

What Distinguishes This Text from Others

- 1) It employs universal design principles in how information is presented. Some examples of this are: simplicity and consistent use of common notation, careful explanation of mathematical 'jargon', vertical rather than horizontal arrangements of visual or tabular information, and avoidance of symbols with multiple meanings.
- 2) Develop marketable skills applicable in a business environment – whether it be a company or organization comprising of one individual, 50 individuals, or a thousand. Many of the lessons include applicable spreadsheet activities that enable the student to visualize the mathematical principles which help to answer meaningful questions.
- 3) With practice, the student will develop confidence toward being able to communicate accurately using mathematical models, formulas, and data tools. Instead of emphasizing procedures, the emphasis is on extrapolation, interpretation, analysis, and critical thinking.
- 4) With the emergence of large language models and intelligent systems, the need for computation and algebraic manipulation will be less relevant. Tools like Mathway, Cymath, and Desmos are constantly improving as the training data and prompt engineering improves. Given that these automations are still developing and still are prone to errors, it will be more necessary than ever before to be able to assess and evaluate information that is presented, determine its reliability, and finally to assess its application (when, how, and to whom).
- 5) The inclusion of a Chapter Zero offers the student more than just elementary mathematical concepts. These foundational concepts are put in context which enriches and broadens the learner's perspective. Numbers are not just objects to be plugged into a formula. They actually mean something contextually. A fraction isn't just a fraction, but a means to engage in commerce or calculate the frequency of a leap year. In a typical semester course, Chapter Zero is not included in the Syllabus. It is there for the student to review basic concepts as needed or desired.

Outline

Chapter 0: Foundations of Mathematical Reasoning and Expression

Section 0.1 The Real Number System

- Real, Rational and Integer Number Systems

- Words We Use for Numbers

Section 0.2 What's the Big Deal About Fractions?

- Pieces of Eight

- Unit Fractions and Other Notation

- Ratio as a Fraction

- Leap Year Calculations

Section 0.3 From Fractions and Decimals to Percents

- What the % Symbol Means

- Some Applications of Percent

Section 0.4 How Big or Small; High or Low; Near or Far

- Measurement and Size

- Context Used to Interpret Scale of Something

- Definition of Magnitude and Distance

Section 0.5 Direction and the Rectangular Coordinate System

- Coordinates on a Flat Surface

- Distance and Direction

- Quadrants in the Coordinate System

Chapter 1: Functions and Linear Models

Section 1.1 Definitions and Terminology of Functions

- Continuous versus Discrete Sets of Numbers

- Functions and Function Notation

- Multiple Representations (graphical, tabular, description, formulaic)

Section 1.2: Characteristics of Functions

- Domain and Range

- Predictor variable and Response variable

Section 1.3: Rates of Change and Bivariate Behavior

- How two quantities correlate
- Analyzing average rate of change
- Patterns in relationships (Increasing/decreasing)
- Section 1.4: Linear Models
 - Definition of a Linear Function and Implications
 - Characteristics of Linear Relationships
- Section 1.5: Graphs of Linear Functions
 - Extracting Meaning From a Graph
 - Creating a Graph From Data or an Equation
- Section 1.6: Interpreting With Linear Models
 - Use Verbal Descriptions In Linear Relationships
 - Applications
 - When Time is the Predictor Variable
 - When the Response is Cost, Revenue, or Profit
 - Supply and Demand
- Section 1.7: Fitting a Linear Model From Data
 - Choosing the Predictor and Response
 - Why Domain Matters
 - Interpolation and Extrapolation

Chapter 2: Input/Output Analysis (Matrices in Economic Systems)

- Section 2.1: Matrix Representation
 - System of Equations and Matrix Equivalent
 - Using Technology to Solve a System
 - Interpreting and Analyzing the Results
- Section 2.2: A Problem in Industrial Production
 - Connecting Verbal Descriptions To Equations
 - Understand The Situation Using Multiple Representations
- Section 2.3: A Problem in Conglomerate Production
 - Connecting Verbal Descriptions To Equations
 - Understand The Situation Using Multiple Representations

