

MSc thesis Computer Science

Select-based random access to variable-byte encodings

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February 26, 2020

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HELSINGIN YLIOPISTO – HELSINGFORS UNIVERSITET – UNIVERSITY OF HELSINKI

Tiedekunta — Fakultet — Faculty		Koulutusohjelma –	Utbildningsprogram — Study programme			
Faculty of Science		Computer Science				
Tekijä — Författare — Author						
Jussi Timonen						
Työn nimi — Arbetets titel — Title	Työn nimi — Arbetets titel — Title					
Select-based random access to variable-byte encodings						
Ohjaajat — Handledare — Supervisors						
Prof. D.U. Mind, Dr. O. Why						
Työn laji — Arbetets art — Level	Aika — Datum — Mo	onth and year	Sivumäärä — Sidoantal — Number of pages			
MSc thesis	February 26, 202	20	15 pages, 17 appendice pages			

Tiivistelmä — Referat — Abstract

Use this other language environment to write your abstract in another language if needed.

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 \rightarrow Text editing

Avainsanat — Nyckelord — Keywords

ulkoasu, tiivistelmä, lähdeluettelo

Säilytyspaikka — Förvaringsställe — Where deposited

Helsinki University Library

Muita tietoja — övriga uppgifter — Additional information

Algorithms specialisation line

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1 Introduction

Enormous datasets are a common case in today's applications. Compressing the datasets is beneficial, because they naturally decrease memory requirements but also are faster when compressed data is read from disk (Zobel and Moffat, 1995).

One of the leading methods of data compression is variable-length coding (Salomon, 2007), where frequent sequences of data are represented with shorter codewords. Because the sequences of data have different lengths when compressed, it is not trivial to determine the exact location of a certain element in the compressed data. If this is required, the usual data compression algorithms are inefficient. Fortunately this is not a requirement compression algorithms usually need to fulfill. However, random access of compressed data is useful in compressed data structures. It saves storage space, bandwith and increases the likelihood of data already being in cache (Scholer et al., 2002). In most compression methods, the only way to do this is to decompress data from the beginning.

A variable-byte encoding based integer compression method with fast random access was first introduced by (Brisaboa et al., 2009). They used clever block reorganizing and rank data structure to achieve random access. Their solution is currently the only published solution for the problem and it has been widely adopted.

An alternative solution with *select* data structure is shown later. (TODO: refer to results) –contributions?

2 Variable-byte encoding

Variable-byte (VB) encoding (Williams and Zobel, 1999) is a method for compressing integers via omitting leading zero bits that would be present in a longer fixed width word. In normal data sets, VB encoding loses in compression performance to generic algorithms like Huffman encoding or Lempel-Ziv encoding, but is generally faster to decode (Brisaboa et al., 2009) and sometimes preferred due to its simplicity. As later shown in Chapter 3, constant time random access is possible with VB encoding.

A good data set for VB encoding is a list of mostly small numbers with a need to support larger ones. A search engine may use an inverted index of words in documents. For each word, a list of document IDs where the word appears is stored. It may also store locations of the word in document for advanced search purposes. Usually these lists are preprocessed and stored as an inverted index or gaps, storing the difference to previous number instead of the actual number (Manning et al., 2008). Common words have a lot of entries in these lists, but because of gap storing the numbers are small. In contrast, rare words have only a few entries but the numbers stored are larger. These lists are excellent data sets for VB encoding.

Variable-byte encoding originates from and is used in MIDI music file (Association, 1996) and several applications have a similar implementation of VB. Apache Lucene has vInt datatype. Wireless Application Protocol has a variable length unsigned integer uintvar, Google Protocol Buffers has a Base 128 Varint (LLC, 2019), Microsoft .Net framework offers "7BitEncodedInt" in BinaryReader and BinaryWriter classes and IBM DB2 has a variable byte (Bhattacharjee et al., 2009).

Elias Delta and Gamma codes (Elias, 1975) are popular encoding methods for forementioned data sets. They assign short bit array codes to small numbers, which allows them to outperform VB encoding on small number datasets (Williams and Zobel, 1999). Elias Delta and Gamma codes can't support fast random access efficiently because of their changing code length.

