

# Network Theorems

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# **SUPERPOSITION THEOREM**

# Superposition Theorem

**Superposition** : the voltage across (or current through) an element in a linear circuits is the algebraic sum of the voltage across (or current through) that element due to each independent source acting alone.

Current Source  $\rightarrow$  open circuit(0 A)

Voltage Source  $\rightarrow$  short circuit (0 V)

# Superposition Theorem

Step to apply:

1. Turn off all independent sources except one source. Find the output (voltage or current) due to that active source.
2. Repeat step 1 for each other independent sources.
3. Find the total contribution by adding algebraically all the contribution due to the independent source.

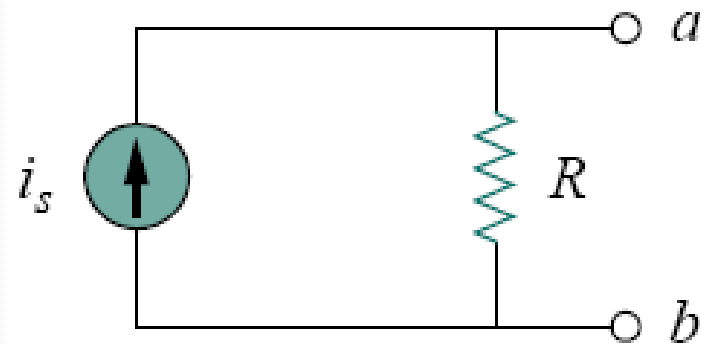
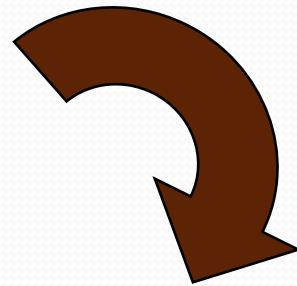
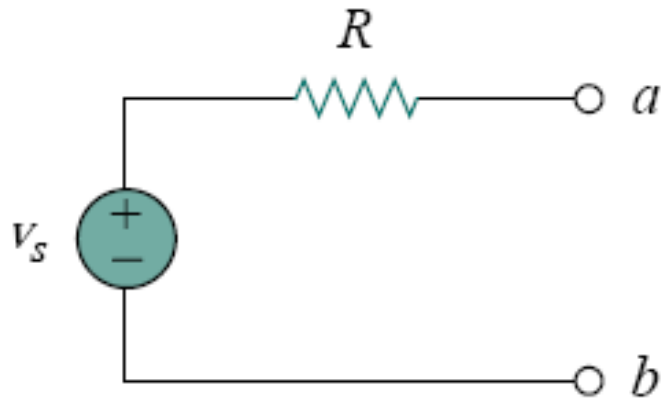


# SOURCE TRANSFORMATION

# Source Transformation

**Source transformation** : replacing a voltage source  $v_s$  in series with a impedance  $Z$  by a current source  $i_s$  in parallel with a impedance  $Z$ , or vice versa.

# Source Transformation





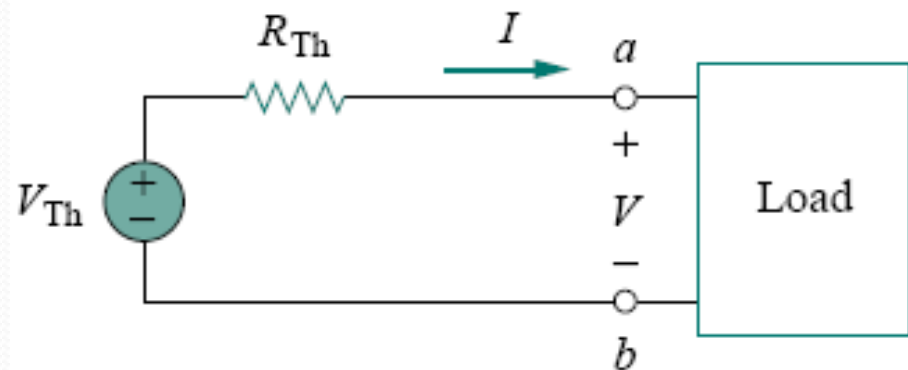
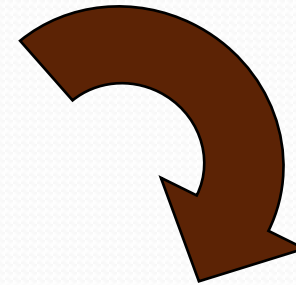
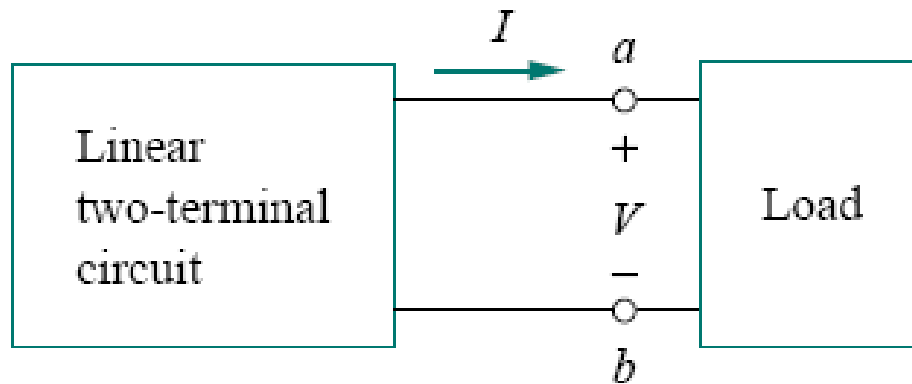
# THEVENIN'S THEOREM



