

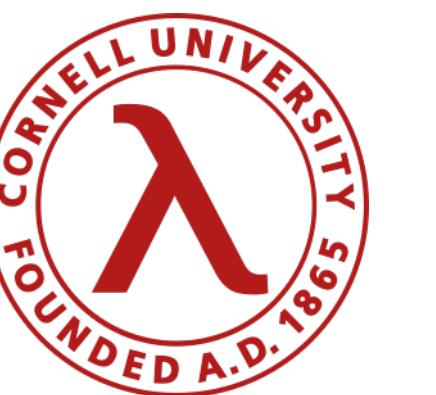
Mica

Automated Differential Testing
for OCaml Modules

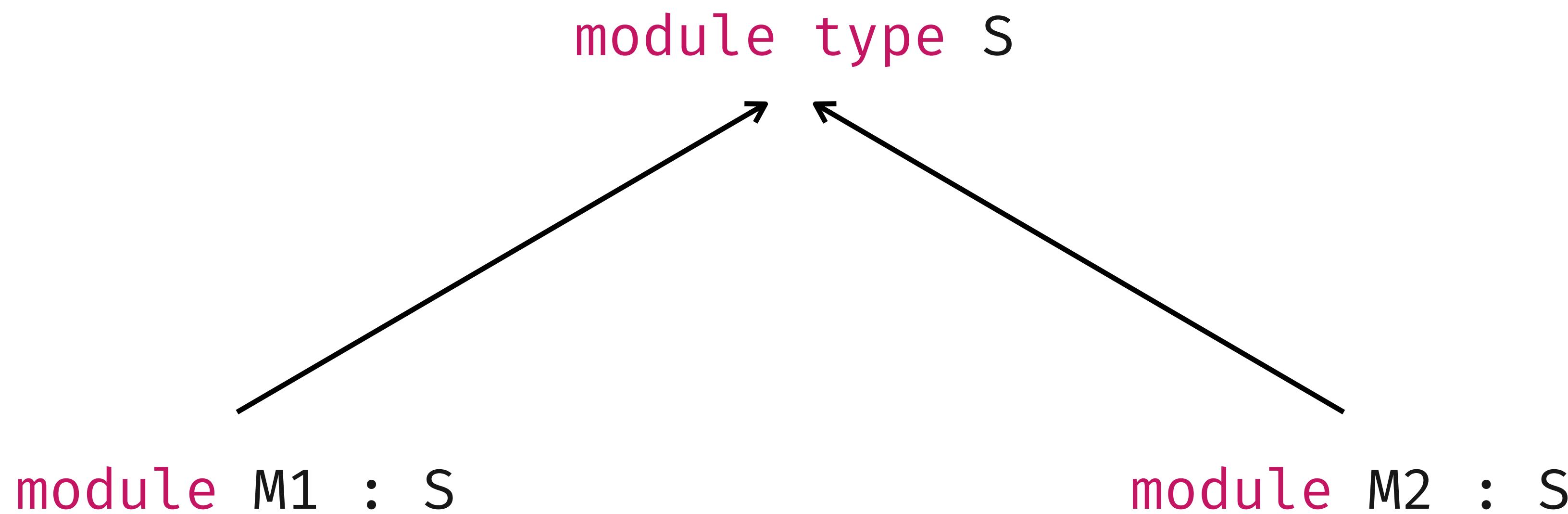
Ernest Ng

Harry Goldstein

Benjamin Pierce



Representation Independence



Example: Finite Sets

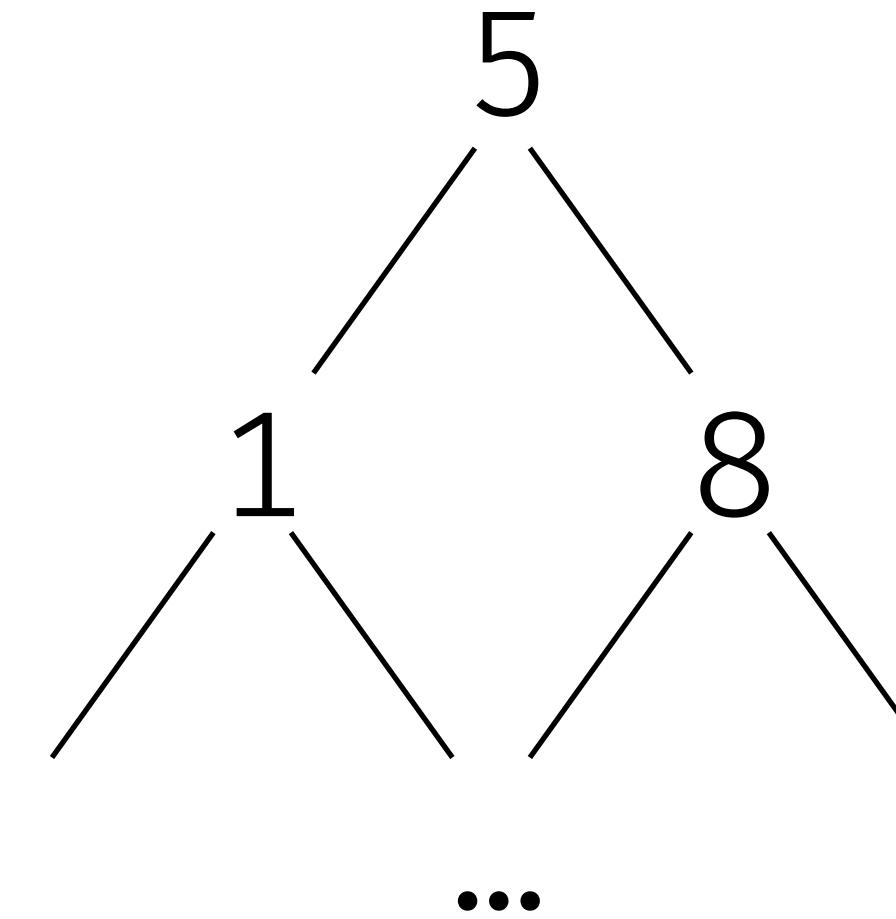
```
module type S = sig
  type 'a t
  val empty    : 'a t
  val insert   : 'a → 'a t → 'a t
  ...
end
```

module type S

{1, 5, 8, ...}

[1; 5; 8; ...]

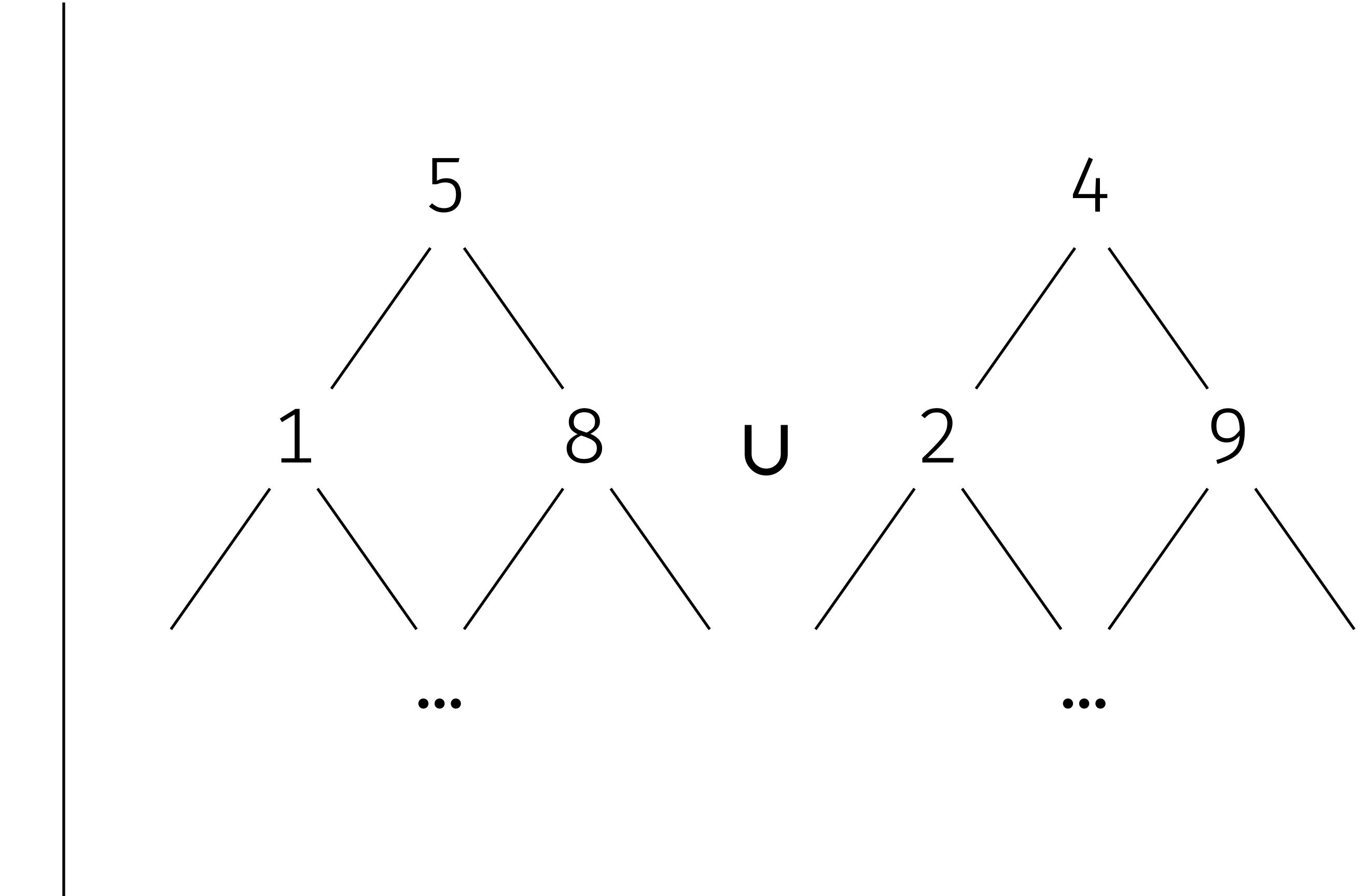
module ListSet : S



module BSTSet : S

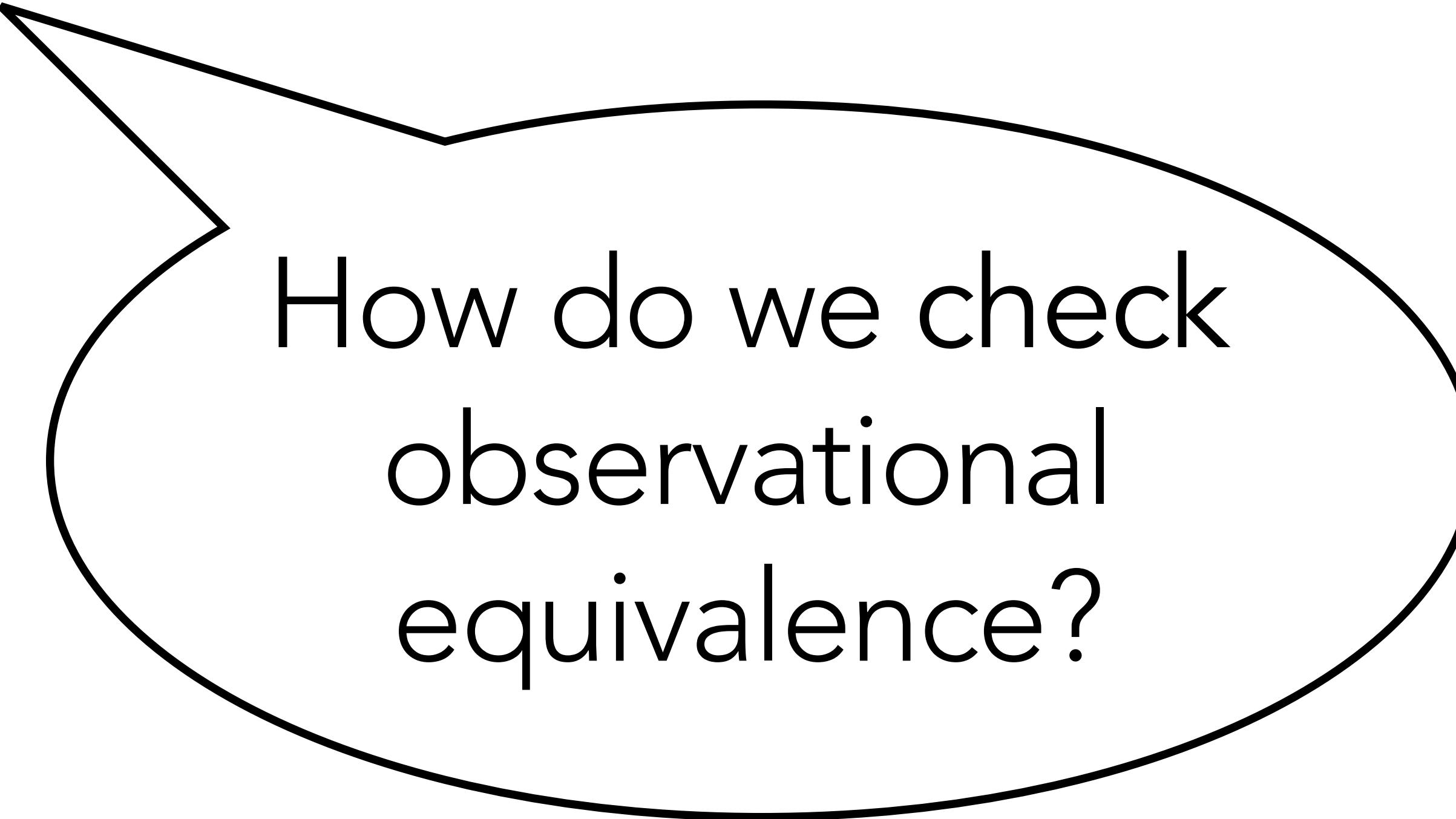
Are these **equivalent**?

$$[1; 5; 8] + [2; 4; 9]$$



Observational Equivalence

equivalent
inputs → equivalent
outputs



How do we check
observational
equivalence?

