Embedded System Design and Modeling

VII. Hierarchical State Machines

Hierarchical state machines

Hierarchical state machines:

- A state in a top-level FSM can be implemented ("refined") as an internal/embedded state machine
  - The top level state = "super-state"
  - An internal state inside it = "sub-state"

Problems:

- Which sub-state is entered?
- What transitions are executed and in what order?

Example

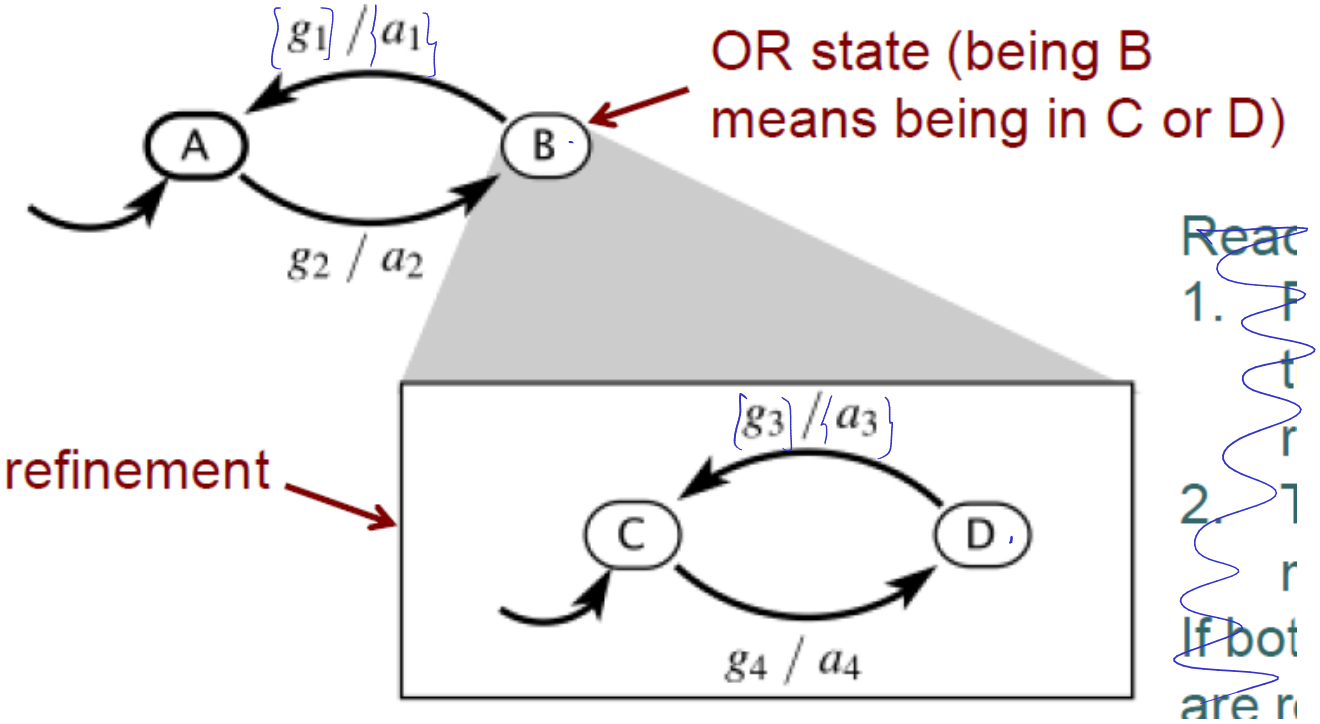


Figure 1: State refinement

Question:

- Suppose the FSM is in sub-state D of B
- If g1 and g3 are both true, which reacts first? The inner FSM or the outer FSM?