VB encoding splits each integer into blocks of b bits and adds a continuation bit to the block to form chunks of length 1+b. The extra bit is set to 1 only on the block containing the least significant bits of the integer. This information is used in decoding to signal if next chunk continues the current integer. For example, let's assume b=4 and let

n=42 be a 16 bit unsigned integer. The standard 8-bit representation of n is 00000000 00101000. When split to blocks of b bits, it becomes 0000 0000 0010 1000. Empty blocks are omitted and continuation bits are added to the remaining blocks. The result is 00010 11000, which is the compressed data.

```
function VBENCODENUMBER(n)
   bytes \leftarrow list
   while true do
       PREPEND(bytes, n \mod 128)
       if n < 128 then
          break
       n \leftarrow n \text{ div } 128
   bytes[Len(bytes)-1] += 128
   return bytes
function VBENCODE(numbers)
   bytestream \leftarrow list
   for each n \in numbers do
       bytes \leftarrow VBENCODENUMBER(n)
       EXTEND(bytestream, bytes)
   return bytestream
      Figure 2.1: VByte encoding
```

Decoding is essentially just reversing the encoding steps: chunks are read until a chunk with 1 as continuation bit is found. Continuation bits are removed from all the chunks and the blocks are concatenated to form the original number. As in the previous example, b=4, encoded message is 00010–11000 and n=0. Block from the first chunk is extracted and added to n, making n=10. A bitwise shift to left equal to b is applied to n, changing n=100000. Then the block is extracted from the next chunk. This block is added n, making n=42. Because the previous continuous bit was 1, decoding this number has finished. An example implementation of encode and decode with block length of 7 is shown in Figure 2.1 and Figure 2.2.

Small lengths of c can yield better compression rate at the cost of more bit manipulation, while longer chunks need less bit manipulation and offer less effective compression. Generally block length of 7 has been used because it gives a good average and handling chunks as bytes is convenient (Manning et al., 2008).

```
function VBDECODE(bytestream)
numbers \leftarrow \text{list}
n \leftarrow 0
for each b \in bytestream do
if b < 128 then
n \leftarrow 128 \times n + b
else
n \leftarrow 128 \times n + b - 128
numbers.\text{append}(n)
n \leftarrow 0
return numbers
```

Figure 2.2: VByte decoding

VB encoding is a well known compression algorithm. It's origins date back to 1980's and the famous MIDI music file format. It stored some of the numbers in a "variable-length quantity" form, which was a 7-bit block VB structure (Association, 1996). Similar data types have existed for example in Apache Lucene (as vInt) and IBM DB2 database (as Variable Byte). Later, VB encoding was found efficient in compressing integer lists. It was first experimented in compressing inverted index lists of word locations in documents (Scholer et al., 2002). That yielded excellent records, and since then many different approaches have been introduced.

Modern studies have looked into machine code for VB and applied SIMD (Single instruction, multiple data) architecture to VB (Lemire et al., 2018; Plaisance et al., 2015). The bit operations in VB are simple and therefore modifying the code to use SIMD instructions is straightforward and the speed improvements are significant.

TODO: might need 1-2 more chapters

3 Directly addressable codes

Ability to handle large amounts of data fast is one of the key challenges in the field of search engines. Compressed data structures are applied to fit the data into cache, memory or even hard drive. Direct access to any element is one of the usual requirements in compressed data strutures. It is not natively possible to decode the i-th element in variable-byte compression algorithms, because the position of the element depends on the length of the preceding compressed data.

Direct access is achievable with supporting data structures. An obvious solution is to store the location of each element, but it adds a very large overhead which removes the benefit of compression.

3.1 Rank and Select

Rank and select are two succinct data structure operations which operate on a bit array B. $Rank_1(B, i)$ gives the sum of 1 bits between B[0] and B[i] and $select_1(b, i)$ gives the index of i-th 1 bit in B. Both operations work in constant time (citation?). Locations of 1 bits in B should represent locations of the items in the encoded data. For most compression algorithms, this requires B to be created in addition to the existing data and the length of B usually has to be close to the length of the data. VB encoding has several advantages with search and rank: it's data is compressed in blocks of equal length which significantly shrinks the length of B. Also the bit array C formed from the continuation bits already stores the locations of items. In this case, $rank_1(C, i)$ would give the sum of end bytes up to i-th index and $select_1(C, i)$ would give the location of the ending byte of i-th compressed element.

