## MATH 308 Assignment 3 Exercises 1.11

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 $\mathbf{2}$ 

**a**)

Observational study.

b)

No, because it is possible that people without dementia are predisposed to drinking alcohol.

3

a)

Observational study.

b)

No, because it is likely that students who already use marijuana would be interested in listening to music that had references to marijuana.

 $\mathbf{c})$ 

No, because the study sample was not collected in a controlled, randomized fashion. Further, it excludes students who are not in high school.

5

Number of unique subsets of size N is  $\binom{N}{n}$ . The number of unique subsets that include a given  $\,$  a half-chance of being in no samples. So, if t samples

individual is  $\binom{N-1}{n-1}$ . :. Required probability

$$= \binom{N-1}{n-1} / \binom{N}{n}$$

$$= \frac{(N-1)!}{(N-n)!(n-1)!} \times \frac{(N-n)!n!}{N!}$$

$$= \frac{(N-1)!}{N!} \times \frac{n!}{(n-1)!}$$

$$= \frac{n}{N} \quad \Box$$

This formula does not change with the individual. Therefore, by symmetry, every person has an equal chance of being in the group.

6 **a**)

From (5), with  $N = 10^8$  and  $n = 10^3$ , required probability  $p = n/N = 10^{-5}$ .

b)

Probability of not being in any of 2000 independently chosen samples =  $(1 - p)^{2000} \approx 98\%$ .

**c**)

A half-chance of being in at least one sample implies

are chosen,

$$q^{t} = 0.5$$

$$\Rightarrow t \log q = \log 0.5$$

$$\Rightarrow t = \frac{\log 0.5}{\log(1 - 10^{-5})}$$

$$= 69315$$