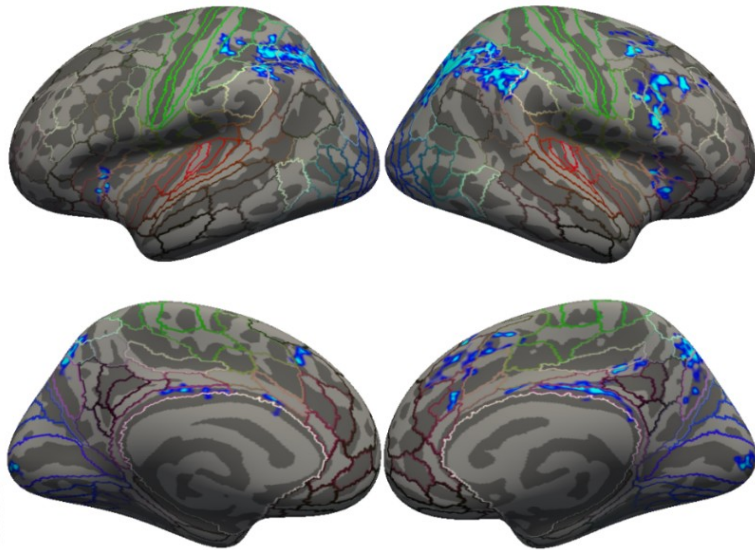




# Functional MRI and data analysis *Encoding models*

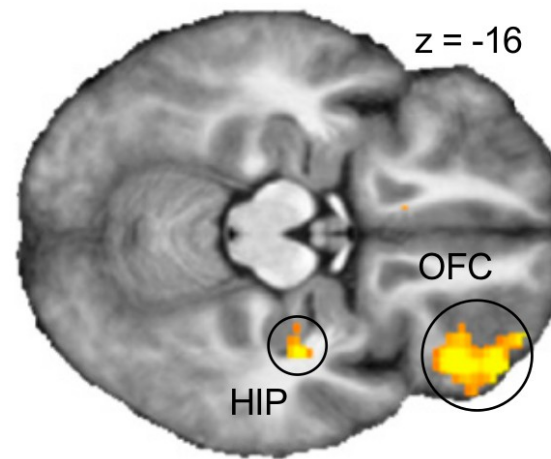
Florent MEYNIEL

Neurospin, CEA, France



*(...) brain regions where activity is significantly correlated with confidence.*

Bounmy, Eger & Meyniel (2023)  
*NeuroImage*



*(...) searchlight decoding analysis [was] used to reveal identity-specific value codes*

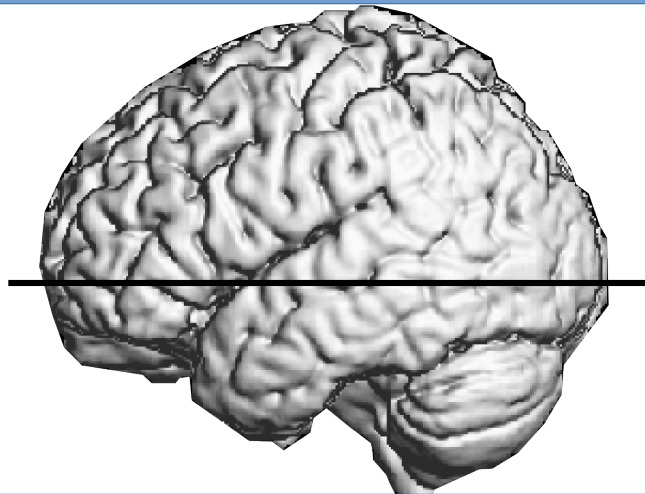
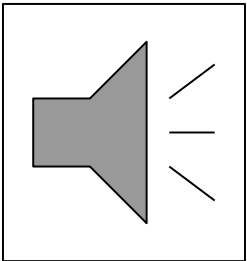
Howard, Gottfried, Tobler & Kahnt (2015)  
*PNAS*

# A general distinction: encoding vs. decoding

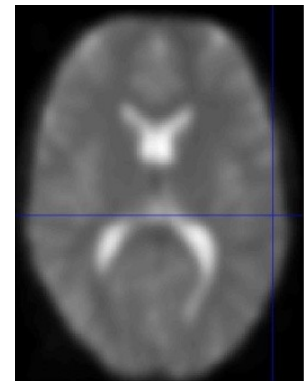
## ENCODING

What are the brain responses triggered  
by this stimulus, task, emotion ... ?  
(related to: forward models, univariate  
analysis, GLM, ...)

Task and stimuli



fMRI activity  
(gray scale)

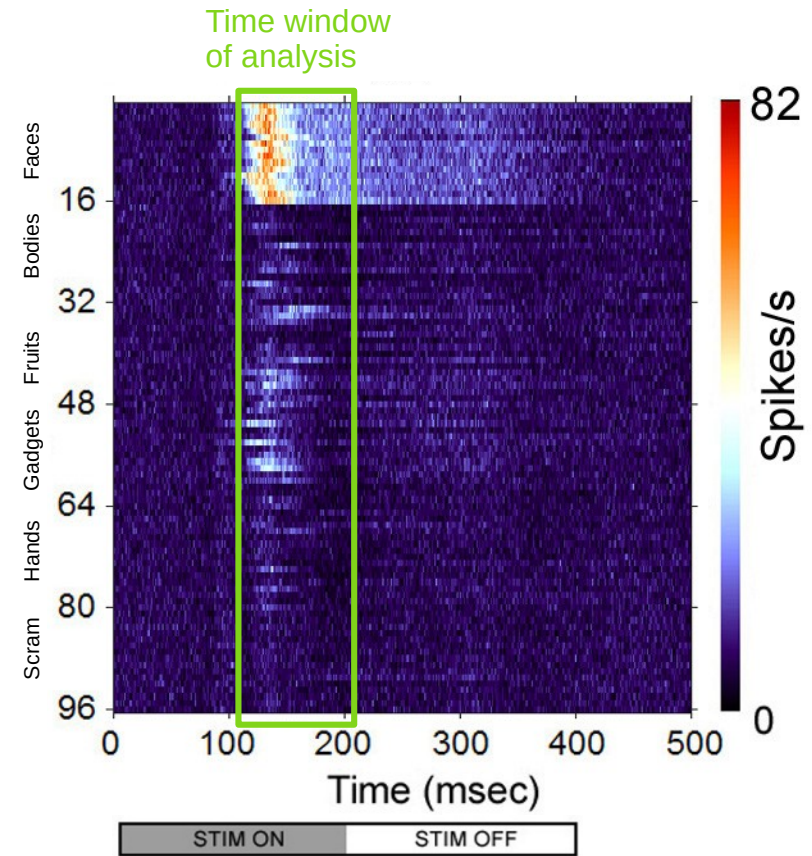
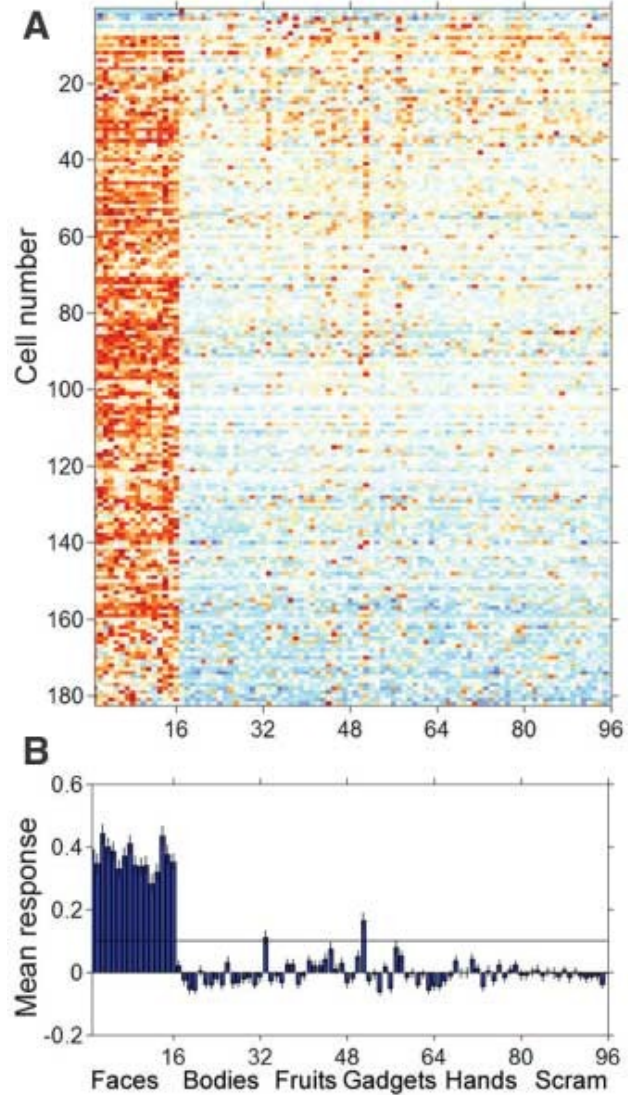


## DECODING

What is the likely cause (stimulus, task,  
emotion ...) of this brain response ?  
(related to: multivariate pattern  
analysis, search light, SVM, ...)

