Embedded System Design and Modeling

VI. Composition of State Machines

Composition of state machines

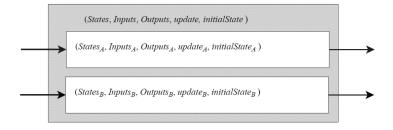
- ▶ How to combine multiple smaller FSMs into a bigger one?
- ► What problems arise?
- Two types of compositions:
 - 1. **Spatial** composition: how are the components connected?
 - 2. **Temporal** composition: how do the components react in time?

Spatial composition

 ${f Spatial}$ composition = how are two components connected, how does the information flow between the components

- ➤ **Side-by-side** composition = no common inputs/outputs, no shared data
- ► Cascade composition = Outputs of one FSM are inputs to another one
- ► Feedback composition = (Some) outputs of a FSM are inputs to the same FSM, or to some other component which is in front

Side-by-side composition



 $\label{eq:Figure 1: Side-by-side composition} Figure \ 1: \ Side-by-side \ composition$

Cascade composition

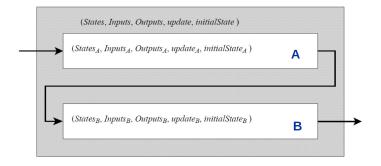


Figure 2: Cascade composition

▶ Outputs of FSM A are inputs to FSM B

Feedback composition

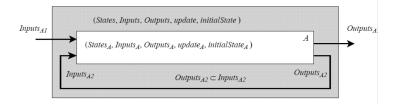


Figure 3: Feedback composition

Some outputs of the FSM are coming back as inputs

Temporal composition

Temporal composition = when do two components react?

- ► Sequential vs Parallel composition:
 - ▶ **Sequential** = the two FSM do not work at the same time
 - ▶ Parallel = the two FSM work at the same time
- ► Asynchonous vs Synchronous composition = only for parallel composition
 - **Synchronous** = transitions are taken at the same time in both FSMs
 - ► **Asynchronous** = transitions are taken at independent times in the FSMs

Sequential composition

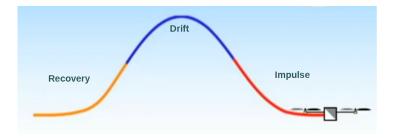


Figure 4: Example of Sequential composition

- ► 13579/:https://wwwoutubeom/watch?vD3QgGpzzIM
- ▶ The drone has three modes of operation, working **in sequence**

Parallel composition



Figure 5: Side-by-side composition

- ► The two FSMs form an equivalent model
- ▶ When do the transitions in these FSM take place?
 - ► Synchronous: simultaneously
 - ► Asynchronous: independently

- ► Consider the two FSM on the left (A and B)
- ► The equivalent model is on the right

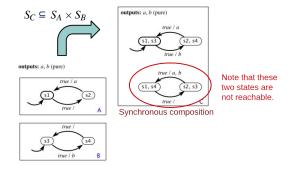
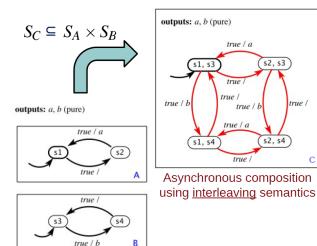


Figure 6: Synchronous composition

Redraw here

- ► In the equivalent model:
 - ► States = combination of states of the two FSMs
 - ► Transition = transition in FSM A and FSM B, happening simultaneously.
 - ► There might exist unreachable states in the equivalent model (states that will never be reached)

Draw here



Note that now all states are reachable.

С

Figure 7: Asynchronous composition

- ► In the equivalent model:
 - States = combination of states of the two FSMs
 - Transitions in the two FSMs can take place at irregular and independent (not synchronized) times
 - ► All states are reachable
 - because one model can be much faster than the other

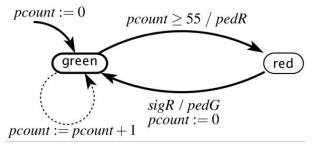
Flavors of asynchronous composition

- ► How are simultaneous transitions handled?
- ► **Interleaving** semantics:
 - ▶ simultaneous transition in models A and B is not allowed (we may have either a transition in model A, or a transition in B)
 - ▶ i.e. transition from A takes place first, then transition from B takes place after a non-zero time delay (or vice-versa)
- ► Simultaneous semantics:
 - simultaneous transition in models A and B is allowed
 - for example, we may have either
 - transition only in model A
 - transition only in model B
 - Simultaneous transition in models A and B

variable: pcount: $\{0, \dots, 55\}$

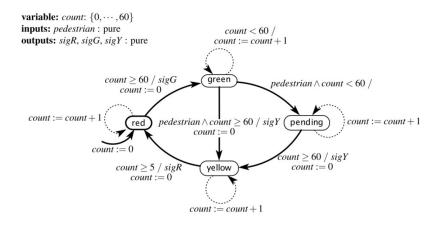
input: *sigR*: pure

outputs: *pedG*, *pedR*: pure



This light stays green for 55 seconds, then goes red. Upon receiving a sigR input, it repeats the cycle.

Figure 8: Composition - Pedestrian Light



 $\mbox{Figure 9: Composition - Car Light} \\$

Pedestrian Light with Car Light variable: count: {0, · · · ,60} inputs: pedestrian : pure count < 60 / outputs: sigR, sigG, sigY: pure count := count + 1sigY count > 60 / sigGgreen $pedestrian \land count < 60 /$ sigG count := count + 1 $pedestrian \land count \ge 60 / sigY$ pending count := count +count := 0sigR count := 0 $ount \ge 60 / sigY$ count := 0 $count \ge 5 / sigR$ yellow count := 0count := count + 1variable: pcount: {0, ..., 55} input: sigR: pure sigR outputs: pedG, pedR: pure What is the size of pedG pcount := 0 $pcount \ge 55 / pedR$ the state space of the pedR composite machine? green red sigR / pedG pcount := 0pcount := pcount +

Figure 10: Cascade Composition - Both Lights

