Duration of Individual Relativistic Electron Microbursts: A Probe Into Their Scattering Mechanism ... Better/shorter title?

M. Shumko^{1,2}, L.W. Blum³, and A.B. Crew⁴

¹NASA's Goddard Space Flight Center, Greenbelt, Maryland, USA
 ³Universities Space Research Association, Columbia, Maryland, USA
 ³University of Colorado Boulder, Boulder, Colorado, USA
 ²Johns Hopkins University Applied Physics Laboratory, Laurel, Maryland, USA

Key Points:

- We identified relativistic microbursts observed by the SAMPEX satellite and quantified their duration
- The microburst duration is shortest at midnight and longest at noon magnetic local times.
- Whistler-mode chorus rising tone element duration has a similar trend

Corresponding author: M. Shumko, msshumko@gmail.com

Abstract

In this study we used the Solar Anomalous and Magnetospheric Particle Explorer to identify relativistic, > 1 MeV, electron microbursts and we quantified their duration. We found the shortest microbursts, with a median duration around 80 milliseconds, near midnight magnetic local time. Microburst duration increases through dawn and to noon magnetic local time, where the median microburst duration roughly doubles to 160 milliseconds. The increasing microburst duration trend in magnetic local time is similar to the whistler mode chorus rising tone element duration, shedding light into the microburst scattering mechanism.

Plain Language Summary

Microbursts are a naturally occurring form of electron precipitation from the near-Earth space into the atmosphere. They are characterized by their short duration, typically defined to be less than a second, or sometimes as 100 milliseconds... Microburst impact on the atmosphere includes the degradation of Mesospheric Ozone through the production of Odd Nitrogen and Odd Hydrogen molecules... We don't know the details on how microburst electrons are scattered, but there is evidence that they are scattered by whistlermode chorus rising tone elements... Talk about duration and how it is a probe into the scattering physics.

1 Introduction

Earth's outer radiation belt particle population is in constant flux, governed by many processes that affect particles via, for example: radial transport with injections from the magnetotail and ultra low frequency waves, local heating and loss into Earth's atmosphere due to wave-particle interactions Cite Ripoll et al., 2019 "Particle Dynamics in the Earth's Radiation Belts: Review of Current Research and Open Questions". Whistler mode chorus (WMC) is just one type of plasma wave characterized by short ($\approx 100 \text{ ms}$) rising tone elements, and perform a dual role in electron dynamics: accelerating electrons from $\approx 10 \text{ keV}$ injection energies up to MeV energies, and pitch angle scattering electrons into the atmosphere (e.g. Li, Thorne, Angelopoulos, Bonnell, et al., 2009; Thorne, 2010; Horne & Thorne, 2003; Summers, 2005). One form of electron precipitation is microbursts: a transient and intense increase of electrons, with a $\approx 100 \text{ ms}$ duration, first observed by balloons in Earth's upper atmosphere, and later by satellites in low Earth orbit (LEO), and recently at high altitude near the magnetic equator (e.g. Anderson & Milton, 1964; Blake et al., 1996; Lorentzen et al., 2001; O'Brien et al., 2003; Douma et al., 2017; Kurita et al., 2016; Shumko et al., 2018).

Rewrite sentence. \rightarrow The observed microburst electron energies span multiple orders of magnitude from tens of keV observed by, for example, Datta et al. (1997) to > 1 MeV observed by, for example, the Solar Anomalous Magnetospheric Particle Explorer (SAMPEX) by Blum et al. (2015). Spatially, microbursts are predominately observed outside the plasmapause; on the radiation belt footprints, $L \approx 4-8$; and in the morning Magnetic Local Time (MLT) (0-12 hours MLT) (Lorentzen et al., 2001; Blum et al., 2015; O'Brien et al., 2003; Douma et al., 2017). If I keep the AE plot, I should discuss the microburst occurrence as a function of AE and Dst (Emma's and Paul's work).

