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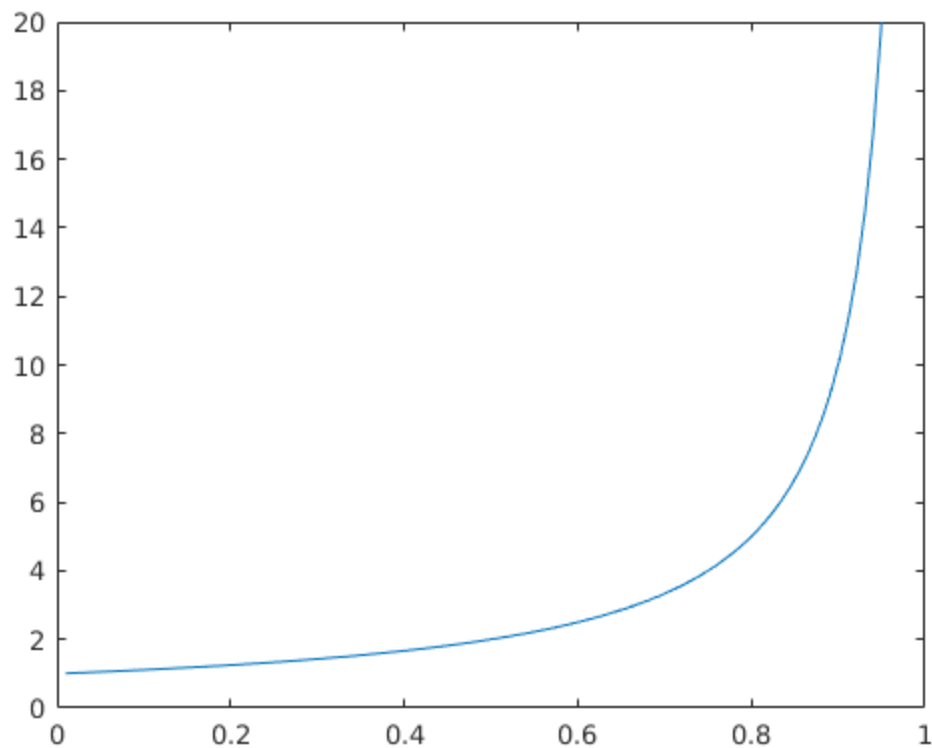
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## HW 3 Prob 2a M/M/1

```
clc;clear;
mu = 1;
numLambda = 100;
numTrials = 100;
T = 1e2;
lambda = linspace(0.01,0.95, numLambda);
meanDelay = zeros;
meanTrialDelay = zeros;
```

## Theoretical Calculations M/M/1

```
expDelay = zeros();
for i = 1:numLambda
    expDelay(i) = inv(mu - lambda(i));
end
plot(lambda,expDelay)
```



## Simulation M/M/1

```
for i = 1:numLambda
    meanDelay = zeros;
    for j = 1:numTrials
        A = 1e6;
        S = expRand(lambda(i));
        delayRS = 0;
        Q = zeros; %Array for holding Queue Delays
        qLen = 1;
        for t = 1:T
            %simulate interarrival times as A ~ EXP(lambda) and S ~
            EXP(mu)
            if(A < S) %arrival case
                [Q, qLen, A, S] =
                markovianArrival(Q,qLen,t,lambda(i),mu,S);
            elseif(S < A) %service case
                [Q, qLen, S, delayRS] =
                markovianDeparture(Q,qLen,t,mu,delayRS);
            end
        end
        meanDelay(j) = delayRS/T;
    end
    meanTrialDelay(i) = sum(meanDelay)/numTrials;
end
```

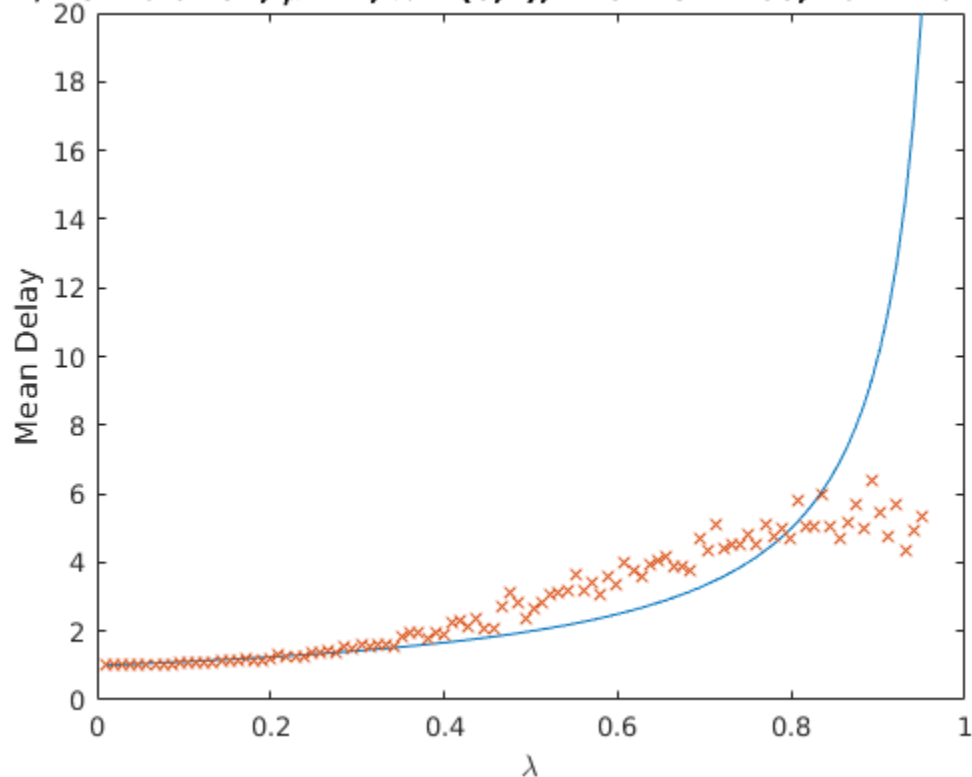
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```