# Typical encoding analysis in neuroscience

Cell responses (firing rate) for each image



## **I/ Encoding: From neural activity to BOLD signal (forward model)**

The haemodynamic response function

Predicting the BOLD signal during a simple experiment

Convolution model for BOLD data

## **II/ Encoding: Testing effects with mass univariate analysis**

The regression approach: intuition and formalization

Statistical parametric mapping with mass univariate analysis

## **III/ Encoding: General Linear Model**

General linear model (GLM) and design matrix

Testing the effect of interest with “contrasts”

Categorical and parametric regressors

Subject and Group level analyses

## **IV/ The problem with multiple comparisons**

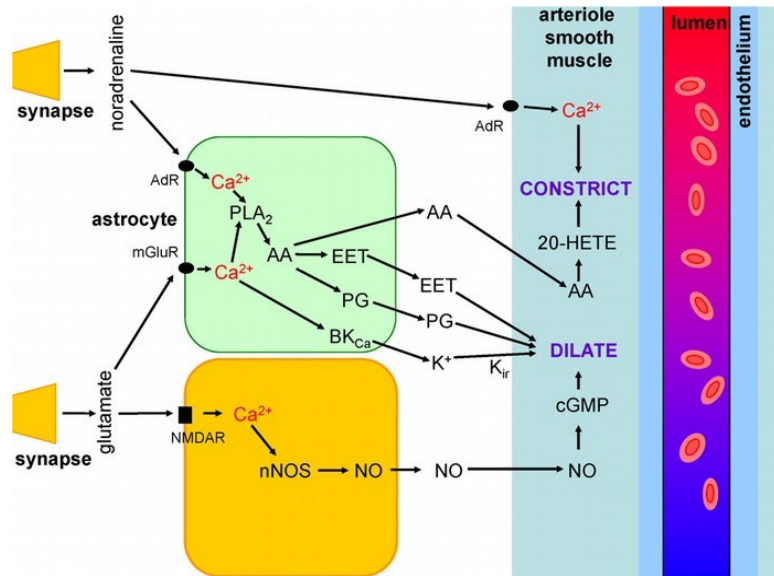
Multiple testing inflates the risk of having a false positive

Statistical methods to correct for multiple comparisons

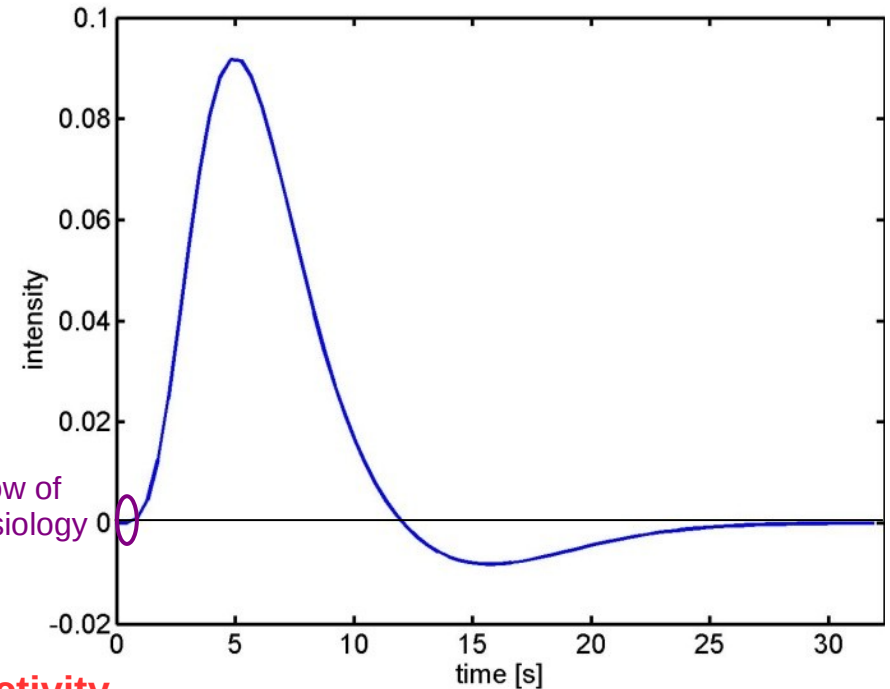
# Applying encoding analysis to fMRI signal is difficult because the fMRI signal is slow and delayed

Stimulus → Neural activity → BOLD signal

BOLD response (a.k.a. *haemodynamic response function*)



Harris, Reynell, Attwell (2011)



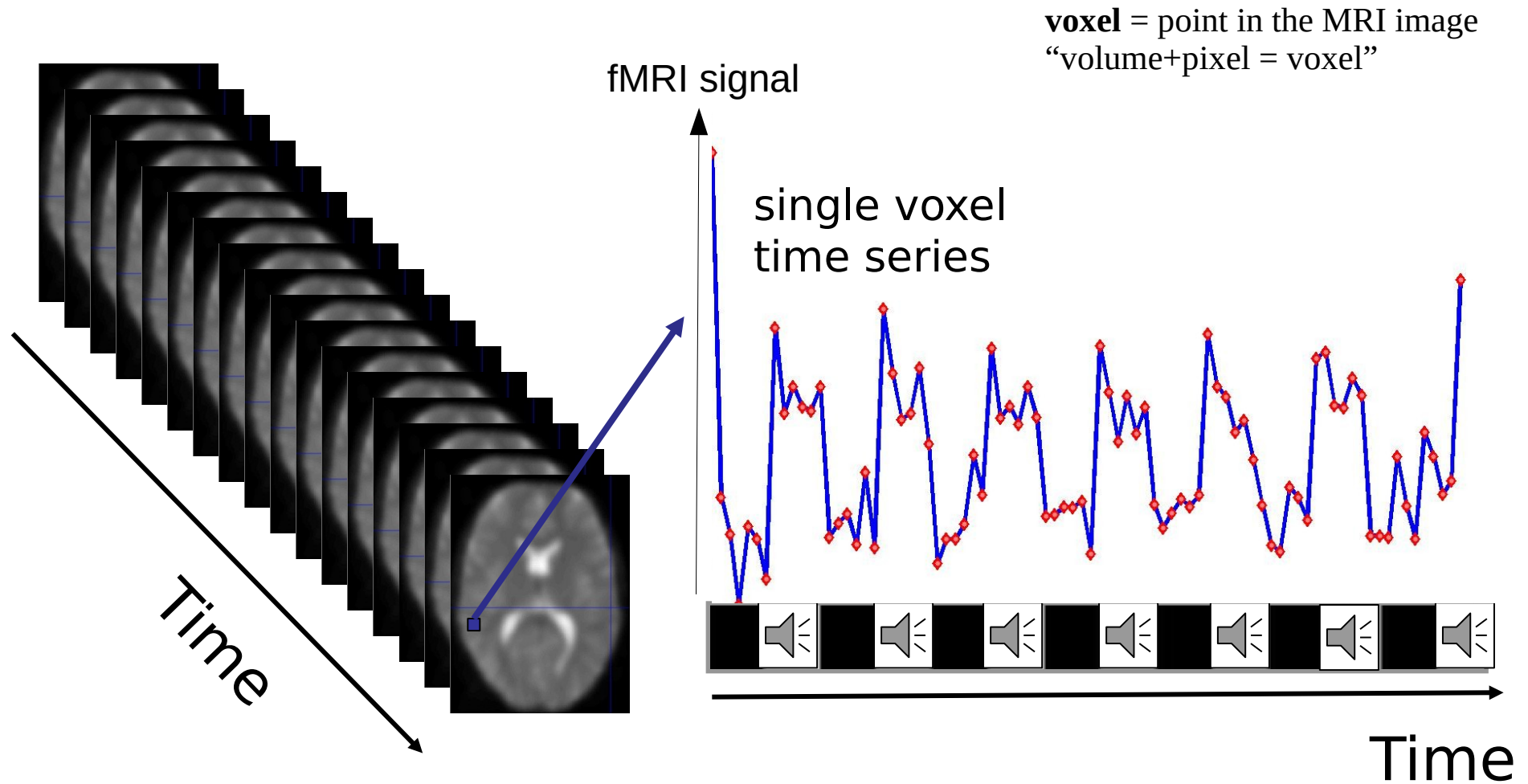
Neural activity



→ Encoding analysis of fMRI signal must be analysis of *timeseries*



# Starting with an example

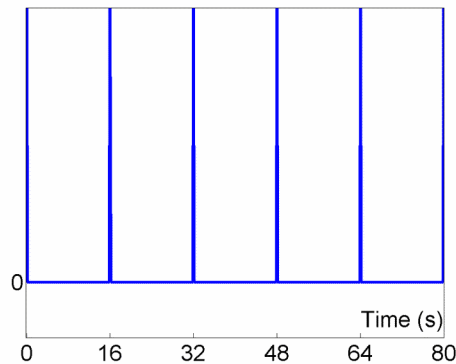


Example question: What are the brain regions (i.e. voxels) whose activity increase when a sound is played?  
fMRI data are noisy timeseries, answering this question requires modeling and a statistical approach.

