

Freie Universität Berlin
Fachbereich Mathematik und Informatik
Takustraße 9, 14195 Berlin

MASTER THESIS

USER POSITION PREDICTION IN 6-DOF MIXED REALITY APPLICATIONS USING RECURRENT NEURAL NETWORKS

Oleksandra Baga

Freie Universität Berlin
Matrikelnummer 5480722
Master Computer Science
E-Mail: oleksandra.baga@gmail.com

Prof. Dr. Daniel Göhring
Fachbereich Mathematik und Informatik
Freie Universität Berlin

Prof. Dr. Tim Landgraf
Fachbereich Mathematik und Informatik
Freie Universität Berlin

Statutory Declaration

I herewith formally declare that I have written the submitted master thesis independently. I did not use any outside support except for the quoted literature and other sources mentioned in the paper.

I clearly marked and separately listed all of the literature and all of the other sources which I employed when producing this academic work, either literally or in content.

I am aware that the violation of this regulation will lead to failure of the thesis.

10.10.2022..... Oleksandra Baga

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Listings

List of Abbreviations

ANN	Artificial Neural Networks
AR	Augmented Reality
CNN	Convolutional Neural Network
CPU	Central processing unit
DoF	Degree of freedom
DL	Deep Learning
FFN	Feed-forward Neural Network
GRU	Gated Recurrent Unit
HMD	Head-Mounted-Display
IEEE	Institute of Electrical and Electronics Engineers
KF	Kalman Filter
LAT	Look ahead time
LSTM	Long-Short-Term Memory
M2P	Motion-to-Photon
MAE	Mean Absolut Error
MEC	Mobile Edge Computing
ML	Machine Learning
MR	Mixed Reality
NLP	Natural Language Processing
ReLU	Rectified Linear Unit
RNN	Recurrent Neural Network
RTT	Round-trip time
SDG	Stochastic Gradient Descent
VR	Virtual Reality
3-DoF	Three degree of freedom
6-DoF	Six degree of freedom

Introduction

This thesis is focusing on designing and evaluation of the approach for the prediction of human head position in a 6-dimensional degree of freedom (6-DoF) of Extended Reality (XR) applications for a given look-ahead time (LAT) in order to reduce the Motion-to-Photon (M2P) latency of the network and computational delays. At the beginning of the work the existing head motion prediction methods were analysed, and their similarities differences will be taken into account when a proposed Recurrent Neural Network-based predictor will be developed. Main goal is the systematic analysis of the potential of recurrent neural networks for head motion prediction. The proposed approach was evaluated on a real head motion dataset collected from Microsoft HoloLens. Based on a discussion of the obtained results, suggestions for future work are provided.

1.1 Problem statement

The correct and fast head movement prediction is a key to provide a smooth and comfortable user experience in VR environment during head-mounted display (HDM) usage. The recent improvements in computer graphics, connectivity and the computational power of mobile devices simplified the progress in Virtual Reality (VR) technology. The way users can interact with their devices changed dramatically. With new technologies of VR environment user becomes the main driving force in deciding which portion of media content is being displayed to them at any time of interaction with VR Applications [19]. Until recently the high-quality experiences with modern Augmented Reality (AR) and VR systems were not widely presented in home usage and were mainly used in research labs or commercial setups. The hardware for displaying the VR environment was once extremely expensive but recent years became more broadly accessible and the 6-DoF VR headset designed for the end-user were released¹. It is possible now to experience virtual reality scenes and watch new type of volumetric media at home and the market interest for development VR and AR applications expected to be huge next years.

In fact, the existing on this moment virtual environments can be divided into two main groups depending on position of the user and their ability to move inside the VR environment. The user motion and prediction within a 3-DoF environment

¹<https://medium.com/@DAQRI/motion-to-photon-latency-in-mobile-ar-and-vr-99f82c480926>

has been intensely researched for years. Extending such approaches to a 6-DoF environment is not straightforward, due to the change of the user's viewing point from inward to outward and additional three degrees of freedom [20].

Although all mentioned above improvements, rendering of volumetric content remains very demanding task for existing devices. Thus the improvement of a performance of existing methods, design and implementation of new approaches specially for the 6-DoF environment could be a promising research topic.