% Plot M/M/1
plot(lambda,expDelay)
hold on;
plot(lambda,meanTrialDelay,'x')
title("M/M/1 Simulation, \mu = 1, \lambda = (0,1), nPoints = 100,
      numTrials = 100")
xlabel("\lambda");
ylabel("Mean Delay");
hold off;

```

**M/M/1 Simulation,  $\mu = 1$ ,  $\lambda = (0,1)$ , nPoints = 100, numTrials = 10**



## HW 3 Prob 2b M/D/1

```

clc;clear;
mu = 1;
numLambda = 100;
numTrials = 100;
lambda = linspace(0.01,0.95, numLambda);
meanDelay = zeros();
meanTrialDelay = zeros();

```

## Simulation M/D/1

```

T = 1e2;
for i = 1:numLambda

```

---

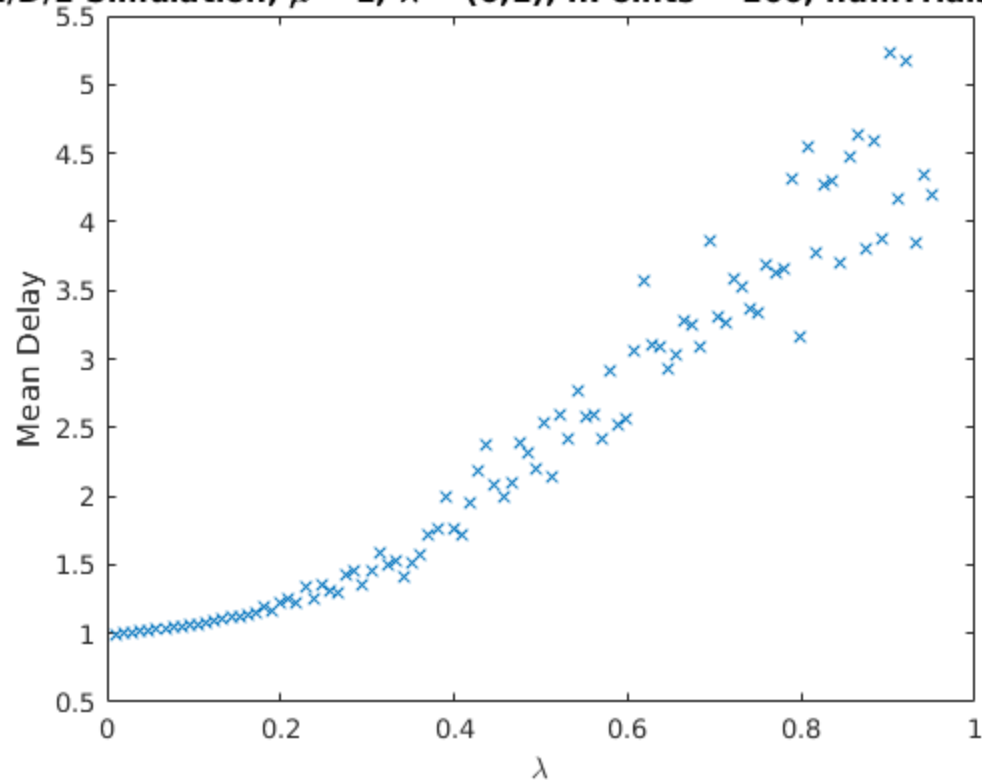
```

    for j = 1:numTrials
        A = expRand(lambda(i));
        S = 1e9;
        delayRS = 0;
        Q = zeros; %Array for holding Queue Delays
        qLen = 1;
        for t = 1:T
            %simulate interarrival times as A ~ EXP(lambda) and S ~
EXP(mu)
            if(A < S) %arrival case
                [Q, qLen, A, S] =
markovianArrival(Q,qLen,t,lambda(i),mu,S);
            elseif(S < A) %service case
                [Q, qLen, S, delayRS] =
deterministicDeparture(Q,qLen,t,mu,delayRS);
            end
        end
        meanDelay(i,j) = delayRS/T;
    end
    meanTrialDelay(i) = mean(meanDelay(i,:));
end