Talk about their impact on the environment

Electron microbursts and chorus waves were associated early on, due to their similar duration and similar occurrence distributions in MLT (e.g. Lorentzen et al., 2001). Recently, Breneman et al. (2017) directly linked a chorus rising tone element to a microburst observed by the Focused Investigation of Relativistic Electron Bursts: Intensity, Range, and Dynamics (FIREBIRD-II) CubeSats (Johnson et al., 2020) during a close

magnetic conjunction. With this evidence, the particle precipitation community is largely in agreement that chorus waves scatter microbursts. A natural follow-on question is how. For example, it is still unclear if relativistic (> 1 MeV) microbursts are scattered via cyclotron resonance at high magnetic latitudes, or a higher resonance harmonic near the magnetic equator (Lorentzen et al., 2001). One way to address this question is by studying for how long microburst electrons are in resonance with a chorus wave. The resulting microburst duration, i.e. the microburst peak width in the time series data, is a probe into the conditions necessary to scatter microburst electrons. From our literature review, we found only qualitative estimates of the microburst duration. Therefore, we used the microburst observed by the SAMPEX satellite to quantify the distribution of > 1 MeV microburst duration. In this letter, we investigated the duration distribution as a function of: L-shell, MLT, and the Auroral Electrojet.

2 Instrumentation

In this study we used the > 1 MeV electron count data, taken by the Heavy Ion Large Telescope (HILT) instrument (Klecker et al., 1993), that was onboard the SAM-PEX satellite (Baker et al., 1993).

SAMPEX was launched in July 1992 and reentered Earth's atmosphere in November 2012. It was in a 520x670 km, 82° inclination low Earth orbit. In general, the SAMPEX had two pointing modes: spin and orbit rate rotation (zenith pointing) modes. To avoid the compounding effects due to the variable pitch angles sampled in the spin mode, we only used the zenith pointing mode data. The International Geomagnetic Reference Field (Thébault et al., 2015, IGRF) magnetic field model was used to derive the meomagnetic coordinates.

We used the HILT electron data, sampled at a 20 ms cadence (state4 in the data archive), that was taken between 1997 and 2012. The HILT instrument consisted of a large rectangular chamber with the aperture on one end, and 16 solid state detectors on the other. The electron counts accumulated over 20 ms were summed from all of the solid state detectors and used in this study.

The HILT instrument is ideal for studying relativistic microbursts and it was used in many prior microburst studies including O'Brien et al. (2003); Lorentzen et al. (2001); Blake et al. (1996); Nakamura et al. (2000); Kurita et al. (2016), and Douma et al. (2017).

3 Methodology

To estimate the microburst duration we first identified microbursts and then we fit them with a Gaussian model with a linear trend to quantify the duration for each microburst.

3.1 Microburst Identification

We identified microbursts using the burst parameter defined by O'Brien et al. (2003) and used in numerous other microburst studies with SAMPEX (e.g. Douma et al., 2017). Assuming Poisson probability for the observed electron counts, the burst parameter is the number of standard deviations of a foreground signal above the background, expressed as

$$n_{\sigma} = \frac{N - A}{\sqrt{A + 1}} \tag{1}$$

where N is the number of foreground electron counts (microburst or otherwise), and A is the centered running average background counts. The 1 in the denominator prevents a division by 0 error. In O'Brien et al. (2003), and in the results in this study, N was summed over 0.1 seconds and is called N_{100} , while A was summed over 0.5 seconds and



Figure 1. Examples > 1 MeV microbursts are shown by the black lines, and the fits are shown by the dashed red lines. The fit full width at half maximum (FWHM) and the \bar{R}^2 goodness of fit metric is annotated in each panel. Microbursts with $\bar{R}^2 > 0.9$ were used for this study. The major time ticks are at every second, while the minor ticks are at every 100 milliseconds.

is called A_{500} . Henceforth we will specify the time window with the subscript for N and A. Times when $n_{\sigma} > 10$ are classified as microburst times, and the peak count rate in each time interval is saved as a microburst to our data set. With A_{500} and N_{100} , we detected a total of 256,764 microbursts over the 15 year period from 1997 to 2012. Four examples of microbursts are shown in Fig. 1 by the solid black curves.

