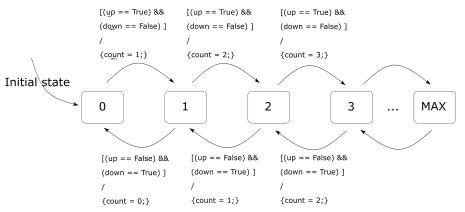
Embedded System Design and Modeling



## FSM example

► Recall the previous FSM example



count = count - 1

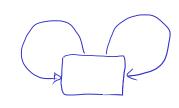


Figure 1: Parking system FSM

Can we make it is simpler to draw?

#### Extended FSMs

count: integer (0, MAX)

Nariables:

► Extended FSM = FSM with internal variables

→ Inputs:
 up: bool
 down: bool
 → Outputs:

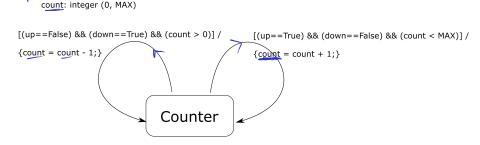


Figure 2: Extended FSM with variable "count"

#### Extended FSM

- The state of the model = the current "bubble" and the values of all the internal variables
- Example: OS hibernation in Windows:
  - ▶ state of computer = all the RAM memory values
  - ▶ if all memory is written down on HDD, and reloaded tomorrow, the system effectively resumes operation from where it left off
- ▶ State is not anymore "the number of bubbles"
  - there is only one "bubble" in our FSM
  - ▶ but there are MAX+1 states (all possible values of the count variable)

### **Declarations**



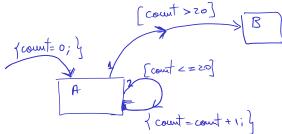
- ► Always make explicit declaration of:
  - model inputs
  - model outputs
  - model internal variables
  - and their data types

#### Measure time

Ts=1 sec.



- Extended FSM are useful for modeling **time-based** conditions:
  - measure passage of time: increment a variable every tick
  - only works if the FSM is time-triggered



# Example: pedestrian crossing light

- How is time measured in the model below?
- How many states does the model below have?

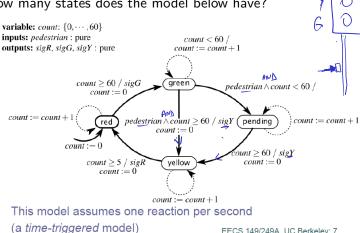
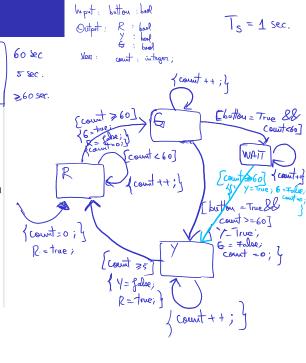


Figure 3: Extended FSM with time measuring <sup>1</sup>

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<sup>&</sup>lt;sup>1</sup>image from Seshia' slides

# Hybrid systems

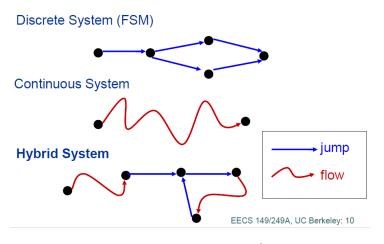


Figure 4: Hybrid systems <sup>2</sup>

<sup>&</sup>lt;sup>2</sup>image from Seshia' slides

# Hybrid systems

- ► **Hybrid systems** = system with mixes discrete and continuous behavior
- Example: a PID controller with different modes:
  - ▶ a set of distinct functioning model (e.g. Startup / Normal / Idle)
  - each state is a sub-system implemented with continuous dynamics
- ▶ State **refinement** = a lower-level implementation of a state

# Types of hybrid systems

- ► **Timed automata** = hybrid system where every state refinement just measures passage of time (differential equation of degree 1)
- ► **Higher-order systems** = hybrid system where every state refinement uses higher-order differential equation (2 or more)
- ► Two-level control systems = complex controllers with two levels of operation
  - high-level discrete modes of operation (e.g. ECU Power Modes: Normal / Startup / Sleep Mode 1 / Sleep Mode 2)
  - low-level refinements with continuous dynamics

#### Timed automata

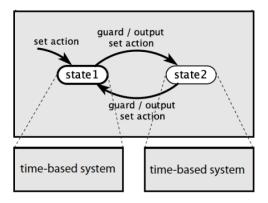


Figure 5: Timed automaton example <sup>3</sup>

<sup>&</sup>lt;sup>3</sup>image from Seshia' slides

## Example

 $\begin{aligned} & \text{continuous variable: } x(t) \in \mathbb{R} \\ & \text{inputs: } click \in \{present, absent\} \\ & \text{outputs: } single, double \in \{present, absent\} \end{aligned}$ 

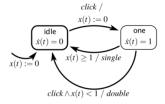


Figure 6: Mouse Double-click detector model <sup>4</sup>

- ▶ Here  $\dot{x}(t) = 1$  means "x(t) increases linearly with time", so it measures time
- ► How many states does this model have?