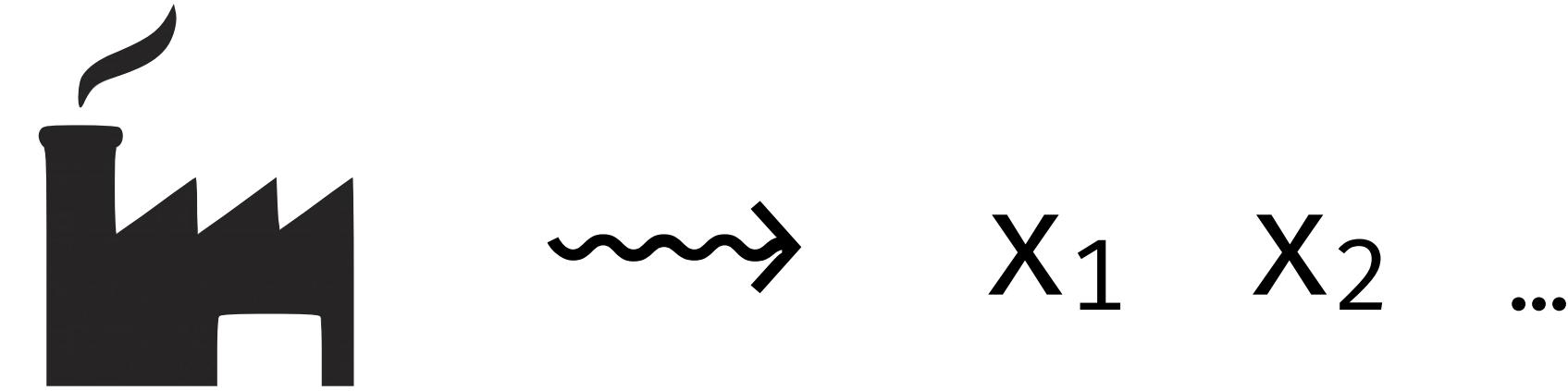
We can use
property-based testing!

Property-Based Testing

1. Write *properties*

$$\forall x. P(x)$$

2. Generate *random inputs*



3. Check if inputs satisfy property

Property-Based Testing



QuickCheck

(Claessen & Hughes '00)

PBT in Practice

Goldstein et al. (ICSE '24)

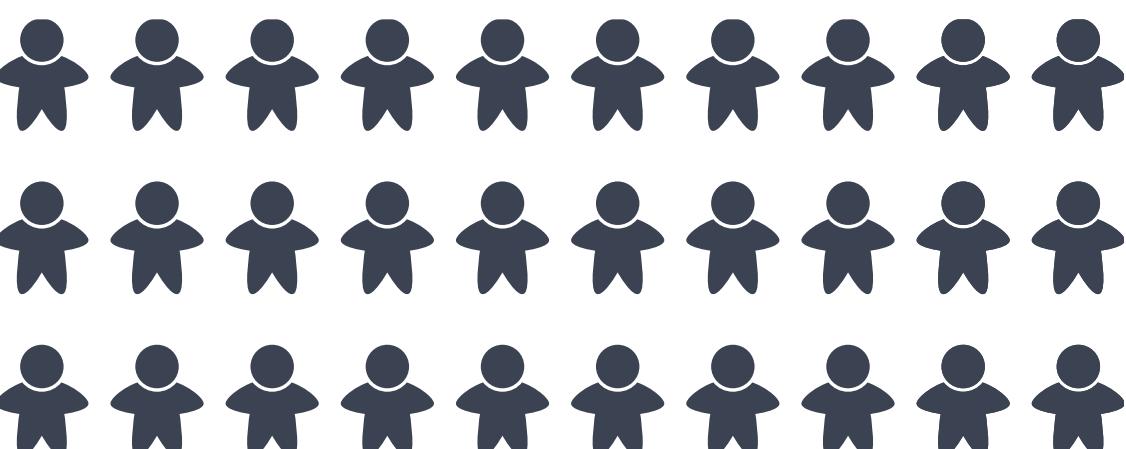
30 OCaml developers
interviewed on their use of PBT

Property-Based Testing in Practice

Harrison Goldstein University of Pennsylvania Philadelphia, PA, USA hgo@seas.upenn.edu	Joseph W. Cutler University of Pennsylvania Philadelphia, PA, USA jwc@seas.upenn.edu	Daniel Dickstein Jane Street New York, NY, USA ddickstein@janestreet.com
Benjamin C. Pierce University of Pennsylvania Philadelphia, PA, USA bcpierce@seas.upenn.edu	Andrew Head University of Pennsylvania Philadelphia, PA, USA head@seas.upenn.edu	

ABSTRACT
Property-based testing (PBT) is a testing methodology where users write executable formal specifications of software components and an automated harness checks these specifications against many automatically generated inputs. From its roots in the QuickCheck library in Haskell, PBT has made significant inroads in mainstream languages and industrial practice at companies such as Amazon, Microsoft, and Jane Street.

The research literature is full of accounts of PBT successes, e.g., in telecommunications software [2], replicated file [31] and key-value [8] stores, automotive software [3], and other complex systems [30]. PBT libraries are available in most major programming languages, and some now have significant user communities—e.g., Python’s Hypothesis framework [37] had an estimated 500K users in 2021 according to a JetBrains survey [32]. Still, there is plenty of



PBT in Practice

Goldstein et al. (ICSE '24)

PBT tools are often used
for differential testing!

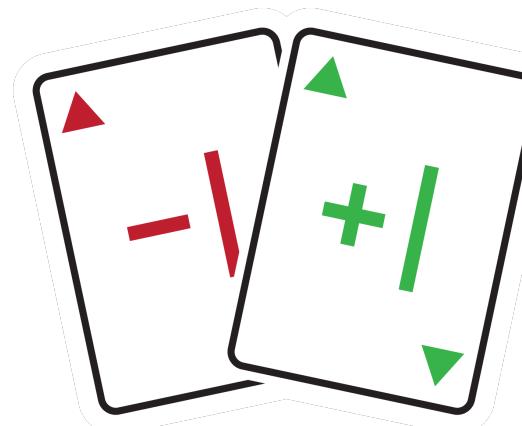
Property-Based Testing in Practice

Harrison Goldstein University of Pennsylvania Philadelphia, PA, USA hgo@seas.upenn.edu	Joseph W. Cutler University of Pennsylvania Philadelphia, PA, USA jwc@seas.upenn.edu	Daniel Dickstein Jane Street New York, NY, USA ddickstein@janestreet.com
Benjamin C. Pierce University of Pennsylvania Philadelphia, PA, USA bcpierce@seas.upenn.edu	Andrew Head University of Pennsylvania Philadelphia, PA, USA head@seas.upenn.edu	

ABSTRACT
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The research literature is full of accounts of PBT successes, e.g., in telecommunications software [2], replicated file [31] and key-value [8] stores, automotive software [3], and other complex systems [30]. PBT libraries are available in most major programming languages, and some now have significant user communities—e.g., Python’s Hypothesis framework [37] had an estimated 500K users in 2021 according to a JetBrains survey [32]. Still, there is plenty of

~60% of developers wrote
differential properties



Why should we care?

1. Testing observational equivalence requires significant programmer effort

- Developers described this process as **"tedious"** & **"overwhelming"**
- High **"overhead"** associated with writing PBT boilerplate

Goldstein et al. (ICSE '24)

in languages like OCaml with rich module structures,
researchers should aim to increase automation around differential
testing and produce a test harness for comparing modules without
requiring any manual setup

Why should we care?

2. Large OCaml software systems
are built using modules that
implement the same signature



MirageOS

Module Signatures Implementations

Module type	Implementations
Mirage_kv.R0	Crunch, Kv_Mem, Kv_unix, Mirage_tar, XenStore, Irmin, Filesystems
Mirage_kv.RW	Wodan
Mirage_fs.S	Fat, Git, Fs_Mem, Fs_unix
Mirage_net.S	tuntap, vmnet, rawlink
ARP, IP, UDP, TCP	IPV4, IPV6, Qubesdb_IP, Udp, Updv4_socket, Tcp, Tcipv4_socket, ...
STACK	Direct, Socket, Qubes, Static_IP, With_DHCP
RANDOM	Stdlib, Nocrypto, Test
HTTP	Cohttp, Httpaf
FLOW	Conduit.With_tcp, Conduit.With_tls
DNS, DHCP, SYSLOG	Dns, Unix, Charrua_unix, Charrua, Syslog.Tcp, Syslog.Udp, Syslog.Tls, Jitsu, Irmin, ...

Radanne et al. (2019)

What if I told you...

You can take two modules that implement the same signature ...

```
module type S  
module M1 : S      module M2 : S
```

...and **automatically** get PBT code that compares them?

Mica

```
module type S = ...
[@@deriving mica]
```



```
type expr = ...
let gen_expr ty = ...
let interp expr = ...
```

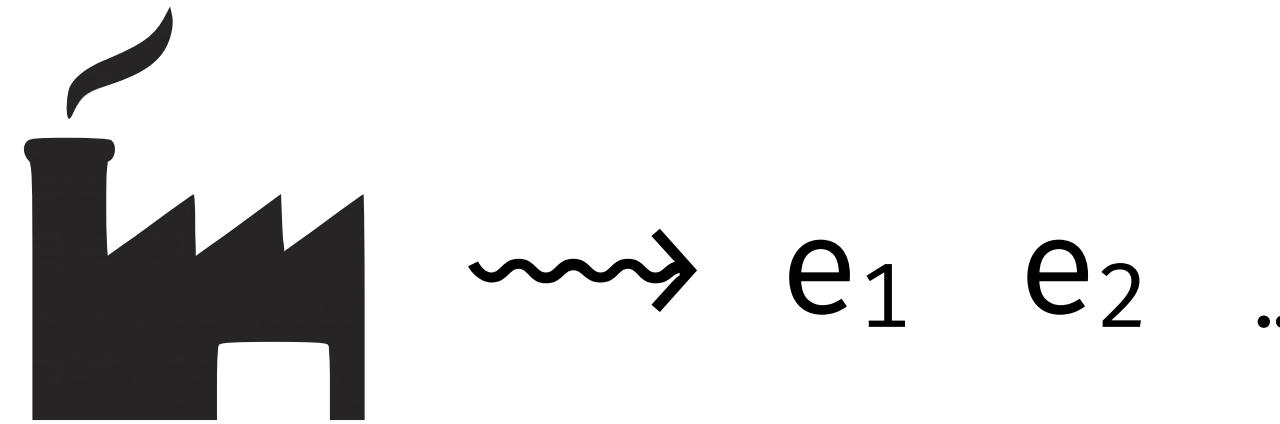


Mica derives the following automatically:

Types

expr
ty
value

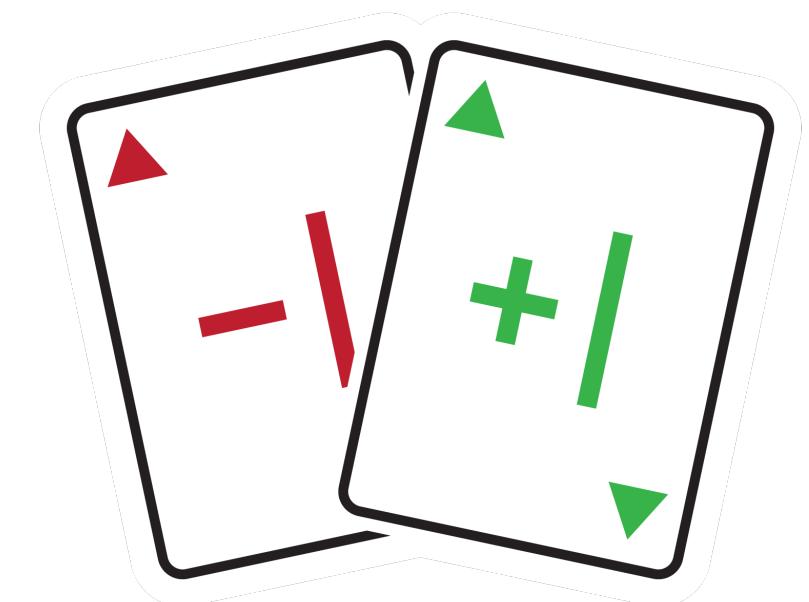
QuickCheck
Generator



Interpreter



Test Harness



Symbolic Expressions

Inductively-defined algebraic data type

	type expr =
val empty : 'a t	↔ Empty
val is_empty : 'a t → bool	↔ Is_empty of expr
val insert : 'a → 'a t → 'a t	↔ Insert of int * expr
...	...

