Front-end Weber-Fechner gain control enhances the fidelity of combinatorial odor coding

Nirag Kadakia

Department of Molecular, Cellular, and Developmental Biology, Yale University, New Haven, CT 06511

Thierry Emonet*

Department of Molecular, Cellular, and Developmental Biology Department of Physics, Yale University, New Haven, CT 06511 and *Corresponding Author

In a previous paper (Gorur-Shandilya et al 2017), we showed that *Drosophila* ORNs adapt their gain according to the Weber-Fechner law of psychophysics. Here we investigate the implications of this front-end mechanism for odor coding capacity in natural environments, where the intensity and timescales of odor signals can span several orders of magnitude, and odors can mix together. We find that ORN adaptation promotes the reconstruction of odor identity from dynamic odor signals, even in the presence of confounding background odors and rapid intensity fluctuations. These enhancements are further aided by known downstream transformations in the antennal lobe and mushroom body. Our results, which are applicable to various odor classification and reconstruction schemes, stem from the fact that ORN adaptation is not intrinsic to the receptor involved. Instead it results from transduction downstream of olfactory ion channel activity, dynamically adjusting receptor sensitivity in accordance with the Weber-Fechner law.

Animals identify and discriminate odors using olfactory receptors (Ors) expressed in olfactory receptor neurons (ORNs) [1–4]. Individual ORNs, which typically express a single Or, respond to many odorants, while individual odorants activate many distinct ORNs [5-8]. Odors are thus encoded by the combinatorial patterns of activity they elicit in the sensing periphery [5–7, 9– 11], patterns decoded downstream into behavioral response [12, 13]. Still, ethologically-relevant odors are often mixed with background ones [14, 15] and intensity can vary widely and rapidly as odors are carried by the wind [16-19]. How are odors recognized reliably despite these confounds? In *Drosophila melanogaster*, ORN dose response curves exhibit similar Hill coefficients but distinct power-law distributed activation thresholds [6, 20], which together with inhibitory odorants enhance coding capacity [6, 20–22]. In antennal lobe (AL) glomeruli, mutual lateral inhibition normalizes population response, reducing the dependency of activity patterns on odor concentration [23, 24]. Further downstream, sparse connectivity to the mushroom body (MB) helps maintain neural representations of odors, and facilitates compressed sensing and associative learning schemes [25–28]. Finally, temporal features of neural responses contribute to concentration-invariant representations of odor identity [29–32].

Here we examine how short-time ORN adaptation at the very front-end of the insect olfactory circuit contributes to the fidelity of odor encoding. Our theoretical study is motivated by the recent discovery of invariances in the response dynamics of ORNs expressing the co-receptor Orco. The responses of ORNs to diverse odorants of the same concentration differ widely, due to differences in odor-receptor affinities [6, 33, 34] and stimulus dynamics [35]. However, downstream from this input nonlinearity, signal transduction and adaptation dynamics exhibit a surprising degree of invariance with respect to odor-receptor identity: reverse-correlation analysis of ORN response to fluctuating stimuli produces highly stereotyped, concentration-invariant response filters [20, 35, 36].

These properties stem in part from an apparently invariant adaptive scaling law in ORNs: gain varies inversely with mean odor concentration according to the Weber-Fechner Law of psychophysics [37, 38], irrespective of the odor-receptor combination [36, 39, 40]. The invariance of this relatively fast adaptation (~250 ms) can be traced back to feedback mechanisms in odor transduction, upstream of ORN firing [36, 39–41], which depend on the activity of the signaling pathway rather than on the identity of its receptor [41]. The generality of the adaptive scaling suggests it could be mediated by the highly conserved Orco co-receptor [42–45]. Indeed, phosphorylation sites have been recently identified on Orco, some being implicated in odor desensitization, albeit over much longer timescales [45, 46].

While in a simple system such as *E. coli* chemotaxis [47], adaptive feedback via the Weber-Fechner Law robustly maintains sensitivity over concentration changes, the implication for a multiple-channel system – which combines information from hundreds of cells with overlapping receptive fields – is less straightforward. Here we combine a biophysical model of ORN adaptive response and neural firing with various sparse signal decoding frameworks to explore how ORN adaptation with Weber-Fechner scaling affects combinatorial coding and decoding of odor signals spanning varying degrees of intensity, molecular complexity, and temporal structure.