Reaction order

Two solutions:

1. [Statecharts language] Inner FSM reacts first, outer FSM reacts later
   - The two reactions are considered simultaneous
   - The output actions are required to not conflict

   In this example:

   - starting from D, inside B
   - check inner transition, g_3 is True $\rightarrow$ a_3 is executed
   - check outer transition, g_1 is True $\rightarrow$ a_1 is executed
   - ending state is A

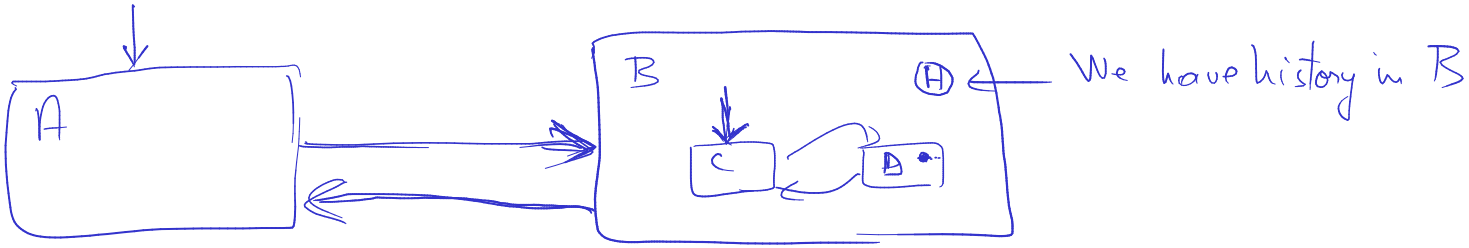
Reaction order

2. [Stateflow, Matlab] Outer FSM reacts first, inner FSM reacts later (if at all)
   - If state is left, the inner FSM will not react at all

   In this example:

   - starting from D, inside B
   - check outer transition, g_1 is True $\rightarrow \{a_1\}$ is executed
   - ending state is A
   - (action a_3 is not executed)