Symbolic Expressions

types

type ty = ...

values

type value = ...

QuickCheck Generator

random, **well-typed** symbolic expressions

```
gen_expr : ty → expr Generator.t
```

Union (Insert (2, Empty), Empty)

✓

Is_empty (Size Empty)

✗

Interpretation Functor

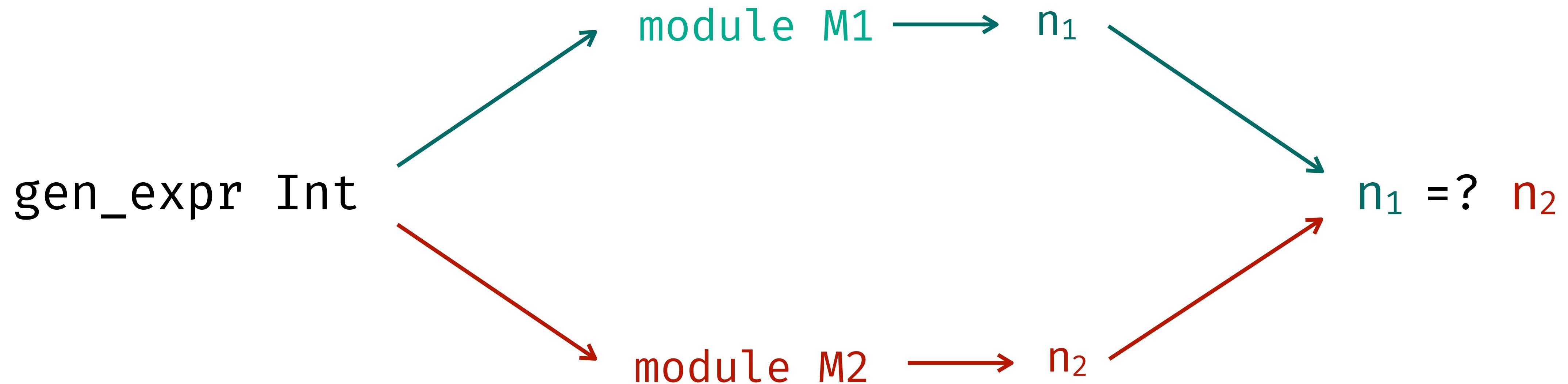
```
module Interpret (M : S) = ...
```

expr → value

Insert (2, Empty) ↪ M.insert 2 M.empty

Test Harness Functor

Checks observational equivalence at **concrete** types



Test Harness Functor

Checks observational equivalence at **concrete** types

```
module TestHarness (M1 : S) (M2 : S) = ...
```

int



'a t



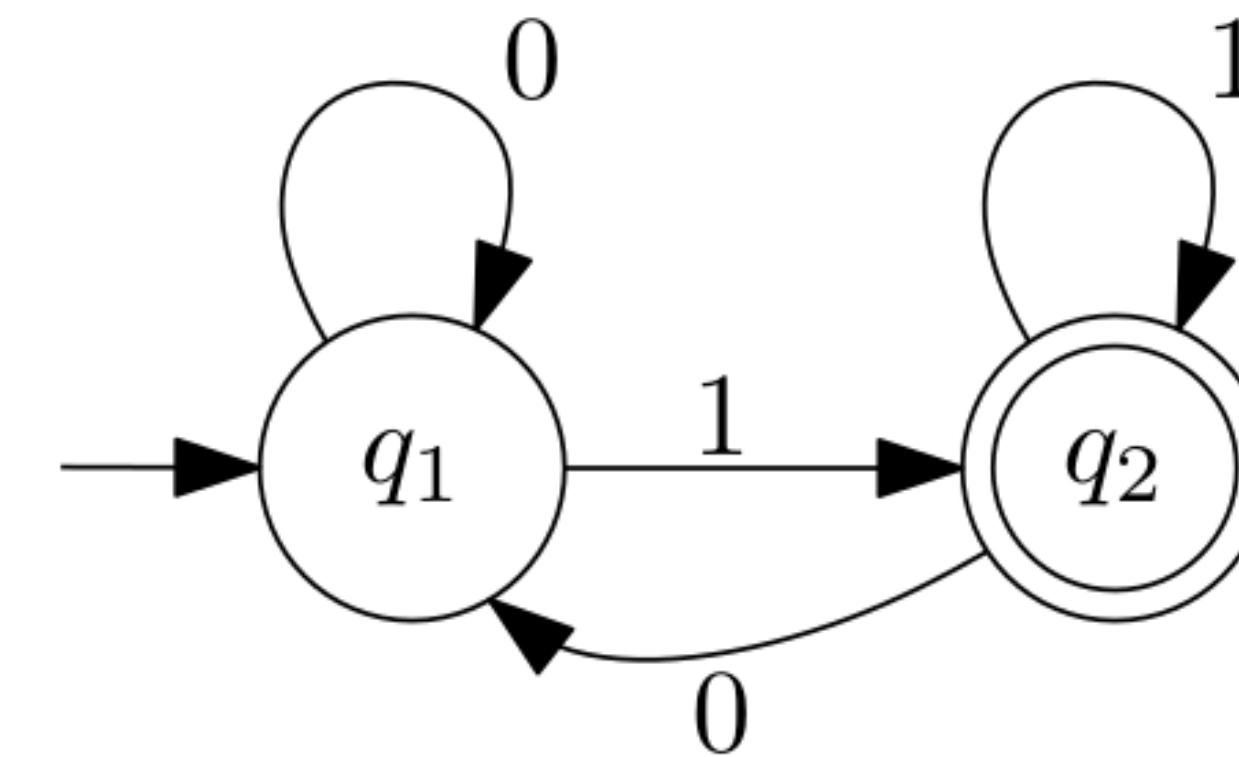
Case Studies

Regular Expressions

Brzozowski Derivatives

$$\begin{aligned}D_c(\emptyset) &= \emptyset \\D_c(\epsilon) &= \emptyset \\D_c(c') &= \begin{cases} \epsilon_c & \text{if } c = c' \\ \emptyset & \text{if } c \neq c' \end{cases} \\D_c(L_1 \cup L_2) &= D_c(L_1) \cup D_c(L_2) \\D_c(L_1 \circ L_2) &= \begin{cases} D_c(L_1) \circ L_2 & \text{if } \epsilon \notin [L_1] \\ (D_c(L_1) \circ L_2) \cup D_c(L_2) & \text{if } \epsilon \in [L_1] \end{cases}\end{aligned}$$

Finite Automata



Unsigned Integer Arithmetic

andrenth/**ocaml-stdint**



Various signed and unsigned integers for OCaml

15
Contributors

21
Issues

83
Stars

15
Forks



yallop/**ocaml-integers**



Various signed and unsigned integer types for OCaml

8
Contributors

5
Issues

2
Discussions

60
Stars

20
Forks

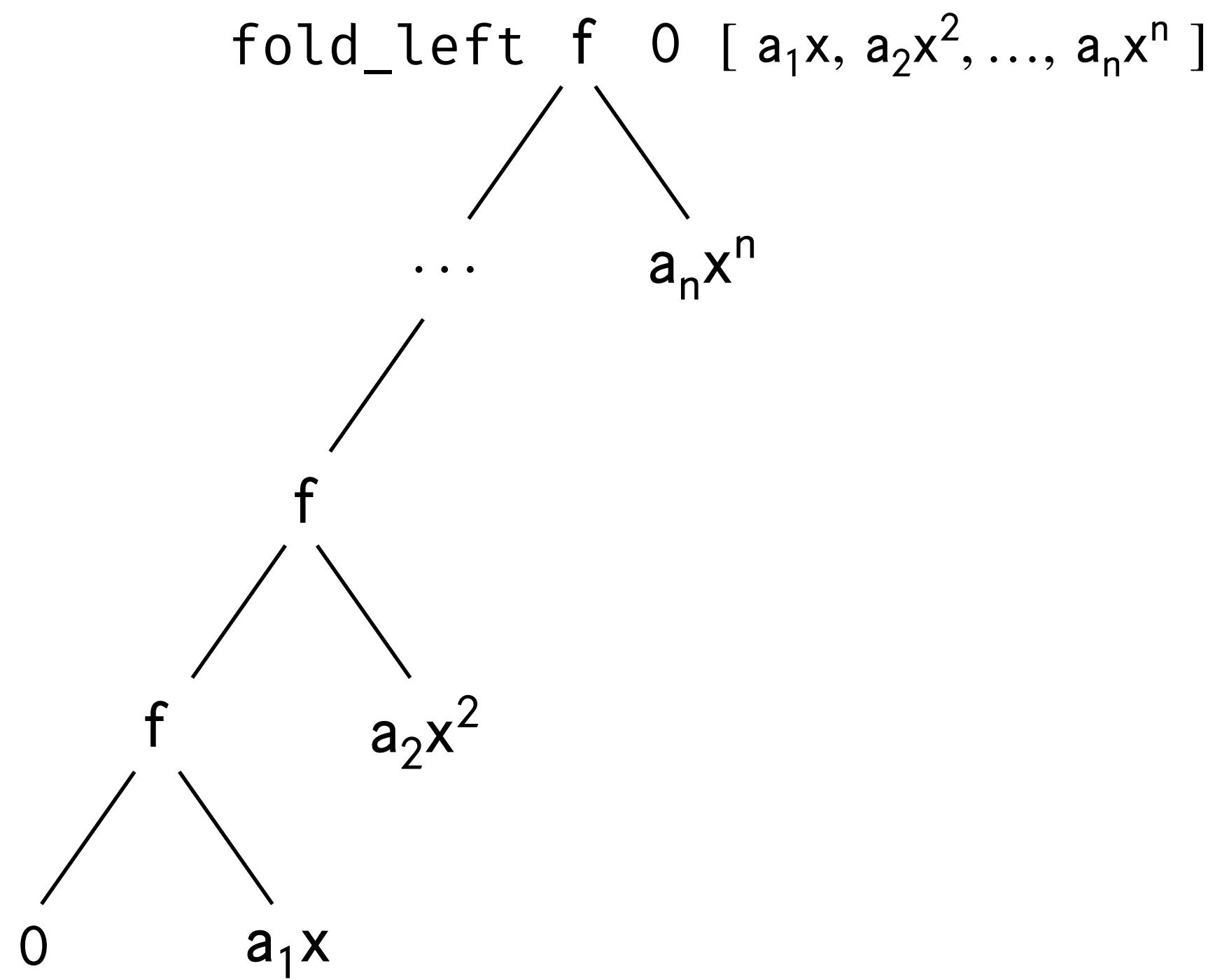


Polynomials

Horner's Algorithm

$$\begin{aligned} p(x_0) &= a_0 + x_0 \left(a_1 + x_0 \left(a_2 + \cdots + x_0 (a_{n-1} + b_n x_0) \cdots \right) \right) \\ &= a_0 + x_0 \left(a_1 + x_0 \left(a_2 + \cdots + x_0 b_{n-1} \right) \right) \\ &\vdots \\ &= a_0 + x_0 b_1 \\ &= b_0. \end{aligned}$$

