

### Actor model of systems

A system can be decomposed as inter-connected building blocks, called "actors"

- Each actor has:
  - ▶ 0, 1 or more input ports
  - ▶ 0, 1 or more output ports
  - ▶ an internal computation / function / what it does
- ► Connections = Signals

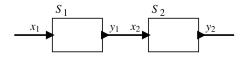


Figure 1: Actor model of systems<sup>1</sup>

<sup>&</sup>lt;sup>1</sup>(Image from Lee & Seshia 2017)

### Actor dynamics

How to describe what a component does?

- ► Continuous dynamics (previous lecture)
- Discrete dynamics (from now on)

Ancient philosophy debate: Heraclitus (continuous) vs Parmenides (discrete)

### Discrete dynamics

- ▶ **Dynamic system** = system whose state evolves in time
- ▶ **Discrete dynamics** = the system operates in a sequence of discrete steps
  - there are no continuous changes (no continuous signals)
  - like digital circuits (values change only on clock front)
- It's more a mathematical model (real-life is continuous), but still extremely useful

## Sample discrete system

Example of discrete system model:

► Sense the cars which enter and leave a parking area (e.g. at barriers), and display the current number of cars inside the parking on a display.

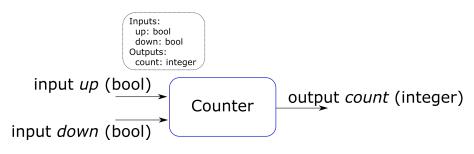


Figure 2: Parking system

### State, reaction, transitions

- ➤ **State** of the system = condition of system at a particular point in time
  - ▶ The state encompasses everything in the past that has any influence at the current moment
- When any input is True, the system reacts
- ► **Reaction** means that the system changes its internal state, and enters a new state
- Moving from one state to the next state means a transition.

## Finite State Machine representation

► Finite State Machine = a system whose operation is described as a set of states and transitions

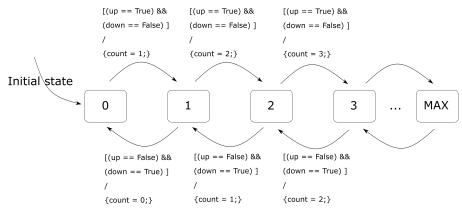


Figure 3: Parking system FSM

# Components of a FSM representation

- ► States = the "bubbles"
- ► Transitions = the arrows
- Conditions (guards) = the conditions on the transitions are taken (inside "[]")
- Actions = the instructions executed when a transition is taken(after "/", inside "{}")

#### FSM notations

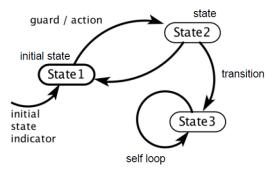


Figure 4: FSM Notations <sup>2</sup>

<sup>&</sup>lt;sup>2</sup>image from Seshia's slides

#### Conditions and actions

- ▶ A transition is taken when its condition becomes True
- When a transition is taken, the actions are executed
- ▶ It is possible that no transition is taken, so the system preserves its state ("default transition")
- The initial transition indicates which is the starting states

#### FSM mathematical model

A FSM is a tuple (States, Inputs, Outputs, update, initialState) consisting of the following:

- ightharpoonup States = a set 0, 1, ...M
- ▶ Inputs = a set of variables with their data types
- Outputs = a set of variables with their data types
- ▶ update = a function f :  $States \times Inputs \rightarrow States \times Outputs$ 
  - ▶ the function takes as inputs = old state + current input values
  - ▶ the function outputs = new state + current output values
- ▶ initialState = the initial state

If all of the above is known, everything is known about the model.

#### Conditions and transitions

- Conditions and transitions can be written in many ways
- ► Here we use a simple C / Matlab instructions:
  - ▶ use == to check equality
  - ▶ ! means negation
  - ► True, False = boolean values
- Examples:
  - ▶ [a == True]
  - ▶ [!a == True]
  - |x>= 3]
  - ► [x < b]
  - ▶ etc . . .

### **Thermostat**

Model example: thermostat

[To draw]

#### When does a reaction occur?

- When are transitions checked? (when do the reactions happen)?
- ► Two variants:
  - Event-triggered model
  - ► Time-triggered model
- Event-triggered model:
  - ▶ The reaction can take time any time.
  - ► The environment triggers the transition, via an **event**
  - Works like an interrupt in microcontrollers
- ▶ Time-triggered model:
  - ► The reaction occurs periodically, on the global *tick* of an **external clock**
  - ightharpoonup e.g. everything runs at  $T_s=10$ ms, 20ms etc.

### Time-triggered models

- ► Simplest case = time-triggered models
- How it works:
  - ▶ the clock ticks, the FSM "wakes up" in a certain state
  - the inputs are read
  - the outgoing transitions from the current state are verified
  - ▶ if a transition is true, it is executed, the system enters a new state
  - the system "goes to sleep" until the next tick

### Event vs time-triggered models

Advantages/disadvantages of time-triggered models:

- ▶ Bad: if a input changes very fast, within a  $T_s$  interval, the model may not see it
- Good: all inputs are read simultaneously
- Good: simple to understand

Advantages/disadvantages of event-triggered models:

- ▶ Bad: the inputs are not synchronized (in a condition a > b, perhaps a changes 1ms faster than b, and this leads to a wrong result
- Good: no risk that values are lost
- Bad: difficult to analyze, difficult to understand

### Properties of discrete models

#### Properties of discrete models

- ▶ **Determinism**: In every state, for all possible input values, at most one transition is enabled
  - if you know the initial state and all the inputs' evolution, you know the complete behavior of the system
- Non-determinism: Models unknown behavior (unknown inputs), or random transitions

### Determinism computation tree

For a fixed input sequence and initial state:

- ► A deterministic system exhibits a single behavior
- ► A non-deterministic system exhibits a set of behaviors, visualized as a **computation tree**

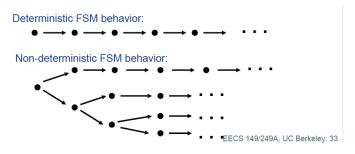


Figure 5: Computation tree <sup>3</sup>

<sup>&</sup>lt;sup>3</sup>image from Seshia's slides