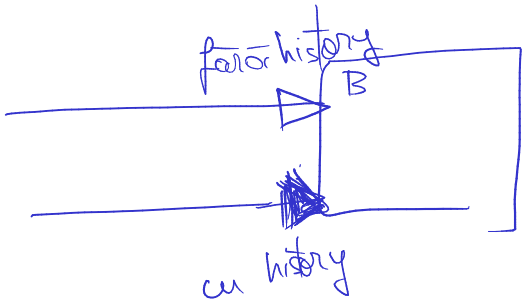
History transitions



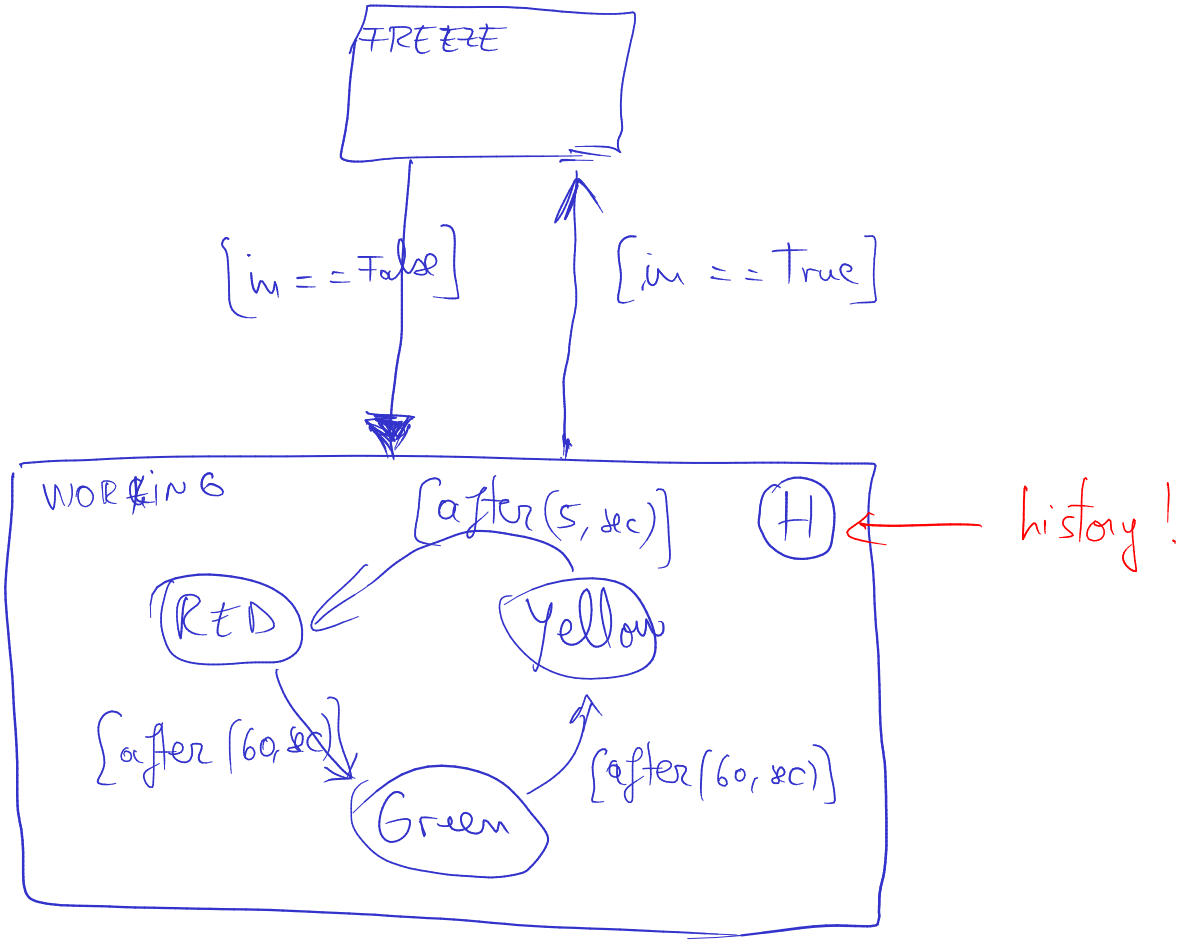
When entering a super-state, which sub-state is entered?

Two solutions:

1. Enter the last sub-state you were in, when you last left the super-state
   - Represented as a **history transition** (marked with a full black arrow on these schematics / a H sign in Matlab)
2. Enter the default sub-state every time
   - Known as a **reset transition** (marked with a white arrow on these schematics / default behavior in Matlab)