<sup>&</sup>lt;sup>4</sup>image from Seshia' slides

## Example: Another Thermostat

Temperature threshold is 20 with minimum times  $T_c$  and  $T_b$  in each mode

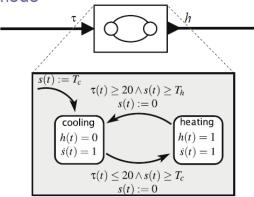


Figure 7: - Another thermostat model as a Timed Automaton <sup>5</sup>

<sup>&</sup>lt;sup>5</sup>image from Seshia' slides

# Example: Another Thermostat

Temperature threshold is 20 with minimum times  $T_c$  and  $T_h$  in each mode

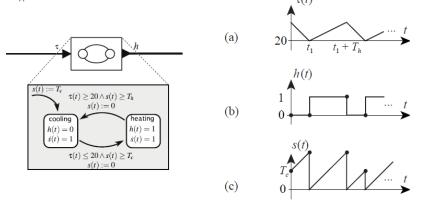


Figure 8: Input and output signals <sup>6</sup>

<sup>&</sup>lt;sup>6</sup>image from Seshia' slides

# Example: Another Traffic Light

### Timed automaton model of a traffic light controller

```
continuous variable: x(t): \mathbb{R}
inputs: pedestrian: pure
outputs: sigR, sigG, sigY: pure
                                            green
             x(t) \ge 60 / sigG
                                           \dot{x}(t) = 1
                                                                  pedestrian \land x(t) < 60 /
                  x(t) := 0
                             pedestrian \land x(t) \ge 60 / sigY
                   red
                                                                     pending
                \dot{x}(t) = 1
                                        x(t) := 0
                                                                      \dot{x}(t) = 1
                                                                x(t) \ge 60 / sigY
                                            yellow
              x(t) \ge 5 / sigR
                                           \dot{x}(t) = 1
                                                                    x(t) := 0
                  x(t) := 0
```

This light remains green at least 60 seconds, and then turns yellow if a pedestrian has requested a crossing. It then remains red for 60 seconds.

Figure 9: Traffic Light controller Timed Automaton <sup>7</sup>

<sup>&</sup>lt;sup>7</sup>image from Seshia' slides

## Example: Tick generator

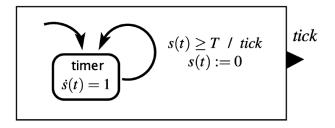


Figure 10: Timed Automaton to generate a *tick* event every T seconds <sup>8</sup>

<sup>&</sup>lt;sup>8</sup>image from Seshia' slides

# Example: Bouncing Ball

Hybrid Automaton for Bouncing Ball

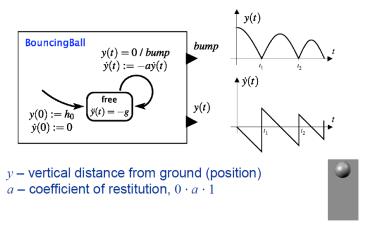


Figure 11: Timed Automaton to simulate a bouncing ball movements <sup>9</sup>

<sup>&</sup>lt;sup>9</sup>image from Seshia' slides

#### FSM simulation software

- ► FSM simulation software
- Used in this class: Stateflow (Simulink / Matlab)
- ► Features:
  - State Actions
  - ► Temporal Logic
  - Other events
  - ▶ ... other ...

#### State actions

- ► Actions can exist not only on transitions, but also **inside states**
- ► Three main types of **State Actions**:
  - entry (en): executed only when a state is entered
  - exit (ex): executed only when a state is exited
  - during (du): executed when we are in state which is neither entered, not exited

### State actions

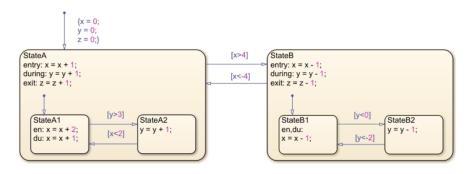


Figure 12: State Actions example <sup>10</sup>

<sup>&</sup>lt;sup>10</sup>image from Matlab docs

### State actions

► State actions can be avoided (use only transitions actions), but sometimes one or the other are more convenient

## Temporal logic

- ► For time-based conditions, states certain predefined variables, which can be used to **measure time spent in a state** 
  - **tick**: measures time steps
    - is incremented at every time step
    - is reset to 0 every time a state is exited or entered
    - actual duration depends on model step size
  - **sec** / **msec**: measures seconds or miliseconds
    - is incremented every second / milisecond
    - is reset to 0 every time a state is exited or entered
    - actual duration is independent on model step size

## Temporal logic

- ► Temporal operators **after()**, **on()**, **every()** can generate events which can be used in conditions
- **Examples**:
  - ► after(10, tick):
    - event is fired after 10 time steps spent in a state
    - evaluates to FALSE for the first 9 steps, is TRUE every time after that
  - on(x, tick):
    - event is fired only **once**, exactly after x time steps spent in a state
    - ightharpoonup evaluates to FALSE for the first x-1 time moments, is TRUE only once at the x-th moment, is FALSE after that
  - every(x, tick):
    - event is fired pariodically after x time steps
    - ightharpoonup evaluates to FALSE for the first x-1 time moments, is TRUE once at the x-th moment, then FALSE for the next x-1 time moments, then TRUE again, and so on

# Temporal logic

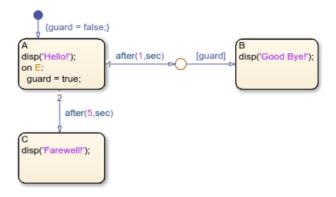


Figure 13: Temporal Logic example  $^{11}$ 

<sup>&</sup>lt;sup>11</sup>image from Matlab docs