

# COMP3130 – Group Project in Computer Science

## Warm-up Project – $4 \times 4 \times 4$ TicTacToe Agent

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### 1. Abstract

The purpose of this project was to implement an intelligent agent to play 3 dimensional 4 by 4 by 4 Tic Tac Toe. We chose to implement this in C, with a pipe interface to python. This allowed us to use python's 3D libraries for visualisation while utilising the speed of a compiled C program.

### 2. Solution Overview

The core of the agent is implemented with a combination of minimax and  $\alpha$ - $\beta$  pruning. Board states are stored simply as a 3 dimensional array of chars; but this data is passed through the program as a struct including extra information such as a heuristic evaluation of the state. Once the minimax program reaches a fixed cut-off depth we select a state based on this heuristic. For testing purposes all code is compiled with the -g flag. This allows us to use the program `gprof` to analyse running time and total number of function calls (this is used to optimise and evaluate the effectiveness of  $\alpha$ - $\beta$  pruning).

Overview of Modules:

`visualisation.py`:

- The python module which takes user input and displays the game board using VPython
- This is the main program, it creates a sub-process (`worker.c`) which returns board states to display
- Contains several visualisation options: press 'g' to switch views and 's' to enable red-cyan stereoscopic 3D.

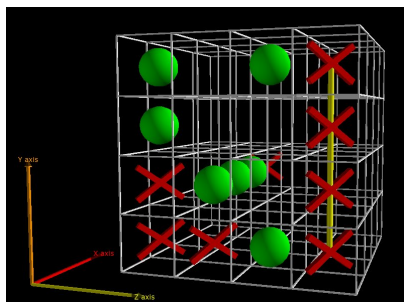


Fig 1: Example of game visualisation

`worker.c`:

- The link module which handles communication between python and C
- Calls code from `state_functions.c` to start minimax and pick the next move

`state_functions.c`:

- Contains all core functionality of the AI agent including minimax functions and state evaluation functions
- Includes a simple victory function which checks if a player has won with a line nearby to the most recent move. (comprehensive victory checks are made in `visualisation.py`)

### 3. State Space for $4 \times 4 \times 4$

In the original scope of this project we had intended to examine the entire state space before making a move. However, the state space is in fact exceedingly large. Considering all possible states we have  $3^{64}$ , but many of these (far more than half) are illegal or unreachable. A mathematical paper by Oren Patashnik<sup>[1]</sup> points out that after 18 moves (under perfect play by player 1) the game will be over or in a state where every move is forced. With this in mind we can consider a more reasonable upper bound on the states we must examine:  
 $64 \text{ choose } 18 = 3601688791018080$ .

If we assume we can examine 1 state per clock cycle (a completely and utterly unreasonable assumption) it would still take 250 hours to search this reduced state space on a 4GHz CPU. Minimax with  $\alpha$ - $\beta$  pruning and other clever tricks could significantly reduce this figure; however it remains obvious that searching to depth 18 for every move is unachievable. Thus we set a depth cut-off where we stop searching and perform a heuristic state evaluation.

Due to this inevitable cut-off it also became impossible to determine if either player has a winning strategy. It is however interesting to note that (in the paper mentioned above) Patashnik determined that the first player does in fact have a winning strategy.

#### 4. Heuristics and Cut-offs

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briefly explain heuristics and cut off decisions

#### 5. Pure Minimax vs. $\alpha$ - $\beta$ pruning

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Some tests were run using the Unix tool `gprof` to determine the effectiveness of heuristics and  $\alpha$ - $\beta$  pruning. By counting the number of calls to our state-evaluation function we get the total number of examined leaf nodes. Furthermore `gprof` returns a summary of how much time (in seconds) is spent running each function and the whole program.

The tables below summarise `gprof` results when the agent is making it's first move; run at various cut-off depths:

Total Leaf Nodes Examined:

Depth	Minimax	$\alpha$ - $\beta$	$\alpha$ - $\beta$ + Heuristics
3	16777216	283793	???
4	???	???	???
5	???	???	???

Total Time Taken (Seconds):

Depth	Minimax	$\alpha$ - $\beta$	$\alpha$ - $\beta$ + Heuristics
3	11.7	0.23	???
4	???	???	???
5	???	???	???

The benefits of  $\alpha$ - $\beta$  pruning are obvious and indisputable, often cutting the number of nodes and total time by a factor of over 100!

The benefits of our heuristic function are however less obvious. We notice a that a great deal less leaf nodes are examined; but the improvement in running time is negligible. This is due to the fact that we must constantly evaluate states for their potential value; taking precious CPU time.

#### 6. Summary and Reflection

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A Summary. Also discuss how this will prepare us for re-versi (language choice, teamwork, gitHub)

#### 7. Bibliography

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Pfft what am I; an Arts student? I don't know how to make a bibliography. Man I should get some sleep.