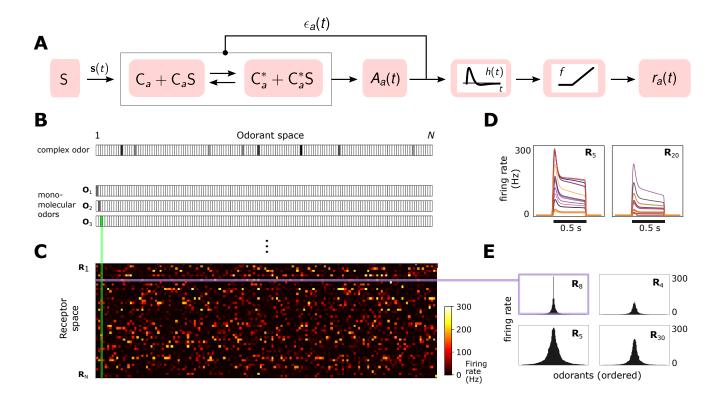


FIG. 1: A Simple ORN model. Or/Orco complexes C_a respond to odor concentration $\mathbf{s}(t) = (s_1(t), ..., s_i(t), ..., s_N(t))$ by binding odorant molecules (S in the diagram) of type i and concentration $s_i(t)$, where t is time. Or/Orco complexes stochastically switch between active and inactive states, where the steady-state active fraction is determined by the free energy difference (in units of k_BT) between active and inactive conformations in the unbound state, $\epsilon_a(t)$, and by odorant binding with dissociation constants K_{ai}^* and K_{ai} (SI text). Adaptation is mediated by a negative feedback [41] from the activity of the channel onto the free energy difference $\epsilon_a(t)$ with timescale τ . ORN firing rates $r_a(t)$ are generated by passing $A_a(t)$ through a linear temporal filter h(t) and a nonlinear thresholding function f. B Odor mixtures are represented by N-dimensional vectors \mathbf{s} , whose components s_i are the concentrations of the individual molecular constituents of \mathbf{s} . C Step-stimulus firing rate of 50 ORNs to the 150-possible monomolecular odors $\mathbf{s} = s_i$, given power-law distributed K_{ai}^* [20]. D Temporal responses of two representative ORNs to a pulse stimulus, for several monomolecular odorants (colors). E Representative ORN tuning curves (a single row of the response matrix in C, ordered by magnitude). Tuning curves are diverse, mimicking measured responses [6].

We find that this front-end adaptive mechanism promotes the accurate discrimination of odor signals from backgrounds of varying molecular complexity, and aids other known mechanisms of neural processing in the olfactory circuit to maintain representations of odor identity across environmental changes.

RESULTS

Model of ORN sensing repertoire

We consider a repertoire of M=50 Orco-expressing ORN types modeled using a simple extension of a minimal model of odor-to-ORN firing [36] that reproduces the type of Weber-Fechner adaptation and firing rate dynamics measured in individual Drosophila ORNs in response to Gaussian and naturalistic signals (code available on GitHub[48]). Within ORNs of type a=1,...,M, we model Or-Orco complexes as non-selective cation chan-

nels [42] (Fig. 1a) that stochastically switch between active and inactive states, while simultaneously binding to odorants i with dissociation constants, K_{ai}^* and K_{ai} , respectively [36, 41]. Assuming these processes are faster than other reactions in the signaling pathway, the quasisteady state active fraction A_a of channels in ORNs of type a reads:

$$A_a(t) = \left(1 + e^{\epsilon_a(t)} \frac{1 + \sum_{i=1}^{N} s_i(t) / K_{ai}}{1 + \sum_{i=1}^{N} s_i(t) / K_{ai}^*}\right)^{-1}.$$
 (1)

 $s_i(t)$ are the time-dependent concentrations of the individual monomolecular components of the odor signal $\mathbf{s}(\mathbf{t})$ at time t, and N=150 is the size of the molecular odorant space (Fig. 1b). Inward currents elicited by activating Or-Orco channels [42] eventually result in a negative feedback onto $A_n(t)$ [36, 40, 41]:

$$\tau \frac{d\epsilon_a(t)}{dt} = A_a(t) - A_0. \tag{2}$$

Here, τ is the adaptation time and $\epsilon_a(t)$ is the free energy difference in units of k_BT between active and inactive conformations of the unbound Or-Orco channel. We assume changes in free energy are limited to the finite range $\epsilon_{L,a} < \epsilon_a(t) < \epsilon_{H,a}$ [36]. Firing rate is minimally modeled by filtering the activity $A_a(t)$ with the bi-lobed filter h(t) and rectifying nonlinearity f [36]:

$$r_a(t) = f\left(h \otimes A_a(t)\right),\tag{3}$$

where \otimes is convolution. When deconvolved from stimulus dynamics, the shapes of the temporal kernels of Drosophila ORNs that express Orco are largely receptorand odor-independent [20, 35, 36]. Moreover, adaptation is not intrinsic to the receptor [41]. Accordingly, for simplicity τ , A_0 , h(t), and f are assumed independent of receptor and odorant identities.