Fold over monomials



Character Sets

Standard Library

`Set.Make(Char)`

Compiler Intrinsics

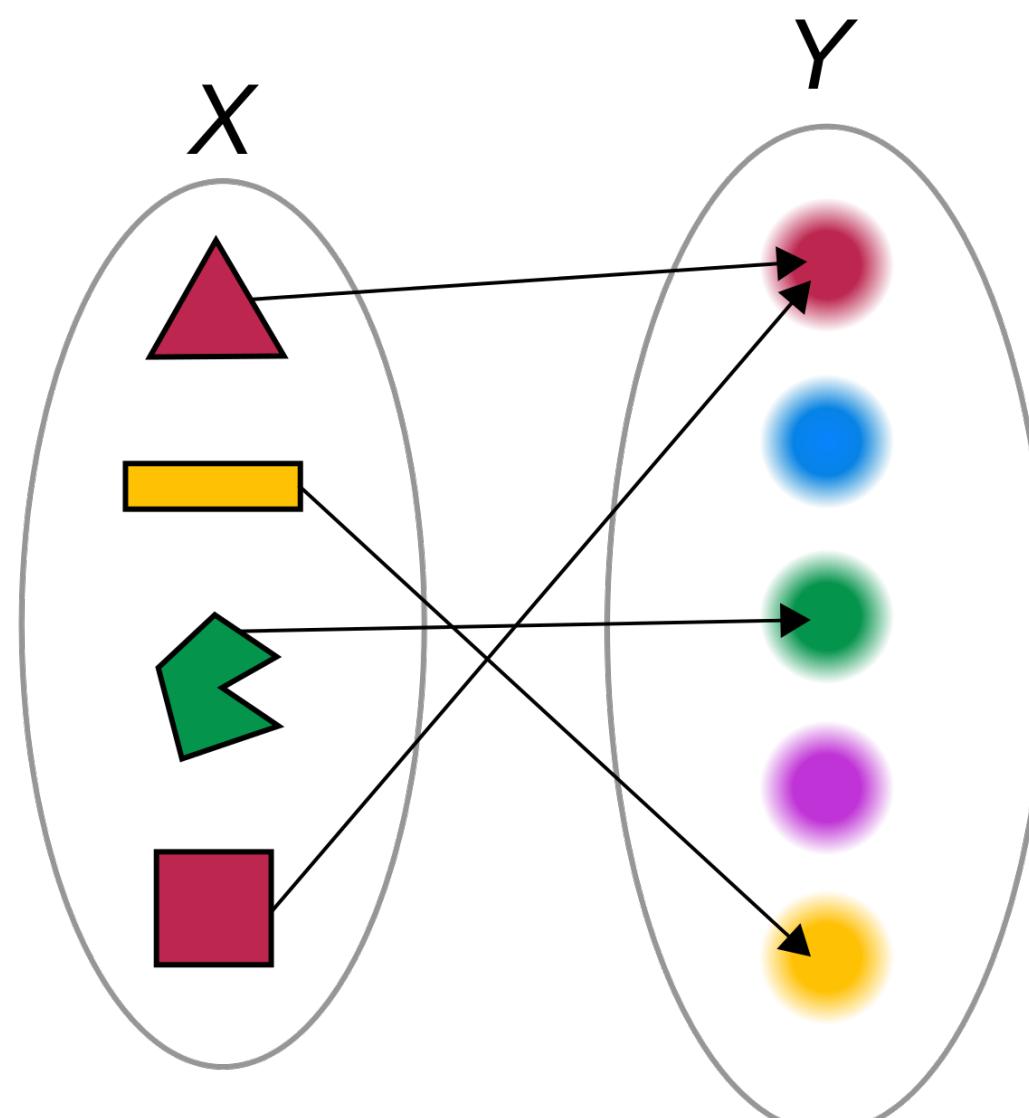
`yallop/ocaml-charset`

Fast char sets

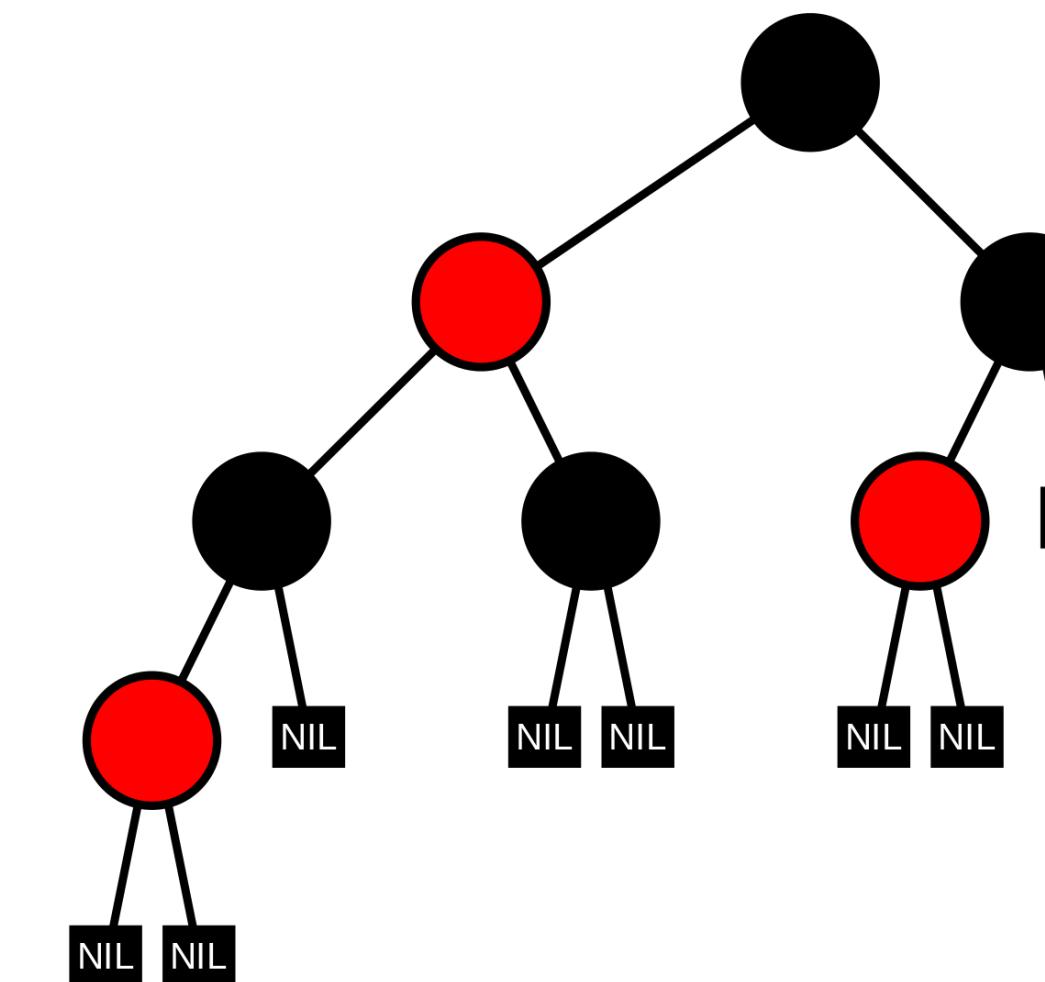


Persistent Maps

Association Lists



Red-Black Trees



Ephemeral Queues

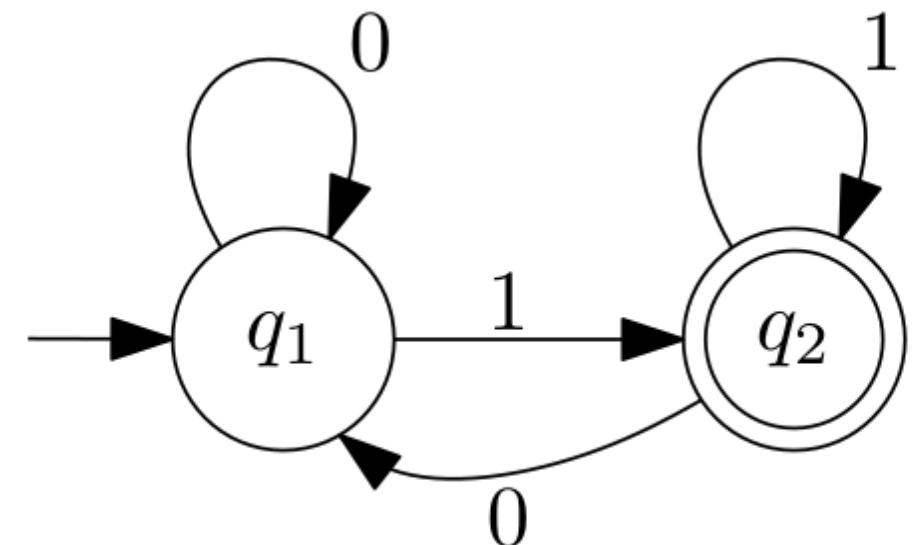
Base.Queue



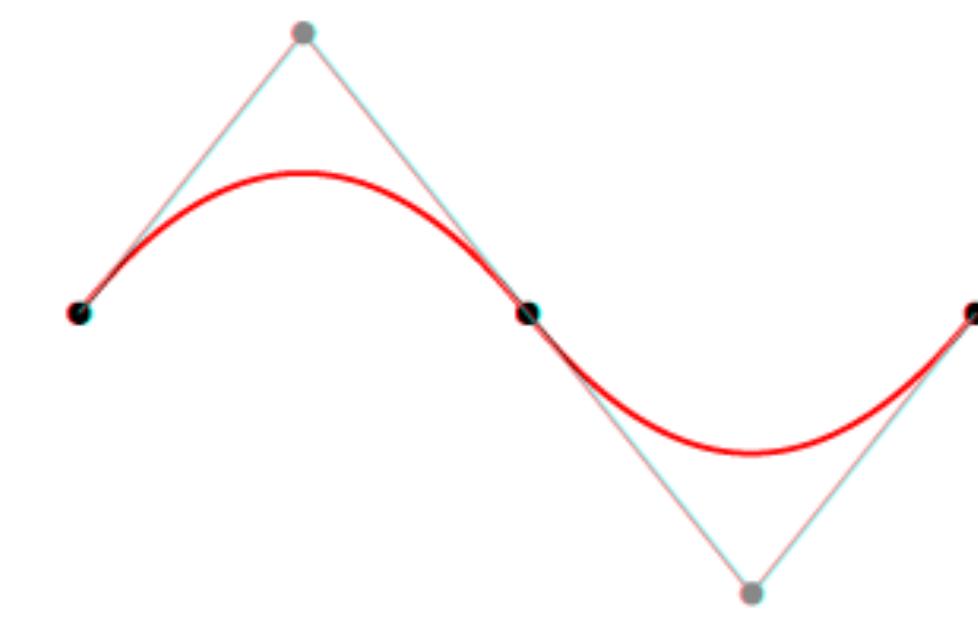
Base.Linked_queue

Case Studies

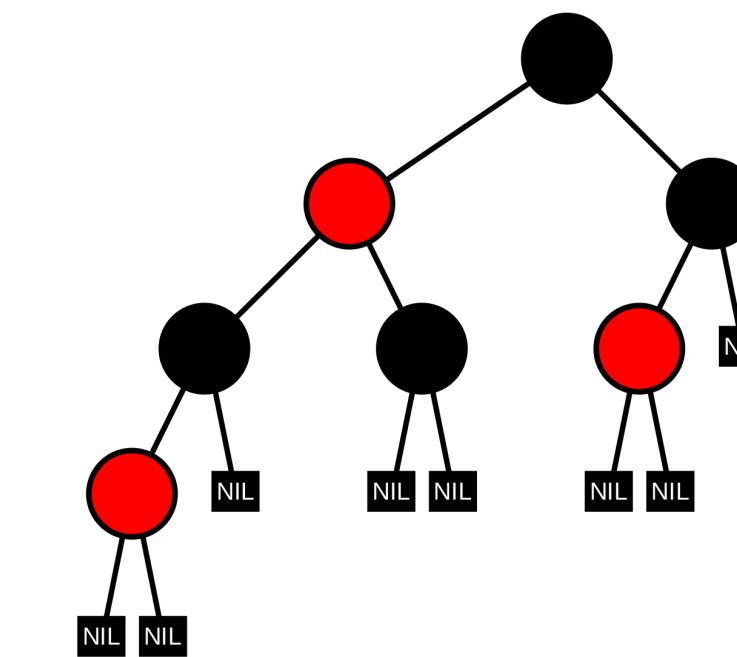
Regex Matchers



Polynomials



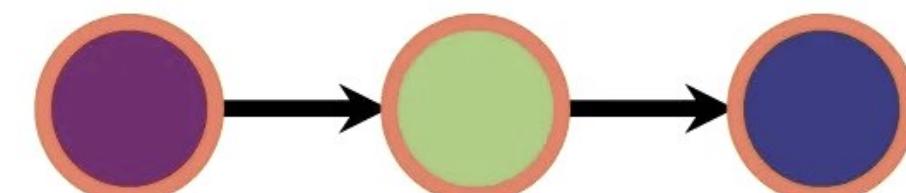
Persistent Maps



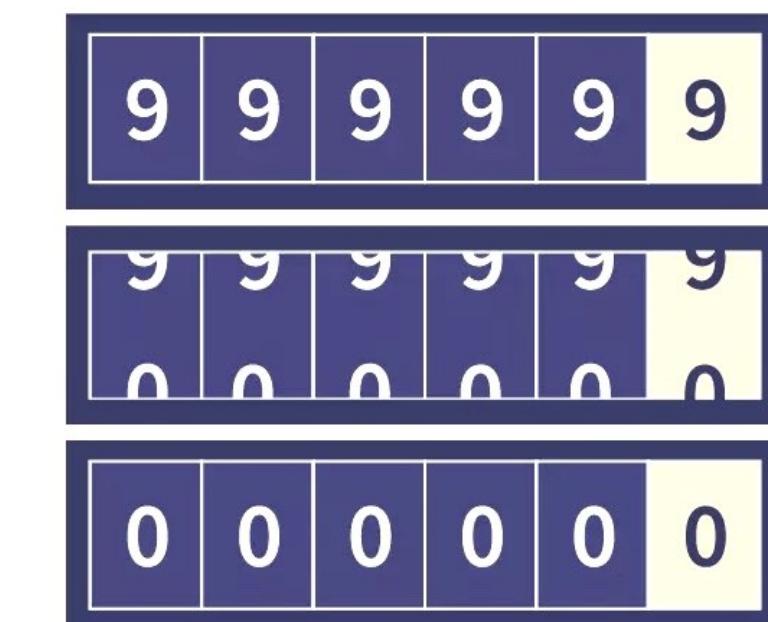
Character Sets

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Ephemeral Queues

