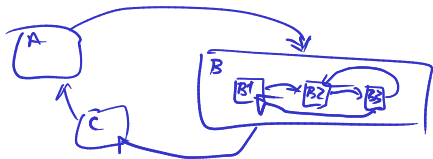


# Embedded System Design and Modeling

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## VII. Hierarchical State Machines

# Hierarchical state machines



Hierarchical state machines:

- ▶ A state in a top-level FSM can be implemented (“refined”) as an internal/embedded state machine
  - ▶ The top level state = “super-state”
  - ▶ An internal state inside it = “sub-state”



Problems:

- ▶ Which sub-state is entered?
- ▶ What transitions are executed and in what order?



# Example

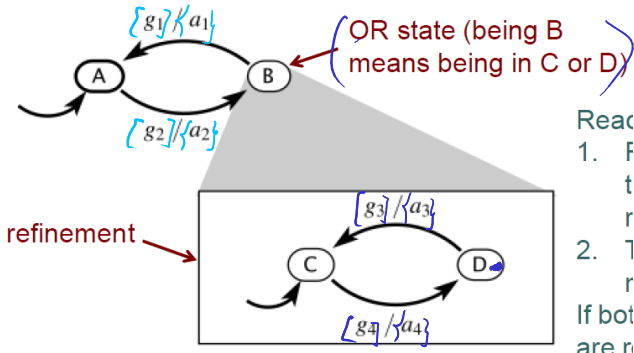


Figure 1: State refinement

Question:

- Suppose the FSM is in sub-state D of B
- If  $g_1$  and  $g_3$  are both true, which reacts first? The inner FSM or the outer FSM?



# Reaction order

Two solutions:

1. [Statecharts language] Inner FSM reacts first, outer FSM reacts later
  - ▶ The two reactions are considered simultaneous
  - ▶ The output actions are required to not conflict

In this example:

- ▶ starting from D, inside B
- ▶ check inner transition,  $g_3$  is True  $\rightarrow a_3$  is executed
- ▶ check outer transition,  $g_1$  is True  $\rightarrow a_1$  is executed
- ▶ ending state is A

2. [Stateflow, Matlab] Outer FSM reacts first, inner FSM reacts later (if at all)
- ▶ If state is left, the inner FSM will not react at all

In this example:

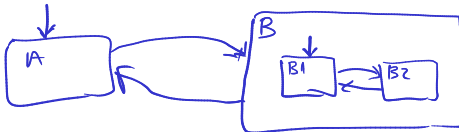
- ▶ starting from D, inside B
- ▶ check outer transition,  $g_1$  is True  $\rightarrow$   $a_1$  is executed
- ▶ ending state is A
- ▶ (action  $a_3$  is not executed)

# History transitions

When entering a super-state, which sub-state is entered?

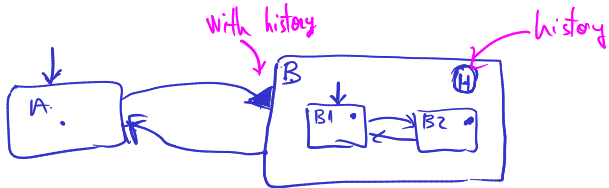
Two solutions:

1. Enter the last sub-state you were in, when you last left the super-state
  - ▶ Represented as a **history transition** (marked with a full black arrow on these schematics / a H sign in Matlab)
2. Enter the default sub-state every time
  - ▶ Known as a **reset transition** (marked with a white arrow on these schematics / default behavior in Matlab)



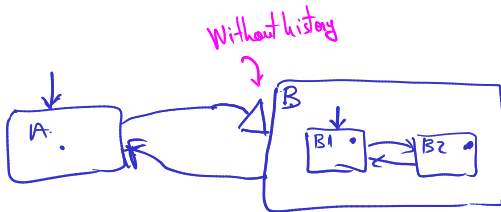
# Example

With history :



$A \rightarrow B(B_1) \rightarrow B(B_2) \longrightarrow A \rightarrow B(B_2)$

Without history :