Example

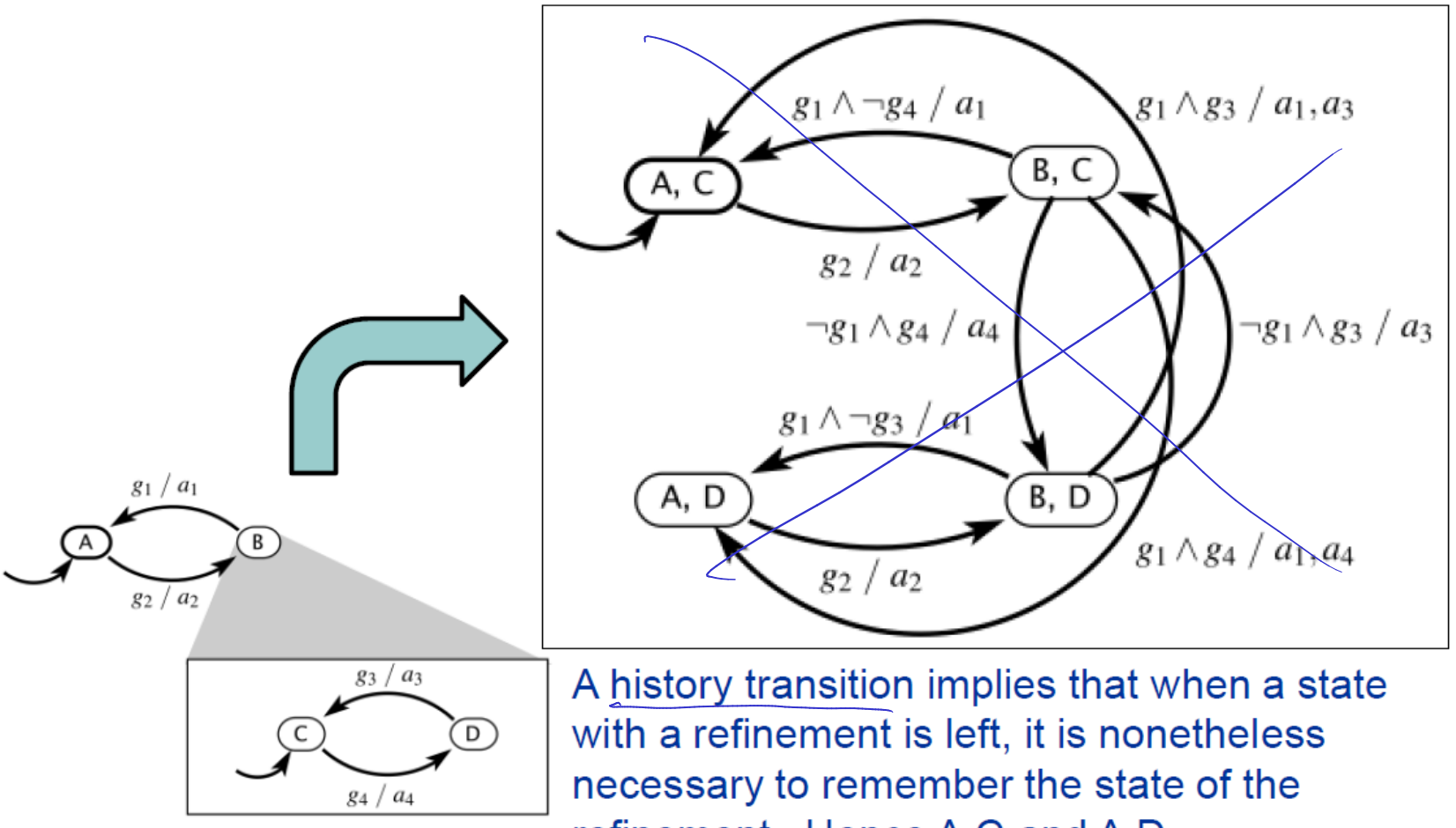

FREEZE
[in == False]
[in == True]
WORKING
[after(5, sec)]
H
history!
RED
Yellow
[after(60, sec)]
Green
[after(60, sec)]

Equivalent flattened FSM

- Any hierarchical FSM can be “flattened”, e.g. converted into an equivalent model with no super-states
  - e.g. Super-state A with two substates B and C is split into to substates AB and AC, transitions from A now leaving from both AB and AC
- Hierarchy in models brings representation efficiency

Example

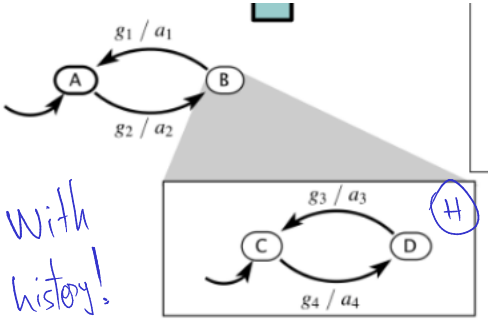
Flattening the state machine (assuming history transitions):



