# Pathway probabilities, total cost and time to treatment initiation for suspected TB patients

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## Introduction

Posterior distributions are generated to provide DES model input parameters.

## Model

#### Cost and time

Independent Bayesian linear regressions on cost and time to starting treatment with covariates of sputum smear results ('Not taken', 'Negative', 'Positive') and TB status (missing, 'E;PTB', 'PTB').

For individual i,

$$c_i \sim N(\phi_i^c, \lambda); \ t_i \sim N(\phi_i^t, \tau)$$

$$\phi_i^c = \mu_c + \gamma_{tb_i}^c + \beta_{ssm_i}^c; \quad \phi_i^t = \mu_t + \gamma_{tb_i}^t + \beta_{ssm_i}^t$$

We used uninformative priors. So, the posterior distribution of the expected cost and time are

$$\hat{\phi}_{tb.ssm}^c = \hat{\mu}_t + \hat{\gamma}_{tb}^c + \hat{\beta}_{ssm}^c; \ \hat{\phi}_{tb.ssm}^t = \hat{\mu}_t + \hat{\gamma}_{tb}^t + \hat{\beta}_{ssm}^t.$$

## Pathway probabilities

Separate multinomial models were fit to counts of sputum smear microscopy results for pulmonary only (p), and both pulmonary and extra-pulmonary (ep) cases.

$$X_{ep} \sim Multi(p_{ep}, N_{ep}); X_p \sim Multi(p_p, N_p)$$

The posterior distributions for  $p_{ep}, p_p$  are reported.

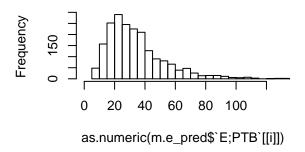
## Data

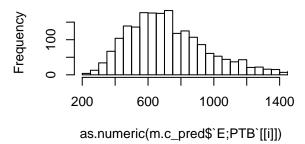
The IDEA dataset for Dosanjh category 1 and 2 patients only.

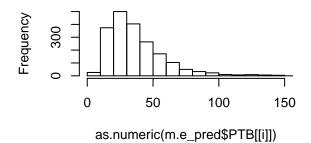
## Output

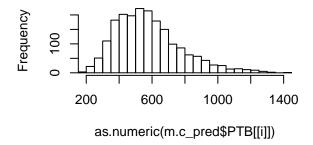
Posterior distributions and summary statistics for mean cost and time to starting treatment.

## Not taken

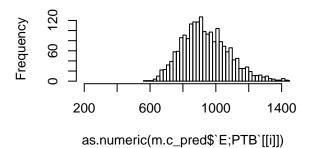


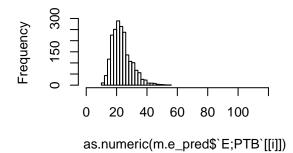


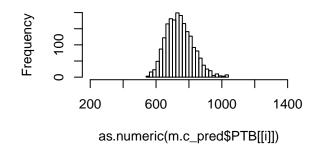


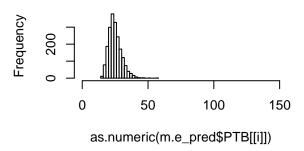


## Negative

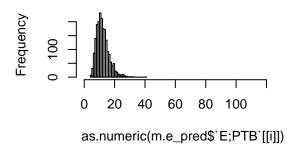


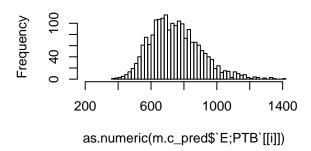


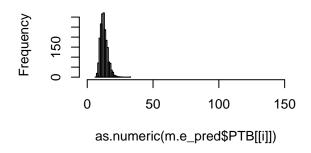


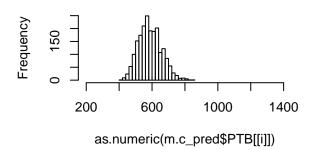


## Positive



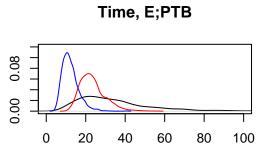






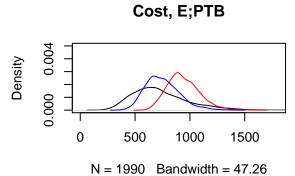
## All smear results on same plot.

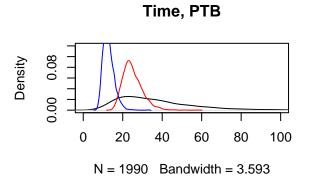
Black - Not taken, Red - Negative, Blue - Positive.

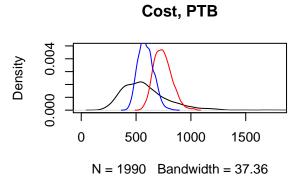


Density

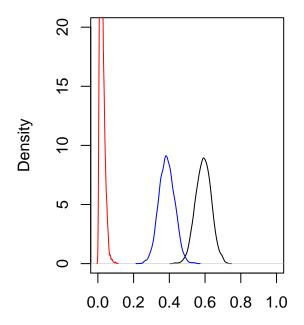
N = 1990 Bandwidth = 3.187





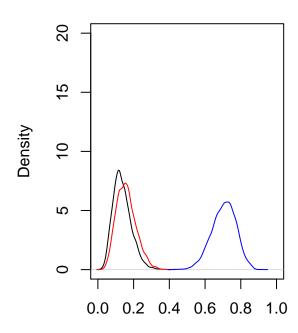






N = 3980 Bandwidth = 0.007473

# SSM prob, E;PTB



N = 3980 Bandwidth = 0.008606

ssm	tb status	mean prob	sd prob	mean cost	sd cost	mean time	sd time
Not taken	E;PTB	0.14	0.05	731.76	261.20	34.61	20.29
Not taken	PTB	0.59	0.04	581.95	206.12	37.59	23.00
Negative	E;PTB	0.16	0.05	939.68	147.53	23.48	6.47
Negative	PTB	0.02	0.01	743.43	81.75	24.97	4.95
Positive	E;PTB	0.70	0.04	749.46	153.40	12.18	4.15
Positive	PTB	0.39	0.04	588.51	69.60	12.76	2.76