

**Directions:** Answer each question to the best of your ability. **Show your reasoning** and/or process used to answer the question(s) where it is appropriate. A calculator will be helpful for this quiz. There are 5 questions.

*Give your answers to probability questions as a fraction or decimal rounded to 3 decimal places.*

1. (3 pts) Complete the table and calculate the Expected Value for this probability distribution.

x	P(x)	$x \cdot P(x)$	Expected Value
0 (no claim)	0.96		
500	0.02		
2000	0.01		
10,000	0.01		

2. (3 pts) The **above table** represents average probabilities of auto insurance policyholders making a claim and what the company pays out per incident/claim. To cover cost, what should the insurance company charge for each policy?

3. (3 pts) A certain politician uses the word 'woke' in public speeches about 81% of the time. Two friends have a bet... when the word is spoken, the first friend must pay \$1. If it is not spoken, the second friend must pay \$4. Which friend is most likely to benefit from this arrangement? Why?

4. (3 pts) A bag contains 1 gold marble, 5 silver marbles, and 22 black marbles. Someone is 'selling' the following game to a crowd of onlookers: You (the player) randomly select one marble from the bag. If it is gold, you win \$6. If it is silver, you win \$3. If it is black, you lose \$1.

What is the (average) expected value if you play this game?

5. (3 pts) A company estimates that 3% of their products will fail *after* the original warranty period but within 2 years of the purchase, with a replacement cost of \$800. [Hint: There are two outcomes for x]  
If they offer a 2-year extended warranty for \$30, what is the company's expected value of each warranty sold?

Formulas:

**Expected Value:** Given a sample space of  $n$  outcomes ( $\mathbf{x}$ ) and their probabilities –  $\mathbf{Pr}(\mathbf{x})$ , the “expected value” of this event or observation is given by:

$$E(x) = x_1 \cdot \text{Pr}(x_1) + x_2 \cdot \text{Pr}(x_2) + \cdots + x_n \cdot \text{Pr}(x_n)$$