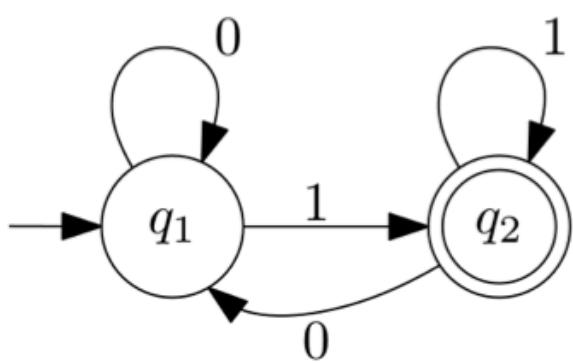


Unsigned Integers

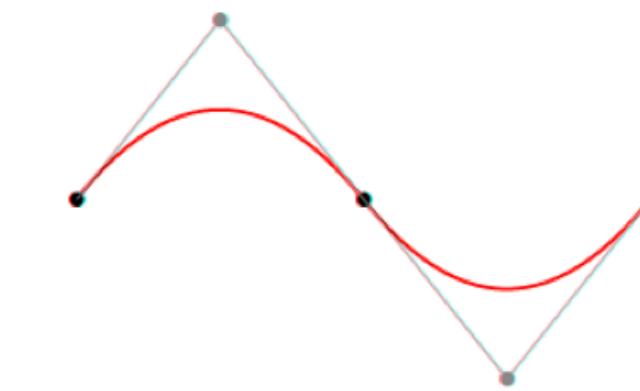


35 manually-inserted bugs caught

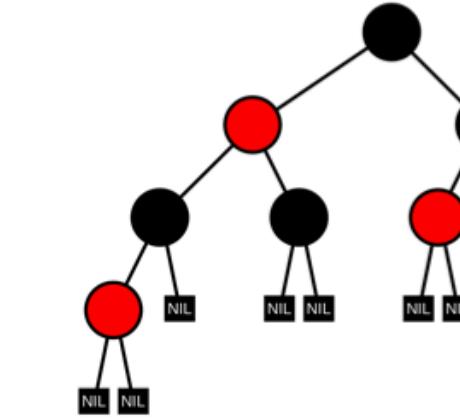
Regex Matchers



Polynomials



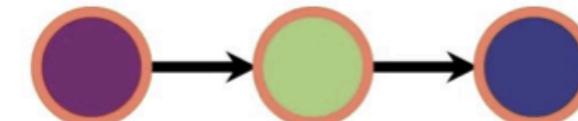
Persistent Maps



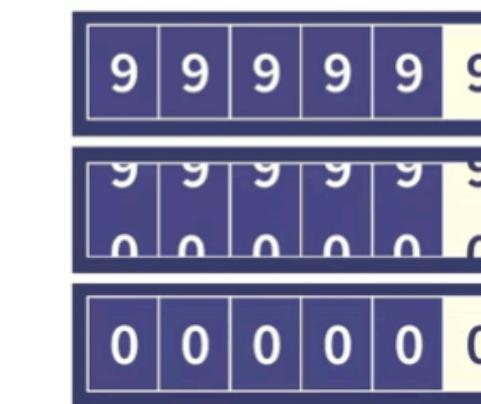
Character Sets

Á Â Ã Ä Å Æ Ç È É
Ñ ò ó ô õ ö × Ø Ù
á â ã ä å æ ç è é

Ephemeral Queues



Unsigned Integers



6 real-world OCaml libraries

Case study: *How to Specify It*

John Hughes



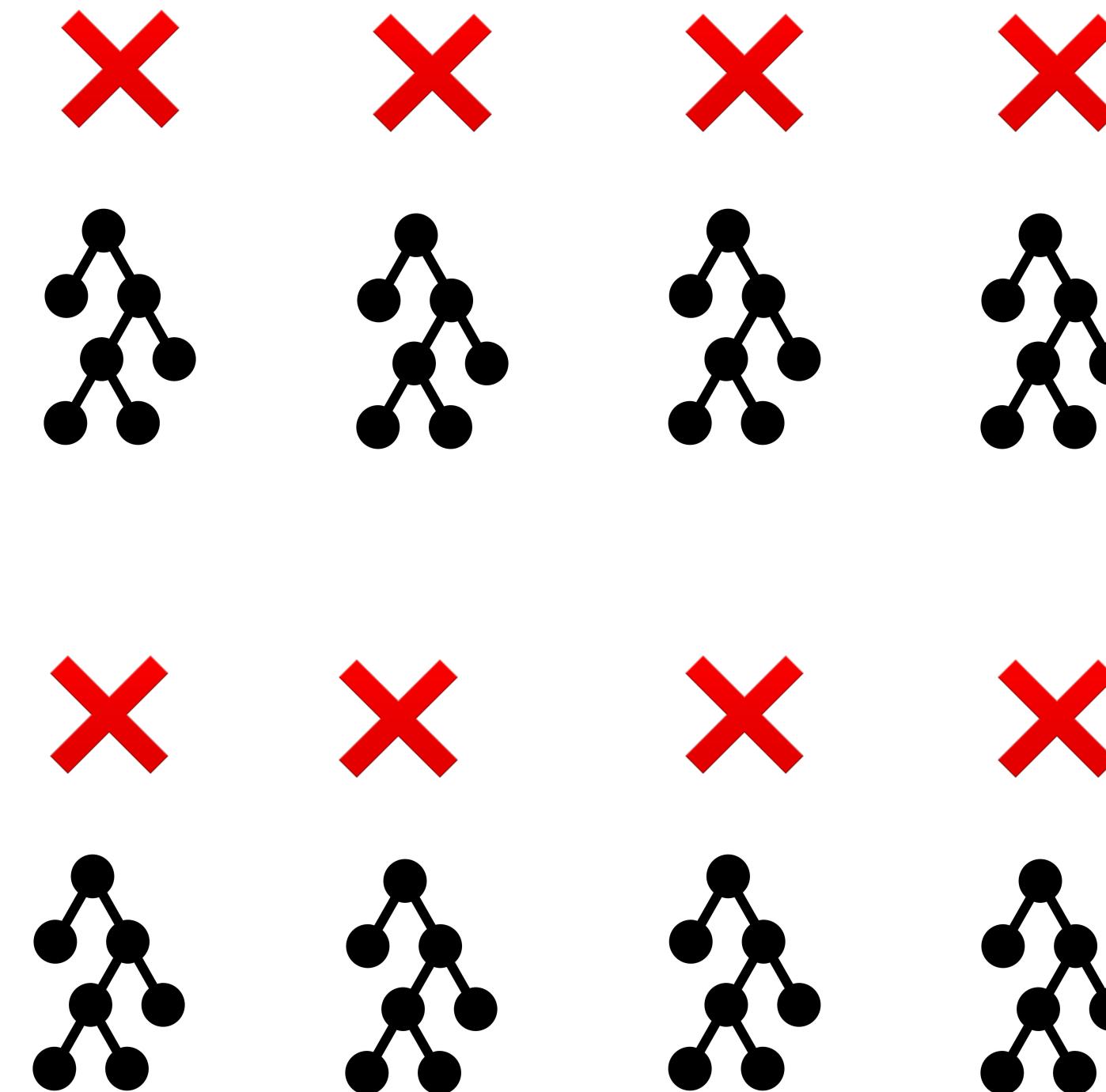
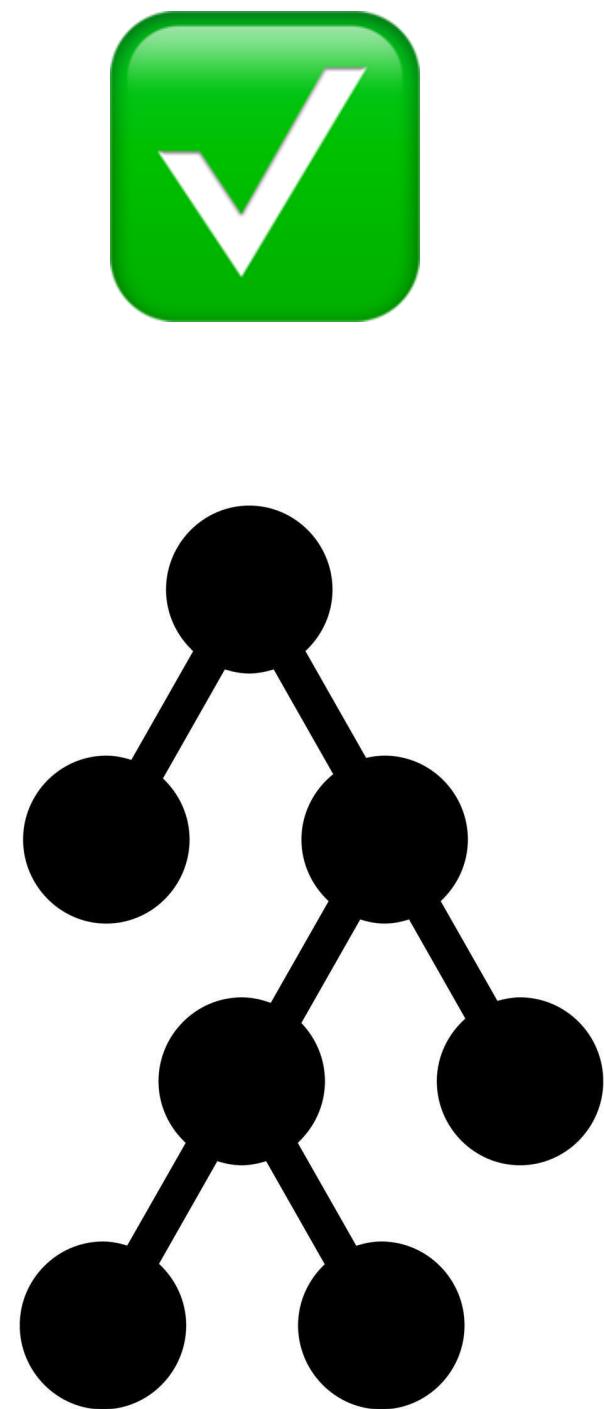
How to Specify it!

A Guide to Writing Properties of Pure Functions.