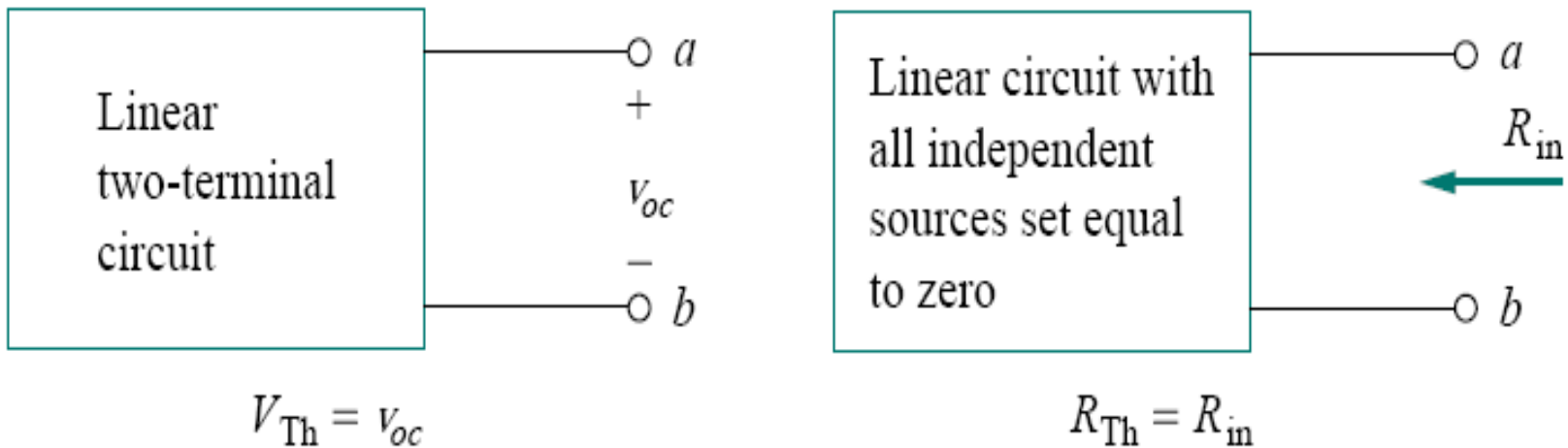
# Thevenin's Theorem

**Thevenin's theorem** : a linear two terminal circuit can be replaced by an equivalent circuit consisting of a voltage  $V_{Th}$  in series with an impedance  $Z_{Th}$  , where  $V_{Th}$  is the open circuit voltage at the terminals and  $Z_{Th}$  is the input or equivalent impedance at the terminals when the independent source are turned off.