We assume that the lower cutoffs $\epsilon_{L,a}$ are receptordependent and choose them from a normal distribution. This variability ensures that ORNs are activated above quiescence (set at 5 Hz) at distinct stimulus levels [35, 36]. Diversity among odor-ORN responses arises mainly from the distribution of chemical dissociation constants (Fig. 1c). For simplicity we only consider agonists, i.e. $K_{ai}^* > K_{ai}$, and assume receptors can only bind one odorant at a time. The analysis can easily be extended to include inhibitory odorants, which increases coding capacity [21]. We choose the dissociation constants from a power law distribution ($\alpha = 0.35$) recently found across ORN-odor pairs in *Drosophila* larvae [20]. For a handful of ORNs we choose a very small value for one of the K_{ai}^* to mimic high responders to private odorants relevant to innate responses [34]. These private odors do not affect the general findings.

While this phenomenological model could be extended to include further details – e.g. we could relax the quasi-steady-state assumption in Eq. 1 and use a more complex model for neural firing [36] – this minimally-parameterized form captures the key dynamical properties of Orco-expressing ORNs relevant to our study: receptor-independent adaptation [41] with Weber-Fechner scaling [36, 39, 40] that maintains response time independent of mean stimulus intensity [35, 36], along with a diversity of both steady state and temporal firing patterns in response to a panel of monomolecular odorants [6, 29–31, 33] (Fig. 1d-1e).

Concentration-invariant preservation of coding capacity and abstract representations of odor identity

To investigate how front-end Weber-Law adaptation might preserve representations of odor identity within the repertoire of ORN response, we project the 50-dimensional firing rates $\bf r$ down to a 2-dimensional space using t-distributed stochastic neighbor embedding (t-

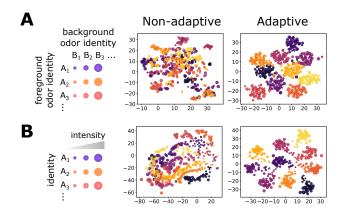
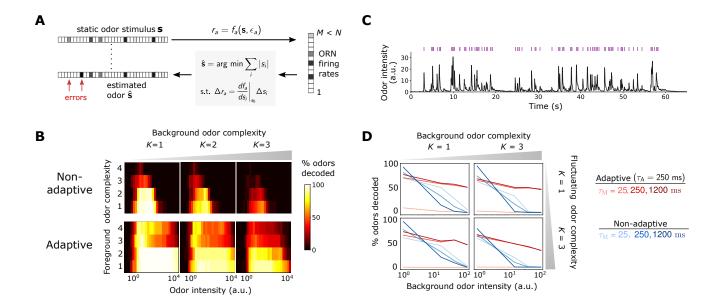


FIG. 2: Front-end adaptation maintains representations of odor identity across background and intensity confounds. A Abstract representation of ORN responses in a low-dimensional embedding. Each point represents the repertoire of ORN firing rates, in response to an odor environment with both a foreground (point color) and background (point size) odor. In the adaptive system, ϵ_a are set to their steady state values given odor B alone. B Similar to A, but now for odors whose concentrations span 4 decades (represented by point size). Here, the background odor identity is the same for all concentrations.

SNE) [49]. We first perform this embedding for an adaptive or non-adaptive system interacting with an odor environment containing a foreground odor A atop a background odor B (Fig. 2a). Both odors are sparse mixtures, with K < N odorants of similar concentrations, odor "identity" being the particular set of odorants in the mixture. Adaptation to the background is enacted by setting ϵ_a to their steady state values (via Eq. 2) in response to odor B alone. With adaptation in place, responses cluster by the identity of odor A, suggesting that ORN responses appropriately encode the identity of novel odors irrespective of background signals – once these backgrounds have been "adapted away" (Fig. 2a). This is notable, since, due to the combinatorics of ORN response (Fig. 1c), the adapted ϵ_a distributions are themselves heavily dependent on background identity. Responses in the non-adaptive system, meanwhile, exhibit no such clustering (Fig. 2a). A similar separation by odor identity is preserved in the adaptive system if we consider responses across different intensities (Fig. 2b).