Check the argument for clarity The choice of A determines the sensitivity of the burst parameter to microbursts of various durations (widths). This sensitivity is best illustrated with an example. Given a 1-second wide microburst, if we use A_{500} , the centered average background at the microburst time is skewed towards the microburst peak and the microburst's bp is reduced, potentially below the detection threshold. On the other hand, if we use A_{1000} , the centered running background will be relatively less elevated at the microburst time so it has a greater bp and is more likely to be detected. In other words, bp will be relatively larger for A_{1000} than A_{500} . This sensitivity manifests itself as a bias towards detecting narrower microbursts that we will address later in this study.

3.2 Microburst Duration

We estimated the microburst duration using two methods that yielded similar results: the duration at half of the microburst's topographic prominence and duration from a Gaussian fit.

The topographic prominence is a simple and robust method to estimate the microburst duration used to identify curtains a similar-looking type of precipitation (Shumko, Johnson, O'Brien, et al., 2020). It is defined as the duration at half of the microburst topographic prominence: the height of the microburst relative to the maximum of the two minima on either side of the microburst peak. On each side of the microburst peak, the minima are searched for between the microburst and a higher peak on that side. While the topographic prominence method of estimating microburst durations is simple and robust, one of its downsides is its inability to automatically verify that the duration is representative of a single microburst. Therefore, we also fit microbursts with a Gaussian, and used the R^2 goodness of fit metric to filter out bad duration estimates.

The other method that we use to estimate the microburst duration is fitting a Gaussian shape to microbursts. The advantage of this method is that it allows us to evaluate the fit using a goodness of fit metric. By screening out bad fits, we exclude super-

position of multiple microbursts that will unintentionally bias our microburst duration estimate.

We assumed a Gaussian superposed with a linear trend fit model. The Gaussian models the shape of the microburst; while the linear trend accounts for the electrons that are either trapped or quasi-trapped in the drift loss cone. The fit model is defined as:

$$c(t|A, t_0, \sigma, c_0, c_1) = Ae^{-\frac{(t-t_0)^2}{2\sigma^2}} + c_0 + c_1t$$
(2)

Reconsider variable names... where A, t_0 , and σ are the Gaussian amplitude, center time, and standard deviation; while the c_0 and c_1 are the background count intercept and slope. The fit was applied over a number of data points determined by the maximum of either: 4x topographic prominence width or 0.5 seconds. A challenge to any robust and automated nonlinear regression algorithm is guessing the initial parameters. The initial parameter guesses for the Gaussian are provided by the topographic prominence and topographic duration estimates. The two linear trend initial parameters were: $c_0 = \text{median}(\text{counts})$ and $c_1 = 0$. The optimal fit parameters were found using scipy's curve_fit() function in Python. We defined the microburst duration as the full width at half maximum (FWHM) of the microburst peak, defined as

$$FWHM = 2\sqrt{2\ln 2}\sigma. \tag{3}$$

To evaluate the fit, we used the R^2 goodness of fit metric. R^2 is defined as

$$R^{2} = 1 - \frac{SS_{res}}{SS_{mean}} = 1 - \frac{\sum (c_{i} - f_{i})^{2}}{\sum (c_{i} - \bar{c})^{2}}$$
(4)

where SS_{res} is the sum of the squared residuals between the observed counts c_i and the fit counts f_i for each time step, and likewise SS_{mean} is the sum of the squared residuals between c_i and the mean of the counts, \bar{c} .

One interpretation of R^2 is: fractionally how much better is the variance in the data explained by the model fit, compared to the null hypothesis horizontal line at \bar{c} . R^2 values vary from 1 when the fit perfectly describes the variance in the data, to $-\infty$ for poor fits (a fit can be much worse than the mean null hypothesis).

