Embedded System Design and Modeling



## FSM example

Recall the previous FSM example

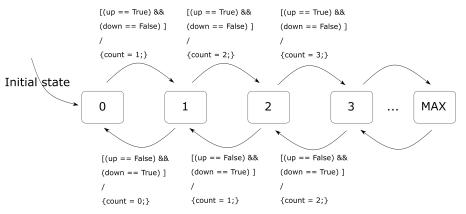


Figure 1: Parking system FSM

Can we make it is simpler to draw?

#### Extended FSMs

#### Extended FSM = FSM with internal variables

```
Inputs:
     up: bool
     down: bool
    Outputs:
                      10
     count: integer (0, MAX)
    Variables:
     count: integer (0, MAX)
[(up==False) && (down==True) && (count > 0)] /
                                                     [(up==True) && (down==False) && (count < MAX)] /
{count = count - 1;}
                                                     \{count = count + 1;\}
                                Counter
```

Figure 2: Extended FSM with variable "count"

#### Extended FSM

- ► The <u>state of the model</u> = the <u>current "bubble</u>" and the <u>values of all</u> the internal variables
- **Example:** OS hibernation in Windows:
  - state of computer = all the RAM memory values
  - ▶ if all memory is written down on HDD, and reloaded tomorrow, the system effectively resumes operation from where it left off
- ► State is not anymore "the number of bubbles"
  - there is only one "bubble" in our FSM
  - ▶ but there are MAX+1 states (all possible values of the count variable)

#### Declarations

- ► Always make explicit declaration of:
  - model inputs
  - model outputs
  - model internal variables
  - and their data types

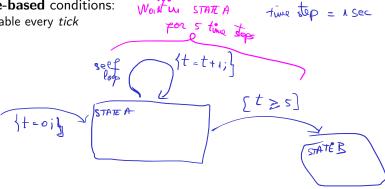
#### Measure time

Variable: + (int)

Extended FSM are useful for modeling **time-based** conditions:

▶ measure passage of time: increment a variable every *tick* 

only works if the FSM is time-triggered



# Example: pedestrian crossing light

- How is time measured in the model below?
- How many states does the model below have?

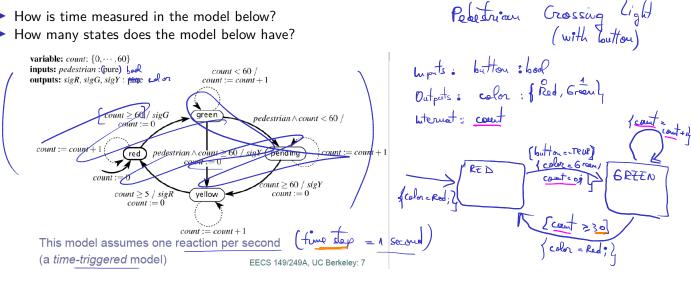


Figure 3: Extended FSM with time measuring (image from Seshia' slides)

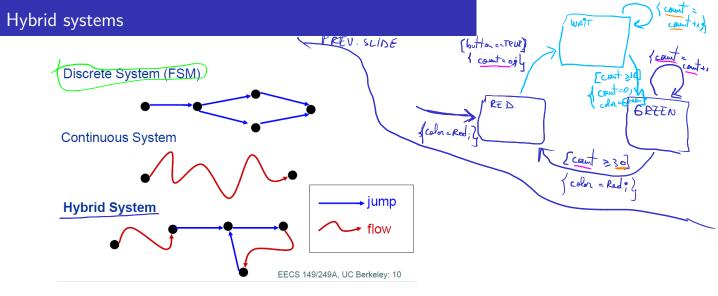
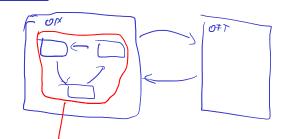


Figure 4: Hybrid systems (image from Seshia' slides)

## Hybrid systems

- ► **Hybrid systems** = system with mixes discrete and continuous behavior
- Example: a PID controller with different modes:
  - ▶ a set of distinct functioning model (e.g. Startup / Normal / Idle)
  - each state is a sub-system implemented with continuous dynamics
- ► State **refinement** = a lower-level implementation of a state



## Types of hybrid systems

- ► **Timed automata** = hybrid system where every state refinement just measures passage of time (differential equation of degree 1)
- ► **Higher-order systems** = hybrid system where every state refinement uses higher-order differential equation (2 or more)
- ► Two-level control systems = complex controllers with two levels of operation
  - high-level discrete modes of operation (e.g. ECU Power Modes: Normal / Startup / Sleep Mode 1 / Sleep Mode 2)
  - low-level refinements with continuous dynamics



### Timed automata

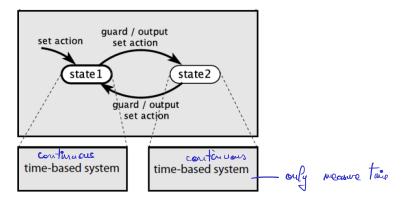


Figure 5: Timed automaton example (image from Seshia's slides)

### Example

Mouse Double-click detector model

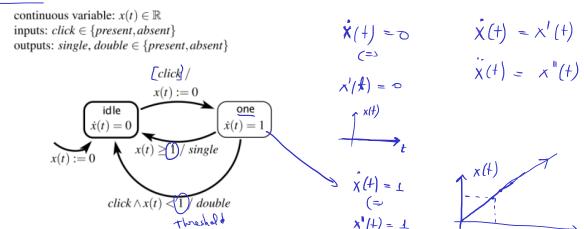


Figure 6: (image from Seshia's slides)

