The Longest Increasing Subsequence

by vkristijan

Problem Submissions Leaderboard Discussions

An Introduction to the Longest Increasing Subsequence Problems

The task is to find the length of the longest subsequence in a given array of integers such that all elements of the subsequence are sorted in ascending order. For example, the length of the LIS for { 15, 27, 14, 38, 26, 55, 46, 65, 85 } is 6 and the longest increasing subsequence is {15, 27, 38, 55, 65, 85}.

Here's a great Youtube video of a lecture from MIT's Open-Coursware, covering the topic.

Here is one approach which solves this in quadratic time using dynamic programming. A more efficient algorithm which solves the problem in N Log N time is available here.

In this challenge you simply have to find the length of the longest strictly increasing sub-sequence of the given sequence.

Input Format

In the first line of input, there is a single number *N*.
In the next N lines input the value of *a[i]*.

Constraints
$1 \le N \le 10^6$
$1 \le a[i] \le 10^5$

Output Format

In a single line, output the length of the longest increasing sub-sequence.

Sample Input

```
5
2
7

4
3
8
```

Sample Output

```
3
```

Explanation

{2,7,8} is the longest increasing sub-sequence, hence the answer is 3 (the length of this sub-sequence).


```
using System;
using System.Collections.Generic;
using System.Linq;
using System.Text;

class Solution {


    // Binary search (note boundaries in the caller)
        static int CeilIndex(List<int> v, int l, int r, int key)
        {
            while (r - l > 1)
            {
                int m = l + (r - l) / 2;
                if (v[m] >= key)
                    r = m;
                else
                    l = m;
            }

            return r;
        }

        static int LongestIncreasingSubsequenceLength(List<int> v)
        {
            if (v.Count == 0)
                return 0;

            List<int> tail = new List<int>();
            for (int i = 0; i < v.Count; i++)
            {
                tail.Add(0);
            }
            int length = 1; // always points empty slot in tail

            tail[0] = v[0];
            for (int i = 1; i < v.Count; i++)
            {
                if (v[i] < tail[0])
                    // new smallest value
                    tail[0] = v[i];
                else if (v[i] > tail[length - 1])
                    // v[i] extends largest subsequence
                    tail[length++] = v[i];
                else
                    // v[i] will become end candidate of an existing subsequence or
                    // Throw away larger elements in all LIS, to make room for upcoming grater elements than v[i]
                    // (and also, v[i] would have already appeared in one of LIS, identify the location and replace it)
                    tail[CeilIndex(tail, -1, length - 1, v[i])] = v[i];
            }

            return length;
        }


        static void Main(string[] args)
        {

               //List<int> v = new List<int>(new int[]{ 2, 5, 3, 7, 11, 8, 10, 13, 6 });
               //Console.WriteLine(LongestIncreasingSubsequenceLength(v));
```

```
62              int n = int.Parse(Console.ReadLine());
63
64              int[] a = new int[n];
65              for (int i = 0; i < n; i++)
66              {
67                  a[i] = int.Parse(Console.ReadLine());
68              }
69
70              Console.WriteLine(LongestIncreasingSubsequenceLength(a.ToList()));
71
72              Console.ReadLine();
73          }
74
75
76  }
```

Line: 5 Col: 1

Upload Code as File Test against custom input Run Code Submit Code

Congrats, you solved this challenge!

- ✔ Test Case #0
- ✔ Test Case #1
- ✔ Test Case #2
- ✔ Test Case #3
- ✔ Test Case #4
- ✔ Test Case #5
- ✔ Test Case #6
- ✔ Test Case #7
- ✔ Test Case #8
- ✔ Test Case #9

Next Challenge