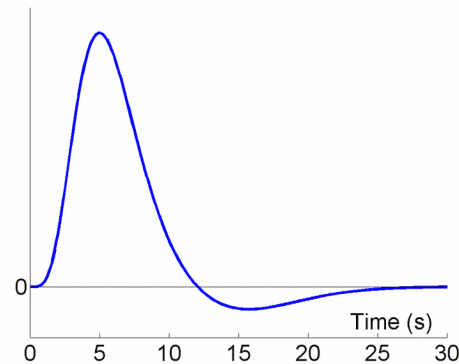
# Predicted BOLD responses in a simple experiment

Task: every 16 s, a sound is played.

Expected neuronal activity  
in the auditory cortex

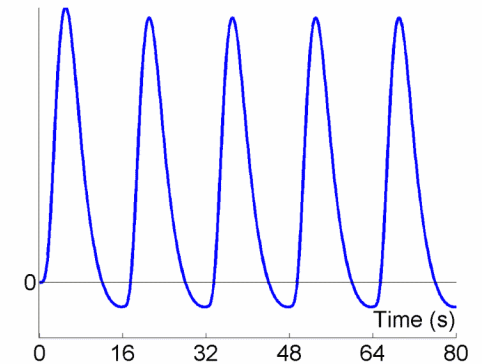


Expected BOLD response for a  
single, transient neural event



=

Expected BOLD timeseries in  
the auditory cortex

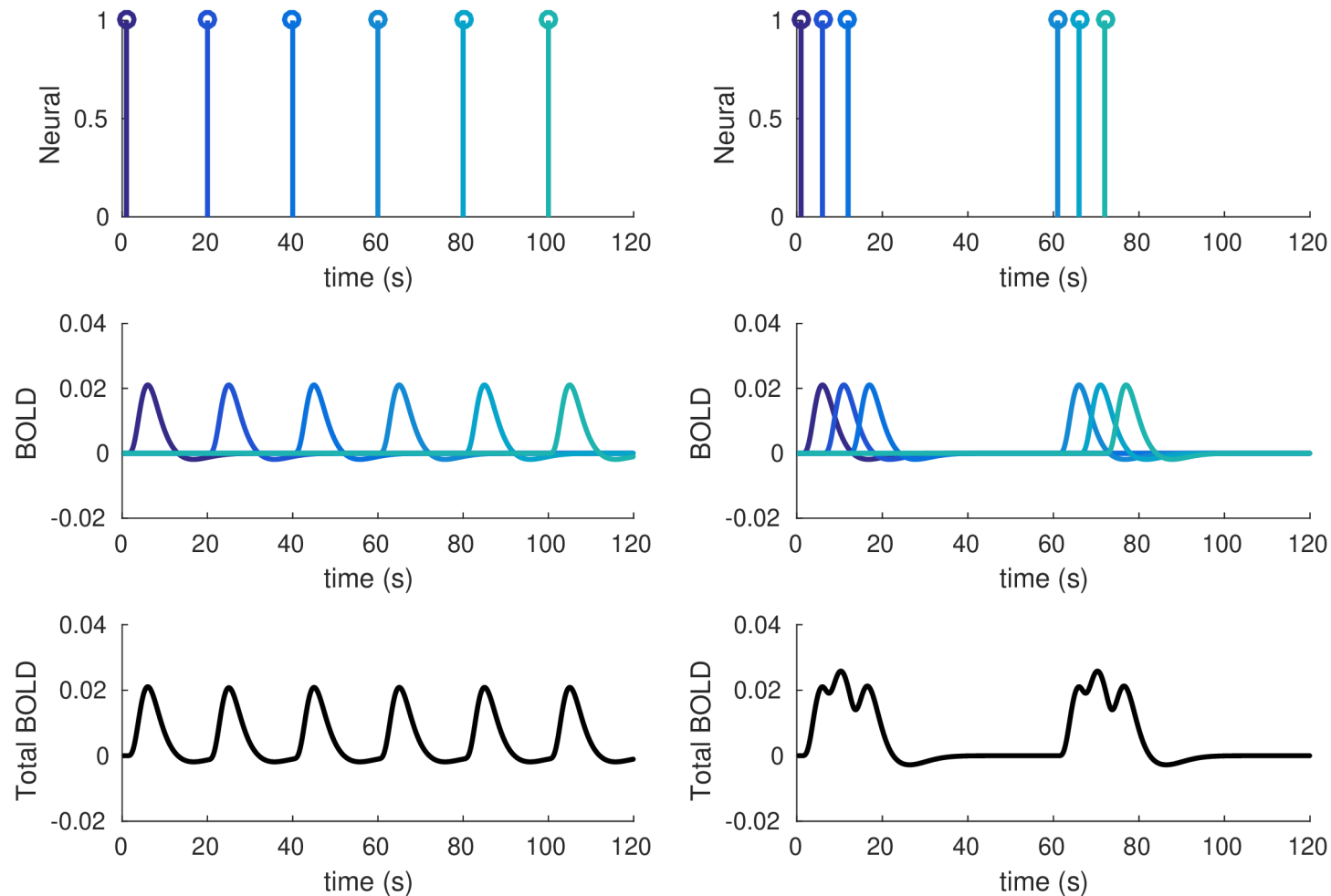


In standard fMRI analyses, we assume that the observed BOLD signal is the superposition of (= the sum of) the BOLD responses evoked by every single neural event.

Mathematically, the expected BOLD signal is therefore the timeseries of neural activity convolved with the hemodynamic response function.



# Overlap of BOLD responses in fast designs



## Implications:

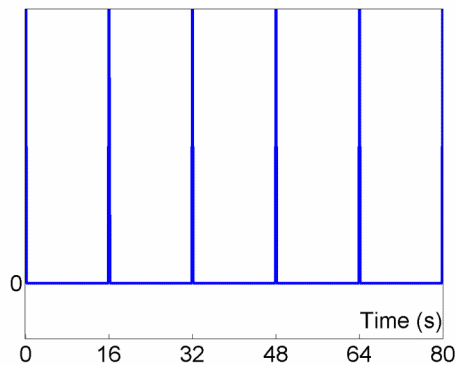
- some experimental designs are better than other (e.g. some neuronal effects may be completely smoothed out at the BOLD level)
- Even in very simple designs, events of interest generate time series of observations (sampled by each repetition of the fMRI measurement).

→ example #1 in the notebook

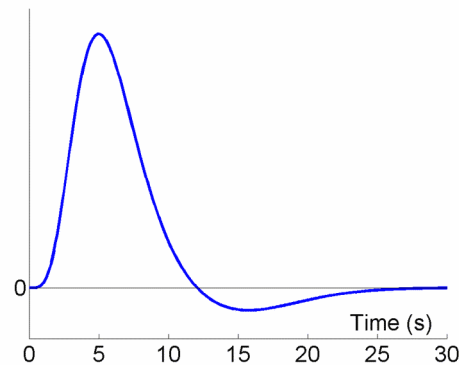
# From neuronal effects to timeseries of BOLD data: The power of forward modelling

FORWARD MODEL OF OBSERVATIONS

Expected neuronal activity in the auditory cortex

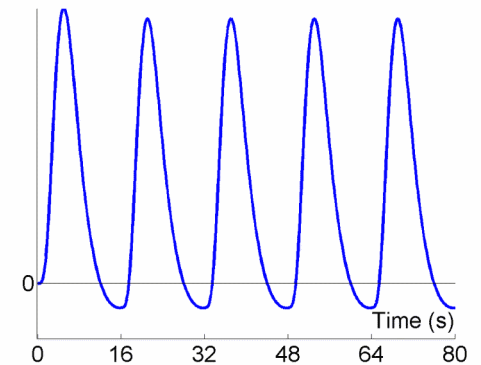


Expected BOLD response for a single, transient neural event



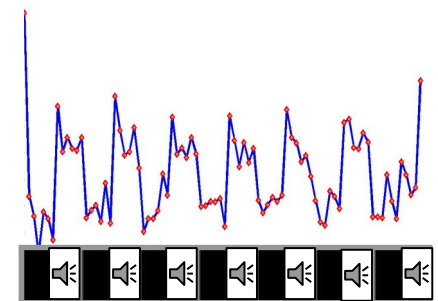
=

Expected BOLD timeseries in the auditory cortex



Match  
???