1.2 Motivation for the research

Research efforts to reduce the computational load are being already wide attempted. However, these approaches designed for the client side. Recently presented technique of the rendering on a cloud server makes possible to decrease the computational load on the client device by offloading of the task to a server infrastructure and then by sending the rendered 2D content instead of volumetric data [13]. The calculated 2D view must correspond the current position and orientation of a user. However, cloud-based streaming approach adds network latency and processing delays due uploading to a server the user position, rendering a new 2D picture from the 3D data and sending it back to a device. Thus, a rendered 2D image can appear even later on a display than with usage of local rendering system.

The promising research topic is a reducing the Motion-to-Photon (M2P) latency by predicting the future user position and orientation for a look-ahead time (LAT) and sending the corresponding rendered view to a client. The LAT in this approach must be equal or larger to the M2P latency of the network including round-trip time (RTT) and time need for calculation and rendering of a future picture at remote server.

1.3 Structure of the thesis

The organization of this thesis is as follows. The thesis starts from introduction and problem statement, followed by theoretical background related to the research topic. Literature review chapter introduces different approaches and technologies of motion prediction algorithms. The chapters 2 and 4 show the implementation of the presented models and evaluation of the results that were obtained during experiments. Last, the discussion regarding method limitations and suggestions for the future work are done.

Chapter 1 - Introduction.

The current chapter shortly introduces a state of development on scientific field achieved at a time of master thesis creation in the context on XR applications. The

necessity of timely action to improve the situation with increasing computational and network latency is shown in problem statement section 1.1. Due to the breadth of the research topic, the section 1.2 focuses and motivates the research topic.

Chapter 2 - Background.

The next chapter includes a review of the area being researched. It starts with a short introduction of the concept of MR applications and presents a 6-DoF environment. The presence and influence of a computational and network latency is covered. In section 2.5 the challenges faced in predicting of the viewer's position are discussed. Last section contains an overview of previous research in the field of prediction of user's head position and orientation and places a master thesis's topic in the context of the existing literature.

Chapter 3 - Implementation.

Chapter describes practical implementation of the approach. The dataset including data collection from head mounted display (HDM) and data understanding and preprocessing are described in section 3.1. Model Inputs, Model architecture and the development steps are covered in section 3.2. The implementation of Unity Application, training and evaluation loop with PyTorch and hyperparameter search described in the section 3.2.3.

Chapter 5 - Evaluation.

A Baseline model, used for comparing the obtained results and tuning the hyperparameters is described. The goal of evaluation and metrics used in this research are covered. The conducted experiments with a data obtained from HMD for each analysed RNN Model can be found in section 4.4.

Chapter 5 - Conclusion.

The last chapter presents a discussion about the limitation of proposed method and provides a conclusion about the received results including suggestions for potential types of future research.

Fundamentals

This chapter introduces theoretical background of the presented research problem. First, the concept of mixed reality (MR) followed by an introduction of six degree of freedom (6-DoF) environment and the difference to the three degree of freedom (3-DoF) are described. The term motion-to-photon latency (M2P) is covered, followed by a short discussion about an influence of M2P latency on the decreasing of user experience. The new developed cloud-based rendering and streaming approach is shortly discussed in this chapter. The last section of this chapter highlights challenges with the prediction of viewer's head pose that arises in modern XR applications in connection especially with the added network latency due the using of remote cloud server for computational offload. The section 2.6 overviews the existing works done in the research field using traditional algorithms and recurrent neural networks.

2.1 Mixed reality with HMD

Mixed reality makes possible to break down the border between the virtual and real world and provides today an experience that just a short-time ago we could only imagine when watching the sci-fi movies. Terms Virtual Reality (VR), Augmented reality (AR) and Mixed reality (MR) are often used interchangeably. VR creates the virtual environment around user and tricks human's senses into thinking one is in a different environment. AR adds a virtual object to the real world that we can see through the lenses of special developed Head Mounted Display (HMD). Thus realistic images, sounds, and other sensations can be generated by a powerful HMD and projected on transparent holographic lenses giving a user the feeling that virtual objects have size and density. However, AR does not allow interactions between users and the virtual objects added to the real-world scene. MR combines the advantages of the VR and AR and adds an interaction between real and artificial elements. Thus users can directly interact with virtual objects (with operations such as scaling, rotation, or translation) in the real environment using their hands. For example, in MR Application virtual objects can be placed on the real table in the user's room, picked up with a hand and moved to another place.