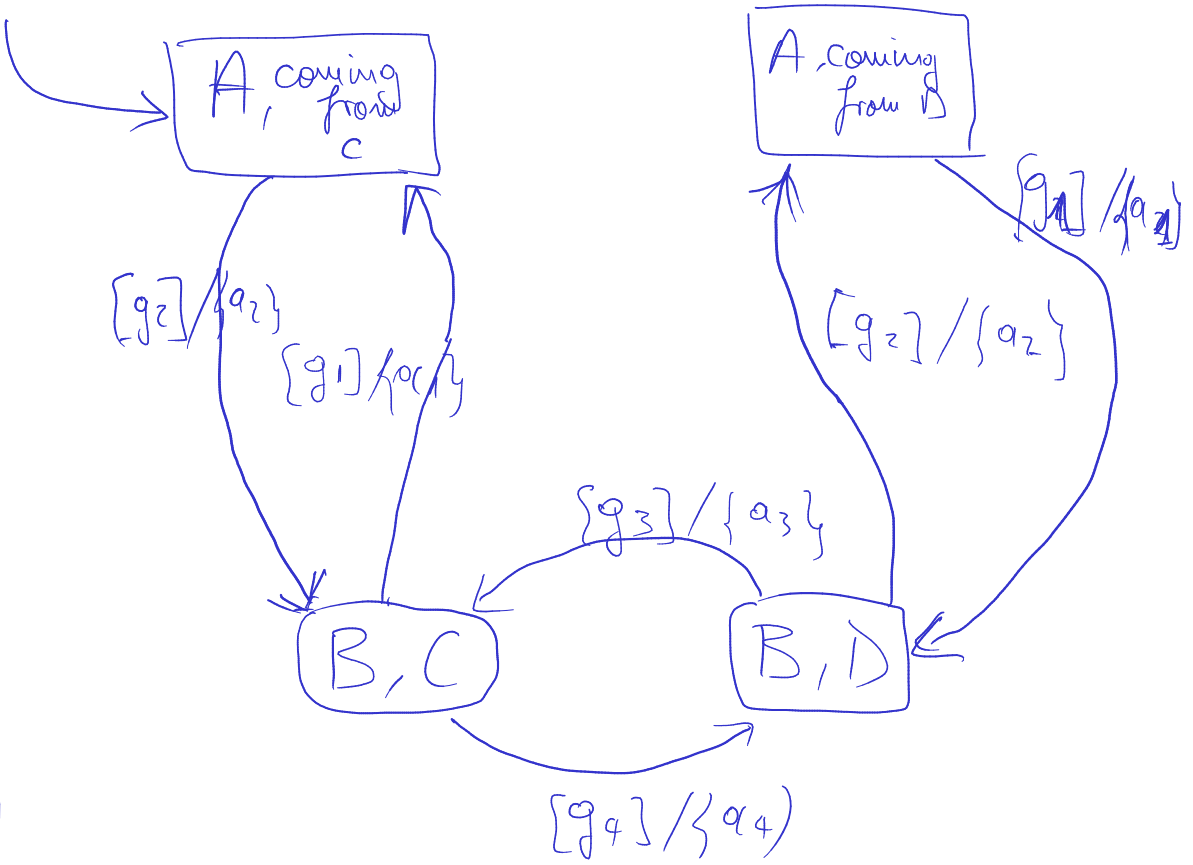
A history transition implies that when a state with a refinement is left, it is nonetheless necessary to remember the state of the refinement. Hence A,C and A,D.