Preservation of these representations is enabled by the preservation of coding capacity. Accordingly, we calculated the mutual information between odor and ORN response in time, verifying that the the adaptive system retains coding capacity as it confronts novel odors (Fig. S1). The non-adaptive system maintains coding capacity, though in a far more limited range of odor concentration.



Front-end adaptation enhances odor discrimination in complex environments

How well does the preservation of coding capacity translate to better signal reconstruction? One potentially complicating factor is the disparity between sensor dimension and stimulus dimension: while *Drosophila* only express ~ 60 Or genes [50], the space of odorants is far greater [27]. However, many naturally-occurring odors are comprised of a small subset of odorants, which is suggestive as the theory of compressed sensing (CS) guarantees their reconstruction [51, 52]. It is unknown whether CS is implemented in the *Drosophila* olfactory circuit [53], and we use it mainly as a tool to quantify how front-end adaptation potentially affects odor decoding, later verifying our conclusions with other classification techniques that incorporate the known architecture of the olfactory system.

To incorporate the linear framework of CS, we treat the nonlinear odor encoding exactly but approximate the decoding to first order (this linearization simplifies the computation, but is not critical for our general results; see SI text and Fig. S7-S8). Odors **s** are assumed sparse, with $K \ll N$ nonzero components s_i with mean concentration s_0 . We first examine how foreground odors are recognized when mixed with background odors of a distinct identity but similar intensities, quantifying decoding accuracy as the percentage of odors correctly decoded within some tolerance (Fig. 3a). Without adaptation, accuracy is maintained within the range of receptor sensitivity for monomolecular backgrounds, but is virtually eliminated as background complexity rises (Fig. 3b). The range of sensitivity is broader in the adaptive system, and is substantially more robust across odor concentration and complexity.

In realistic odor environments, the concentration and duration of individual odor whiffs vary widely [18]. We wondered how well a front-end adaptation mechanism with a single timescale τ could promote odor identity detection in such environments. As inputs to our coding/decoding framework, we apply a naturalistic stimulus intensity recorded using a photo-ionization detector [36] (Fig. 3c) to which we randomly assign sparse identities from the N-dimensional odorant space. To mimic background confounds, we combine these signals with static odor backgrounds, and then calculate the percentage of decoded whiffs. We assume the decoder has short-term memory: detected odor signals are only retained for $\tau_{\rm M}$ seconds in the immediate past. Without ORN adaptation, sufficiently strong backgrounds eliminate the ability to reconstruct the identity of individual odor whiffs, irrespective of the complexity of either the foreground or background odor (Fig. 3d, blue lines). In the adaptive system, this is substantially mitigated (red lines in

Fig. 3d), provided the memory duration $\tau_{\rm M}$ is at least as long as the adaptation timescale τ (darker red lines). Because this short-term adaptation depends on the activity of the Or-Orco channel rather than on the identity of the receptor [35, 36, 41], the values of τ and A_0 were assumed the same for all ORNs; still, our results hold if these invariances are relaxed (SI, Fig. S4-S5).

Front-end adaptation enhances primacy coding

The primacy coding hypothesis has recently emerged as an intriguing framework for combinatorial odor Here, odor identity is encoded by the set (but not temporal order) of the p earliest responding glomeruli/ORN types, known as primacy set of order p [32]. If the activation order of ORNs were invariant to the strength of an odor step or pulse, primacy sets would in principle form concentration-invariant representation of odor identity. Though our coding framework uses the full ORN ensemble in signal reconstruction, some of these responses may contain redundant information, and a smaller primacy subset may suffice. To examine this, we apply our model to a sigmoidal stimulus that rises to half-max in 50 ms, calculating decoding accuracy in time. Since ORNs activate sequentially, the primacy set is defined by the ORN subset active when the odor is decoded. For simple odors, a limited set of earliest responding neurons fully accounts for the odor identity (Fig. 4a), in agreement with primacy coding. As expected for more complex odor mixtures, the full repertoire is required for accurate decoding. Primacy coding also predicts that for stronger stimuli, responses occur earlier, since the primacy set is realized quicker, which our framework replicates (Fig. S2).

