

B.Tech. Degree III Semester Regular/Supplementary Examination January 2023

CE/CS/EC/EE/IT/ME/SE 19-200-0301 LINEAR ALGEBRA AND TRANSFORM TECHNIQUES
(2019 Scheme)

Time: 3 Hours

Maximum Marks: 60

Course Outcomes

On successful completion of the course, the students will be able to:

CO1: Solve linear system of equations and to determine eigen values and eigen vectors of a matrix.

CO2: Understand the concept of vector space and subspace.

CO3: Determine Fourier series expansion of functions and transform.

CO4: Solve linear differential equation and integral equation using Laplace transform.

Bloom's Taxonomy Levels (BL): L1 – Remember, L2 – Understand, L3 – Apply, L4 – Analyze,

L5 – Evaluate, L6 – Create

PO – Programme Outcome

PART A(Answer **ALL** questions)

	(8 × 3 = 24)	Marks	BL	CO	PO
I. (a) Find eigen values and eigen vectors of $\begin{bmatrix} 5 & 4 \\ 1 & 2 \end{bmatrix}$.	3	3	L2, L3	1	1
(b) Form quadratic form corresponding to $A = \begin{bmatrix} 5 & -3 \\ -3 & 8 \end{bmatrix}$.	3	3	L1, L2	1	2
(c) Find a non zero vector W that is orthogonal to $(1, 3, 2)$ and $(1, 2, 3)$ in \mathbb{R}^3 .	3	3	L3	2	2
(d) Find the value of λ for which the following set of vectors $(\lambda, 0, 2)$ $(2, 1, 0)$ $(0, 3, 6)$ form a basis of \mathbb{R}^3 .	3	3	L3, L4	2	1
(e) Obtain the Fourier series expansion of $f(x)$ if $f(x) = \begin{cases} 1 & \text{for } 0 \leq x \leq 1 \\ x & \text{for } 1 < x < 2 \end{cases}$ and $f(x+2) = f(x)$.	3	3	L2, L3	3	2
(f) Obtain half range sine series for e^x in $0 < x < 1$.	3	3	L2, L3	3	2
(g) Find the Laplace transform of $f(t)$ where $f(t) = \begin{cases} \cos t & 0 < t < \pi \\ \sin t & t > \pi \end{cases}$.	3	3	L3	4	2
(h) Find $L^{-1}\left(\frac{e^{-2s}}{s-3}\right)$.	3	3	L4	4	3

PART B

(4 × 12 = 48)

II. (a) Find the values of λ and μ for which the equation $x + y + z = 3$; $x + 2y + 2z = 6$; $x + \lambda y + 3z = \mu$ have (i) no solution (ii) unique solution (iii) more than one solution.	6	6	L4	1	2
(b) State Cayley-Hamilton theorem. Using this theorem find inverse of the matrix $A = \begin{bmatrix} 1 & 3 & 7 \\ 4 & 2 & 3 \\ 1 & 2 & 1 \end{bmatrix}$.	6	6	L2, L3	1	2

OR

(P.T.O.)

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		Marks	BL	CO	PO
III. (a)	Find the rank of the matrix.	6	L2, L3	1	2
	$A = \begin{bmatrix} 1 & 1 & 2 & 3 \\ 3 & 4 & 7 & 10 \\ 5 & 7 & 11 & 17 \\ 6 & 8 & 13 & 16 \end{bmatrix}$				
(b)	Diagonalise the matrix $A = \begin{bmatrix} 2 & 1 & -1 \\ 1 & 1 & -2 \\ -1 & -2 & 1 \end{bmatrix}$ by means of an orthogonal transformation.	6	L4	1	3
IV. (a)	Let V consists of all real polynomials of degree ≤ 4 with usual polynomial addition and scalar multiplication. Let $W = \{\text{polynomials of degree } \leq 4 \text{ with coefficient of } x^2 = 0\}$. Then verify W is a subspace or not.	6	L4	2	2
(b)	$T: \mathbb{R}^3 \rightarrow \mathbb{R}^2$ be a transformation defined by $T \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} x+y \\ z \end{bmatrix}$. Verify T is a linear transformation or not.	6	L3	2	2
OR					
V. (a)	Find the dimension and basis of the vector space $V = \text{set of all } 2 \times 2 \text{ matrices.}$	6	L4	2	2
(b)	Using Gram Schmidt orthonormalisation process find an orthogonal and orthonormal basis $V = P_2(x)$, $x \in [0,1]$ $B = \{1, x, x^2\}$	6	L3	2	2
VI. (a)	Find the Fourier series to represent the function $f(x) = \begin{cases} x & \text{for } 0 \leq x \leq \pi \\ 2\pi - x & \text{for } \pi \leq x \leq 2\pi \end{cases}$ and deduce that $\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{\pi^2}{8}.$	6	L4, L3	3	2
(b)	Find the Fourier cosine transform of e^{-x^2} .	6	L4	3	2
OR					
VII. (a)	Develop $x \sin x$ in half range cosine series in the range $0 < x < \pi$	6	L4, L3	3	2
(b)	Using Fourier integral show that $\int_0^\infty \frac{1 - \cos \pi \lambda}{\lambda} \sin x \lambda d\lambda = \begin{cases} \frac{\pi}{2} & \text{in } 0 < x < \pi \\ 0 & \text{in } x > \pi \end{cases}$	6	L4	3	2

(Continued)

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- VIII. (a) Solve the integral equation $y(t) = 1 + \int_0^t y(u) \sin(t-u) du$. 6 L4, L5 4 3
- (b) State convolution theorem. Find $L^{-1} \frac{1}{(s^2 + 4)^2}$ using convolution theorem. 6 L1, L3 4 2
- OR**
- IX. (a) (i) Prove the symmetric property of beta function. 3 L1, L3 4 2
- (ii) Define gamma function and prove that $\Gamma_{1/2} = \sqrt{\pi}$. 3 L1, L3 4 2
- (b) Solve the equation $y'' - 3y' + 2y = 4t + e^{3t}$ when $y(0) = 1$ and $y'(0) = -1$. 6 L4, L5 4 3

Bloom's Taxonomy Levels

L1 = 6%, L2 = 12%, L3 = 38%, L4 = 40%, L5 = 4%.
