DESCRIBING DATA

Research Methods in Psychology I & II • Department of Psychology • Colorado State University

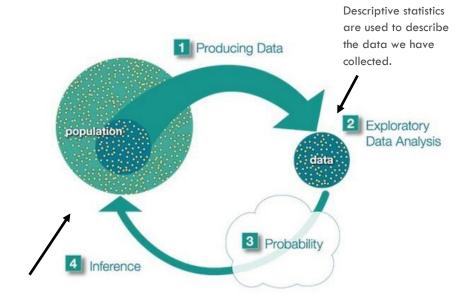
BY THE END OF THIS SECTION YOU WILL HAVE A REFRESHED MEMORY ON:

- The difference between descriptive and inferential statistics.
- Methods for describing central tendency.
- 3. Methods for describing variability.
- The normal distribution, z-scores, and the empirical rule.

Descriptive & Inferential Statistics

Descriptive statistics are used to organize, summarize, simplify, and present data — usually about a sample that we have collected from a population. Inferential statistics are used to generalize from our sample to the larger population, to test hypotheses, and to make predictions (and understand the accuracy of those predictions).

In this unit we will focus on descriptive statistics, in Unit 3, we will focus on inferential statistics.



Inferential statistics are used to make inferences or generalizations about the population based on our sample.

Image produced by Carnegie Melon University, Open Learning Institute.

Unit 2: Visualizing, Wrangling & Describing Data

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Height of Adult Males and Females in the US

In this section we will learn about descriptive statistics and related topics using data from the National Health and Nutrition Examination Study that were collected during 2011-2012 by the CDC. We will consider the height of the participants in the study. The 5,000 individuals in the dataframe are resampled from the larger NHANES study population to mimic a simple random sample, so the data are representative of the total US population.

The data are in the Unit 2 folder in dropbox, the file is called nhanes.csv. There is also a file called nhanes data dictionary which summarizes these data. Please copy both of these into your MyClassActivities folder. Next, open up your MyClassActivities project in RStudio, and then create a new R Notebook. Call this Notebook: Describing_Height_Notebook.

To begin our notebook, add the following two code chunks. Notice that you need to install two new packages — descriptr and mosaic. Once you execute this code chunk, you can put a hashtag in front of install.packages so R doesn't reinstall each time you execute this chunk.

```
Describing_Height_Notebook.Rmd* **
     1 - --
     title: "R Notebook for Heights of Men and Women in the US"
   2
   3
      output:
   4
       pdf_document: default
       html_notebook:
   6
         theme: readable
       html_document: default
  8
  9
  10
     In this notebook we will learn about descriptive statistics and related topics using data from the National Health and
      Nutrition Examination Study collected during 2011-2012. These data are collected by the CDC. The 5,000 individuals
      in the dataframe used here are resampled from the larger NHANES study population to mimic a simple random sample, so
      it is representative of the total US.
  11
  12
  13 - # Install and load libraries
                                                                                                                 14 -
        `{r, message = FALSE}
  15
  16
     library(tidyverse)
  17
  18
      #install.packages("descriptr")
  19
     library(descriptr)
  20
      #install.packages("mosaic")
  21
  22
     library(mosaic)
  23
  24
  25
  26
    # Import the data
  27 -
        `{r, message = FALSE}
  28
  29
      nhanes <- read_csv("nhanes.csv")</pre>
  30
  31
```

Prepare the Dataframe for Exploration

Let's begin by transforming Height, which is expressed in cm, to a new variable called ht_inches that is expressed in inches. We will also create a new variable called sex, that is a copy of gender, and we will specify it to be a factor. We are interested here in only adults (i.e., people who are likely done growing), so we will use filter to choose only people 20 years or older. Last, we will subset to keep just the variables we will use today. Let's do all of this with a pipe.

```
height <- nhanes %>%

filter(Age >= 20) %>%

mutate(ht_inches = Height/2.54, sex = factor(Gender)) %>%

select(ht_inches, sex) %>%

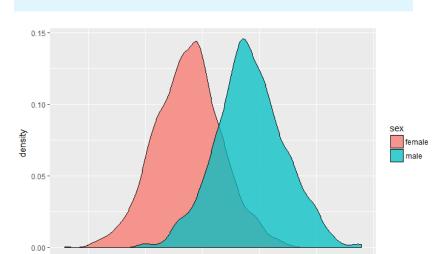
na.omit()
```

na.omit() takes the height dataframe and removes all rows with missing data on any of the variales — i.e., ht_inches and sex, since we subsetted to include just these variables in the prior step.