Beyond mere consistency, however, front-end adaptation might also enhance primacy coding in different environments, such as background odors, which could scramble primacy sets. To investigate this, we considered again a sigmoidal odor step (odor A), now atop a static background (odor B) to which the system has adapted. We compared the primacy sets of odor A for 1000 different choices of odor B, finding that primacy sets are highly consistent across background confounds for all but the smallest primacy orders (Fig. 4b-4c). This also holds true for backgrounds of different concentrations (Fig. S2), suggesting a central role for front-end adaptation in reinforcing primacy codes across differing environmental conditions.

Contribution of front-end adaptation for odor recognition within the *Drosophila* olfactory circuit

Signal transformations in the sensing periphery are propagated through the remainder of the olfactory cir-

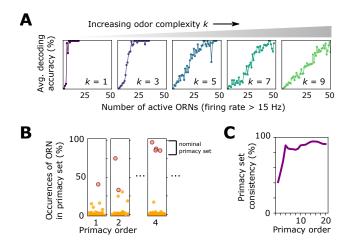


FIG. 4: A Decoding accuracy as a function of the number of active ORNs, for different odor complexities. The primacy set consists of those ORNs required to be active for accurate decoding. B Frequency of particular ORNs in primacy sets of an odor placed atop different backgrounds. Individual plots show, for given primacy order p, the percentage of backgrounds for which the primacy set of odor A contains a given ORN (dots). Those with purple borders are the p most highly occurring – i.e. a nominal background-invariant primacy set for odor A. Points are jittered horizontally for visualization. C Consistency of primacy sets across backgrounds, as a function of p. Consistency is defined as the likelihood that an ORN in the nominal primacy set appears in any of the individual background-dependent primacy sets, averaged over the nominal set (average of the y-values of the purple dots in B). 100% consistency means that for all backgrounds, the primacy set of odor A is always the same pORNs.

How does front-end adaptation interact with these subsequent neural transformations? ORNs expressing the same OR converge to a unique AL glomerulus, where they receive lateral inhibition from other glomeruli [23, 54]. This inhibition implements a type of divisive gain control [24], normalizing the activity of output projections neurons, which then synapse onto a large number of Kenyon cells (KCs) in the mushroom body. To investigate how odor representations are affected by interactions between front-end ORN adaptation and this lateral inhibition and synaptic divergence, we extended our ORN encoding model by adding uniglomerular connections from ORNs to the antennal lobe, followed by sparse, divergent connections to 2500 KCs [25, 26, 55]. Inhibition was modeled via divisive normalization, with parameters chosen according to experiment [24]. quantified decoding accuracy by training and testing a binary classifier on the KC activity output of sparse odors of distinct intensity and identity, randomly categorized as appetitive or aversive. For simplicity, odor signals of the same identity but differing intensity were assigned the same valence. We trained the classifier on $N_{\rm ID}$ sparse odor identities at intensities chosen randomly over 4 orders of magnitude, then tested the classifier accuracy on the same odor identities but of differing concentrations.

Classification accuracy degrades to chance level as $N_{\rm ID}$ becomes very large (Fig. 5a). When acting alone, either divisive normalization or ORN adaptation can help, although the effect of ORN adaptation is stronger. When both are active, accuracy improves further, suggesting that these distinct adaptive transformations may act jointly at different stages of neural processing in preserving representations of odor identity. As expected, these gains mostly vanish for the same odors chosen from a narrower range of concentrations (Fig. S3).

If we train the classifier to distinguish odors by identity rather than valence, the benefits conferred by divisive normalization do not appear until $N_{\rm ID}$ is substantial, with accuracy below 65% for $N_{\rm ID} > 50$ (Fig. 5b). On the other hand, with ORN adaptation accuracy remains above 85% for more than 1000 odor identities, strongly implicating front-end adaptation as a key player in maintaining odor identity representations, before signals are further processed downstream.

