



B.Tech. Degree IV Semester Examination April 2017

CS 15-1404 AUTOMATA LANGUAGES AND COMPUTATIONS (2015 Scheme)

Time: 3 Hours

Maximum Marks: 60

PART A

(Answer *ALL* questions)

(10 × 2 = 20)

- I. (a) Define NFA and DFA. Give an example of each and list an application of DFA.
- (b) Explain Finite automata with output. Give an example each.
- (c) How do we express the language of any finite automata? Use the method to represent the following languages.
- (i) Binary strings starting with two 0's and ending with two 1's.
- (ii) Strings made of a, b, c containing 'aa' or 'bb' or 'cc' as a substring.
- (d) What is meant by regular grammars? Write a regular grammar for an automata which accepts 'one or more 0's, followed by one or more 1's followed by one or more 2's'.
- (e) Explain Chomsky normal form and Greibach normal form. Convert the following grammar to CNF. $S \rightarrow AbC, A \rightarrow aB, B \rightarrow cd, C \rightarrow a$.
- (f) Define a Push Down Automata (PDA). Design a PDA to accept the language $L(G) = \{a^n b^n \mid n \geq 1\}$.
- (g) Explain the working of a Turing machine. Design a turing machine to verify whether an input string is a binary string.
- (h) Explain Chomsky classification of languages.
- (i) What are Context Sensitive Languages and Linear Bounded Automata?
- (j) State Ardens Theorem. What is its application?

PART B

(4 × 10 = 40)

- II. (a) Convert the following NFA to equivalent DFA.

(5)

Present State	Next State	
	$a = 0$	$a = 1$
$\rightarrow A$	B	A, C
B	B	C
C	A, D	B
D	D	B

Final state = D

- (b) Construct NFA for the following regular expression.

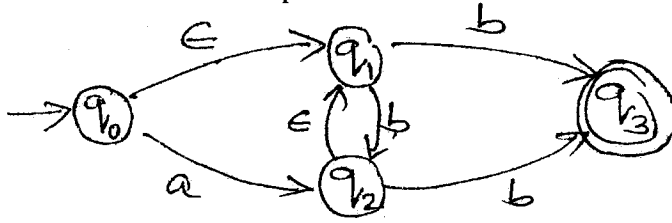
(5)

(i) $(1+0)^* + 10(1^*0)^*$.(ii) $00((10)^* + (111)^*)$.

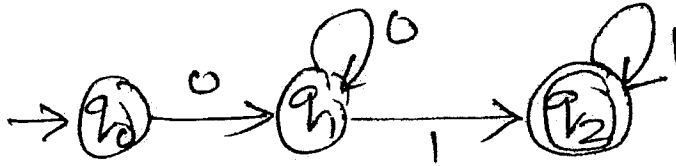
OR

(P.T.O.)

- III. (a) Prove that for every NFA there exists an equivalent DFA. (5)
 (b) What do you mean by ϵ -closure (q)? Eliminate epsilon from the following NFA and draw the NFA without epsilon. (5)



- IV. (a) Develop finite automata for the following regular expressions. (5)
 (i) $10 + (0+11)^*01$ (ii) $(a^*ab + ba)^*a$
 (b) Using Ardens theorem, find the regular expression corresponding to the following automata. (5)



OR

- V. (a) State the Pumping Lemma for regular languages. Show that the set of perfect squares is not a regular language. (5)
 (b) Construct regular grammar for the following regular expressions. (5)
 (i) $aa^*bb^*cc^*$
 (ii) $(0+1)^*000(0+1)^*$

- VI. (a) Convert the following grammar to Greibach Normal Form. (5)

$$S \rightarrow AA \mid a$$

$$A \rightarrow SS \mid b$$

- (b) Simplify the following CFG: (5)

$$S \rightarrow aAB \mid bX$$

$$A \rightarrow Ba \mid bSX \mid a$$

$$B \rightarrow aAB \mid b \mid \epsilon$$

$$X \rightarrow aC$$

OR

- VII. (a) Design a PDA to accept the language $L = \{a^n b^n c^m d^m \mid m, n \geq 1\}$ by empty stack. (5)

- (b) Construct an equivalent PDA for the following context free grammars. (5)

$$S \rightarrow aB \mid bA$$

$$A \rightarrow aAB \mid bBB \mid a$$

$$B \rightarrow aS \mid bA \mid b$$

- VIII. (a) Design a turing machine to accept the language $L = \{a^n b^n c^m \mid n, m \geq 1\}$. (5)

- (b) Explain multi-tape and mutli-track turing machines. (5)

OR

- IX. (a) Design a turing machines to accept the language (5)

$$L(M) = \{ww^R \mid \text{where } |w| > 0\}$$

- (b) Explain any two of the following: (5)

(i) Halting problem of turing machines.

(ii) Storage in finite control.

(iii) Universal Turing Machines.