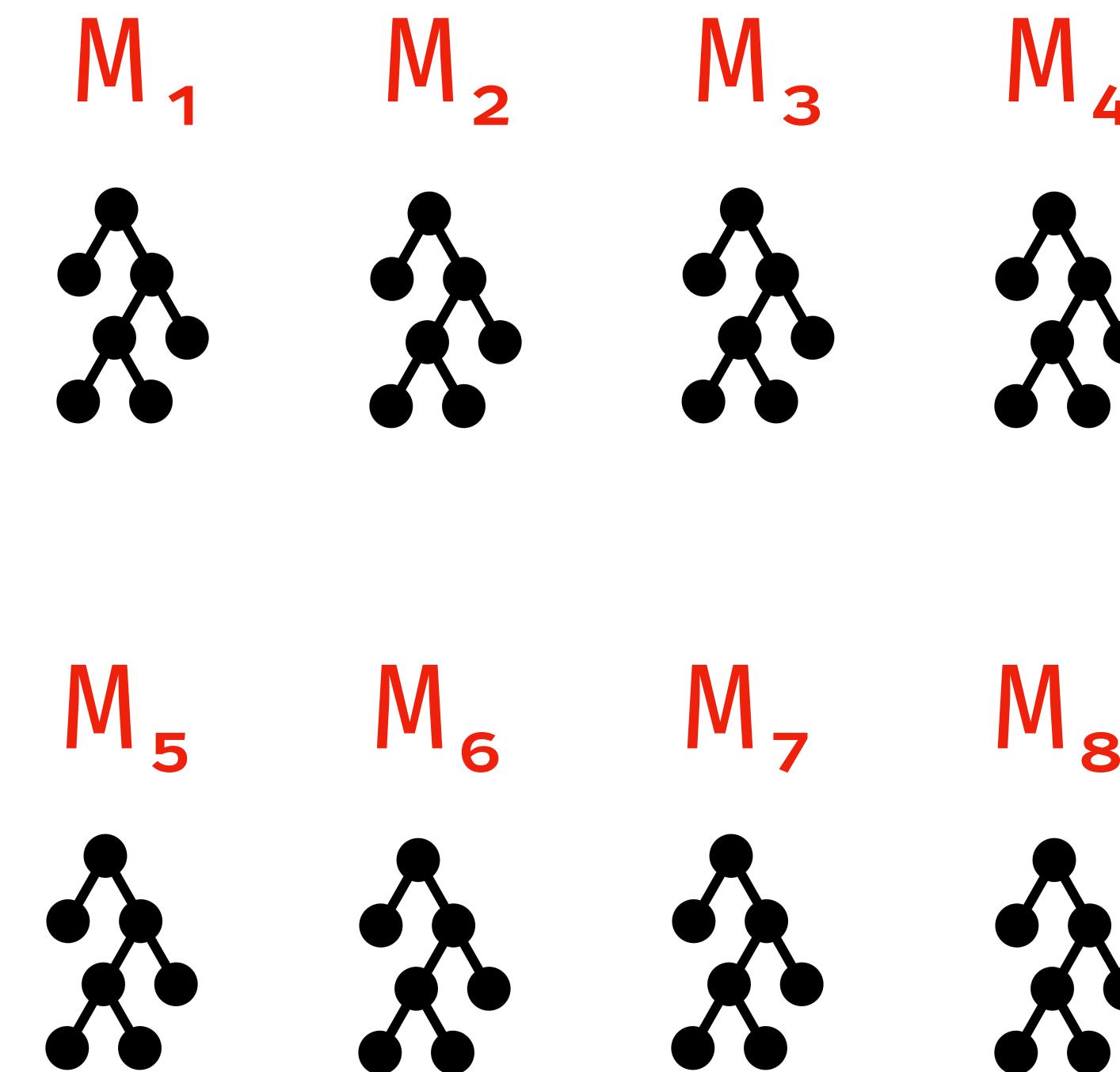
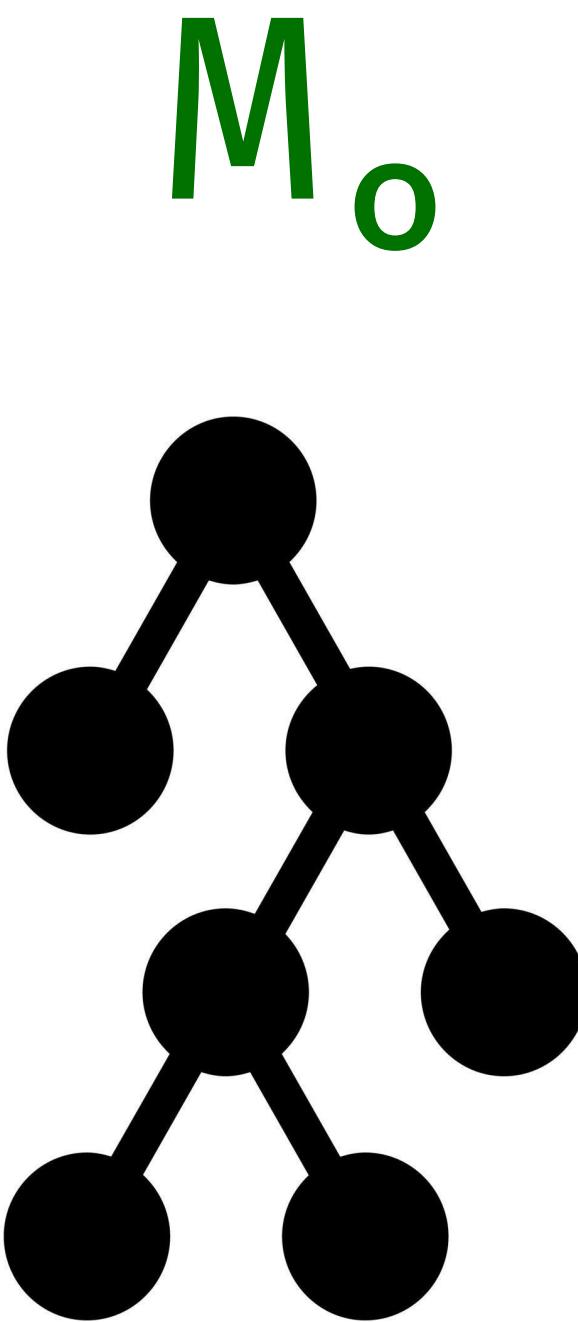
(TFP '19)



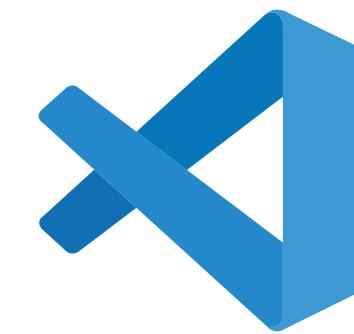
Case study: BSTs done 9 ways



Case study: BSTs done 9 ways



Each bug caught within ~170 random inputs (on average)



VS Code Integration with Tyche

Goldstein et al. (to appear at UIST '24)

TYCHE: Making Sense of Property-Based Testing Effectiveness

Harrison Goldstein

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Jeffrey Tao

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Philadelphia, PA, USA
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Tyche

[Harrison Goldstein](#) | 226 installs |

A VSCode extension for visualizing data produced when testing a Hypothesis property.

Install

VS Code Integration with Tyche

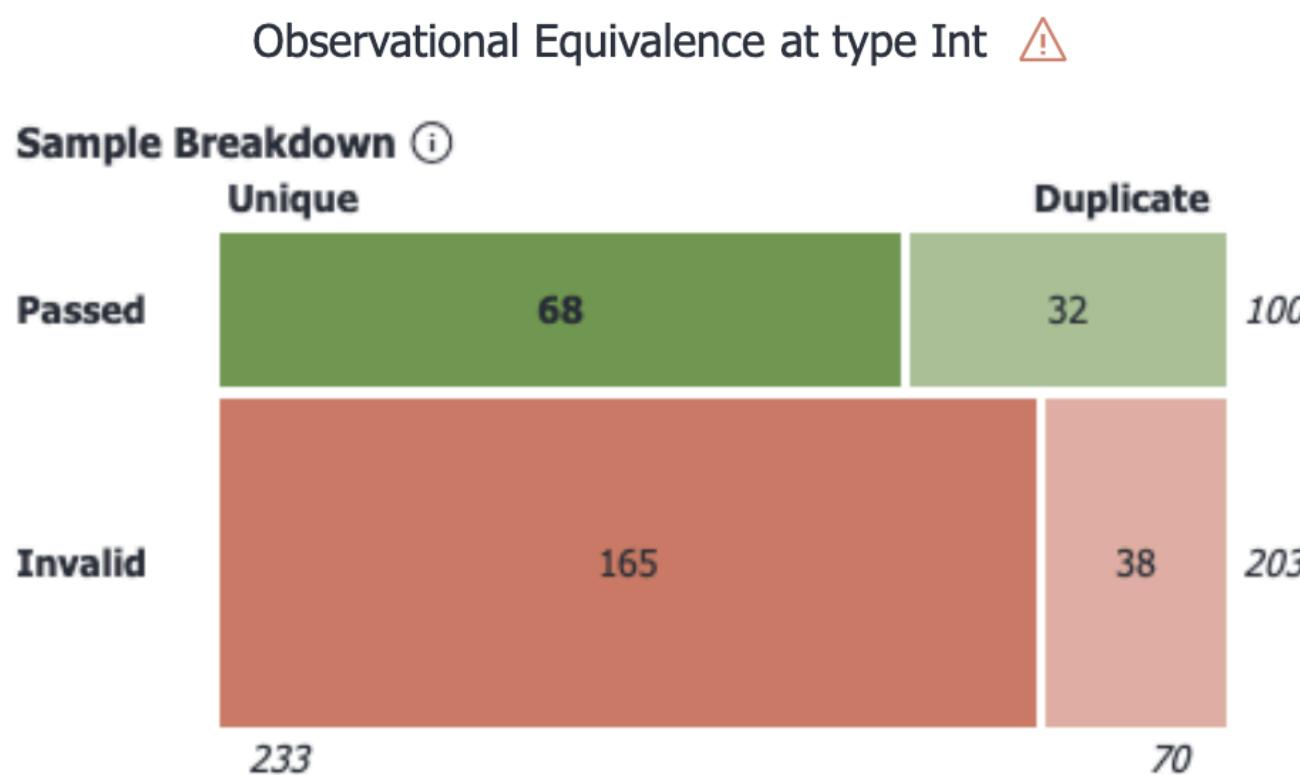
```
module type S = ... [@@deriving mica]  
  
TestHarness(M1)(M2).run_tests ();;
```

