



# Recent improvements to JuMP

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# What is JuMP?

## An algebraic modeling language in Julia

- Under development since 2013
- Supports all major problem types, including MIP, NLP, SDP
- > 50 connected solvers
- > 60 repositories in [github.com/jump-dev](https://github.com/jump-dev)

In the last year

- > 10,000 downloads/month
- > 1,000 pull requests
- > 300 issues opened
- > 50 contributors

# Outline

Improving nonlinear programming support in JuMP

Complex number support

Generic number support

Constraint programming

Multiobjective support

MathOptAI.jl

# Improving nonlinear programming support in JuMP

<https://jump.dev/JuMP.jl/stable/manual/nonlinear/>



Improving nonlinear programming support in JuMP | Oscar Dowson | JuliaCon 2022



Improving nonlinear programming support in JUMP | Oscar Dowson | JuliaCon 2023



# Improving nonlinear programming support in JuMP

<https://jump.dev/JuMP.jl/stable/manual/nonlinear/>

```
using JuMP, Gurobi

model = Model(Gurobi.Optimizer)

# OR: model = Model(Xpress.Optimizer)

@variable(model, -5 <= x[1:2] <= 5, Int)

@objective(model, Min, x[2]^3 * sin(x[1])^2)

my_func(y) = sum(2^y[1] .+ exp.(y))

@expression(model, expr, 2 * my_func(x))

@constraint(model, expr <= 100)

@constraint(model, sqrt(x' * x) <= 1)
```

# Improving nonlinear programming support in JuMP

<https://jump.dev/JuMP.jl/stable/manual/nonlinear/>

```
using JuMP, Ipopt
model = Model(Ipopt.Optimizer)
backend = MOI.Nonlinear.SymbolicMode()
# OR: backend = MOI.Nonlinear.SparseReverseMode()
set_attribute(model, MOIAutomaticDifferentiationBackend(), backend)
@variable(model, x[1:2])
@objective(model, Min, (1 - x[1])^2 + 100 * (x[2] - x[1]^2)^2)
optimize!(model)
```

# Complex number support

<https://jump.dev/JuMP.jl/stable/manual/complex/>

```
using JuMP
```

```
model = Model()
```

```
@variable(model, x in ComplexPlane())
```

```
#   real(x) + imag(x) im
```

```
@variable(model, y[1:2, 1:2] in HermitianPSDCone())
```

```
#   2x2 LinearAlgebra.Hermitian{...}:
```

```
#   real(y[1,1])           real(y[1,2])+imag(y[1,2])*im
```

```
#   real(y[1,2])-imag(y[1,2])*im   real(y[2,2])
```



**Benoît Legat**  
blegat

# Generic number support

[https://jump.dev/JuMP.jl/stable/tutorials/conic/arbitrary\\_precision/](https://jump.dev/JuMP.jl/stable/tutorials/conic/arbitrary_precision/)

```
using JuMP, Clarabel

model = GenericModel{BigFloat}(Clarabel.Optimizer{BigFloat})

@variable(model, x[1:2, 1:2] in PSDCone())

@variable(model, t)

y = rand(2, 2)

@constraint(model, [t; vec(x .- y)] in SecondOrderCone())

@objective(model, Min, t)

optimize!(model)

value.(x) # Returns Vector{BigFloat}
```



**Paul Goulart**  
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# Constraint programming

[https://jump.dev/JuMP.jl/stable/tutorials/linear/constraint\\_programming/](https://jump.dev/JuMP.jl/stable/tutorials/linear/constraint_programming/)

```
using JuMP, MiniZinc

model = Model{() -> MiniZinc.Optimizer{Int}}("chuffed"))

@variable(model, 1 <= x[1:3] <= 3, Int)
@variable(model, 0 <= z[1:2] <= 1, Bin)
@constraint(model, x in MOI.AllDifferent(3))
@constraint(model, z[1] <--> {x[1] == 1})
@constraint(model, z[1] || z[2] := true)
@constraint(model, z[1] && z[2] := false)
```



Chris Coey  
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**RelationalAI**

