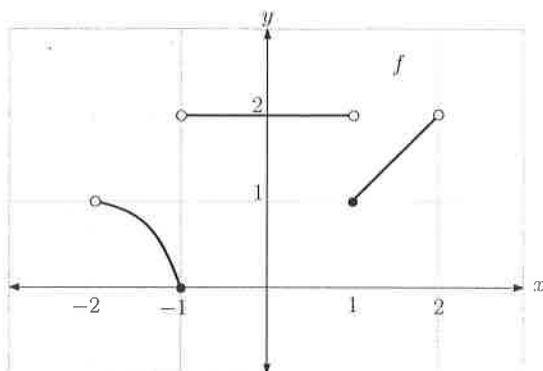


Score: \_\_\_\_\_ out of 10.

Math 201 - Quiz #2

Name: \_\_\_\_\_

1. Use the graph of the given function  $y = f(x)$  below to compute the following limits (if they exist):



(a)  $\lim_{x \rightarrow -1^-} f(x) =$  0

(d)  $\lim_{x \rightarrow 1^-} f(x) =$  2

(b)  $\lim_{x \rightarrow -1^+} f(x) =$  2

(e)  $\lim_{x \rightarrow 1^+} f(x) =$  1

(c)  $\lim_{x \rightarrow -1} f(x) =$  D.N.E.

(f)  $\lim_{x \rightarrow 1} f(x) =$  D.N.E.

2. (a)  $\lim_{x \rightarrow -3^-} \frac{x+2}{x+3} =$   $+\infty$   
*Handwritten notes: "goes to -1 (and is -)" with an arrow pointing to the denominator, and "x < -3" with an arrow pointing to the limit process.*

(b) Part (a) shows that the function  $f(x) = \frac{x+2}{x+3}$  has a vertical asymptote at  $x =$   $-3$

3. Pick ONE of the following (please circle which one you will solve). Otherwise, I will grade the first one you work on. You must show work on this problem.

(a)  $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x^2 + x - 6}$

(b)  $\lim_{x \rightarrow 7} \frac{\sqrt{x+2} - 3}{x - 7}$

(c)  $\lim_{x \rightarrow -4} \frac{\frac{1}{4} + \frac{1}{x}}{4 + x}$

See next page for solutions //

Please put your final answer in this box  $\rightarrow$

$$\begin{aligned}
 (a) \lim_{x \rightarrow 2} \frac{x^2 - 4}{x^2 + x - 6} &= \lim_{x \rightarrow 2} \frac{\cancel{(x-2)}(x+2)}{\cancel{(x-2)}(x+3)} \\
 &= \lim_{x \rightarrow 2} \frac{x+2}{x+3} \\
 &= \frac{2+2}{2+3} = \boxed{\frac{4}{5}}
 \end{aligned}$$

$$\begin{aligned}
 (b) \lim_{x \rightarrow 7} \left( \frac{\sqrt{x+2} - 3}{x-7} \right) \left( \frac{\sqrt{x+2} + 3}{\sqrt{x+2} + 3} \right) \\
 = \lim_{x \rightarrow 7} \frac{(\sqrt{x+2})^2 - \cancel{3\sqrt{x+2}} + \cancel{3\sqrt{x+2}} - 9}{(x-7)(\sqrt{x+2} + 3)} \\
 = \lim_{x \rightarrow 7} \frac{x+2-9}{(x-7)(\sqrt{x+2} + 3)} \\
 = \lim_{x \rightarrow 7} \frac{\cancel{(x-7)}}{\cancel{(x-7)}(\sqrt{x+2} + 3)} = \lim_{x \rightarrow 7} \frac{1}{\sqrt{x+2} + 3} \\
 = \frac{1}{\sqrt{9} + 3} = \frac{1}{3+3} = \boxed{\frac{1}{6}}
 \end{aligned}$$

$$\begin{aligned}
 (c) \lim_{x \rightarrow -4} \frac{\frac{1}{4} + \frac{1}{x}}{4+x} &= \lim_{x \rightarrow -4} \frac{\frac{x+4}{4x}}{\frac{4+x}{1}} = \lim_{x \rightarrow -4} \left( \frac{\cancel{x+4}}{4x} \right) \left( \frac{1}{\cancel{4+x}} \right) \\
 &= \lim_{x \rightarrow -4} \frac{1}{4x} = \boxed{-\frac{1}{16}}
 \end{aligned}$$