# Thevenin's Theorem

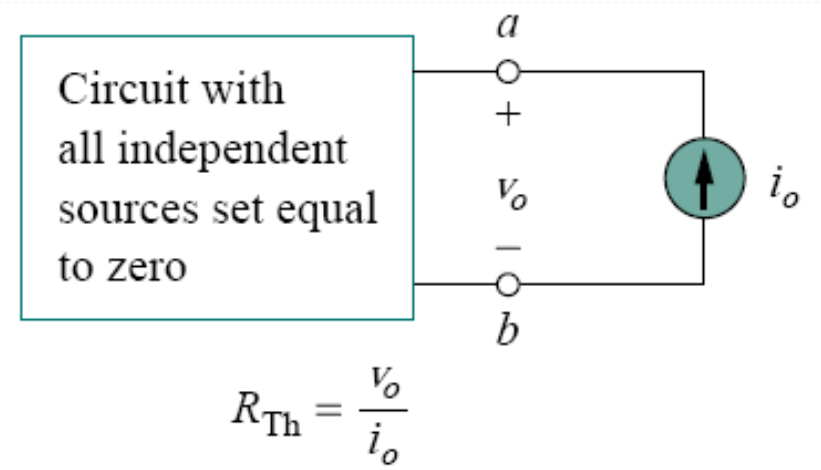
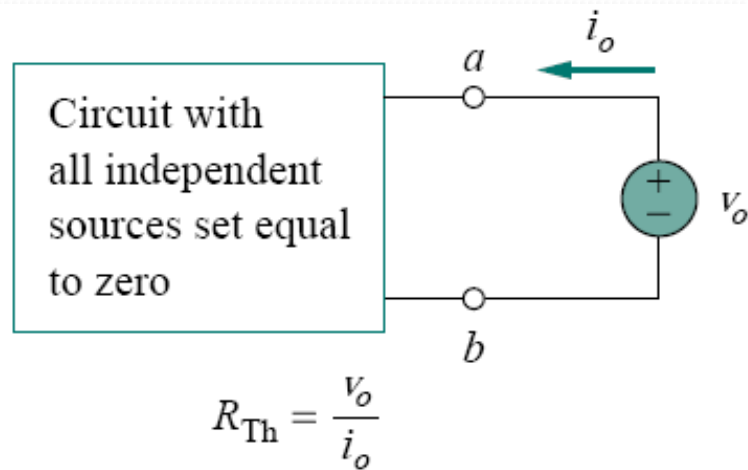


# Thevenin's Theorem



## Finding $V_{Th}$ and $Z_{Th}$

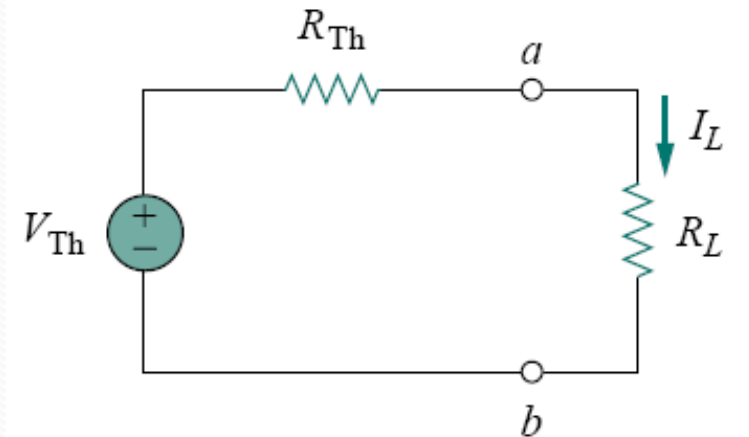
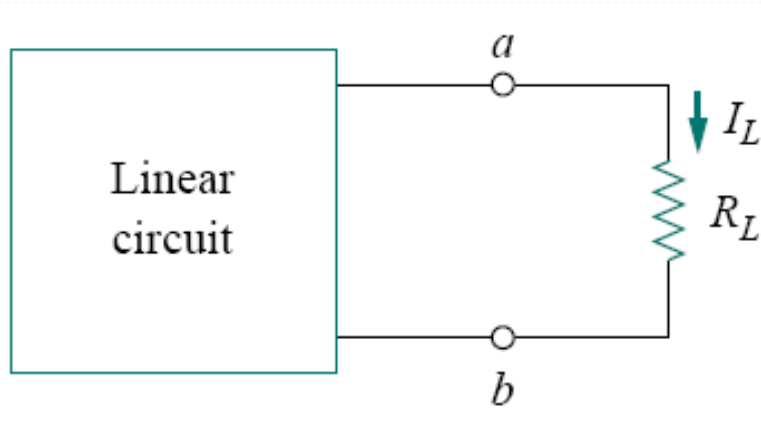
# Thevenin's Theorem