Figure 2: Flattenning example

Example



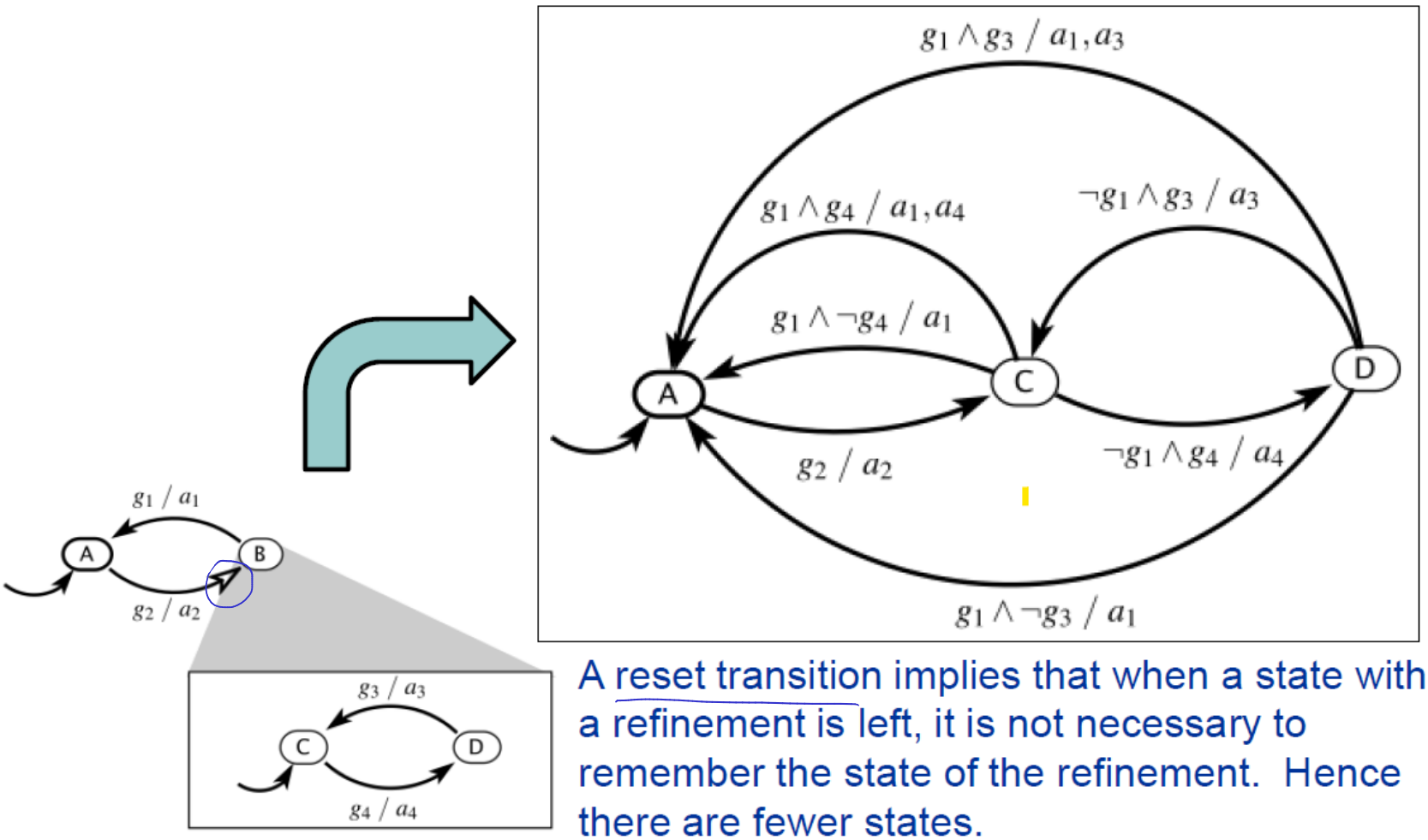
Redraw here



(Assuming
~~Simulink~~
Matlab
Reaction
order)

Example

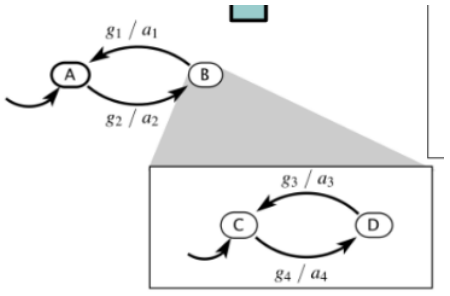
Flattening the state machine
(assuming reset transitions):



A reset transition implies that when a state with a refinement is left, it is not necessary to remember the state of the refinement. Hence there are fewer states.

Figure 3: Flattenning example

Example



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Without history.