

$$\begin{bmatrix}
840B_{40} + 5040B_{60} & 0 & -720\sqrt{7}B_{66} & 0 & 60\sqrt{70}B_{40} - 7560\sqrt{70}B_{60} & 0 & 720\sqrt{7}B_{66} \\
0 & -1260B_{40} - 21420B_{60} & 0 & 1080\sqrt{7}B_{66} & 0 & 300\sqrt{7}B_{40} + 3780\sqrt{7}B_{60} & 0 \\
-720\sqrt{7}B_{66} & 0 & -660B_{40} + 27720B_{60} & 0 & 0 & 0 & 900B_{40} + 52920B_{60} \\
0 & 1080\sqrt{7}B_{66} & 0 & 540B_{40} + 1260B_{60} & 0 & -2520B_{66} & 0 \\
60\sqrt{70}B_{40} - 7560\sqrt{70}B_{60} & 0 & 0 & 0 & 1080B_{40} - 25200B_{60} & 0 & 0 \\
0 & 300\sqrt{7}B_{40} + 3780\sqrt{7}B_{60} & 0 & -2520B_{66} & 0 & 540B_{40} + 1260B_{60} & 0 \\
720\sqrt{7}B_{66} & 0 & 900B_{40} + 52920B_{60} & 0 & 0 & 0 & -660B_{40} + 27720B_{60} \\
0 & 2520B_{66} & 0 & 300\sqrt{7}B_{40} + 3780\sqrt{7}B_{60} & 0 & 1080\sqrt{7}B_{66} & 0 \\
0 & 0 & 720\sqrt{7}B_{66} & 0 & 60\sqrt{70}B_{40} - 7560\sqrt{70}B_{60} & 0 & -720\sqrt{7}B_{66}
\end{bmatrix}$$

Subspace 1

Base: $|4\rangle, |2\rangle, |0\rangle, |-2\rangle, |-4\rangle$

$$H_1 = \begin{bmatrix}
840B_{40} + 5040B_{60} & -720\sqrt{7}B_{66} & 60\sqrt{70}B_{40} - 7560\sqrt{70}B_{60} & 720\sqrt{7}B_{66} & 0 \\
-720\sqrt{7}B_{66} & -660B_{40} + 27720B_{60} & 0 & 900B_{40} + 52920B_{60} & 720\sqrt{7}B_{66} \\
60\sqrt{70}B_{40} - 7560\sqrt{70}B_{60} & 0 & 1080B_{40} - 25200B_{60} & 0 & 60\sqrt{70}B_{40} - 7560\sqrt{70}B_{60} \\
720\sqrt{7}B_{66} & 900B_{40} + 52920B_{60} & 0 & -660B_{40} + 27720B_{60} & -720\sqrt{7}B_{66} \\
0 & 720\sqrt{7}B_{66} & 60\sqrt{70}B_{40} - 7560\sqrt{70}B_{60} & -720\sqrt{7}B_{66} & 840B_{40} + 5040B_{60}
\end{bmatrix}$$

$$\lambda_{1,1}^{(1)} = 1680B_{40} - 100800B_{60}$$

$$\lambda_{1,2}^{(2)} = 240B_{40} + 80640B_{60}$$

$$\lambda_{1,3}^{(1)} = -360B_{40} - 10080B_{60} - 240\sqrt{25B_{40}^2 + 630B_{40}B_{60} + 3969B_{60}^2 + 252B_{66}^2}$$

$$\lambda_{1,4}^{(1)} = -360B_{40} - 10080B_{60} + 240\sqrt{25B_{40}^2 + 630B_{40}B_{60} + 3969B_{60}^2 + 252B_{66}^2}$$

Subspace 2

Base: $|3\rangle, |1\rangle, |-1\rangle, |-3\rangle$

$$H_2 = \begin{bmatrix}
-1260B_{40} - 21420B_{60} & 1080\sqrt{7}B_{66} & 300\sqrt{7}B_{40} + 3780\sqrt{7}B_{60} & 2520B_{66} \\
1080\sqrt{7}B_{66} & 540B_{40} + 1260B_{60} & -2520B_{66} & 300\sqrt{7}B_{40} + 3780\sqrt{7}B_{60} \\
300\sqrt{7}B_{40} + 3780\sqrt{7}B_{60} & -2520B_{66} & 540B_{40} + 1260B_{60} & 1080\sqrt{7}B_{66} \\
2520B_{66} & 300\sqrt{7}B_{40} + 3780\sqrt{7}B_{60} & 1080\sqrt{7}B_{66} & -1260B_{40} - 21420B_{60}
\end{bmatrix}$$

$$\lambda_{2,1}^{(2)} = -360B_{40} - 10080B_{60} - 240\sqrt{25B_{40}^2 + 630B_{40}B_{60} + 3969B_{60}^2 + 252B_{66}^2}$$

$$\lambda_{2,2}^{(2)} = -360B_{40} - 10080B_{60} + 240\sqrt{25B_{40}^2 + 630B_{40}B_{60} + 3969B_{60}^2 + 252B_{66}^2}$$