Secure Two Party Computation

Preliminary presentation

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Presentation overview

- ▶ My project focuses on Secure Multiparty Computation, in particular the two party case using Yao Garbled Circuits.
- ▶ The final aim is to implement the as yet unimplemented protocol laid out by Lindell in "Fast Cut-and-Choose based Protocol for Malicious and Covert Adversaries" (henceforth Lindell 2014).
- ▶ By the end of this presentation you should know,
 - What is Secure Multiparty Computation?
 - ▶ What can it be used for?
 - ▶ The basics of Yao Garbled Circuits.
 - ▶ What progress have we made so far.

What is Secure Multiparty Computation?

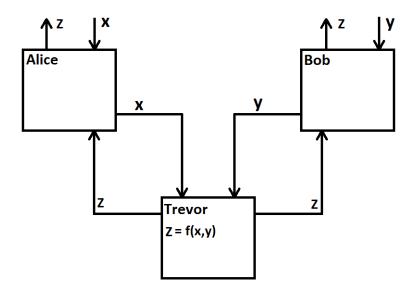
- ▶ In the problem of Secure Multiparty Computation we have a set of parties, each of whom has a secret input.
- The parties wish to co-operate to compute a function upon their collective inputs without revealing said inputs to one another.
- Some example applications are,
 - ► The Millionaires problem.
 - Distributed secrets.
 - Sugar Beets (Auctions).
 - Database query.

Desired security properties

Before we go any further we need to define what properties we want an SMC protocol to fulfill before we consider it Secure.

- ▶ **Privacy**, the only knowledge parties gain from participating is their proper outputs.
- ► **Correctness**, the output is indeed that of the intended function.
- ▶ Independence of inputs, no party can choose it's inputs as the function of other parties inputs.

The Ideal Model



Security Definitions

- We measure the security of an SMC protocol in terms of what adversaries it is secure against.
- We define adversaries in terms of their capabilities.
- We say that an SMC protocl is secure against an adversary if the adversary can achieve no more than they would be able to achieve attacking the Ideal Model.
- We focus on three adversaries,
 - Semi-Honest
 - Malicious
 - Covert

Semi-Honest Adversaries

- Semi-Honest(SH) adversaries are the weakest adversary we shall consider.
- ▶ They are sometimes also called "honest, but curious".
- ▶ SH adversaries are limited to looking at information given to them in the process of the protocol.
- ▶ They have to follow the protocol (they cannot cheat).
- SH adversaries are very similar to traditional "Passive" adversaries.

Malicious and Coverts Adversaries

- Malicious adversaries are the strongest adversary.
- ▶ Malicious adversaries can use any arbitrary strategy. We do not assume that they follow the protocol.
- Covert Adversaries are slightly weaker than Malicious Adversaries.
- Covert Adversaries can also use any arbitrary strategy, but they are adverse to being caught.
- ► They are willing to accept a certain probability of getting caught.

Oblivious Transfer

- ▶ A key component we will need later is Oblivious transfer(OT).
- Security definitions for OTs is are very similar to SMC, though we don't really look at the Covert case.

ReceiverSenderInputs : $b \in \{0,1\}$ Inputs : X_1 , X_2 Outputs : X_b Outputs : \emptyset

Figure 1: Definition of the functionality of a one-out-of-two OT protocol. Note k-out-of-n OT is also possible.

Even-Goldreich-Lempel Semi Honest OT

 $\begin{array}{lll} \textbf{Receiver} & \textbf{Sender} \\ \textbf{Inputs}: b \in \{0,1\} & \textbf{Inputs}: \textit{X}_0, \textit{X}_1 \\ \textbf{Outputs}: \textit{X}_b & \textbf{Outputs}: \emptyset \\ \end{array}$

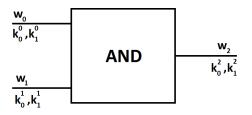
- ▶ Receiver: Generates a public/private key pair (E, D), where E is the public key.
- ▶ **Receiver:** Sets $PK_b = E$, choose PK_{1-b} at random from the same distribution as the public keys. Send PK_0 and PK_1 to the Sender.
- ▶ **Sender:** Encrypt X_0 using PK_0 as C_0 and encrypt X_1 using PK_1 as C_1 . Send C_0 and C_1 to the Receiver.
- ▶ Receiver: Receives C₀ and C₁, then decrypt C_b using D. Output this decrypted value.

Figure 2: The abstracted Even-Goldreich-Lempel protocol. Who can suggest why this is only Semi Honest?

Yao Garbled Circuits

- First we need some notation for binary circuits.
- ▶ We denote the value of wire w_i as b_i , we generate two random "garble value", denote these by k_i^0 and k_i^1 .
- ▶ We then generate a random permutation for each wire w_i , denote this by π_i .
- For each gate we create an encryption table indexed by c_i and c_j (where the input wires to the gate are w_i and w_j).

Yao Garbled Circuits



$$c_0, c_1 : E_{k_0^{b_0}}(E_{k_1^{b_1}}(k_2^{G(b_0,b_1)}||c_2))$$

where $c_i = \pi_i(b_i)$ and $G(b_i, b_j)$ is the function taking the input of the gate and returning the output of the gate.

Yao Garbled Circuits

- We extend this to all gates of the circuit.
- The Builder then sends the circuit to the Executor, stripped of the values of the permutations and keys.
- ▶ The Builder then sends the keys and permuted bit values relating to the its inputs (e.g. if the Builder's i^{th} input is 0, the builder sends k_i^0 and $\pi_i(0)$).
- ► The Builder also sends the permutations for the Executor's input wires and the Executor's output wires.
- ► The Executor then obtains the keys for its inputs by running Oblivious transfers with the Builder.
- ▶ Finally the Executor uses the keys evaluate the circuit.

Yao Garble Circuits - Malicious Security

- ► Naively implemented Yao Garbled Circuits are only Semi-Honest secure.
- Can anyone suggest why this might be?

Yao Garble Circuits - Malicious Security

- Yao Garbled Circuits are only secure up to Semi-Honest adversaries because we are trusting that the Circuit builder is building the correct circuit.
- ► There are several ways to extend Yao Garbled Circuits to achieve security in the presence of Malicious adversaries.
- In particular let's look at "Cut-and-choose", a method loosely inspired by the solution to dividing a cake evenly between two parties.
- One person cuts the cake into two halves, the other person chooses which half they want.

Cut-and-Choose

- ▶ In Cut-and-choose the Builder generates many circuits.
- ► The Executor then picks a random subset of the circuits and "opens" them, to check that they are correct.
- If any of the "Check-Circuits" fail the Executor knows the Builder is trying to cheat.
- ► The Executor then evaluates all the remaining un-opened circuits and returns the majority output.

Cut-and-Choose - Not so simple

- Cut-and-choose seems like an incredibly simple solution to solve all our problems, but it creates several new problems.
- For example we need to ensure the Builder gives the same input for every circuit, without knowing what their input should be!
- ► The Executor also has to careful about how they react to detecting cheating, they can't just immediately abort.

Why Lindell 2014 is Great

- ► The best result for a Cut-and-choose based protocol before Lindell 2014 gave an error rate of 2^{-0.32s} where s is the number of circuits.
- ▶ Lindell's new protocol gives an improved error rate of 2^{-s} .
- ► This means we get the same level of security as before for three times less circuits.

Questions?