DISCUSSION

We have found that Weber-Law adaptation at the very front-end of the insect olfactory circuit [36, 39, 40] may contribute significantly to the preservation of neural representations of odor identity amid confounding odors and intensity fluctuations. Drawing on experimental evidence for a number of ORN-invariant response features [20, 22, 35, 36, 41], we have found that this mechanism of dynamic adaptation confers significant benefits in coding fidelity, without the need for ORN-specific parameterizations. Still, our results hold when these invariances such as adaptation timescale or baseline activity are relaxed (SI Figs. S4-S5). In the olfactory periphery, front-end Weber Law adaptation therefore appears fairly robust, a consequence of controlling gain via feedback from channel activity [36, 41, 47], rather than through intrinsic, receptor-dependent mechanisms. While our framework incorporates many observed features of the Drosphila olfactory system – Weber-Law adaptation, power-law distributed receptor affinities, temporal filter invariance, connectivity topologies – it is minimal. We considered only one of the chemoreceptor families expressed in the fly antenna [1] and ignored possible contributions of odor binding proteins [56, 57], inhibitory odorants [21], and odorant-odorant antagonism [58], which could further boost coding capacity and preserve representation sparsity. Useful extensions to our nonlinearlinear-nonlinear model might incorporate ephaptic coupling between ORNs housed in the same sensillum [59], global inhibition in the mushroom body [60], and the effects of long-term adaptation [45].

Previous studies have characterized various neural mechanisms that help preserve combinatorial codes. Lat-

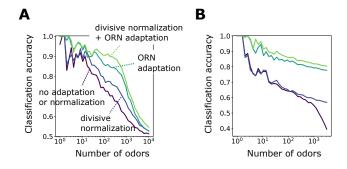


FIG. 5: A Accuracy of binary classification by odor valence, as a function of the number of distinct odor identities classified by the trained network (concentrations span 4 orders of magnitude), in systems with only ORN adaptation, only divisive normalization, both or neither. B Same as (A) but now classifying odors by identity.

eral inhibition between glomeruli helps tame saturation and boost weak signals [24]. The sparse degree of connectivity to either the olfactory bulb (vertebrates) or mushroom body (insects) may also be precisely tuned to optimize the capacity to learn associations [26]. In this work, we find that some of these downstream features act in concert with front-end dynamic adaptation in maintaining representations of odor identity.

Other studies have implicated the unique temporal patterns of neural response as signatures of odor identity [29–31, 61]. ORN and projection neuron time traces form distinct trajectories in low-dimensional projections, and cluster by odor identity, much as we have found here (Fig. 2). In locusts PNs, the trajectories elicited by foreground odors when presented in distinct backgrounds exhibit some degree of overlap; though partial, these overlaps were nonetheless sufficient to maintain background-invariant decoding from Kenyon cell responses [14]. It was therefore suggested, somewhat presciently, that background filtering likely occurs at the level of ORNs themselves [14]. Likewise, in our framework, temporal coding is implicit: because the input nonlinearity depends on the diversity of binding affinities, odor signals are naturally formatted into temporal patterns that are both odor- and ORN-specific (Figs. 1d-1e). Further, the short required memory timescales $(\tau_{\rm M} \sim \tau \sim 250 \text{ ms})$ suggest that only brief time windows are needed for accurate odor identification, consistent with previous findings [14, 29]. Moreover, we find that front-end adaptation enhances the robustness of other combinatorial coding schemes, such as primacy coding [32], which relies on the temporal order of ORN activation but not absolute firing rate (Fig. 4).

In the well-characterized chemosensory system of bacterial chemotaxis, Weber Law adaptation is enacted through a feedback loop from the output activity of the receptor-kinase complexes onto the enzymes modifying receptor sensitivity [47]. It is interesting that some aspects of this logic are also present in ORNs: although the molecular players are different (and still largely unknown), it has been shown that transduction activity feeds back onto Or-Orco cation channel opening, enabling the Weber-Fechner relation [36, 40, 41]. That this adaptation mechanism appears to act similarly across ORNs [35, 36, 40] suggests the possible involvement of the universal co-receptor Orco, whose role in long-term adaptation has recently been reported [43–45]. Further, the identification of 4 subunits comprising the Orco-Or ion channel suggest that generic Or/Orco complexes may contain multiple odorant binding sites, which when included in our model supports our general findings (Fig. S6).