$A \rightarrow B(B_1) \rightarrow B(B_2) \longrightarrow A \rightarrow B(B_1)$



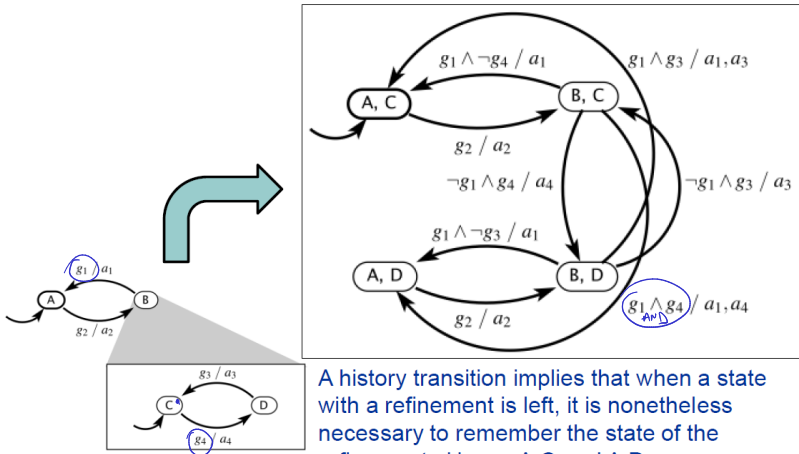
# Equivalent flattened FSM

- ▶ Any hierarchical FSM can be “flattened”, e.g. converted into an equivalent model with no super-states
  - ▶ e.g. Super-state A with two substates B and C is split into to substates AB and AC, transitions from A now leaving from both AB and AC
- ▶ Hierarchy in models brings representation efficiency

# Example

Flattening the state machine  
(assuming history transitions):

Non-Markov order :  
- inner first  
- outer later

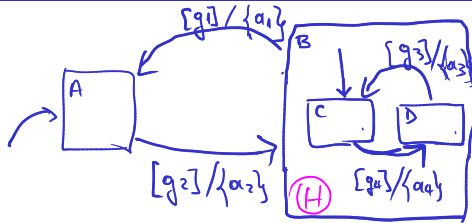


A history transition implies that when a state with a refinement is left, it is nonetheless necessary to remember the state of the refinement. Hence A,C and A,D.

Figure 2: Flattening example

# Example

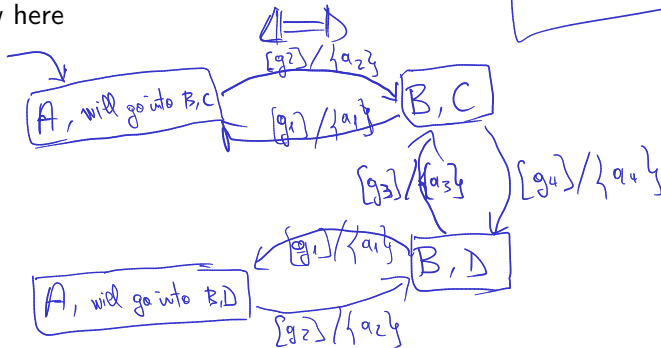
With history for B



Matlab's order of checking transitions:

- outer first
- inner later, if at all

Redraw here

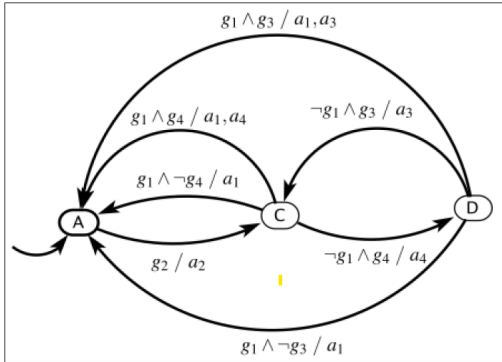
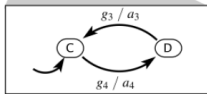


# Example

Flattening the state machine  
(assuming reset transitions):

No history

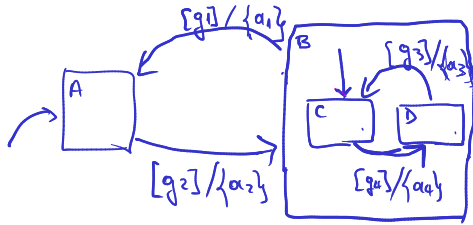
With history



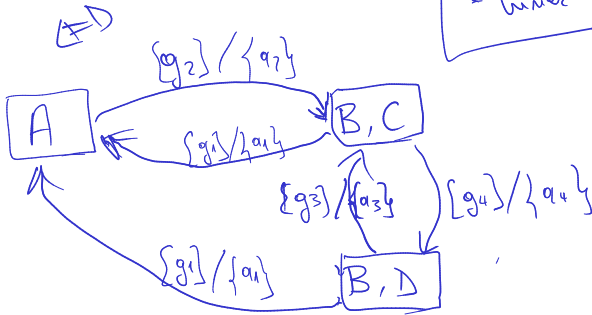
A reset transition implies that when a state with a refinement is left, it is not necessary to remember the state of the refinement. Hence there are fewer states.

Figure 3: Flattenning example

# Example Without history for B



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! Matlab's order of checking transitions:  
- outer first  
- inner later, if at all