Actual data measured



## **I/ Encoding: From neural activity to BOLD signal (forward model)**

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The regression approach: intuition and formalization

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General linear model (GLM) and design matrix

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Categorical and parametric regressors

Subject and Group level analyses

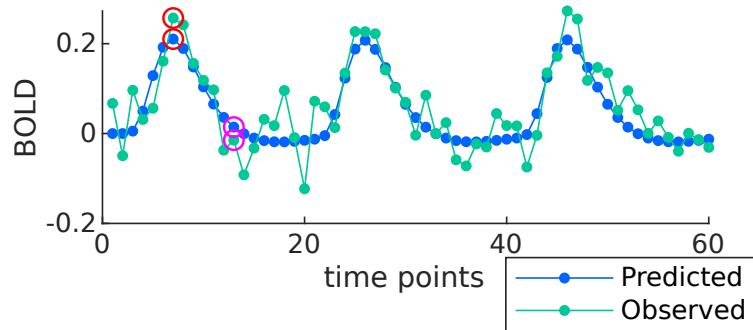
## **IV/ The problem with multiple comparisons**

Multiple testing inflates the risk of having a false positive

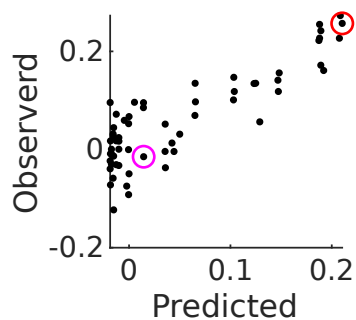
Statistical methods to correct for multiple comparisons

# From neuronal effects to timeseries of BOLD data: The regression approach

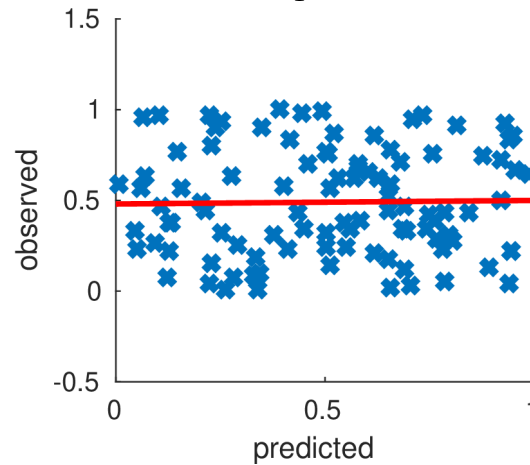
Compare predicted and observed time series



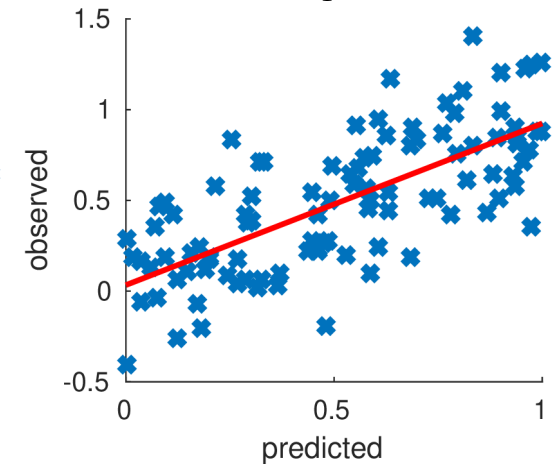
Re-plot X(t) and Y(t)  
As X vs. Y



Example: no effect  
( $\beta_1 \approx 0$ )



Example: an effect!  
( $\beta_1 \neq 0$ )



Observed data

Predicted value

Error (what is not captured by the prediction)

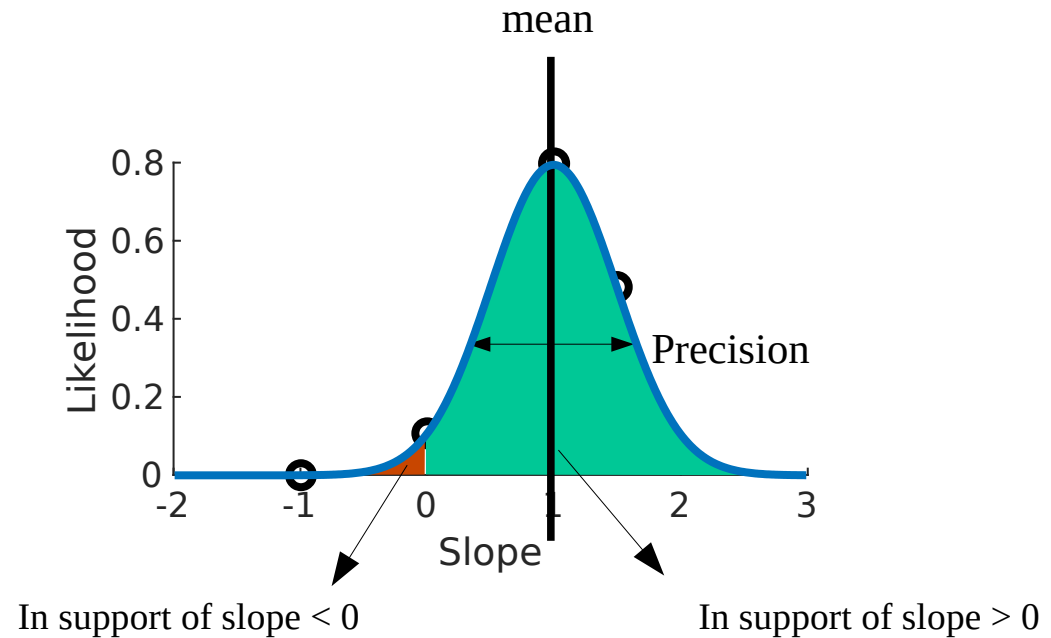
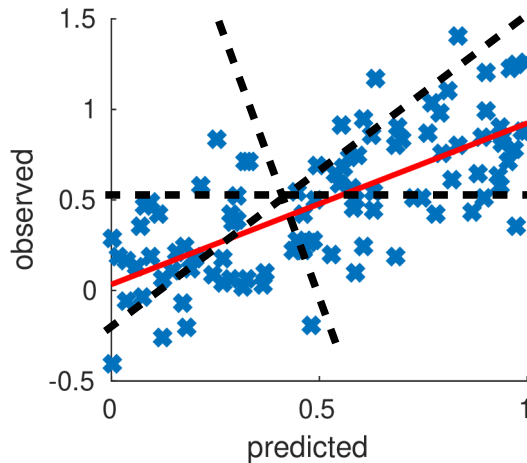
$$y = \beta_0 + \beta_1 x_1 + \varepsilon$$

“intercept”

“slope”

# Quantifying the significance of a regression

## The Student T-test: a signal-to-noise measure to quantify “Is $\beta$ different from 0 ?”



The Student T-test tests whether the (central) value of a noisy variable, observed through a limited number of data points (X), is non-zero.

T-value =  $\beta / SE[\beta]$  : more extreme values indicate that  $\text{mean}(X) \neq 0$

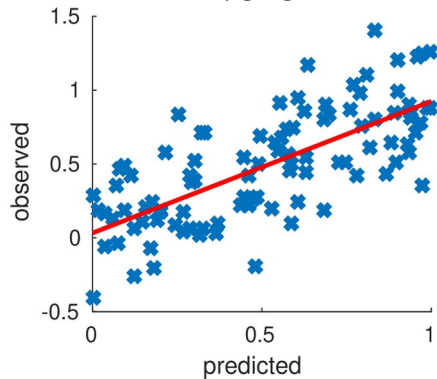
estimated  
slope

standard error of the slope  
= ratio of standard deviations of  
residuals and predictor, weighted  
by the number of observations

$$\frac{1}{\sqrt{n-2}} \frac{\sigma_{\text{res}}}{\sigma_{\text{predictor}}}$$

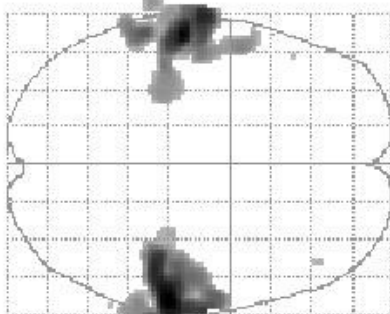
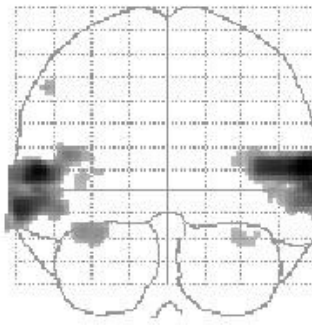
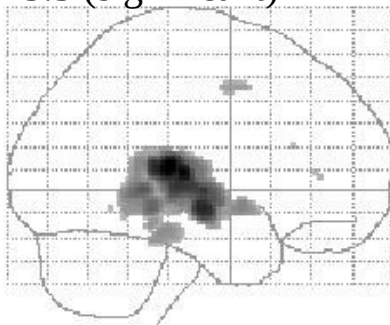
# The regression approach applied to the entire brain: statistical parametric mapping and the mass univariate approach

1 voxel

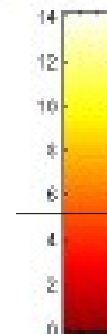
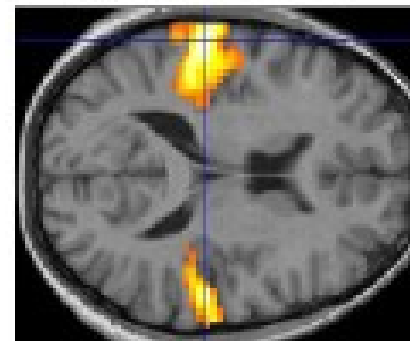
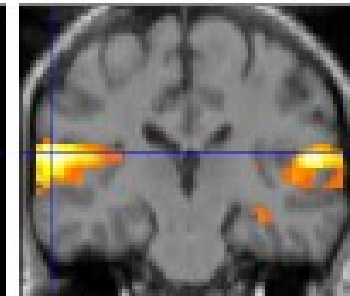
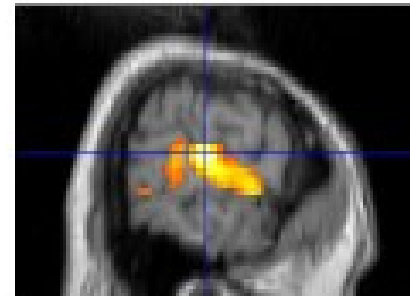


What are the brain regions whose activity is modulated by the sound?  
→ Repeat the same analysis for all voxels (mass univariate approach).

