

## Embedded System Design and Modeling

## VII. Hierarchical State Machines

# Hierarchical state machines

Hierarchical state machines:

- ▶ A state in a top-level FSM can be implemented (“refined”) as an internal/embedded state machine
  - ▶ The top level state = “super-state”
  - ▶ An internal state inside it = “sub-state”

Problems:

- ▶ Which sub-state is entered?
- ▶ What transitions are executed and in what order?

## Example

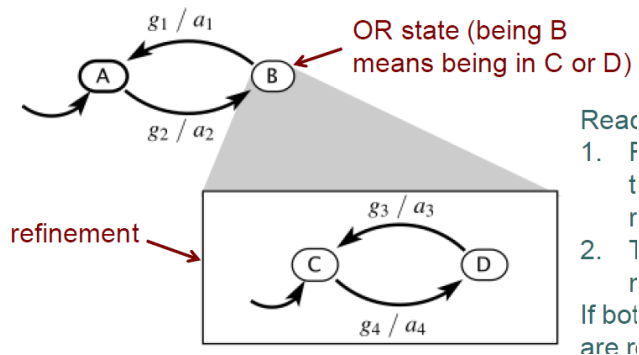


Figure 1: State refinement

- If  $g_1$  and  $g_3$  are both true, which reacts first? The inner FSM or the outer FSM?

Two solutions:

- ▶ 1. [Statecharts language] Inner FSM reacts first, outer FSM reacts later
  - ▶ The two reactions are considered simultaneous
  - ▶ The output actions are required to not conflict
- ▶ 2. [Stateflow, Matlab] Outer FSM reacts first, inner FSM reacts later (if at all)
  - ▶ If state is left, the inner FSM will not react at all

## Reaction order

Specify here the order of checks/operations in both cases

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# History transitions

When entering a super-state, which sub-state is entered?

Two solutions:

- ▶ 1. Enter the last sub-state you were in, when you last left the super-state
  - ▶ Represented as a **history transition** (marked with a full black arrow on these schematics / a H sign in Matlab)
- ▶ 2. Enter the default sub-state every time
  - ▶ Known as a **reset transition** (marked with a white arrow on these schematics / default behavior in Matlab)



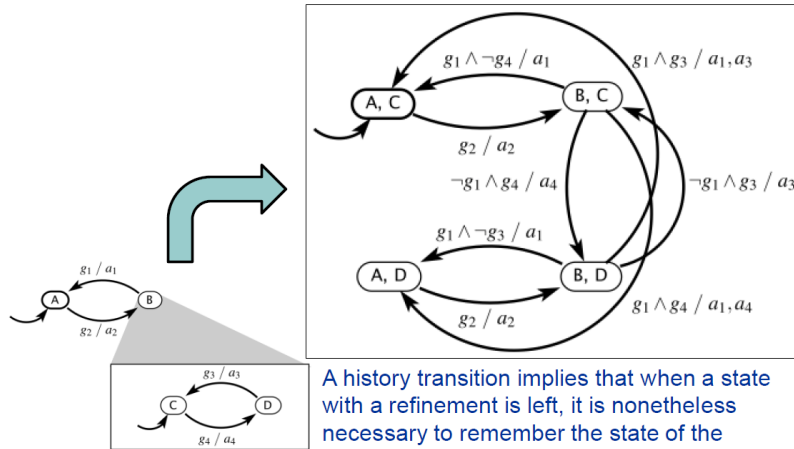
## Example

## Equivalent flattened FSM

- ▶ Any hierarchical FSM can be “flattened”, e.g. converted into an equivalent model with no super-states
  - ▶ e.g. Super-state A with two substates B and C is split into two substates AB and AC, transitions from A now leaving from both AB and AC
- ▶ Hierarchy in models brings representation efficiency

## Example

Flattening the state machine  
(assuming history transitions):



A history transition implies that when a state with a refinement is left, it is nonetheless necessary to remember the state of the refinement. Hence A,C and A,D.

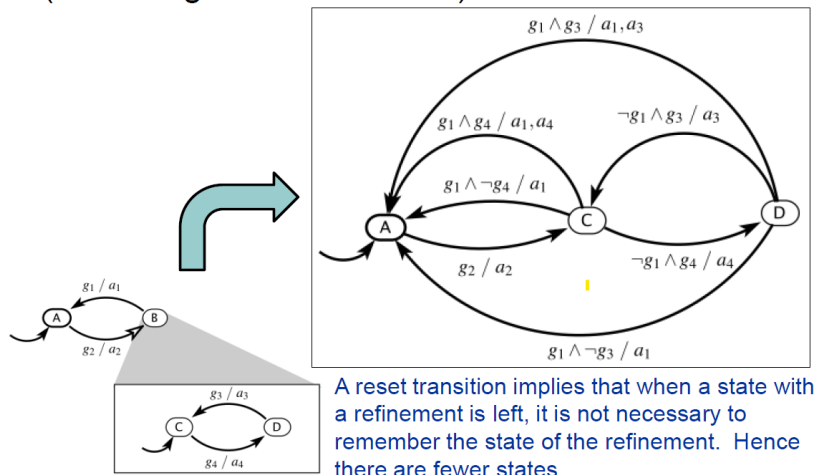
Figure 2: Flattenning example

# Example

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## Example

Flattening the state machine  
(assuming reset transitions):



A reset transition implies that when a state with a refinement is left, it is not necessary to remember the state of the refinement. Hence there are fewer states.

Figure 3: Flattenning example

# Example

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