

**Supplementary homework problems for week 2.**

1. Let  $T = \begin{bmatrix} 1 & 0 & -1 & 2 & 1 \\ 2 & 0 & -2 & 4 & 2 \\ 0 & 1 & 1 & 1 & 1 \end{bmatrix}$

Suppose that  $T$  is used to define a function in the usual way.

- (a) Compute the rank of  $T$ .
- (b) What is the domain of  $T$ ?
- (c) What is the codomain of  $T$ ?
- (d) Is  $T$  onto? Why or why not?
- (e) Is  $T$  one-to-one? Why or why not?
- (f) Is  $T$  a one-to-one correspondence? Why or why not?

2. Find the *rank* of each matrix from question (5)1 on page 18 of the book. You need to show work at least for those matrices where you cannot tell me the answer immediately.