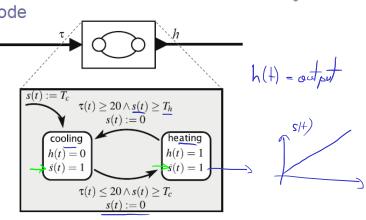
► Here  $\dot{x}(t) = 1$  means "x(t) increases linearly with time", so it measures time

x (+) measures time

## Example: Another Thermostat

Another thermostat model as a Timed Automaton

Temperature threshold is 20 with minimum times  $T_c$  and  $T_h$  in each mode



Tc = Tooling Th = Theoting

Figure 7: (image from Seshia's slides)

## Example: Another Thermostat

Another thermostat model as a Timed Automaton

Temperature threshold is 20 with minimum times  $T_c$  and

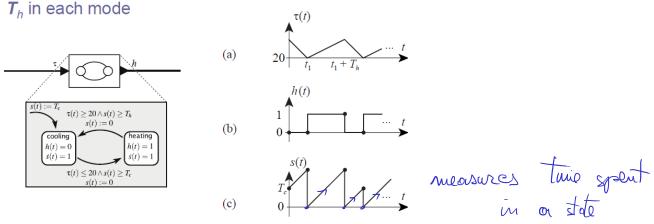
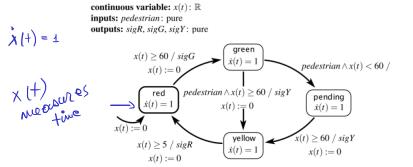


Figure 8: (image from Seshia's slides)

## Example: Another Traffic Light

Traffic Light controller Timed Automaton

## Timed automaton model of a traffic light controller



This light remains green at least 60 seconds, and then turns yellow if a pedestrian has requested a crossing. It then remains red for 60 seconds.

Hybrid cystem

### Example: Tick generator

► Timed Automaton to generate a *tick* every T seconds

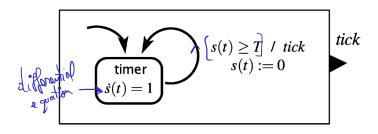
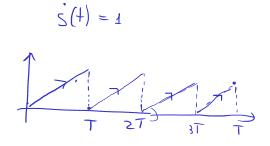


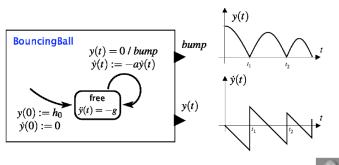
Figure 10: (image from Seshia's slides)



## Example: Bouncing Ball

▶ Timed Automaton to simulate a bouncing ball movements

Hybrid Automaton for Bouncing Ball

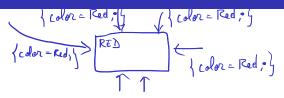


- *y* vertical distance from ground (position)
- a coefficient of restitution,  $0 \cdot a \cdot 1$

### FSM simulation software

- ► FSM simulation software
- Used in this class: Stateflow (Simulink / Matlab)
- ► Features:
  - State Actions
  - ► Temporal Logic
  - Other events
  - ▶ ... other ...

### State actions



- ▶ Actions can exist not only on transitions, but also **inside states**
- ► Three main types of **State Actions**:
  - entry (en): executed only when a state is entered
  - exit (ex): executed only when a state is exited
  - during (du): executed when we are in state which is neither entered, not exited

### State actions

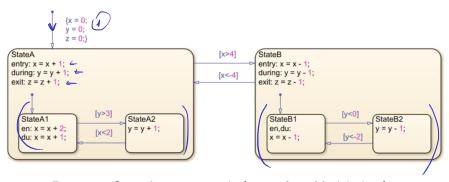


Figure 11: State Actions example (image from Matlab docs)

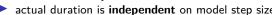
### State actions

► State actions can be avoided (use only transitions actions), but sometimes one or the other are more convenient

## Temporal logic

(tick 25)

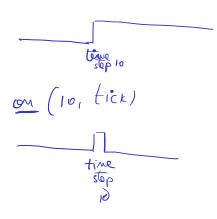
- ► For time-based conditions, states certain predefined variables, which can be used to measure time spent in a state
  - tick: measures time steps
    - is incremented at every time step
    - is reset to 0 every time a state is exited or entered
    - actual duration depends on model step size
  - **sec** / **msec**: measures seconds or miliseconds
    - is incremented every second / milisecond
    - is reset to 0 every time a state is exited or entered
    - actual duration is independent on model step size





## Temporal logic

- ► Temporal operators <u>after()</u>, <u>on()</u>, <u>every()</u> can generate events which can be used in conditions
- Examples:
  - after(10, tick):
    - event is fired after 10 time steps spent in a state
    - evaluates to FALSE for the first 9 steps, is TRUE every time after that
  - **►** on(x, tick):
    - event is fired only **once**, exactly after x time steps spent in a state
    - ightharpoonup evaluates to FALSE for the first x-1 time moments, is TRUE only once at the x-th moment, is FALSE after that
  - every(x, tick):
    - event is fired pariodically after x time steps
    - evaluates to FALSE for the first x-1 time moments, is TRUE once at the x-th moment, then FALSE for the next x-1 time moments, then TRUE again, and so on



## Temporal logic

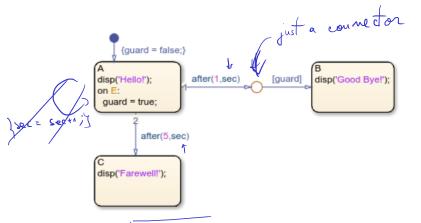


Figure 12: Temporal Logic example (image from Matlab docs)