The sound modulates activity  
 $T=5.3$  (significant)



$SPM\{T_{73}\}$



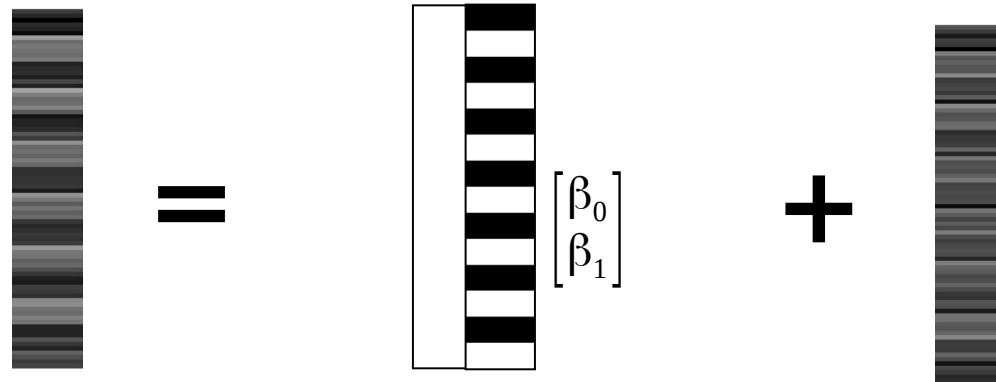
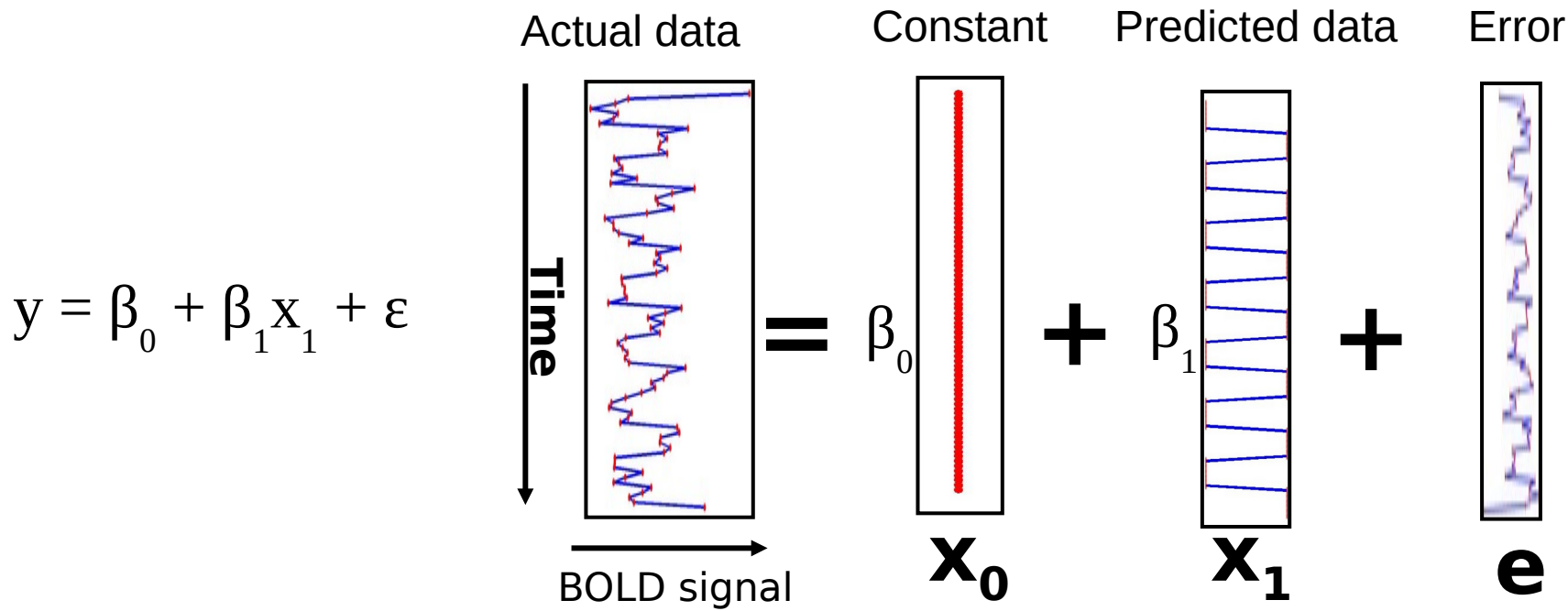
Visualization is thresholded for significance (only the most significant voxels are shown)

→ examples #2, #3 in the notebook

Adapted from: SPM courses

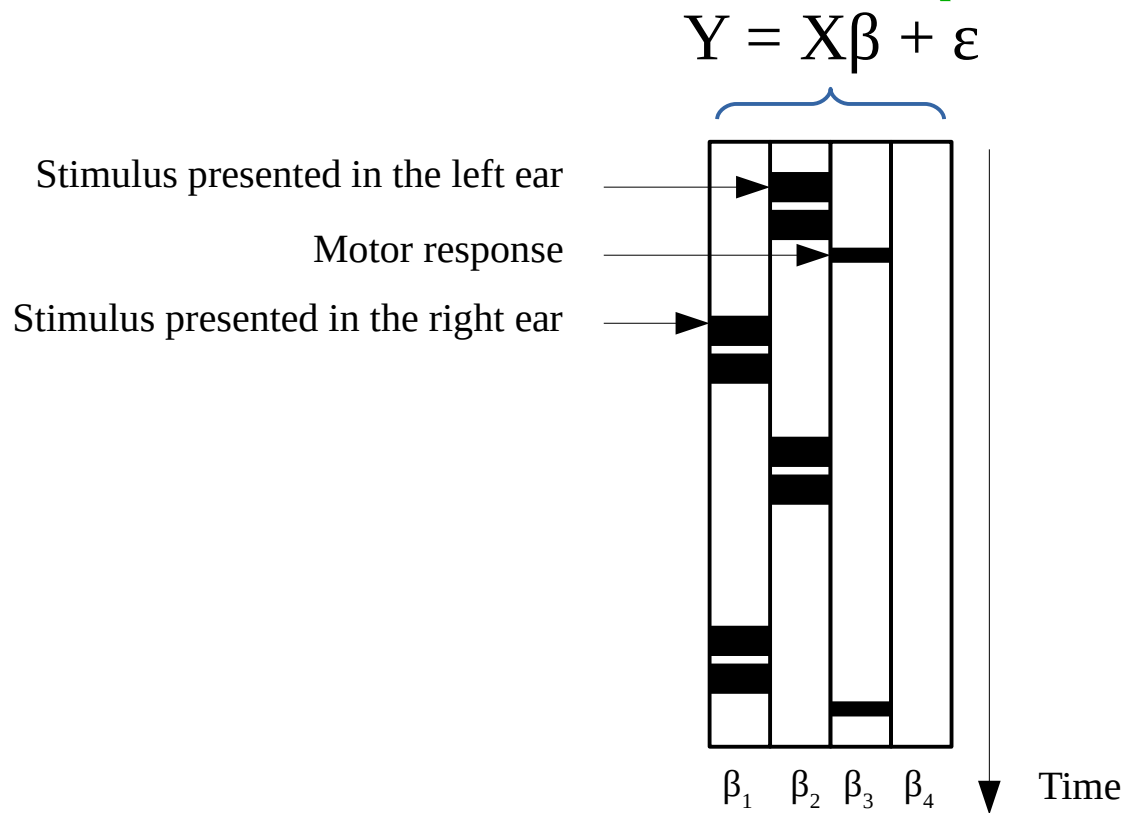


# Modelling BOLD response in a task: Matrix notations for regression and the General Linear Model (GLM)



$$\mathbf{Y} = \mathbf{X}\boldsymbol{\beta} + \boldsymbol{\varepsilon}$$

# Modelling BOLD response in a task: The “design matrix” models observations as a linear combination of factors (multiple regression)