Create a Density Plot of Height by Sex

As a first step in describing height, we will create a density plot of height, and group our plot by sex. This will give us an idea of the distribution of height among adult males and females.

```
ggplot(height, aes(x = ht_inches, group = sex, fill = sex)) +
    geom_density(alpha = .75)
```



ht inches

70

60

As we would expect, males are, on average, taller than females.

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Descriptive Statistics: Central Tendency & Dispersion

When we approach a new analysis, we typically begin by examining the distribution of our variables. For a continuous variable (like the height of people), assessment of central tendency and dispersion is a good place to start.

A measure of central tendency captures a central or typical value for the distribution of the variable. Common measures of central tendency include the arithmetic mean, the median, and the mode.

Dispersion describes the extent to which a distribution is stretched or squeezed. Common measures of dispersion are the variance, the standard deviation, the range, and interquartile range.

For a thorough display of measures of central tendency and dispersion, I like the descriptr package.

Let's use the summary_stats function to obtain descriptive statistics for ht_inches.

In many R functions, a "data =" argument is not available, and in these cases, we need to specify the name of the dataframe and the variable of interest inside the dataframe using the following convention:

data_frame_name\$variable_name

861

497

920

Where data frame name is the name of your dataframe, and variable name is the name of your variable.

summary_stats(height\$ht_inches)

		Univariate /	Analvsis				
N Missing Mean Median Mode Trimmed Mean Skewness Kurtosis		3561.00 0.00 66.47 66.46 68.19 66.45 0.06 -0.35	Variance Std Deviation Range Interquartile Range Uncorrected SS Corrected SS Coeff Variation Std Error Mean	15790421.91 57380.15			
Quantiles							
	Quantile			Value			
	Max 99% 95% 90% Q3 Median Q1 10% 5% 1% Min			78.90 75.16 71.73 73.15 69.29 66.46 63.54 61.26 60.08 57.68 52.95			
Extreme Values							
	Low			нigh			
obs		Value	obs	Value			

3364

3365

748

1586

1587

78.8976377952756

78.8976377952756

78.7007874015748

78.503937007874 78.503937007874

52.9527559055118

55.1181102362205

55.5905511811024

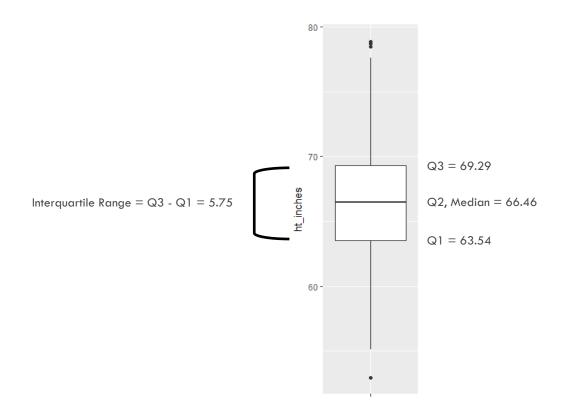
55.5905511811024

55.6299212598425

Measures of Central Tendency

Mean	The average value. The mean can be highly affected by outliers.	
Median	The central value of an ordered distribution.	
Mode	The value that occurs most often.	
Trimmed Mean	Extreme cases are discarded, and the average is computed on the remainder. The descriptr package trims the lowest 5% of cases and the highest 5% of cases.	

A boxplot displays many of the key descriptive statistics.

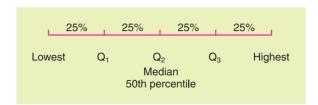


In R, the default is for the whiskers to extend to the extremes (min and max), but no further than 1.5 times the IQR (i.e., 1.5 = IQR = 1.5 = 5.75 = 8.63) above Q3 or 1.5 times the IQR below Q1. In other words, the upper whisker is located at the **smaller** of the maximum y value and Q3 + 1.5 IQR, and the lower whisker is located at the **larger** of the smallest y value and Q1 - 1.5 IQR. You can change this behavior with the range argument in geom_boxplot. An outlier (the individual points that you see) is a value that is outside of the defined whiskers. Therefore the boxplot also displays that minimum and maximum values.