To account for overfitting that results from the variable number of data points used for each fit, the adjusted R^2 , \bar{R}^2 , was used. It is defined as

$$\bar{R}^2 = 1 - (1 - R^2) \frac{n - 1}{n - p - 1} \tag{5}$$

where n is the number of data points fit, and p is the number of parameters. Intuitively, n-1 is the number of degrees of freedom for the null hypothesis, and n-p-1 is the degrees of freedom for the fit model. Fits with $\bar{R}^2>0.9$ are considered good fits and are used for the rest of this analysis. We compared the microburst duration estimated with the prominence and fit methods. With the $\bar{R}^2>0.9$ constraint, we found that for 85% of microbursts, the duration estimated by both methods agreed to within 25%.

Figure 1a shows an example of two superposed microbursts that had a fit $\bar{R}^2 = 0.83$ that were excluded from this study. On other hand, Fig. 1b-d show microbursts that were included in this study because the fit $\bar{R}^2 > 0.9$.

Lastly, Fig. 1c,d demonstrate the necessity of the linear fit to account for the changing background. The linear fit accounts for the non-zero mean background counts and the different amplitudes of the edges of the Gaussian. Of the 256,764 detected microbursts, 109,231 had $R^2 > 0.9$ and are used for the remainder of this study.

Distribution of > 1 MeV Microburst Duration SAMPEX/HILT

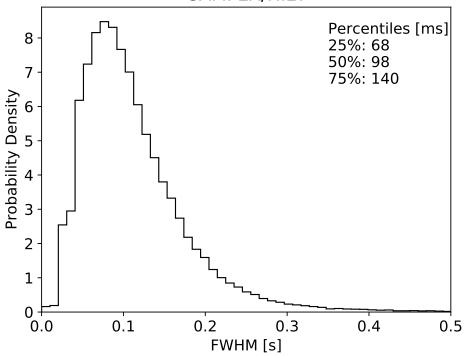


Figure 2. The distribution of all microburst full width at full maximum (FWHM). Maybe merge this plot with the AE plot?

4 Results

The well-fit microbursts are used to quantify the distribution of microburst duration (FWHM) for all microbursts, as a function of L and MLT, and as a function of the Auroral Electroject (AE). We begin with the overall microburst distribution.

Figure 2 shows the distribution of all well-fit microbursts. This distribution is peaked with the median at 98 ms and quickly drops off. The interquartile range spans about a factor of two in microburst duration, from 67 to 140 ms.

Figure 3 shows the joint distribution of microburst duration as a function of L and MLT. Figure 3a-c show the 25%, 50%, and 75% percentiles of microbursts in each L-MLT bin. The sparse bins with less than 100 well-fit microbursts are white. For reference, Fig. 3d shows the number of well-fit microbursts observed as a function of L and MLT.

In Fig. 3, the microburst duration trend is almost identical for the different percentiles, but lets focus on the median distribution, Fig. 3b. In MLT, the median microburst duration increases by a factor of two: from 80 ms at midnight to 160 ms at noon. In L-shell, the median microburst duration slightly increases with L shell, most apparent near midnight MLT. To disentangle the L and MLT distribution, Fig. 4 shows the marginalized distributions; MLT was marginalized out in Fig. 4a and L-shell was marginalized out in Fig. 4b. Figure 4a shows a slight broadening of the microburst duration at higher L-shells; in contrast to Fig. 4b that clearly shows that the microburst duration increases from midnight to noon MLT.

Distribution of SAMPEX microburst durations in L-MLT

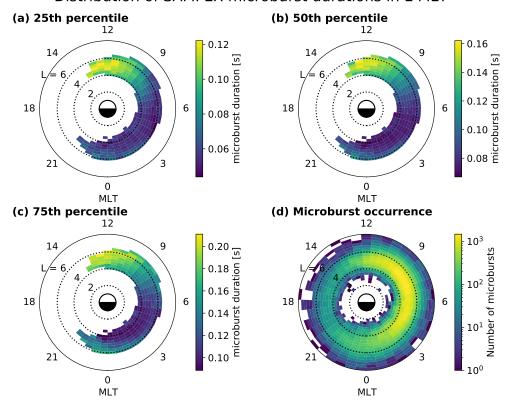


Figure 3. The joint distributions of microburst duration (FWHM) as a function of L and MLT. In each L-MLT bin with more than 100 good microburst fits, the 25th, 50th, and 75th percentiles of the duration were calculated and shown in panels a-c, respectively. The white bins in panels a-c have less than 100 good microburst fits. Panel d shows the distribution of the number of microbursts with 0 microbursts shown with the white bins.

