Comments for Lecture 6 2.3.2010

Start homework 2 as soon as possible!

"The Function".

Given a system of linear equations with an $m \times n$ coefficient matrix C, the system looks like:

$$c_{11}x_1 + c_{12}x_2 + \dots + c_{1n}x_n = k_1$$

$$c_{21}x_1 + c_{22}x_2 + \dots + c_{2n}x_n = k_2$$

$$\vdots \qquad \vdots \qquad \vdots \qquad = \vdots$$

$$c_{m1}x_1 + c_{m2}x_2 + \dots + c_{mn}x_n = k_m$$

We talked about how we can actually think of this as a function. The input here would be the n-tuple: $\mathbf{x} = (x_1, x_2, \dots, x_n)$ and the output would be the m-tuple: $\mathbf{k} = (k_1, k_2, \dots, k_m)$. So now we think of C as a function having domain \mathbb{R}^n and codomain \mathbb{R}^m written:

$$C: \mathbb{R}^n \to \mathbb{R}^m$$

(NOTE: The dimentions of C as a matrix are $m \times n$) and we write

$$C(\mathbf{x}) = \mathbf{k}$$

As we discussed in class **Theorem 1.6.2** was extremely nice because we were able to determine exactly when C is *onto* and when it is *one-to-one*. An amazing thing is that we can get this information for free when we compute rank of C!