Tyche visualizes test metadata produced by Mica

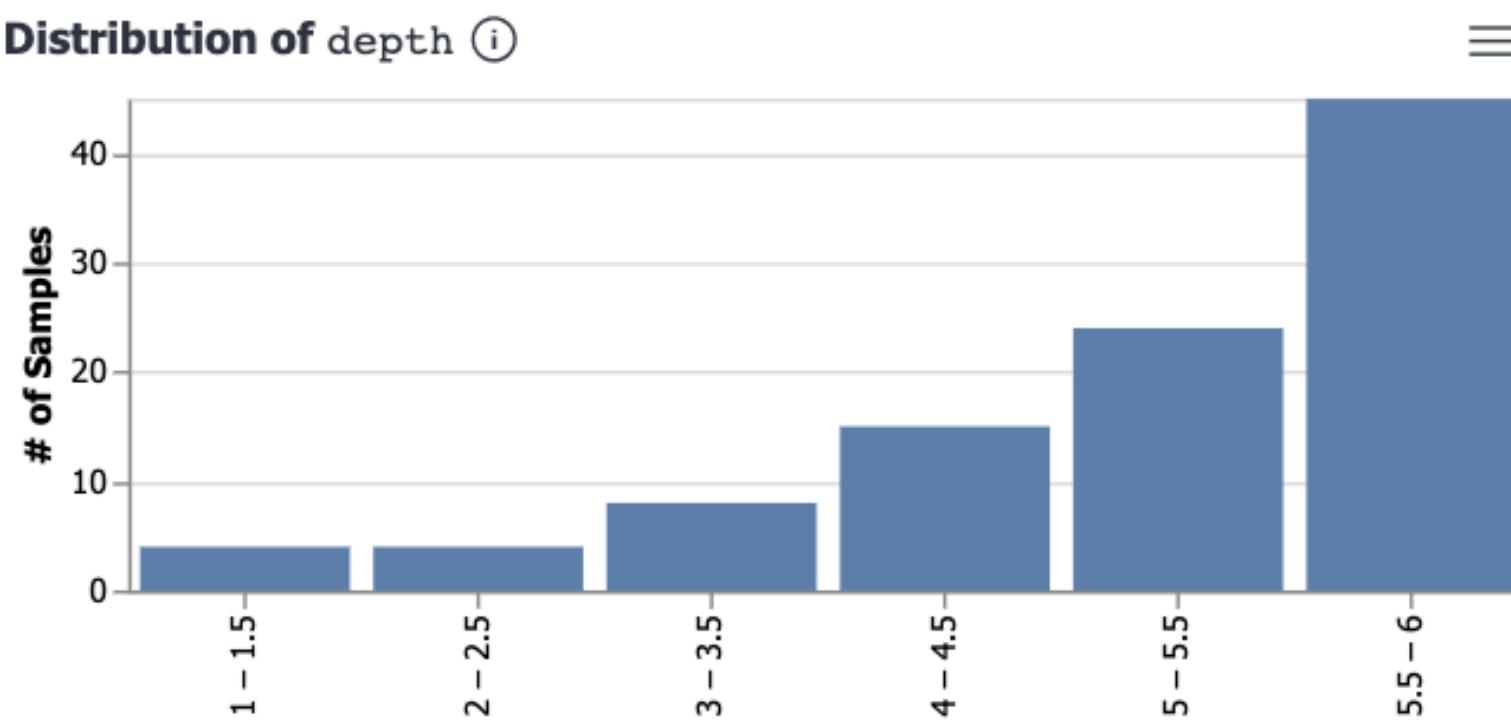


Using Tyche to visualize Mica's test results

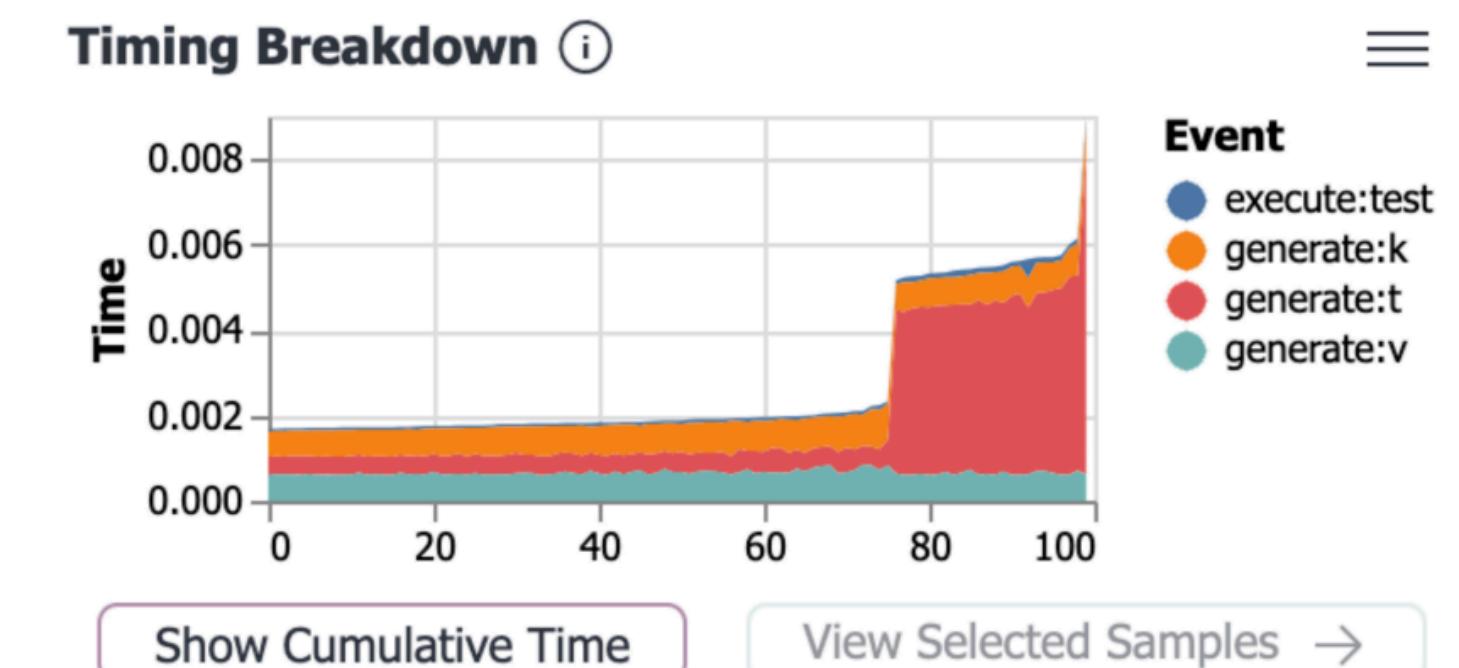
Observational equivalence
test results



Distribution of
symbolic expressions



Timing information



(Size (Add 4 Empty)) 4x

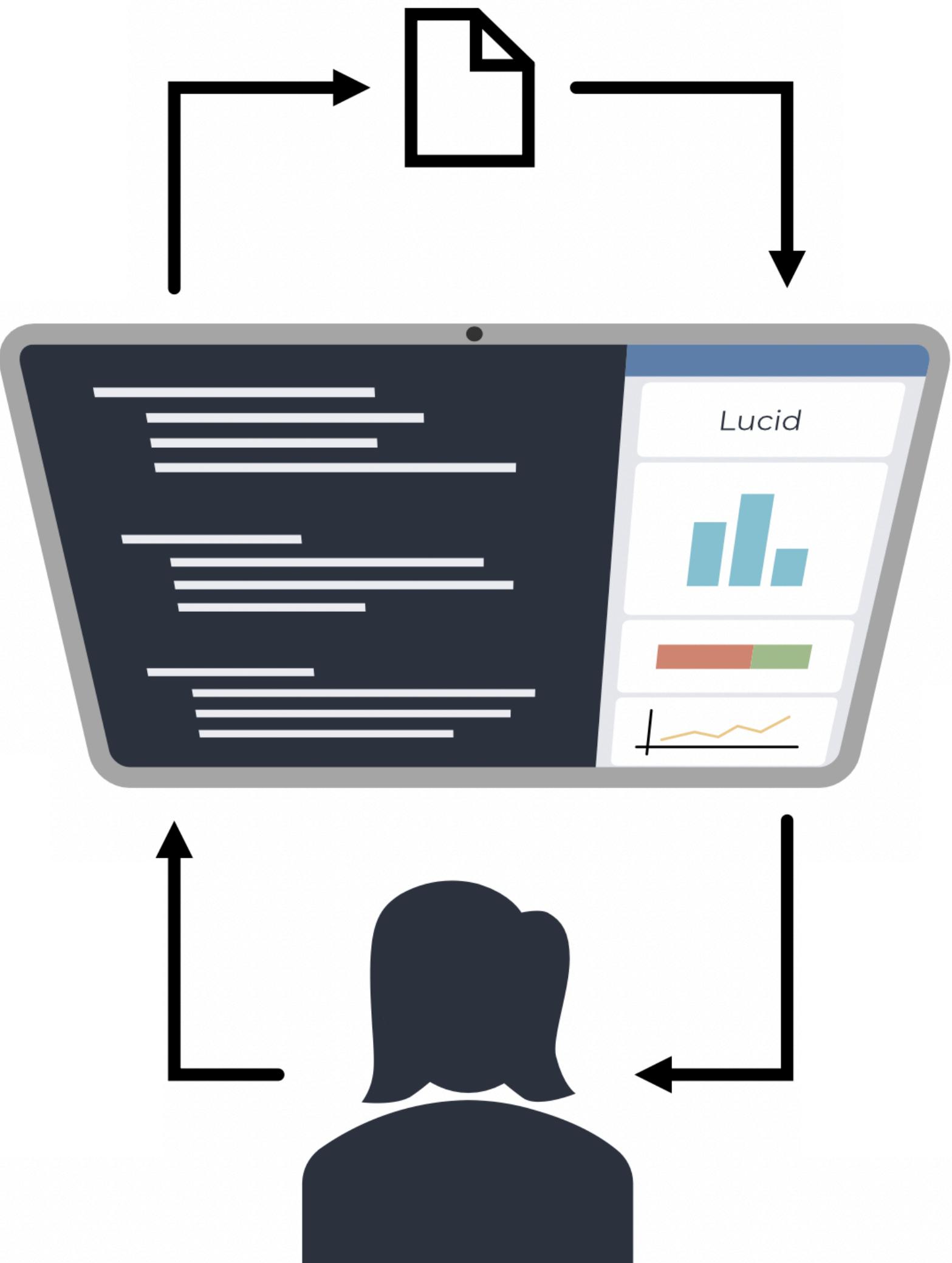
(Size (Add 6 Empty)) 3x

(Size
(Union (Intersect (Add 6 (Add 6 Empty)) (Rem 7 (Add 7 Empty)))
(Add 7 Empty)))

Interacting with Mica + Tyche

1. Annotate module signature & invoke Mica test harness

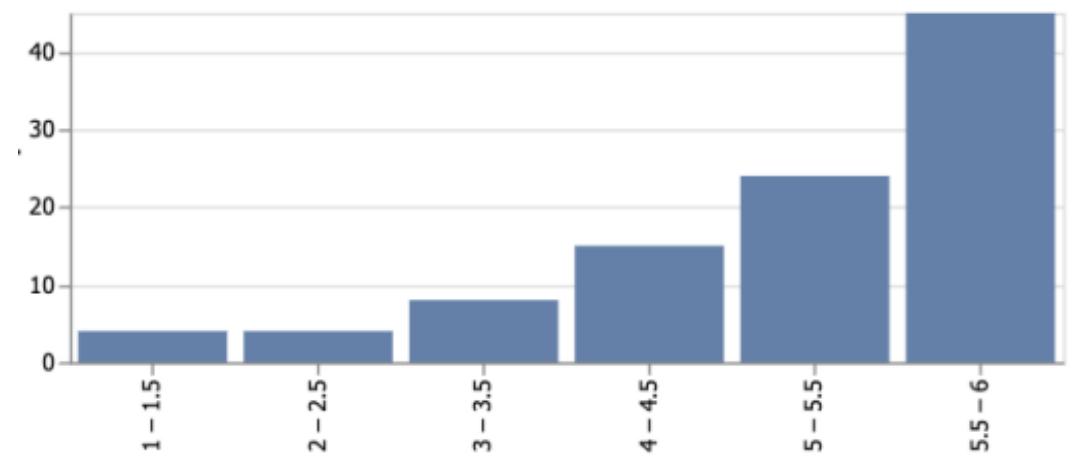
```
module type S = ...  
[@@deriving mica]
```



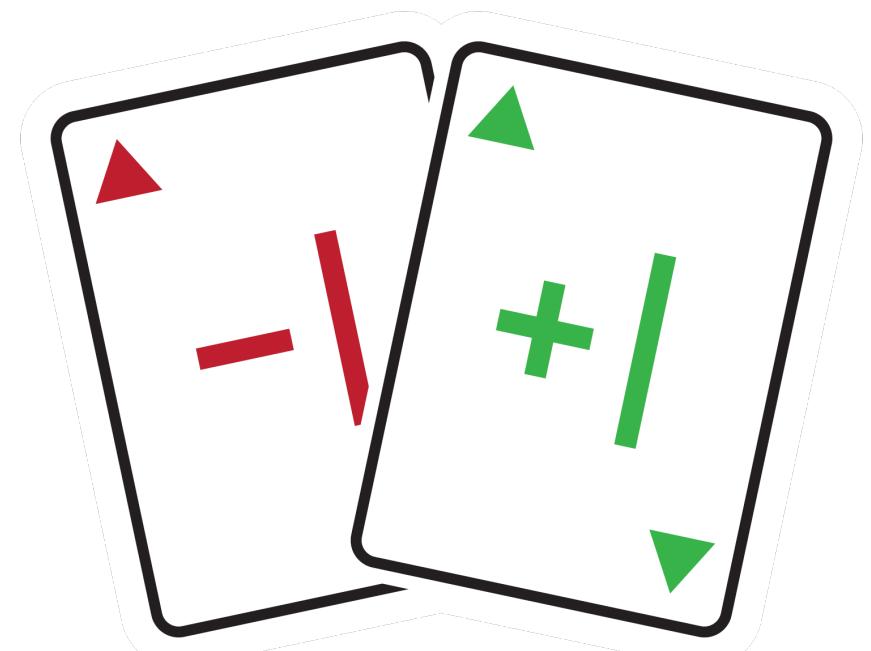
4. Update module implementations

```
module M1 : S = ...  
module M2 : S = ...
```

