

Part A

Giving $x-z=0.2, -0.5x+y+0.25z=-1.425, x-0.5y+z=2$ to Wolfram leads to:

$$x \approx 0.806667, y \approx -1.17333, z \approx 0.606667$$

And with our code:

```
In [3]: def gauss_seidel(A, b):
        solution = [0, 0, 0]
        previous_solution = [0, 0, 0]
        for _ in range(300):
            for k in range(3):
                sum_of_other_side = b[k]
                for j in range(3):
                    if k != j:
                        sum_of_other_side -= solution[j] * A[k][j]
                previous_solution[k] = solution[k]
                solution[k] = sum_of_other_side / A[k][k] # dividing by the coefficient
        return solution
```

```
In [4]: gauss_seidel([[1, 0, -1], [-0.5, 1, 0.25], [1, -0.5, 1]], [0.2, -1.425, 2])
```

```
Out[4]: [0.8066666666666667, -1.1733333333333333, 0.6066666666666666]
```

So, the result for part (a) is around $x = 0.81, y = -1.17, z = 0.61$.

Part B

Giving $x-2z=0.2, -0.5x+y-0.25z=-1.425, x-0.5y+z=2$ to Wolfram leads to:

$$x \approx 1.15789, y \approx -0.726316, z \approx 0.478947$$

And with our code:

```
In [5]: gauss_seidel([[1, 0, -2], [-0.5, 1, -0.25], [1, -0.5, 1]], [0.2, -1.425, 2])
```

```
Out[5]: [2.1568728252933877e+41, 1.3480455158083672e+41, -1.482850067389204e+41]
```

As this matrix is not diagonally dominant (for the first row, $1 > 0 + |-2|$ is wrong) so there is the possibility that it can diverge.