Finding  $Z_{Th}$  when circuit has dependent sources

# Thevenin's Theorem

Circuit with load



$$I_L = \frac{V_{Th}}{R_{Th} + R_L}$$

$$V_L = R_L I_L = \frac{R_L}{R_{Th} + R_L} V_{Th}$$

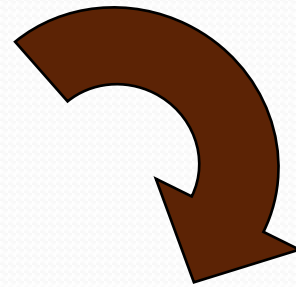
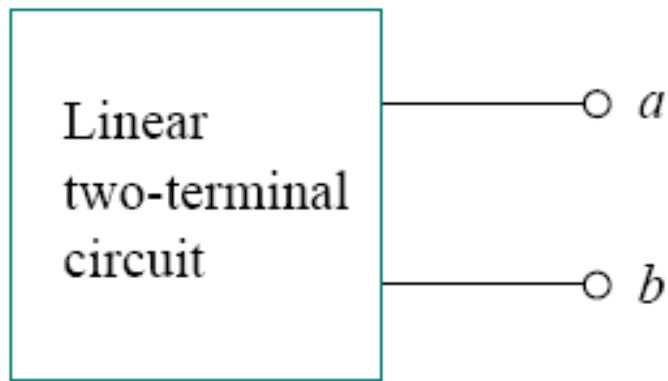


# NORTON'S THEOREM

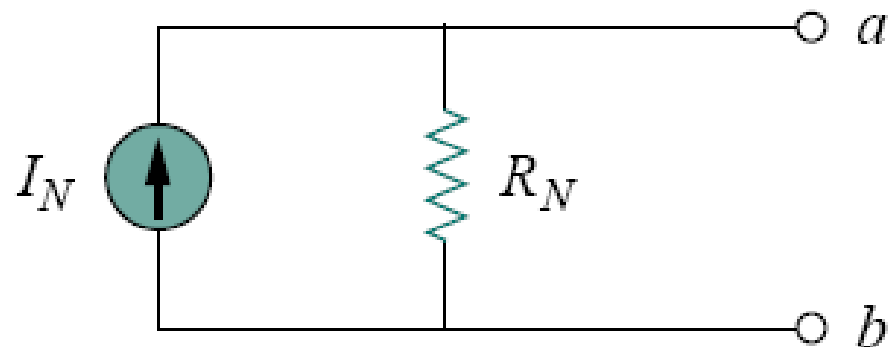
# Norton's Theorem

**Norton's Theorem** : a linear two-terminal circuit can be replaced by an equivalent circuit consisting of a current source  $I_N$  in parallel with an impedance  $Z_N$ , where  $I_N$  is the short circuit current through the terminals and  $Z_N$  is the input or equivalent impedance at the terminals when the independent source are turned off.

# Norton's Theorem



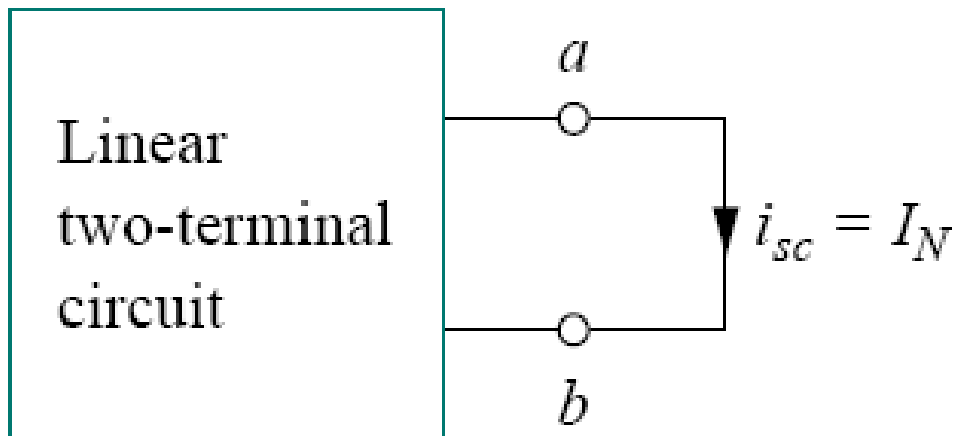
$$R_N = R_{Th}$$





# Norton's Theorem

Finding Norton current  $I_N$ .