Measures of Dispersion

Range	The difference between the largest and smallest value (max - min = range)
Quantile Scores	Quantiles are the values of a variable that divide a distribution into equal parts. Quartiles are commonly used. Quartiles divide the distribution into 4 equals parts. The first quartile Q1 is the 25th percentile, the second quartile Q2 is the median, and the third quartile Q3 is the 75th percentile. See the Quartiles figure below.
Variance	The average of the squared differences between each value and the mean. It captures how far a set of numbers are spread out from the mean.
Standard Deviation (SD)	The square root of the variance.
Uncorrected SS (Sum of Squares)	Sum of the squared values.
Corrected SS	Sum of the squared differences between each value and the mean.
Coefficient of Variation	The ratio of the standard deviation to the mean, expressed as a percentage, so (SD/Mean) = 100. It captures the extent of variability of the variable in relation to the mean.
Skewness	Measures the degree and direction of asymmetry in the distribution of the variable. A symmetric distribution has a skewness of 0. A distribution that is skewed to the left (i.e., the mean is less than the median) has a negative skewness, while a distribution that is skewed to the right has a positive skewness. See skewness figure below.
Kurtosis	Measures the heaviness of the tails of a distribution. Given the way kurtosis is scaled here (type 1), a normal distribution has kurtosis 0. Kurtosis is positive if the tails are heavier than for a normal distribution (leptokurtic) and negative if the tails are lighter than for a normal distribution (platykurtic). See Kurtosis figure below.
Standard Error of the Mean	The estimated standard deviation of the sampling distribution. This isn't a descriptive statistic, but rather an inferential statistic. We'll cover this in the next unit.

Quartiles



Skewness

The coefficient of Skewness is a measure for the degree of symmetry in the variable distribution.



or Skewed to the left Skewness <0

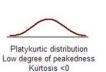




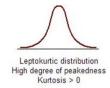
Positively skewed distribution or Skewed to the right Skewness > 0

Kurtosis

The coefficient of Kurtosis is a measure for the degree of peakedness/flatness in the variable distribution.







Descriptive Statistics for Height by Sex

Let's request descriptive statistics for males and females separately.

group_summary(height\$ht_inches, fvar = height\$sex)

ht_inches by sex

Statistic/Levels	female	male
Obs	 1784	1777
Minimum	52.95	59.88
Maximum	72.64	78.9
Mean	63.76	69.19
Median	63.82	69.02
Mode	63.27	68.19
Std. Deviation	2.91	3.01
Variance	8.45	9.08
skewness	0.01	0.06
Kurtosis	0.09	0.12
Uncorrected SS	7268321	8522101
Corrected SS	15071.59	16127.44
Coeff Variation	4.56	4.36
Std. Error Mean	0.07	0.07
Range	19.69	19.02
Interquartile Range	3.83	3.74

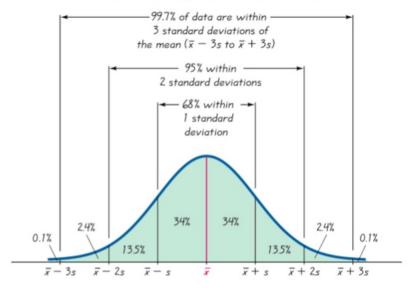
What is a Normal Distribution and Why is it Important?

A random variable with a Gaussian (e.g., bell-shaped) distribution is said to be normally distributed. A normal distribution is a symmetrical distribution. The mean, median and mode are in the same location and at the center of the distribution. The empirical rule provides a quick estimate of the spread of data in a normal distribution given the mean and standard deviation. Specifically, the empirical rule states that for a normal distribution:

- 68% of the data will fall within about one standard deviation of the mean.
- 95% of the data will fall within about two standard deviations of the mean.
- Almost all (99.7%) of the data will fall within about three standard deviations of the mean.

The empirical rule helps us to gain a sense of the distribution of scores in our dataframe. For example, if all we knew was that the average height for a female is 63.76 inches, with a standard deviation of 2.91, we would know that about 95% of all females are between 57.95 inches and 69.58 inches (that is, $63.76 \pm 2 = 2.91$). This premise will serve as the basis for the inferential statistics that we will cover this semester, so it is important to understand.

