

pCMFD for RM

October 30, 2019

Abstract

Following Daniele Tomatis's notes.

1 Theoretical background

The partial currents are defined according to (Duderstadt 1979):

$$\mathbf{J}^\pm(x) \approx \frac{\phi(x)}{4} \pm \frac{\mathbf{J}^D(x)}{2} , \quad (1)$$

Adding the partial currents (surface) correction factors

$$\mathbf{J}_{i+1/2}^\pm = \frac{1}{4}\phi_{i+1/2} \pm \frac{1}{2}\mathbf{J}_{i+1/2}^D \pm \frac{1}{2}\delta\mathbf{J}_{i+1/2}^\pm , \quad (2)$$

where

$$\mathbf{J}_{i+1/2}^D = -2D_{i+1/2} \frac{\phi_{i+1} - \phi_i}{\Delta_{i+1} + \Delta_i} \quad (3)$$

$$D_{i+1/2} \equiv \frac{\Delta_i D_i + \Delta_{i+1} D_{i+1}}{\Delta_i + \Delta_{i+1}} \quad (4)$$

$$\phi_{i+1/2} \equiv \frac{\Delta_i \phi_i + \Delta_{i+1} \phi_{i+1}}{\Delta_i + \Delta_{i+1}} . \quad (5)$$

Substituting

$$\frac{1}{2}\delta\mathbf{J}_{i+1/2}^+ \equiv -\delta D_{i+1/2}^+ \phi_i \quad (6)$$

$$\frac{1}{2}\delta\mathbf{J}_{i+1/2}^- \equiv -\delta D_{i+1/2}^- \phi_{i+1} , \quad (7)$$

yields for CCFs

$$\mathbf{J}_{i+1/2}^+ = \frac{1}{4}\phi_{i+1/2} + \frac{1}{2}\mathbf{J}_{i+1/2}^D - \delta D_{i+1/2}^+ \phi_i \quad (8)$$

$$\mathbf{J}_{i+1/2}^- = \frac{1}{4}\phi_{i+1/2} - \frac{1}{2}\mathbf{J}_{i+1/2}^D + \delta D_{i+1/2}^- \phi_{i+1} . \quad (9)$$

Recall that \mathbf{J}^\pm are calculated using the integral expression. Solving for CCFs

$$\delta D_{i+1/2}^+ = \frac{\frac{1}{4}\phi_{i+1/2} + \frac{1}{2}\mathbf{J}_{i+1/2}^D - \mathbf{J}_{i+1/2}^+}{\phi_i} \quad (10)$$

$$\delta D_{i+1/2}^- = \frac{-\frac{1}{4}\phi_{i+1/2} + \frac{1}{2}\mathbf{J}_{i+1/2}^D + \mathbf{J}_{i+1/2}^-}{\phi_{i+1}} \quad (11)$$

In case the diffusion current is accurate, the CCFs should vanish and Eqs. (??)–(??) reduces back to Eq. (??), as expected, which imply for the total (accurate) current

$$\mathbf{J}_{i+1/2} = \mathbf{J}_{i+1/2}^+ - \mathbf{J}_{i+1/2}^- = \mathbf{J}_{i+1/2}^D \quad (12)$$

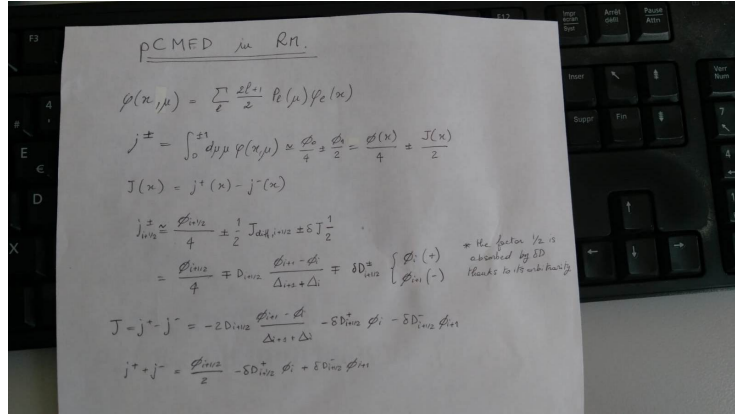


Figure 1: Tomatis's notes.

2 Numerical implementation