$$I_N = i_{sc}$$
$$I_N = \frac{V_{Th}}{R_{Th}}$$

# Thevenin and Norton Equivalent

$$V_{Th} = v_{oc}$$

$$I_N = i_{sc}$$

$$R_{Th} = \frac{v_{oc}}{i_{sc}} = \frac{V_{Th}}{I_N} = R_N$$

# Millman's Theorem

- A number of voltage sources in parallel can be replaced by a single ideal voltage source  $V$  in series with an impedance  $Z$  where

$$V = \frac{\sum_{i=1}^n V_i Y_i}{\sum_{i=1}^n Y_i}$$

$$Z = \frac{1}{\sum_{i=1}^n Y_i}$$

# Millman's Theorem

- A number of current sources in series can be replaced by a single ideal current source  $I$  in parallel with an impedance  $Z$  where

$$I = \frac{\sum_{i=1}^n (I_i / Y_i)}{\sum_{i=1}^n (1 / Y_i)}$$

$$Y = \frac{1}{\sum_{i=1}^n (1 / Y_i)}$$



# MAXIMUM POWER TRANSFER THEOREM

# Maximum Power Transfer Theorem

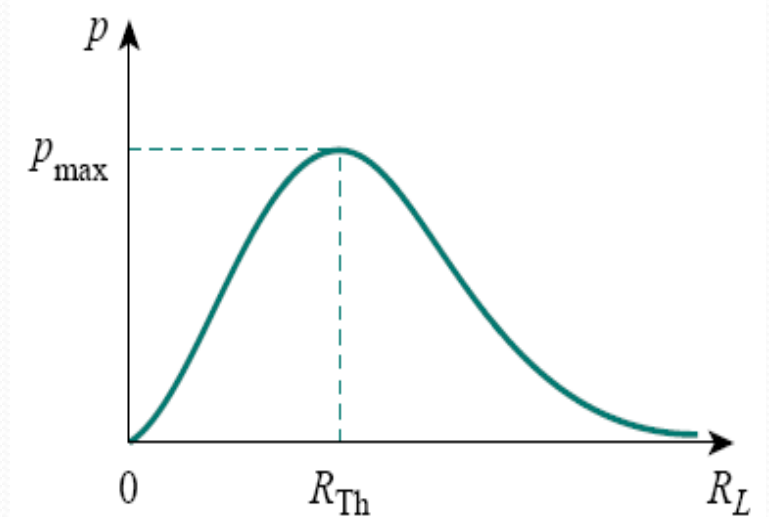
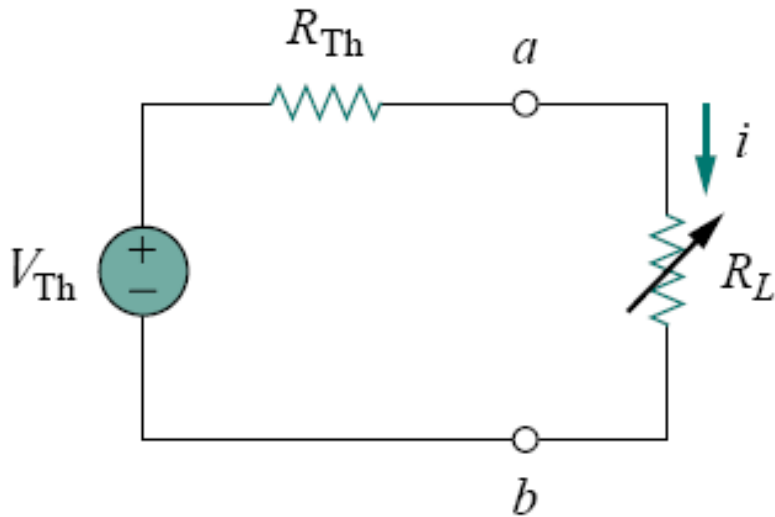
**Maximum power** : transferred to the load when the load resistance equals the Thevenin resistance as seen from the load

$$R_L = R_{Th}$$

**Maximum power** : transferred to the load when the load impedance equals the conjugate of the Thevenin impedance as seen from the load

$$Z_L = Z_{Th}^*$$

# Maximum Power Transfer



$$R_L = R_{Th}$$

$$p_{max} = \frac{V_{Th}^2}{4R_{Th}}$$