Lastly, we investigated the dependence of microburst duration as a function of geomagnetic activity. To be consistent with the prior wave and microburst studies, we use the Auroral Electrojet (AE) index to quantify the level of geomagnetic disturbance. We adopt the same three AE intensity levels used in prior studies, such as Li, Thorne, Angelopoulos, Bortnik, et al. (2009), Douma et al. (2017), and Meredith et al. (2020): AE < $100,\,100 <$ AE < $300,\,$ and 300 < AE < $1000,\,$ in nanotesla units. Figure 5 shows the distribution of microburst duration as a function of AE. This distribution is similar across the three AE intensity levels. However, the distribution is more prominently peaked at $0.1\,$ s at the highest intensity level.

5 Discussion and Conclusions

To address the burst parameter preferential bias to narrower microbursts, as introduced in section 3.1, we ran the microburst identification algorithm with three background values: A_{500} , A_{1000} , and A_{2000} . As described in section 3.1, an detection algorithm who's centered running average is over wider time periods will be more sensitive to wider and less prominent microbursts. Therefore we can identify the bias if there is a relative excess of longer duration microbursts when the average time was increased. We found no such excess for microburst data sets that were made using A_{1000} , and A_{2000} .

Distribution of SAMPEX microburst durations in L and MLT

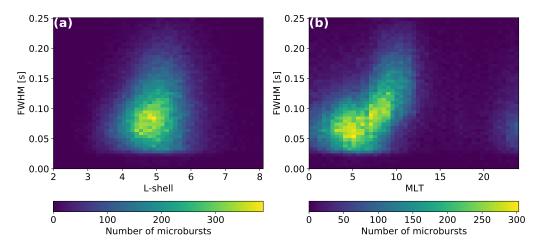


Figure 4. The marginalized distributions of the number of microbursts as a function of microburst duration (FWHM) and L shell in panel a and MLT in panel b.

Therefore, we believe that > 1 MeV microbursts are truly narrower than 250 ms and the A_{500} is adequate to identify > 1 MeV microbursts.

The overall microburst duration distribution, shown in Fig. 3 shows that the median microbust duration is approximately 100 ms, in agreement with prior studies (e.g. Anderson & Milton, 1964; Trefall et al., 1966; Nakamura et al., 2000). However, we found an unexplored trend in the literature where the microburst duration at lower energies is wider (e.g. Johnson et al., 2020; Shumko, Johnson, Sample, et al., 2020). This trend is consistent with recent modeling by Chen et al. (2020) and Miyoshi et al. (2020), but needs to be fully explored with energy-resolved measurements provided by, for example, FIREBIRD-II.

Perhaps in the modeling discussion below, it will be more clear to discuss the microburst duration separately for non-relativistic and relativistic electron energies. The microburst duration trend in L-shell is subtle; the higher-duration tail of the duration distribution shown in in Fig. 3c near midnight MLT slightly increases at higher L-shells, and is also noticeable in Fig. 4a. In contrast, the duration trend as a function of MLT is significant. The MLT trend correlates well with a similar trend in chorus rising tone element duration (Teng et al., 2017; Shue et al., 2019). However, the chorus wave properties that control the microburst duration are complex. Figure 4 in Chen et al. (2020) shows a test particle model result and describe what wave properties bound the microburst duration in time-energy space. The upper and lower microburst energy bounds are roughly driven by the initial and final magnetic latitudes of the chorus wave propagation, as expected from the cyclotron resonance condition (Lorentzen et al., 2001).