Weber Law ensures that sensory systems remain in the regime of maximum sensitivity, broadening dynamic range and maintaining information capacity [62]. For a single-channel system, this requires matching the midpoint of the dose-response curve to the mean ligand concentration [63], a strategy which may fail in multi-channel systems with overlapping tuning curves: adaptation to one signal could inhibit identification of others, if the signals excite some but not all of the same sensors. Our results show that this strategy is still largely functional. This can be traced to the observation that in CS, accuracy is guaranteed when sufficiently distinct odor identities produce sufficiently distinct ORN responses, a condition known as the restricted isometry property [52]. Indeed, the Weber-Fechner scaling increases the likelihood that this property is satisfied, beyond that in the non-adaptive system (SI text and Figs. S7-S8). Still, restricted isometry does not require that response repertoires are *invariant* to environmental changes. That is, even if the subset of active ORNs were concentrationdependent, odors could still in principle be fully reconstructible by CS. Nonetheless, our results in t-SNE clustering (Fig. 2), primacy coding (Fig. 4b-4c), and odor classification (Fig. 5) suggest that some signature of response invariance emerges as a natural byproduct of front-end adaptation. Together, this implies that Weber Law adaptation, whether required by the olfactory circuit for precise signal reconstruction (as in CS) or for developing odor associations (as in classification), can play an integral part in maintaining combinatorial codes amid changing environmental conditions.

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AUTHOR CONTRIBUTIONS

N.K. and T.E. conceived the project, analyzed the results, and wrote the manuscript. N.K. performed all calculations. T.E. supervised the project.

DECLARATION OF INTERESTS

The authors declare no competing interests.

METHODS

Equations 1-2 are integrated numerically using the Euler method with a 2 ms time step. For ORN firing (Eq. 3), h(t) is bi-lobed [35]: $h(t) = Ap_{\text{Gam}}(t; \alpha_1, \tau_1) - Bp_{\text{Gam}}(t; \alpha_2, \tau_2)$, A = 190, B = 1.33, $\alpha_1 = 2$, $\alpha_2 = 3$, $\tau_1 = 0.012$, and $\tau_2 = 0.016$, where p_{Gam} is the pdf of Gamma(α , $1/\tau$). Nonlinearity f is modeled as a linear rectifier with 5 Hz threshold. For t-SNE dimensionality reduction, ORN responses were generated for odor signal combinations consisting of 1 (among 10) distinct foreground odors A atop 1 (among 50) distinct background odors B, each of complexity K = 5, for Fig. 2a. Fig. 2b plots responses for 10 odors (K = 5) at 40 concentrations spanning 4 decades, atop a random sparse background odor (K = 5) of similar magnitude.

For compressed sensing decoding, sparse components s_i are chosen as $s_i = s_0 + \Delta s_i$ where s_0 is set as the center of linearization and $\Delta s_i \sim \mathcal{N}(s_0/3, s_0/9)$. Reconstructed signal components $\hat{s}_i = s_0 + \Delta s_i$ are computed by minimizing $\sum_{i} |\Delta s_{i}|$ subject to $\Delta r_{a} = \sum_{i} dr_{a}/ds_{i}|_{s_{0}} \Delta s_{i}$ where $\Delta r_a = r_a(\mathbf{s}) - r_a(s_0)$ are the "excess" ORN firing rates about the linearization point. For static stimuli, ϵ_a equals the fixed point of Eq. 2 in response to the background stimulus. For fluctuating stimuli, ϵ_a is updated in time by continuously integrating $r_a(t)$, via Eqs. 2 and 3; thus, only knowledge of $r_a(t)$ is needed by the decoder. The naturalistic odor signal (Fig. 3d) was generated by randomly varying flow rates of ethyl acetate and measuring the concentration with a photo-ionization detector [36]. Statistics mirroring a turbulent flow [18] were verified (Fig. S9).

For the network model, the AL-to-MB connectivity matrix \mathbf{J}_1 , is chosen such that each KC connects presynaptically to 7 randomly chosen AL glomeruli [25, 26]. The results shown in Fig. 5 are an average of 10 distinct instantiations of this random topology. The Z=2500 KCs are then connected by a matrix \mathbf{J}_2 to a readout layer of dimension Q, where Q=2 for binary and $Q=N_{\mathrm{ID}}$ for multi-class classification. Both AL-to-MB and MB-to-readout connections are perceptron-type with rectified-linear thresholds. The weights of \mathbf{J}_1 and \mathbf{J}_2 are chosen randomly from $\sim \mathcal{N}(0,1/\sqrt{7})$ and $\sim \mathcal{N}(0,1/\sqrt{Z})$, respectively. Only the \mathbf{J}_2 and the MB-to-output thresh-

olds are updated during supervised network training, via logistic regression (for binary classification) or its higherdimensional generalization, the softmax cross entropy (for multi-class classification).

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