2. Tyche visualizes test statistics



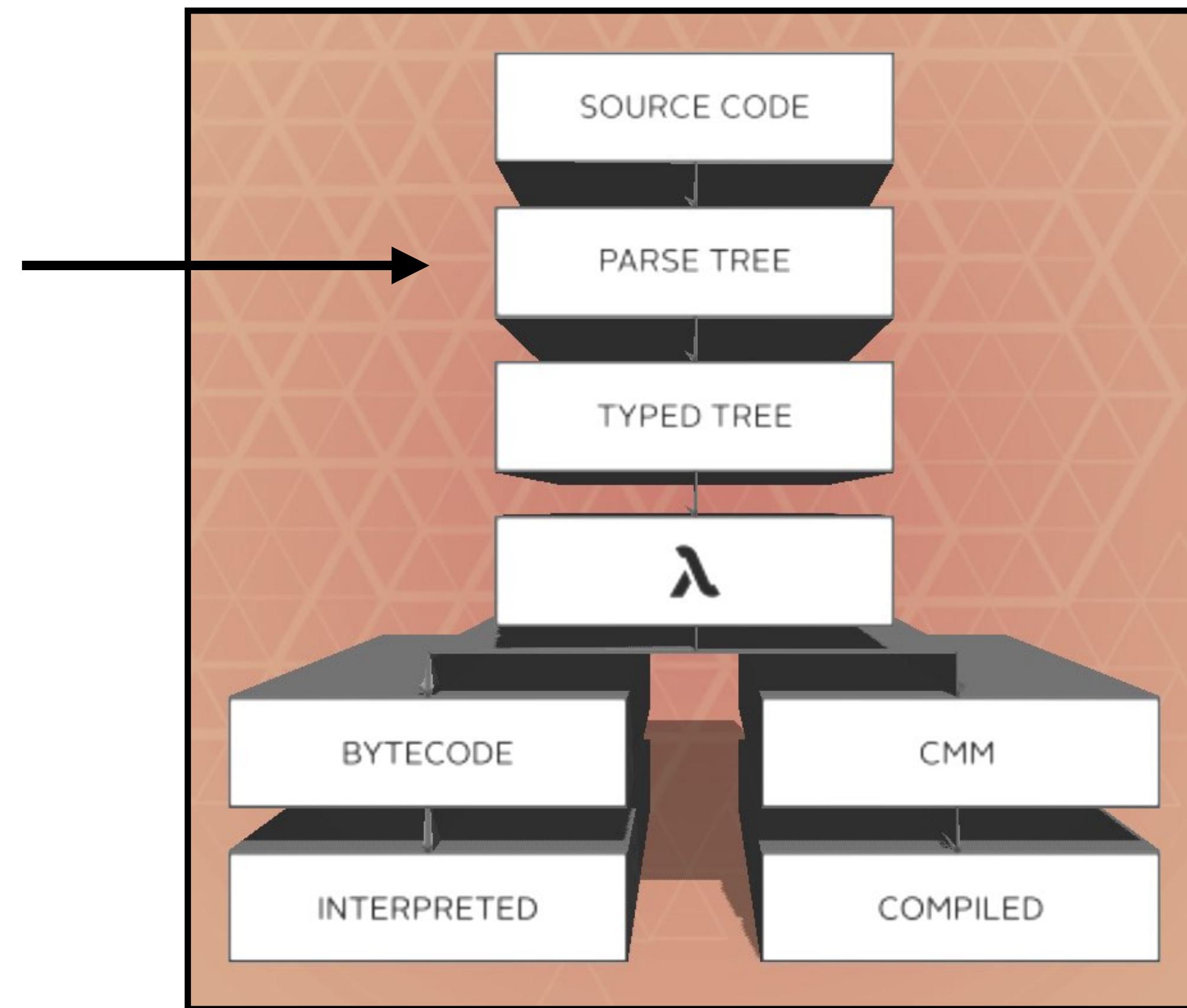
3. Examine test results



Engineering

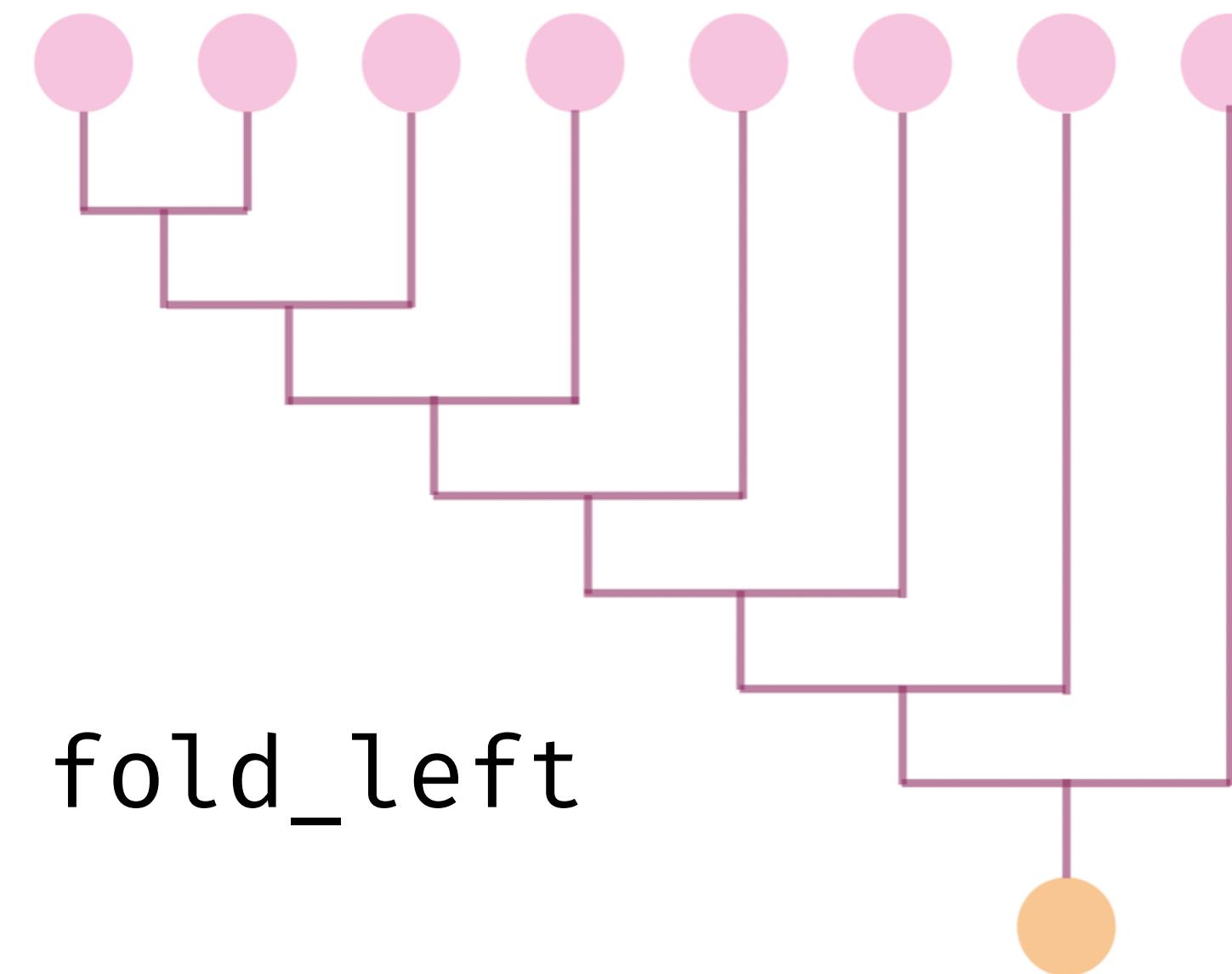
Ppxlib
Produce new AST nodes

~3500 LoC



Future Work

Support more **higher-order functions**



Future Work

Support differential testing of **functors**

```
module F (M1 : S1) ... (Mn : Sn) = ...
```

```
module G (N1 : S1) ... (Nn : Sn) = ...
```

Future Work

Use **coverage-guided fuzzing** to guide Mica's QuickCheck generator

Crowbar
(OCaml '17)



Jane Street

FuzzChick
(OOPSLA '19)



ParaFuzz
(OCaml '21)



Future Work (Engineering)

Contact us if you're interested in contributing to Mica!

- Shrinking
- Modules with multiple abstract types
- Compute “module coverage” for tests
- Support other OCaml PBT libraries

eyn5@cornell.edu

Mica is:

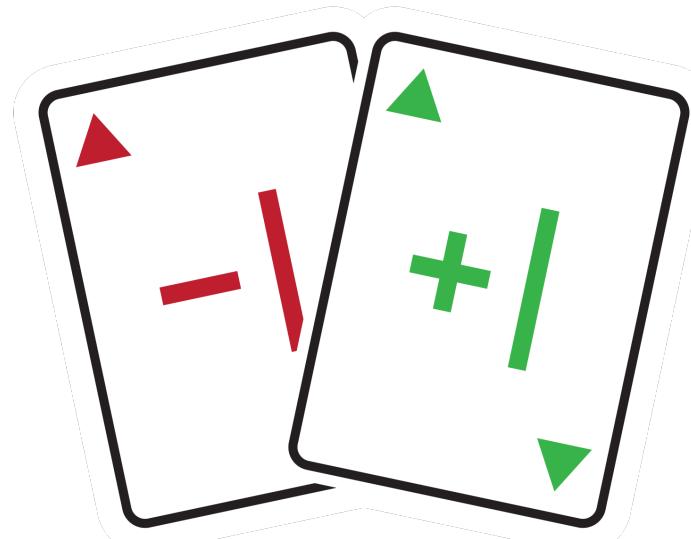
a *PPX extension*

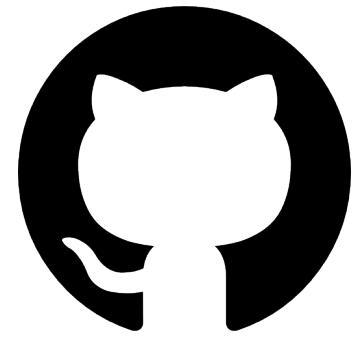
[@deriving mica]

that *automatically* derives
PBT code



for testing
module observational equivalence



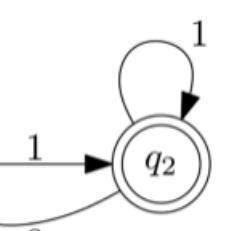


ngernest/mica

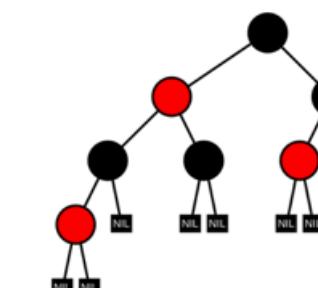
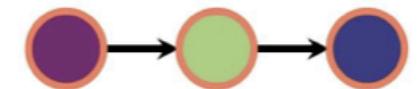
PPX Extension [@deriving mica]



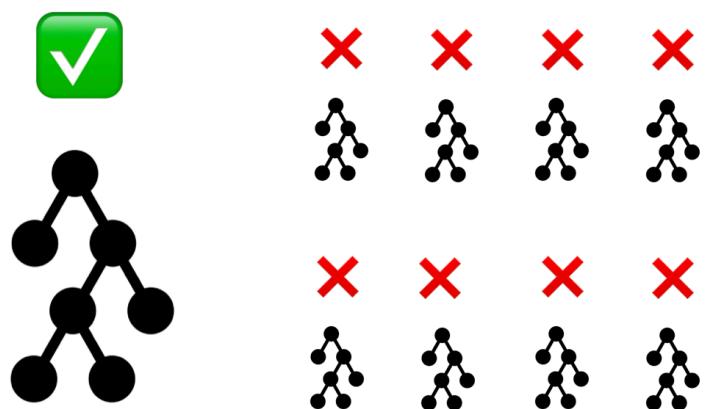
M_1
 M_2



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Ñ Ò Ö Ö Ö × Ø Ù
á â ä å å æ ç è é



9	9	9	9	9	9
9	9	9	9	9	9
0	0	0	0	0	0



Thank you!

Case Studies

VS Code Integration

Goldstein et al. (UIST '24)



Appendix

Monomorphization + Higher-Order Functions for Symbolic Expressions

$\text{`a} \rightsquigarrow \text{int}$

$\text{map} : (\text{`a} \rightarrow \text{`b}) \rightarrow \text{`a t} \rightarrow \text{`b t}$ **Map** of $(\text{int} \rightarrow \text{int}) * \text{expr}$

BST Case Study Statistics

	Bug #1	Bug #2	Bug #3	Bug #4	Bug #5	Bug #6	Bug #7	Bug #8
Min	6	8	504	7	42	10	17	20
Mean	20	62	553	20	286	44	163	229
Max	118	262	765	94	546	238	312	438

Fig. 3. Average mean no. of trials required to provoke failure in an observational equivalence test

Intrinsically-typed Symbolic Expressions via GADTs: Attempt

```
module type S = sig
  type 'a t
  val empty : 'a t
  val is_empty : 'a t → bool
  ...
end

module Interpret (M : S) = struct
  (** GADT for intrinsically typed symbolic expressions *)
  type _ expr =
    | Empty : int M.t expr
    | Is_empty : int M.t expr → bool expr
  ...
end
```

Intrinsically-typed Symbolic Expressions via GADTs: Attempt

```
type _ expr =
| Empty : int M.t expr
| Is_empty : int M.t expr → bool expr
```

...

```
let rec gen_expr ty =
  match ty with
  | IntT → return Empty
  | Bool →
    let%bind (e : int M.t expr) = gen_expr IntT in
    let b_expr : bool expr = Is_empty e in
    return b_expr
```

Error: This expression has type **bool expr Generator.t**
but an expression was expected of type **int M.t expr Generator.t**
Type **bool** is not compatible with type **int M.t**

Interpreting GADT-based intrinsically-typed exprs

```
module type S = sig
  type 'a t
  val empty : 'a t
  val is_empty : 'a t → bool
  ...
end
```

```
module Interpret (M : S) = struct
  type _ value = ...
  type _ expr = ...

  (** [a] is a locally abstract type – [a] is instantiated w/
     different concrete types in the function body *)
  let eval_value (type a) (v : a value) : a =
    match v with
    | ValInt x → x
    | ValIntT intT → intT
    ...

  (** [interp] uses polymorphic recursion *)
  let rec interp : type a. a expr → a =
    fun expr →
      match expr with
      | Value v → eval_value v
      | Empty → M.empty
      | Is_empty e →
          let b = M.is_empty (interp e) in
          eval_value (ValBool b)
    ...
```

Invoking QuickCheck generators for opaque types

```
module type MapInterface = sig
  type t
  val from_list : AssocList.t → t
  ...
end
```

```
let rec gen_expr (ty : ty) : expr Generator.t =
  match ty, QC.size with
  | (T, _) → ...
    let%bind xs = [%quickcheck.generator: AssocList.t] in
    G.return @@ From_list xs
  ...

```

Related Work



Monolith
(Pottier 2021)

Articheck
(Braibant et al. 2014)

- GADT-based DSLs for testing ML modules
- Mutation-based fuzzing
- Mica *automatically* derives the requisite PBT code

Related Work



QCSTM
(Midtgård 2020)

Model_quickcheck
(Dumont 2020)

- Algebraic data types for representing symbolic expressions
- Mica adds support for binary operations on abstract types