Furthermore, the start and end of the microburst enhancement shown in Chen et al. (2020), is more complicated and is roughly driven by the chorus rising tone element bandwidth (roughly as it is more accurate for medium energy electrons, but for the highest energy electrons the upper magnetic latitude of the chours wave plays a roll). It is complicated because the time of flight of electrons (their arrival time at LEO) depends on their velocity and at what magnetic latitude they were scattered (Saito et al., 2012). Higher energy electrons scatter at higher magnetic latitudes, so they have to traverse a longer path into the atmosphere in the opposite hemisphere, but they are moving quicker.

Distribution of >1 MeV microburst duration as a function of AE

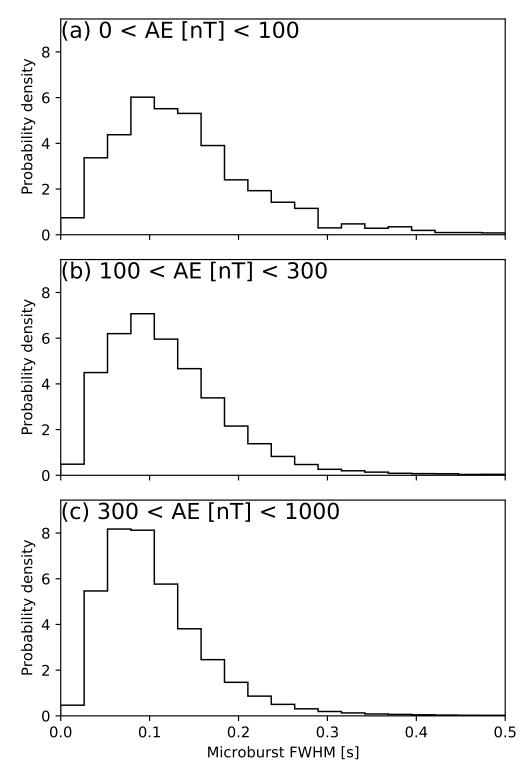


Figure 5. The distribution of the microburst duration (FWHM) for three ranges of the Auroral Electroject: AE < 100, 100 < AE < 300,and 300 < AE < 100nT in Panels a-c, respectively. The x- and y-axis share identical limits between the three panels.

The result of the two competing effects is non-trivial: sometimes the mid-energy microburst electrons are the first to arrive in LEO, followed by the low and high microburst electrons. This effect is theoretically predicted by Saito et al. (2012), Miyoshi et al. (2020), and Chen et al. (2020), but has not yet been confirmed by observations. Unfortunately, since we are using the integrated, > 1 MeV, electron counts, we can not look into this futher. Neverthelss, recent missions such as Electron Losses and Fields Investigation (ELFIN), and FIREBIRD-II have the energy resolution to look at the microburst electron arrival time as a function of energy and time. Mention that Shue et al., 2019 did not find a significant trend of chorus rising tone bandwidth or normalized bandwith... so much for the Chen curves for mid-energy microbursts.

In summary, we found that the > 1 MeV microburst duration distribution is peaked at 100 ms, with 75% of microbursts narrower than 140 ms. We found no significant trend in the microburst duration as a function of L-shell, but we did find a strong trend as a function of MLT—the median microburst duration roughly doubles from 80 ms at midnight, to 160 ms at noon MLT. We found that the microburst duration trend in MLT to be similar to the trend in the rising tone element duration. However, contrary to the theoretically expected dependence of micriburst duration on chorus bandwidth, Shue et al. (2019) did not find an incerase in the chorus rising tone bandwith between midnight and noon MLT.

Acknowledgments

We are thankful for the engineers and scientists who made the SAMPEX mission possible. M. Shumko is thankful for the support provided by the NASA Postdoctoral Program at the NASA's Goddard Space Flight Center, administered by Universities Space Research Association under contract with NASA. Lauren's and Alex's funding sources The SAMPEX HILT and attitude data are located at http://www.srl.caltech.edu/sampex/DataCenter/data.html and the minute cadence Auroral Electroject data is located at ftp://ftp.ngdc.noaa.gov/STP/GEOMAGNETIC_DATA/INDICES/AURORAL_ELECTROJET/ONE_MINUTE/. The analysis software is archived at https://github.com/mshumko/sampex_microburst_widths.

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