# Multi-objective support

[https://jump.dev/JuMP.jl/stable/tutorials/linear/multi\\_objective\\_examples/](https://jump.dev/JuMP.jl/stable/tutorials/linear/multi_objective_examples/)

```
using JuMP, HiGHS

import MultiObjectiveAlgorithms as MOA

model = Model(() -> MOA.Optimizer(HiGHS.Optimizer))
set_attribute(model, MOA.Algorithm(), MOA.Dichotomy())

@variable(model, 0 <= x[1:2] <= 3)

@objective(model, Min, [3x[1] + x[2], -x[1] - 2x[2]])

@constraint(model, 3x[1] - x[2] <= 6)

optimize!(model)

X = [value.(x; result = i) for i in 1:result_count(model)]
```



Gökhan Kof  
kofgokhan



XavierG  
xgandibleux

# MathOptAI.jl

<https://lanl-ansi.github.io/MathOptAI.jl/stable/>



Robert Parker  
Robbybp

Embed machine learning predictors into a JuMP model. Similar to

- OMLT
- gurobi-machinelearning
- PySCIPOpt-ML
- GAMSPy (talk on Tuesday)
- ...

$$\begin{aligned} \min \quad & f(x, y) \\ & g(x, y) \leq 0 \\ & \mathbf{y} = \mathbf{F(x)} \end{aligned}$$

where  $F$  is a neural network/decision tree/logistic regression/...

# MathOptAI.jl

<https://lanl-ansi.github.io/MathOptAI.jl/stable/>

```
#!/usr/bin/python3
```

```
import torch
```

```
from torch import nn
```

```
model = nn.Sequential(nn.Linear(10, 16), nn.ReLU(), nn.Linear(16, 2))
```

```
torch.save(model, "model.pt")
```

# MathOptAI.jl

<https://lanl-ansi.github.io/MathOptAI.jl/stable/>

```
#!/usr/bin/julia
```

```
using JuMP, Ipopt, MathOptAI, PythonCall
```

```
model = Model(Ipopt.Optimizer)
```

```
@variable(model, 0 <= x[1:10] <= 1)
```

```
predictor = MathOptAI.PytorchModel("model.pt")
```

```
y, formulation = MathOptAI.add_predictor(model, predictor, x)
```

# Three-ways to formulate a problem

Each with a different trade-off

Parker et al. (2025). Formulations and scalability of neural network surrogates in nonlinear optimization problems

|            | Full-space | Reduced-space | Gray-box |
|------------|------------|---------------|----------|
| Pros       |            |               |          |
| Cons       |            |               |          |
| Bottleneck |            |               |          |

# Full-space

## Add intermediate variables and constraints

```
y, _ = MathOptAI.add_predictor(model, predictor, x)
```

```
model = Model()
```

```
@variable(model, x)
```

```
@variable(model, y[1:2])
```

```
@constraint(model, y[1] == a * x + b)
```

```
@constraint(model, y[2] == max(0, y[1]))
```

```
@objective(model, Min, y[2])
```

# Reduced-space

## Represent as nested expressions

```
y, _ = MathOptAI.add_predictor(model, predictor, x; reduced_space = true)
```

```
model = Model()
```

```
@variable(model, x)
```

```
@expression(model, y, max(0, a * x + b))
```

```
@objective(model, Min, y)
```



# Gray-box

## Use external function evaluation

```
y, _ = MathOptAI.add_predictor(model, predictor, x; reduced_space = true)
```

```
fn(x) = max(0, a * x + b)
```

```
fn_dx(x) = ifelse(a * x + b >= 0, a, 0)
```

```
model = Model()
```