%Plot M/D/1
plot(lambda,meanTrialDelay,'x')
title("M/D/1 Simulation, \mu = 1, \lambda = (0,1), nPoints = 100,
numTrials = 100")
xlabel("\lambda");
ylabel("Mean Delay");
hold off;

```

**M/D/1 Simulation,  $\mu = 1$ ,  $\lambda = (0,1)$ , nPoints = 100, numTrials = 10**



## HW 3 Prob 2c M/G/1

```
clc;clear;
mu = 1;
numLambda = 100;
numTrials = 100;
lambda = linspace(0.01,0.95, numLambda);
meanDelay = zeros();
meanTrialDelay = zeros();
k = 1;

% Simulation M/G/1
T = 1e2;
for p = [0.1, 0.05, 0.01]
    for i = 1:numLambda
        for j = 1:numTrials
            A = expRand(lambda(i));
            S = 1e9;
            delayRS = 0;
            Q = zeros; %Array for holding Queue Delays
            qLen = 1;
            for t = 1:T
                %simulate interarrival times as A ~ EXP(lambda) and S
                ~ EXP(mu)
                if(A < S) %arrival case
```

---

```

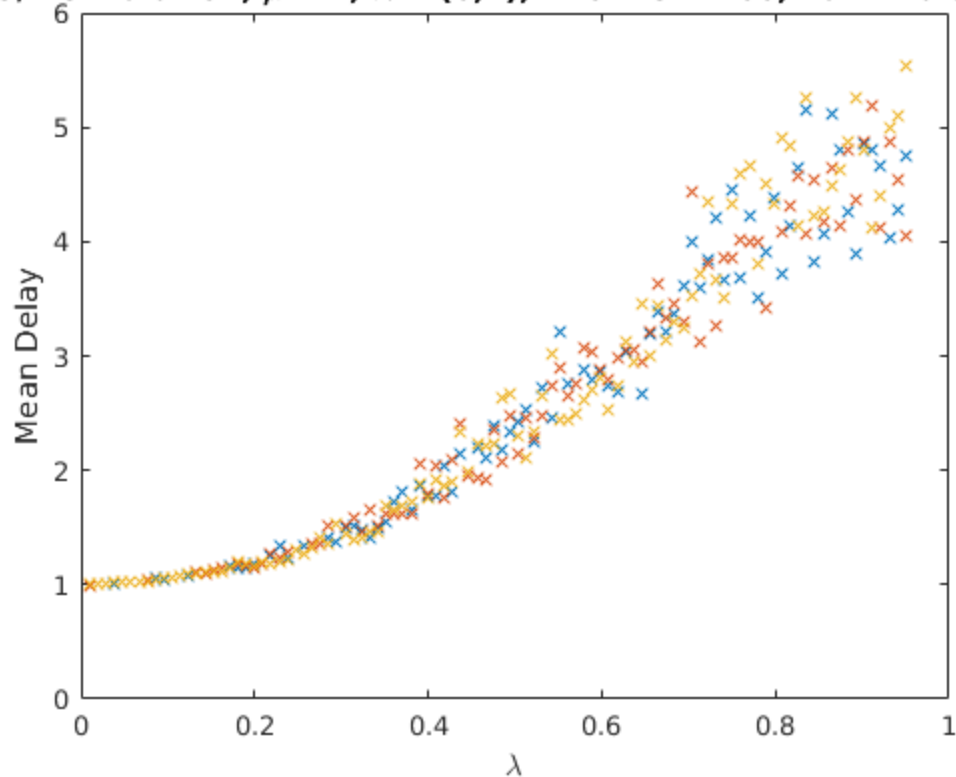
        [Q, qLen, A, S] =
markovianArrival(Q,qLen,t,lambda(i),mu,S);
        elseif(S < A) %service case
            [Q, qLen, S, delayRS] =
generalDeparture(Q,qLen,t,p,delayRS);
        end
    end
    meanDelay(i,j) = delayRS/T;

end
meanTrialDelay(i,k) = sum(meanDelay(i,:))./numTrials;
end
k = k+1;
end

%Plot M/D/1
plot(lambda,meanTrialDelay(:,1),'x')
hold on
plot(lambda,meanTrialDelay(:,2),'x')
plot(lambda,meanTrialDelay(:,3),'x')
title("M/G/1 Simulation, \mu = 1, \lambda = (0,1), nPoints = 100,
numTrials = 100")
xlabel("\lambda");
ylabel("Mean Delay");
hold off;

```

**M/G/1 Simulation,  $\mu = 1$ ,  $\lambda = (0,1)$ , nPoints = 100, numTrials = 10**



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