded into more than one block. The difference is explained with how *rank* and *select* use the data structure. *Select* is always called once, while *rank* is called once for each block beyond the first. Figure 6.1 shows average times of one million *rank* and *select* calls with different average block lengths. The effect of multiple *rank* calls is visible, as is the single *select* call behavior.

The 8-bit versions tend to perform better than the 4-bit versions. This is because 8-bit version stores more data in one block and less block readings are required. However, 4bit versions achieve better compression in data sets containing small integers. Select versions do not depend as much on the block size, because all the blocks in the compressed element are read at the same time. Interestingly the 4-bit version of *select* performs better than the 8-bit version with some data sets, even though 4-bit version should execute at least the same commands as the 8-bit version in every scenario. This is most likely due to cache, because the stored data set is smaller in the 4-bit version.

In rank, the v5 version naturally has worse performance because more calculations are needed to locate the correct index. As a trade-off, it requires significantly less memory, as seen on Figure 3.1.

Figures 6.2 and 6.3 show memory size requirements for *rank* and *select* data structures. The data sets consist of 50 million 64-bit numbers and the compressed size is a sum of
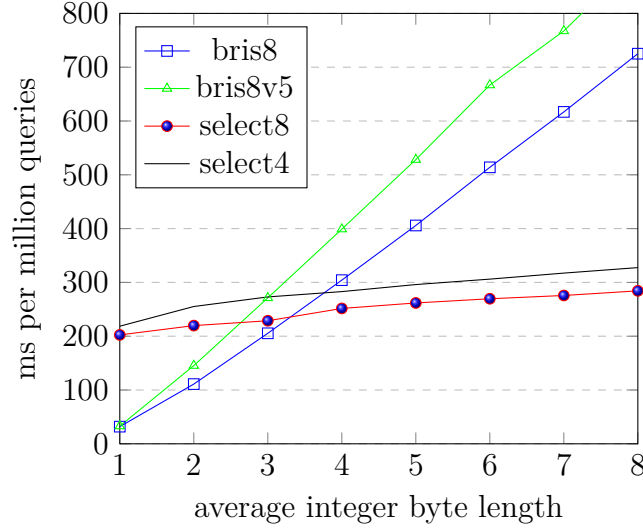
Figure 6.1: Rank and select performances

dataset	compressed size	bris8	bris8v5	select8
all	168.4MB	4.67MB	1.17MB	1.54MB
twolarge	112.4MB	3.12MB	781kB	1.48MB
onelarge	63.2MB	1.76MB	439kB	1.43MB
onlysmall	56.3MB	1.56MB	391kB	1.43MB

Table 6.2: Memory requirement for 50M 64-bit numbers 8bit blocks, smaller is better.

continuation bit array and the data blocks.

The static memory requirement of *select* is easily noticeable, as is the relation between the memory requirement of *rank* and the total number of blocks. Data structures in versions with smaller block size naturally take more space, but smaller block size allows a better data compression in some data sets and therefore a smaller total size. This can be seen when comparing the two forementioned figures: All 4-bit versions of the algorithms require more space than the 8-bit versions, but the compressed size of the data is significantly smaller in the bottom two data sets. The data structure memory usage for the bottom row is similar in both versions due to the fact that the continuation bit array is exactly the same.

- TODO figure out why 4bit crashes sometimes with 500M_all

- see how cache matters

- better dataset might be something with larger (like 60bit) numbers

dataset	compressed size	bris4	bris4v5	select4
all	177.7MB	7.65MB	1.91MB	1.63MB
twolarge	116.1MB	4.66MB	1.14MB	1.54MB
onelarge	42.5MB	2.12MB	531kB	1.44MB
onlysmall	31.3MB	1.56MB	391kB	1.43MB

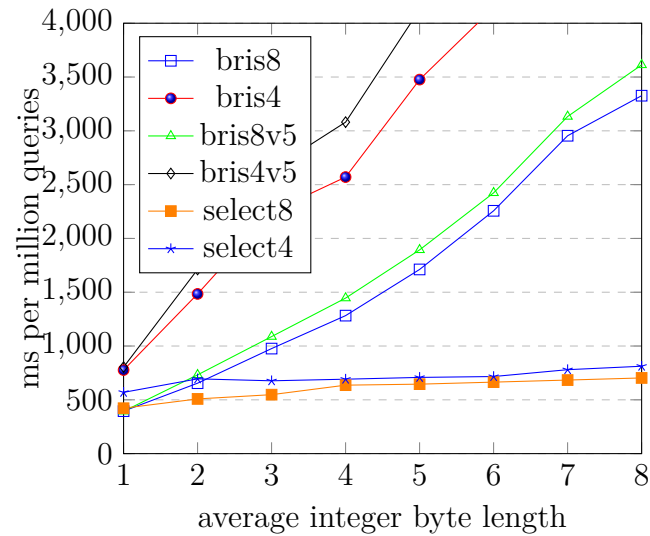**Table 6.3:** Memory requirement for 50M 64-bit numbers 4bit blocks, smaller is better.

Figure 6.2: Rank and select performances with subarray fetching

- subarray access

- bris has advantage of different size blocks (in different levels)

- figure out why data size matters

- do we need to support search()?

- *rank* vs rank? should formulas have a specific style?

7 Future work

There has already been a few successful attempts to decompress VB encoded integers with SIMD (Lemire et al., 2018; Plaisance et al., 2015). It is worthwhile to check if the presented approach benefits from SIMD. The data needs less manipulation because the data is already written as it is, but calculating the integer block lengths might benefit from SIMD.

Another improvement to VB encoding is to see whether the compressed numbers can be changed. This is trivial until the block length of the compressed number changes. Then an additional data structure or cache is needed and the supporting rank/select data structure needs to be recalculated.

8 Conclusions

It is good to conclude with a summary of findings. You can also use separate chapter for discussion and future work. These details you can negotiate with your supervisor.

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