The model of observations is estimated by finding the best-fitting values for the  $\beta$  parameters.  
The least-square estimates (those that minimize the residual sum-of-square):

$$\hat{\beta} = (X^T X)^{-1} X^T Y$$

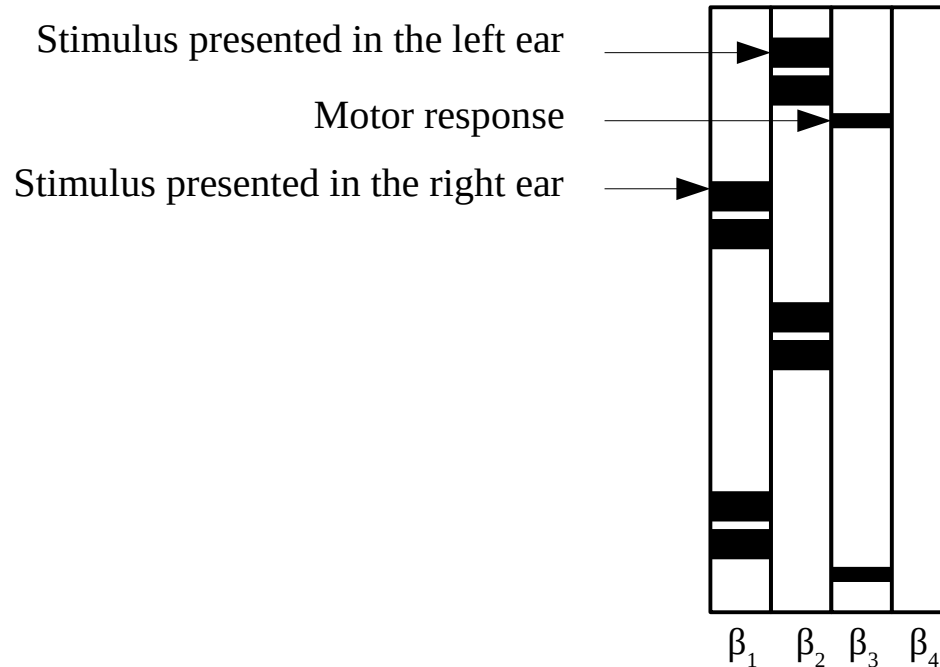
NB: the error should be normally, identically and independently distributed

→ data are spatially smoothed (it improves many aspects, including the issue of normal errors)

→ data must be “whitened” to remove the temporal autocorrelation of the data (which is inherent given the BOLD response)

# From neuronal effects to timeseries of BOLD data: Testing effects with linear contrast

$$Y = X\beta + \varepsilon$$



$C^T = [0 \ 0 \ 1 \ 0]$  Contrast testing for more activity when there is a motor response (is  $\beta_3 > 0$ ?).

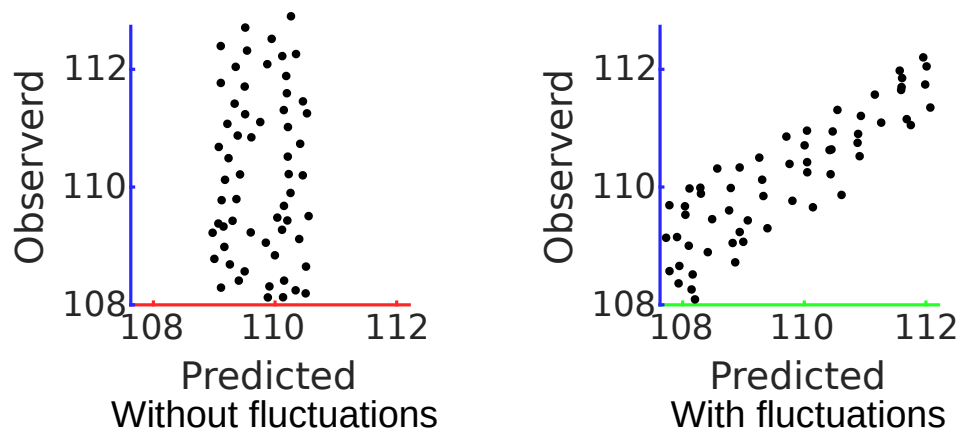
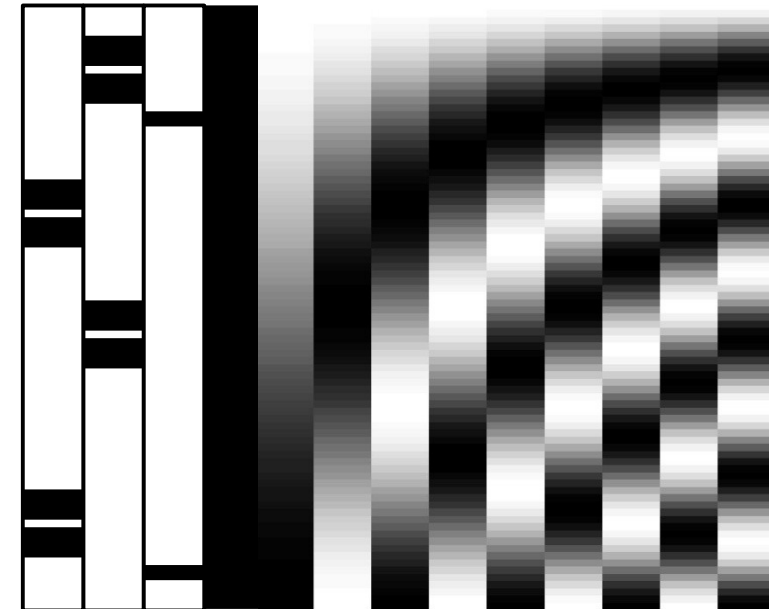
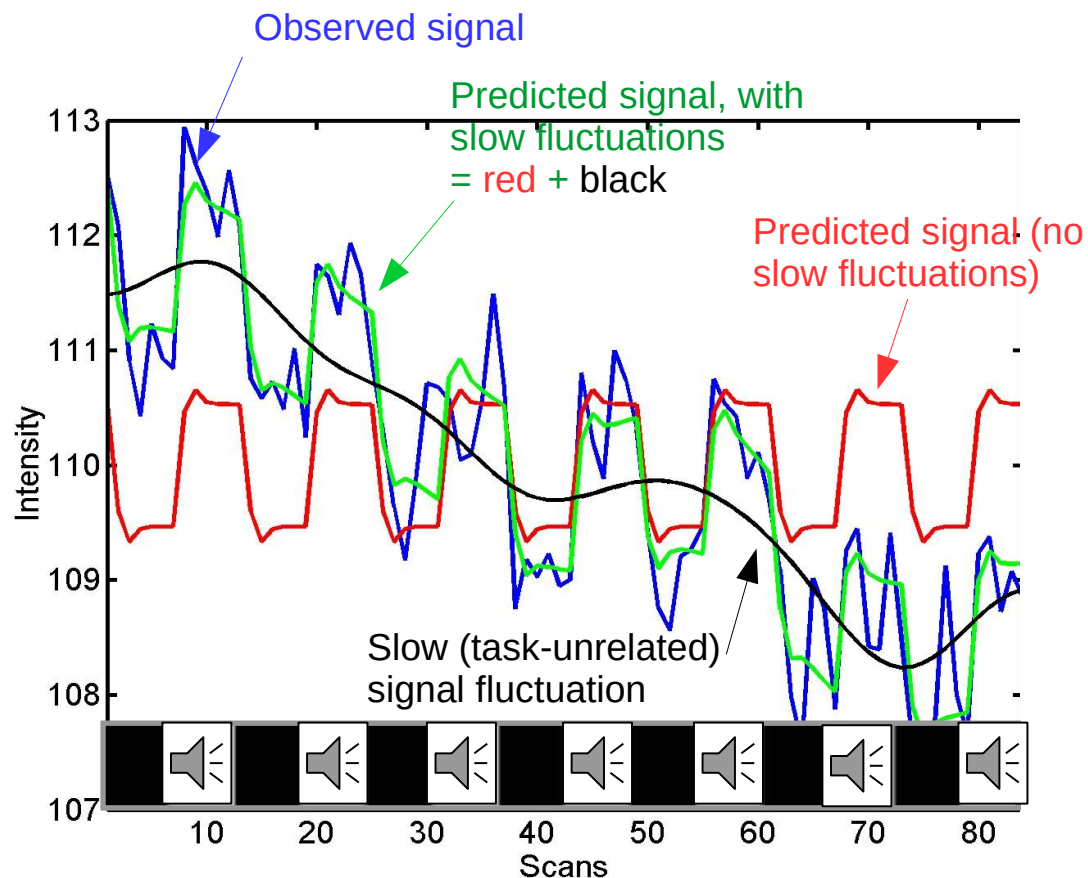
$C^T = [1 \ -1 \ 0 \ 0]$  Contrast testing for more activity when the stimulus is presented on the right compared the to left (is  $\beta_1 > \beta_2$ ?)