Chapter 3: Optimization With Multiple Variables (Linear Optimization – A Case Study)

- Section 3.1: Description of a Problem
 - Connecting Verbal Descriptions To Equations
 - Understand The Situation Using Multiple Representations
 - Naming the Function To Be Optimized
- Section 3.2: Matrix Representations
 - From System of Equations To Matrix
- Section 3.3: Finding Solutions
 - Using Software To Do the Dirty Work
 - Meaning Behind the Numbers
- Section 3.4: Interpretation and Analysis

Chapter 4: Polynomials As Models

Section 4.1: Quadratic Models

- Definition of a Quadratic Function and Implications

- Characteristics of Quadratic Type Relationships

Section 4.2: Graphs of Quadratic Functions

- Extracting Meaning From a Graph

- Creating a Graph From Data or an Equation

Section 4.3: Interpreting With Quadratic Models

- Use Verbal Descriptions In Quadratic Relationships

- Applications

 - When time is the predictor variable

 - When the response is cost, revenue, or profit

Section 4.4: Polynomial Models

- Definition of a Polynomial Function and Implications

- Characteristics of Polynomial Type Relationships

Chapter 5: Exponential and Logarithm As Models

Section 5.1: Exponential Models

- Definition of an Exponential Function and Implications

- Characteristics of Exponential Relationships

- Exponential Growth and Decay

Section 5.2: Graphs of Exponential Functions

- Extracting Meaning From a Graph

- Creating a Graph From Data or an Equation

Section 5.3: Logarithm Models

- Definition of a Logarithm Function and Implications

- Characteristics of Logarithmic Relationships

- Logarithm in Population Growth Models

Section 5.4: Graphs of Logarithm Functions

- Extracting Meaning From a Graph

- Creating a Graph From Data or an Equation

Section 5.5: Applications of Exponential and Logarithm Models

- Population Growth and Decay Case Studies

- Compound Interest

- Applying a Logarithmic Scale to Stock Market Data

Chapter 6: Finance

Section 6.1: Simple and Compound Interest

Section 6.2: Annuities

Section 6.3: Payout Annuities

Section 6.4: Loans and Amortization

Section 6.5: Putting It All Together

Chapter 7: Sets and Probability

Section 7.1: Basics of Set Notation and “Belonging”

Section 7.2: Venn Diagrams and Applications (Survey Problems)

Section 7.3: Events and Outcomes

Section 7.4: Basic Probability

Probability of a Single Event

Complement Rule For Probability

Addition Rule in Probability

Section 7.5: Conditional Probability and Contingency Tables

Section 7.6: Expected Value

Application: Insurance Premiums

Application: Warranties

Application: Game Theory

Chapter 8: Descriptive Statistics

Section 8.1: Sampling and Data Collection

Section 8.2: Visualization With Data

Section 8.3: Summarization of Data

Section 8.4: Discrete Distributions

Section 8.5: Continuous Distributions

Section 8.6: Central Limit Theorem

How it Applies to Population Proportions

How it Applies to the Mean of a Distribution

Section 8.7: Probabilities With the Normal Distribution

Chapter 9: Calculus of the Derivative

Section 9.1: Review of Functions, Toolkit Functions

Properties of Each Type of Function

Recognizing Patterns

Section 9.2: The Derivative – Slope Introduction

What “slope” means on a curved graph

Intuitive definition of a tangent line to a curve

Approximating slope from the graph

Section 9.3: More Estimation of the Derivative at a Point

Intuitive definition of a secant line

Using secant lines to estimate the derivative

Intuitive development of the concept of a limit
Section 9.4: Average Rate of Change on an Interval
Example from the NYSE
Connection to the Derivative
Applications
Section 9.5: Marginal Cost and Revenue
Interpreting Meaning from Equations
Using the derivative in marginal cost/revenue situations
Section 9.6: More Applications of the Derivative
Cost, Revenue, and Profit
Decisions About “What Math to Use”

Possible Chapter 10

Intuitive Development of Area (Integration)
Probability Density Functions and Area as Probability of a Continuous Random Variable
More Applications of the Derivative in Optimization

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