3.2 Rank and Select implementation

The rank and select implementations used in this article are C++ libraries from (Gog et al., 2014). The library has several implementations of both rank and select as well as an implementation of a bit array. Table 3.1 has rank and select size requirements of

Table 3.1: Memory requirements of SDSL rank and select data structures

Structure	Extra size taken
Rank	25% of bit array
Rankv5	6.25% of bit array
Select	8.3% of bit array (on average)

implementations used in this experiment. Both rank implementations have a constant space requirement, while select's needed size depends on the number of 1's in the data.

For every 512th bit in the array, rank stores the absolute value of 1's preceding that bit in a superblock. For every 64th bit in a superblock, a relative count is stored. With this setup, an rank can be instantly calculated for every 64th bit. To get rank(i), superblock[i/512] and it's relative value (i%512)/64 are fetched. Then 1 bits from (i-i%64) to i are counted and added to get the correct sum. For Rankv5, superblock size is 2048 and relative count is stored every 384th bit, which offers a tradeoff between performance and memory usage.

Select data structure works similarly to rank. Index location of every 4096th set bit is stored in the superblock and location of every 64th set bit is stored relative to the superblock.

3.3 DAC via rank

Directly addressable codes in VB was first introduced by (Brisaboa et al., 2009) in 2009. Their solution was to divide chunks in encoded bytes to separate arrays A_1 to A_n and then use $rank_0$ to get direct access. If i is the requested index, then $rank_0(A_k, i)$ returns the number of elements preceding i that have continuation bit set at 0. In other words, the number of elements that continue to A_{k+1} .

For example, if an element needed 3 chunks when encoded, the least significant bits would go to A_1 , second least significant bits to A_2 and the most significant bits would go to A_3 . When fetching i-th element, getting the first chunk is just fetching $A_1[i]$. If the continuation bit is set at 0 (meaning there are more chunks to this element), getting the correct index for A_2 is calculated with $rank_0(A_1, i)$. A pseudo code example of DAC with rank is shown in Figure 3.1 with block length of 8. (TODO: example needed?)

```
\begin{split} i &\leftarrow \text{wanted index} \\ A &\leftarrow \text{block arrays} \\ B &\leftarrow \text{continuation bit arrays} \\ level &\leftarrow 0 \\ number &\leftarrow 0 \\ \textbf{while } B[level][index] = 0 \textbf{ do} \\ block &\leftarrow A[level][index] \\ number &\leftarrow number \ll 8 \\ number &\leftarrow number \mid block \\ index &\leftarrow \text{Rank}(B[level], index) \\ level &\leftarrow level + 1 \\ block &\leftarrow A[level][index] \\ number &\leftarrow number \ll 8 \\ number &\leftarrow number \mid block \end{split}
```

Figure 3.1: Example pseudo code of DAC with rank by Brisaboa et al.

4 DAC with select query

Using $select_1$ on the continuation bit array to achieve direct access is more intuitive than using $rank_1$. The element locations are already marked with 1's in B and a single $select_1$ query gets the desired starting point, while the forementioned version (Brisaboa et al., 2009) used one rank query for each chunk beyond the first. Minimizing the amount of select and rank queries is important. They run in constant time but their impact is huge, because rest of the VB decoding consists of a few bit operations.

To use $select_1$ with VB, continuation bits need to be separated from chunks to their own bit array and a $select_1$ structure built over it. Select(i) returns the location of the end byte of i-th element. Therefore the start of j-th element in the block array is at block $b_s = select_1(j-1) + 1$. To simplify calculations even further, block sizes of 4 and 8 were used to avoid splitting of blocks between bytes.

Unlike the standard VB encoding, the continuation bits are not in the middle of the data blocks. The compressed number can be read from the memory block and concatenation of blocks is not needed. The data in blocks is be written into memory as it is, so that when reading a large unsigned integer from the block byte array, the bits are already in correct order.

If the original element size is 32 bits and the data was compressed to k blocks of length b. The starting byte s of the element is select(i) * b div 8 where div is the integer division. Offset o is the remainder of previous division, o = x*b mod 8. The 32-bit value is read from memory from byte location s. Then bit shift left for 32-b*k-o is applied to remove trailing bits and bit shift right 32-b*k to re-align bits. If block size is one byte, offset calculation is not needed and thus the process is slightly faster.