**Statistical test: is  $c^T \beta \neq 0$ ?**  
→ Use a Student T-test.

$$T = \frac{c^T \hat{\beta}}{\sqrt{\hat{\sigma}^2 c^T (X^T X)^{-1} c}}$$

NB:  $\sigma^2$  is the residual variance  
→ any effect that can be accounted for should be included in the design matrix

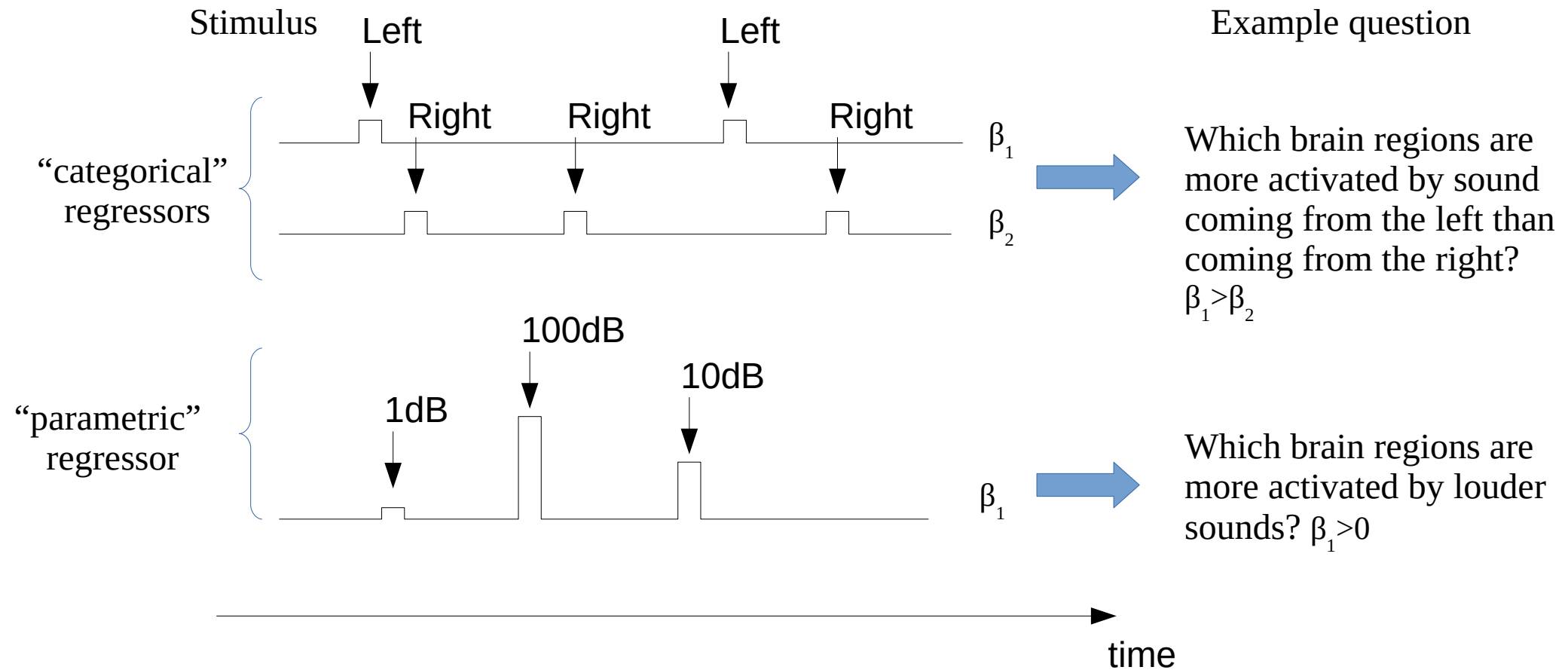
# From neuronal effects to timeseries of BOLD data: Include covariates in the design matrix



The fMRI signal is often corrupted by slow drifts (instability of the scanner)

Other “confound” variables typically included: subject's motion parameters

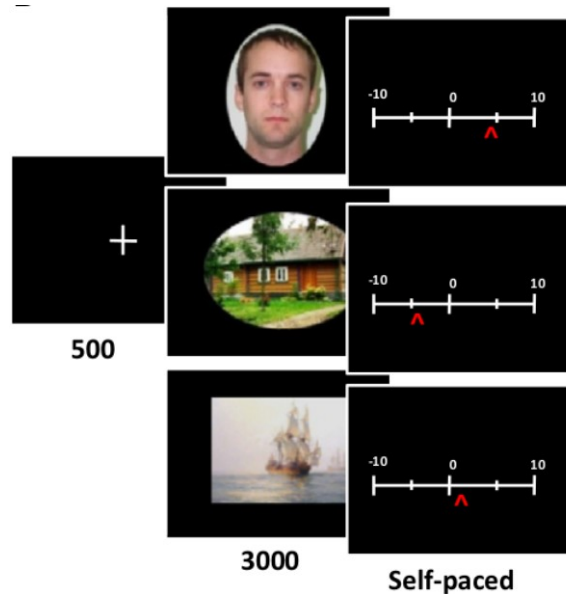
# GLM: A conceptual distinction between categorical regressors and parametric regressors



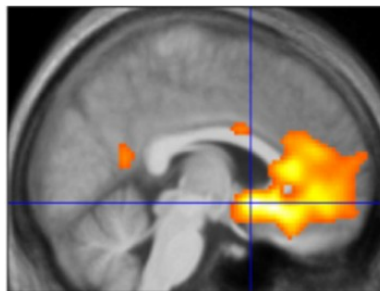
In the end, both types boil down to a regression of time-series in the GLM...

“Parametric” regressors may reflect a property of the stimulus, or some variable computed from a model of cognitive function

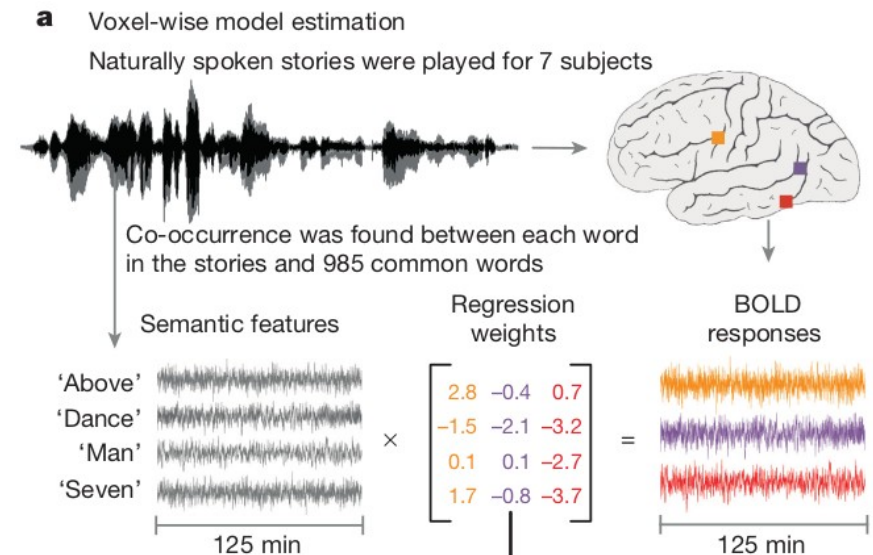
# Simple vs. sophisticated parametric regressors



