

Show all work clearly and in order. Please box your answers. 10 minutes.

1. Let $T = \begin{bmatrix} 1 & 3 & -1 & 2 & 1 \\ -2 & -6 & 3 & 4 & 2 \end{bmatrix}$

Suppose that T is used to define a function in the usual way.

- (a) Compute the rank of T .
- (b) What is the domain of T ?
- (c) What is the codomain of T ?
- (d) Is T onto? Why or why not?
- (e) Is T one-to-one? Why or why not?
- (f) Is T a one-to-one correspondence? Why or why not?

2. Let

$$A = \begin{bmatrix} 1 & 1 \\ 2 & 1 \end{bmatrix}, \quad B = \begin{bmatrix} -1 & 0 & 2 \\ 0 & 3 & 5 \end{bmatrix}$$

- (a) Is the product AB defined? If so compute it.
- (b) Is the product BA defined? If so compute it.