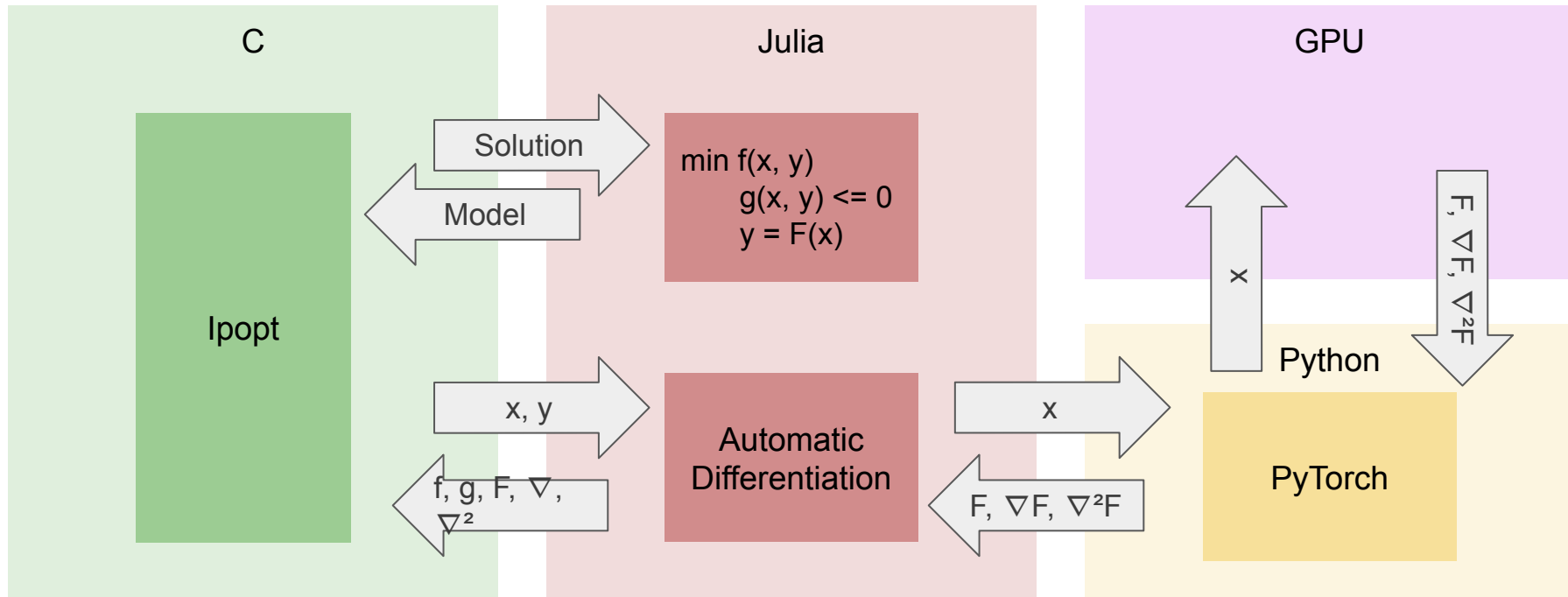
```
@variable(model, x)
```

```
@operator(model, op_gray_box, 1, fn, fn_dx)
```

```
@objective(model, Min, op_gray_box(x))
```

# Gray-box: Julia, C, Python, working together

JuMP problems call Ipopt in C, which calls back to Julia for oracles, which calls Python and PyTorch



**JuMP problems call Ipopt in C, which calls back to Julia for oracles, which calls Python and PyTorch**

using JuMP, Ipopt, MathOptAI, PythonCall

```
@variable(model, 0 <= x[1:10] <= 1)
```

[illegible]

# Three-ways to formulate a problem

Each with a different trade-off

Parker et al. (2025). Formulations and scalability of neural network surrogates in nonlinear optimization problems

|            | Full-space                                      | Reduced-space  | Gray-box   |
|------------|---|--|--|
| Pros       | Sparsity<br><br>Solvers can exploit linearity   | Fewer variables and constraints                                      | Can use external evaluation for oracles.<br><br>Scales with input/output dimension, not intermediate dimension |
| Cons       | Many extra variables and constraints            | Complicated dense expressions  | Requires oracle-based NLP. Cannot be used by global MINLP solvers  |
| Bottleneck | Computing linear system because of problem size | Computing derivatives (JuMP's AD does not do well at dense problems) | Moving data between Julia/Python/GPU   |