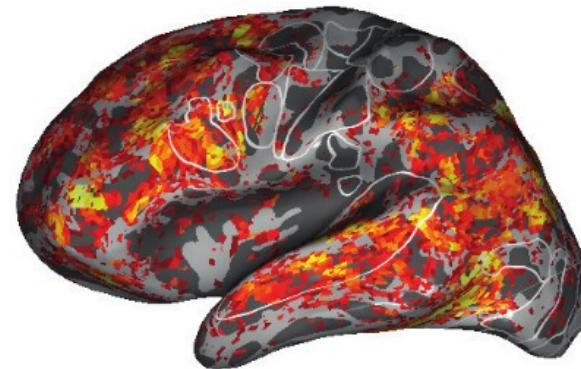
Parametric regressor: value rating



Lebreton et al, *Neuron* 2009



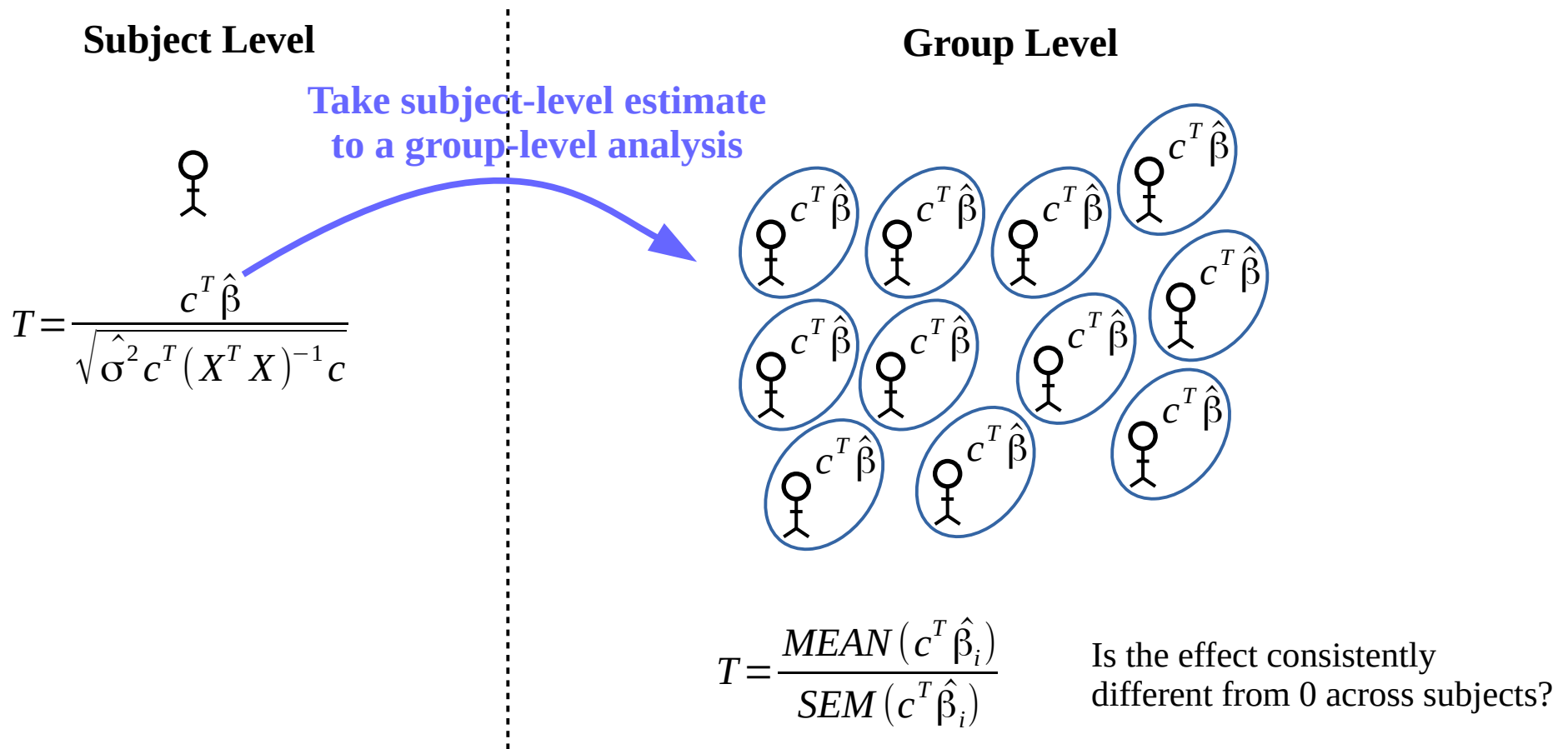
Parametric regressors: semantic features (from a word embedding model)



Huth et al, *Science* 2016



# Subject-level and group-level analyses



NB1: This method ignores the variance ( $\sigma$ ) of the parameters from different subjects. Mixed-models and hierarchical models can take into account the subject-level variance for the group-level inference.

NB2: To compare different subjects voxel-wise, the anatomy first needs to be “**normalized**”, i.e. aligned with one another. Usually, they are realigned to a standard anatomical space (e.g. MNI) so that a given voxel can be compared across studies. “functional alignment” is an alternative (e.g. Haxby et al, 2020 *eLife*)

# The flexibility of General Linear Models

The GLM approach allows different statistical methods:

- Student T-test: Is my effect  $E_1 \neq 0$ ? Is effect  $E_1 > E_2$ ?
- Categorical variables and continuous variables
- F-test (ANOVA): Is there a difference between any level of factor  $E_1$  (one-way ANOVA)? Is there a difference between any level of factor  $E_1$  while controlling for the effects of  $E_2, \dots, E_N$  (N-way ANOVA)
- T-test and F-test can be performed at the subject-level and at the group-level.

→ This is why we say *General* linear models

# Comparison of the multivariate and univariate approaches

## Univariate / encoding

- Look at voxels independently from one another
- Look for spatially smoothed signal
- Based on a regression approach
- One must fully specify the type of representation looked for
- Statistics: T-test, F-test (parametric or not)
- Computationally cheap. Parametric tests suffice

## Multivariate / decoding

- Look at the information conveyed jointly by multiple voxels
- Look for spatially structured signals
- Based on a classification approach (+ extension for continuous variables)
- The classification automatically extracts the relevant features
- Statistics: classification/prediction accuracy
- Computationally expensive. Requires permutation, cross-validation

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## **IV/ The problem with multiple comparisons**

**Multiple testing inflates the risk of having a false positive**

**Statistical methods to correct for multiple comparisons**

# It is likely that a rare event occurs if you try multiple times



## Bet 1

You throw a pair of dice.  
I give you 10€ if you have a double 6.  
You give me 10€ otherwise.

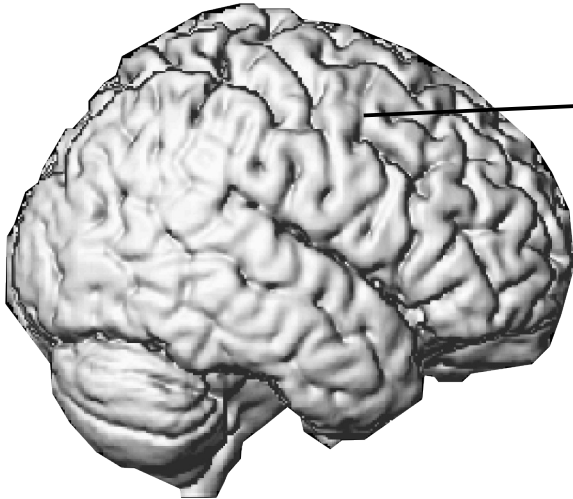
Probability that I win:  
 $1 - (1/6)^2 = 97\%$

## Bet 2

You throw a pair of dice 100 times.  
I give you 10€ if you have a double 6 at least once. You give me 10€ otherwise.

Probability that I win:  
 $[1 - (1/6)^2]^{100} = 6\%$

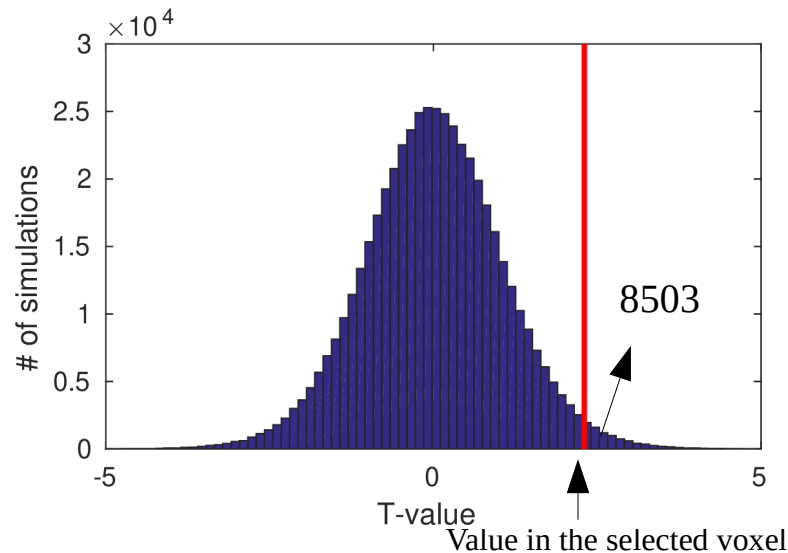
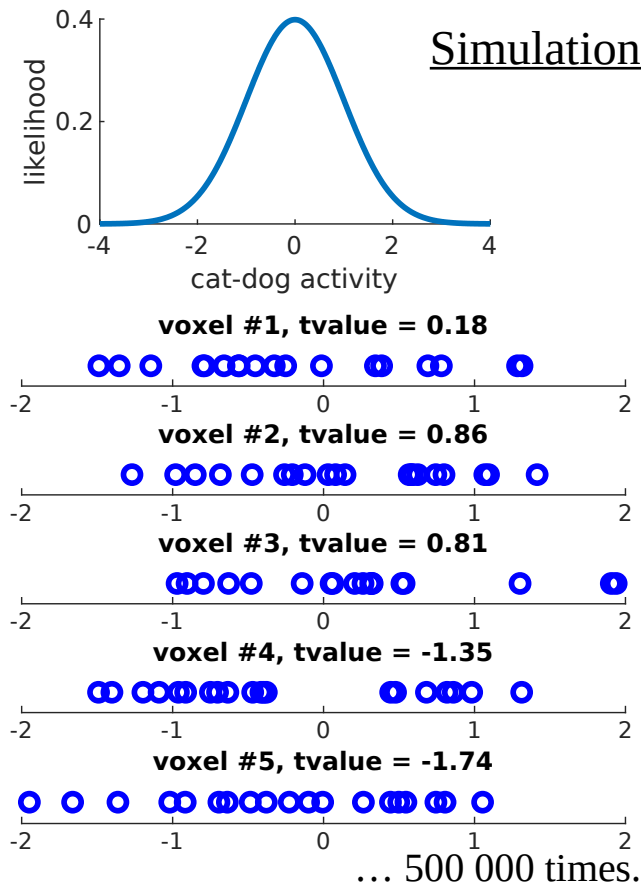
# The problem of multiple testing across voxels



You find a voxel with different activity for “tone” and “no tone” in 20 subjects, at  $t=2.3$  ( $p=0.016$ , one-tail t-test)!

Number of voxels that can be considered as grey matter after smoothing, at a resolution of 1.5 mm:  $\sim 500\,000$ .

## Simulation of the chance level (null effect) in that experiment



8503 simulations / 500000 yield the same (or a higher) t-value as the one found.  
NB: using the parametric distribution:  
 $500000 \times 0.016 = 8000$ .

→ we need to correct for the inflation of false positives.

Corrections (See Thomas Nichols 2003 for a review):

- Family wise error (Bonferroni, Gaussian random fields)
- False discovery rate