The intuitive way to calculate block length k of i-th element is from $select_1(i+1)$ and subtract previously calculated start block index from it. This however causes a second $select_1$ query, which is costly. A much faster option is to iterate forward in bit array until the next 1. Alternatively, the block length can be calculated by reading an integer from the bit array, aligning it's offset and counting the trailing zeros. Figure 4.1 contains an example of VB encoding with DAC with select and block size 8. Different block sizes need extra calculation to get the block location from the byte array. In the example, CalculateLength returns the length of the number in blocks and ByteMask(k) returns a

bit mask for k bytes.

(maybe to future work) Storing bytes in this fashion may have benefits when reading subsequent (fast next() and previous()?) elements. With some modifications, SIMD instructions can possibly be applied.

```
i \leftarrow \text{wanted index}
A \leftarrow \text{block byte array}
B \leftarrow \text{continuation bit array}
begin \leftarrow \text{Select}(index)
len \leftarrow \text{CalculateLength}(begin)
mask \leftarrow \text{ByteMask}(len)
number \leftarrow A[begin] \qquad \triangleright \text{ read a larger number from the byte array}
number \leftarrow number \& mask
```

Figure 4.1: Pseudo code of DAC with select with block length 8

TODO: try bitvector SD performance + size (select)

TODO: look into select implementation, may need optimizing

5 Experimental results

The following experiments are run on jat the moment my work Lenovo Thinkpad T480s, TODO run on a server and write specs here. The algorithms were implemented with C++ (TODO: list compile tags and whatnot here) using data structures and functions from (Gog et al., 2014).

Five different kinds of VB decoding algorithms were used. Bris-implementations are from (Brisaboa et al., 2009).

- Bris4v5 Bris implementation with block size 4, using rank support v5
- Bris8 Bris implementation with block size 8, using rank support v
- Bris8v5 Bris implementation with block size 8, using rank support v5
- Our4 Our implementation with block size 4, using select support mcl
- Our8 Our implementation with block size 8, using select support mcl

Eight kinds of datasets were used. For each number in the dataset, p was randomly selected from P and then number was randomly selected from range $[0,2^p]$.

- all 5M 5 million numbers, P = 7.8, 15, 16, 23, 24, 30, 31
- all 50M 50 million numbers, P = 7.8, 15, 16, 23, 24, 30, 31
- byte5M 5 million numbers, P = 7,7,7,8,8,8,16,31
- byte50M 50 million numbers, P = 7,7,7,8,8,8,16,31
- small5M 5 million numbers, P = 3,4,5,6,7,8,16,31
- small50M 50 million numbers, P = 3,4,5,6,7,8,16,31
- vsmall5M 5 million numbers, P = 2,2,3,3,3,4,4,15
- vsmall50M 50 million numbers, P = 2,2,3,3,3,4,4,15

Experiment	all5M	all50M	byte5M	byte50M	small5M	small50M	vsmall5M	vsmall50M
Bris4v5	348.41	768.83	345.16	772.84	344.54	768.45	346.86	771.61
Our4	127.92	263.22	127.44	263.5	127.9	262.67	127.88	262.58
Bris8	97.75	308.17	98.47	309.6	98.14	307.81	97.99	308.09
Bris8v5	127.83	287.46	127.7	288.63	128.14	291.32	127.99	287.84
Our8	103.85	230.16	103.92	230.14	103.86	230.02	103.95	230.6

Table 5.1: Results in milliseconds, smaller is better.

All algorithms save the data to memory and randomize one million index numbers to an array. The time taken is calculated from looping through the index array and VB decoding the number in the index. The times shown in Table 5.1 are an average of 100 such runs.

- Run with 32 bit values, see what happens (some operations may be 32b?) do cachegrind
- - use array instead of vector; uint8 t $_{\ddot{c}}$ for bris? - comparison to basic implementation + Bri09 - compare with b=2,4,8
- do we need to support search()? SIMD?
- rank vs rank? should formulas have a specific style?

6 Future work

- something to improve / research?

7 Conclusions

It is good to conclude with a summary of findings. You can also use separate chapter for discussion and future work. These details you can negotiate with your supervisor.

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