The Empirical Rule



Simulate and Explore a Normal Distribution

We can use the rnorm function in R to simulate data according to a normal distribution. Here, we create a sample of size 10,000, with a mean of 0 and a standard deviation of 1. We can plot the data to confirm that the distribution is normal. Finally, we can compute the number of cases within 1 SD, 2 SDs, and 3SDs from the mean, and then summarize these new variables to see what proportion of cases fall into each range.

```
set.seed(12345)

myvar <- rnorm(n=10000, m=0, sd=1)

example <- data.frame(myvar)

ggplot(example, aes(x = myvar)) +

geom_histogram(binwidth = .1)

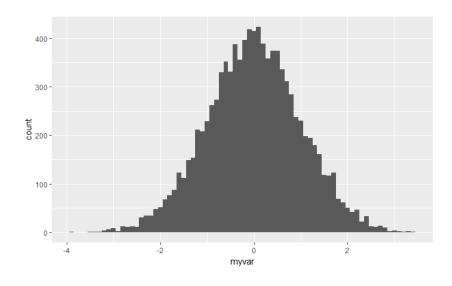
example <- example %>%

mutate(within1 = ifelse(myvar <= 1 & myvar >= -1, 1, 0),

within2 = ifelse(myvar <= 2 & myvar >= -2, 1, 0),

within3 = ifelse(myvar <= 3 & myvar >= -3, 1, 0))

summarize(example, prop_within1 = mean(within1), prop_within2 = mean(within2), prop_within3 = mean(within3))
```

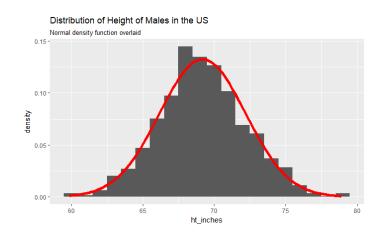


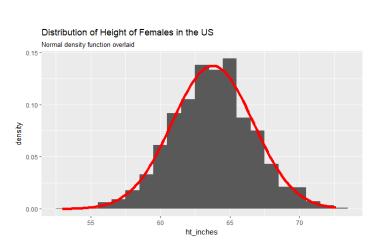
prop_within1	prop_within2	prop_within3
<dbl></dbl>	<dbl></dbl>	<dbl></dbl>
0.684	0.9528	0.9975

Do these match what we would expect based on the empirical rule?

Compare our Distributions to a Normal Distribution Function

```
# for males
males <- filter(height, sex == "male")
qqplot(males, aes(x = ht inches)) +
 geom histogram(aes(y = ..density..), binwidth = 1) +
 stat function(fun = dnorm,
          args = list(mean = mean(males$ht_inches), sd = sd(males$ht_inches)),
          lwd = 2,
          col = 'red') +
 labs(title = "Distribution of Height of Males in the US", subtitle = "Normal density function overlaid")
# for females
females <- filter(height, sex == "female")
ggplot(females, aes(x = ht_inches)) +
 geom_histogram(aes(y = ..density..), binwidth = 1) +
 stat_function(fun = dnorm,
          args = list(mean = mean(females$ht_inches), sd = sd(females$ht_inches)),
          lwd = 2,
          col = 'red') +
 labs(title = "Distribution of Height of Females in the US", subtitle = "Normal density function overlaid")
```





Both of the height distributions match a normal distribution very well. When this is the case, then we can use the principles of the empirical rule to consider the expected number of cases in various parts of the distribution. For example:

What percentage of males do we expect to be shorter than 65 inches?/What's the probability that we would randomly select a male from the population who is shorter than 65 inches?

What percentage of females do we expect to be between 60 and 70 inches tall?/What's the probability that we would randomly select a female from the population who is between 60 and 70 inches tall?

Where are You on the Distribution of Height?

```
# for females

females <- filter(height, sex == "female")

ggplot(females, aes(x = ht_inches)) +

geom_histogram(aes(y = ..density..), binwidth = 1) +

stat_function(fun = dnorm,

args = list(mean = mean(females$ht_inches), sd = sd(females$ht_inches)),

lwd = 2,

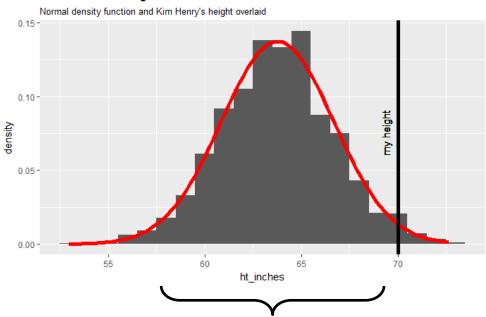
col = 'red') +

geom_vline(xintercept = 70, colour = "black", lwd = 2) +

geom_text(aes(x=70, label="my height", y=.075), colour="black", angle=90, vjust = -1, text=element_text(size=11)) +

labs(title = "Distribution of Height of Females in the US", subtitle = "Normal density function and Kim Henry's height overlaid")
```

Distribution of Height of Females in the US



The empirical rule tells us that about 95% of females will be within 2 standard deviations of the mean, so 57.95 inches to 69.58 inches. Only about 2.5% of the population is likely to be shorter than 57.95, and only about 2.5% of the population is likely to be taller than 69.58 inches.

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Raw Scores and Z-Scores

A Z-Score is a standardized score based on some raw variable (e.g., height in inches, ht_inches) that has been transformed by first subtracting the mean, and then dividing by the standard deviation. Let's consider Kim Henry's height (70 inches):

$$Z$$
-Score = (70 - 63.76) / 2.91 = 2.15

So, Kim Henry is 2.15 standard deviations above the mean height for females. What is your Z-Score for height?

```
mean_m <- mean(males$ht_inches)

sd_m <- sd(males$ht_inches)

mean_f <- mean(females$ht_inches)

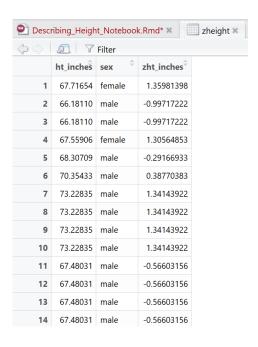
sd_f <- sd(females$ht_inches)

myzscore <- (70 - mean_f)/sd_f
```

[1] 2.145213

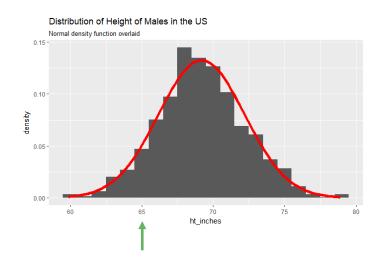
We can use the mosaic package to convert the raw scores to Z-Scores in the NHANES data. Because we use group_by first, then the sex specific mean and sd is used to form the Z-Scores for males and females respectively.

```
zheight <- height %>%
group_by(sex) %>%
mutate(zht_inches = zscore(ht_inches)) %>%
ungroup()
```



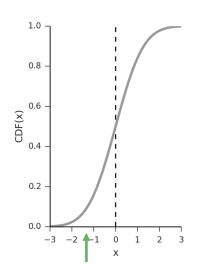
The Cumulative Distribution Function

The cumulative distribution function (cdf) is the probability that a variable takes on a value less than or equal to x. We can use the cdf of our normal distribution to ask a question such as "What is the probability that a randomly selected male from the population will be shorter the 65 inches tall?"





[1] 0.0823984



male65 <- (65 - mean_m)/sd_m male65

[1] -1.389118

What is the probability that a randomly selected male is taller than 80 inches?

pnorm(80, mean = mean_m, sd = sd_m, lower.tail=FALSE)

[1] 0.0001662314

What is the probability that a randomly selected male is between 70 and 75 inches?

pnorm(75, mean = mean_m, sd = sd_m, lower.tail=TRUE) - pnorm(70, mean = mean_m, sd = sd_m, lower.tail=TRUE)

[1] 0.3666908

We can use gnorm to do the inverse. Here we might ask "What height does a male need to be, to be in the top 10%?"

qnorm(.10, mean = mean_m, sd = sd_m, lower.tail=FALSE)

Let's Finish with Your Height & Z-Score

What is the probability that a randomly selected adult of your same sex will be shorter than you?

[1] 0.9840321

You can obtain the same answer using Z-Scores (notice the change to mean and sd)

myzscore <- (70 - mean_f)/sd_f

myzscore

[1] 2.145213

[1] 0.9840321

pnorm(myzscore, mean=0, sd=1, lower.tail = TRUE)