Volumetric video (VV) is a new content creation approach to be used within AR and MR applications [25]. Volumetric video allows to view recorded information from a range of different angles, as if an observer was physically presented in the

room when video was captured by cameras and could move around the object. This thesis uses volumetric video object placed in the real environment when running developed MR Application for collection the user's position and rotation data. Refer sections 2.4 and 3.2.3 for more details about VV and how it was used in thesis.

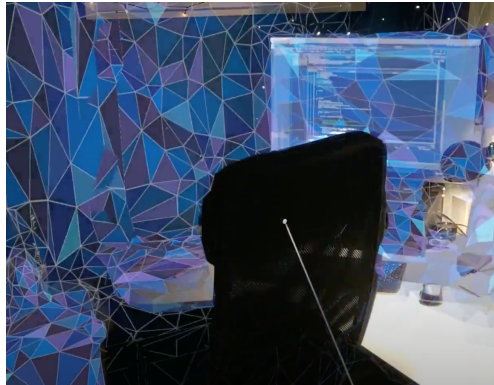


Figure 1: HoloLens 2 maps itself with a mesh.

Nowadays different HMD with varying performance levels and prices are available on the market. In this thesis, Microsoft HoloLens 2 was used for MR experience and data collection. It is an updated version of the previous generation HoloLens 1 headset from Microsoft with such improved feature as display resolution, field of view, weight, battery lifetime. By using the AHAT (Articulated HAnd Tracking) depth camera, the HoloLens 2 can capture hand movements to obtain hand tracking data. The build-in tracking systems allows HoloLens to understand the environment around the user and to place stable and accurate holograms on the correct places where they intended to be by the developer of MR Application. The data used to track users is represented in the spatial map¹. When VR Application is starting on HoloLens, HoloLens uses unique environmental landmarks to locate itself in a space. The mesh graphic spreading over the space is seen, as illustrated in Fig. 1, during the Application launch and this means a device is mapping to surroundings. As user moves with HMD on their head, built-in cameras continuously scan the environment and construct virtual world geometry for real-world objects. The primary stereo rendering component attached to HMD can be accessed from Unity and thus the position and orientation can be obtained for thesis purposes.

2.2 Six degrees of freedom

Term *degrees of freedom* describes how users interact with a virtual environment and how they can move inside it. Within 3-DoF space user has only three possibilities: look left and right, look up and down and pivot left and right. 3-DoF space does not allow to move throughout the virtual space. Thus only rotational movement can be tracked. In 3-DoF VR Application multimedia content is the omnidirectional or spherical video, which represents an entire 360° environment on a virtual sphere [20]. In 3-DoF space HMD enables to display only a portion of the environment

¹<https://docs.microsoft.com/en-us/hololens/hololens-environment-considerations>.

around a user. User is virtually positioned at the centre of a sphere as shown in Fig. 2, media is displayed from an inward position and user can only change the viewing direction (i.e., by looking up/down or left/right or tilting the head side to side) [20] but can not interact with a media by moving closer/further. Wherever user moves with a HMD on their head, they will remain placed in the at the centre of a sphere and distance to a content can not be changed.

The new VR concept 6-DoF means tracking both position and rotation and refers to the freedom of movement of a rigid body in three-dimensional space. In 6-DoF VR Application user can also change viewing perspective by moving (e.g., walking, jumping) inside the virtual space [20]. Thus the scene is observed from an outward position in 6-DoF environment and extra degree of freedom transforms the virtual experience to be more natural and reflects to human movement in a three-dimensional space. Thus the VV and other volumetric objects such meshes or point clouds are used in MR Applications for 6-DoF scene population. User can freely walks inside the 6-DoF environment with a HMD on a head and observe the placed on scene volumetric objects from all points of view, and if the settings in Unity application allow physical interaction with objects, pick and move them on the new place.

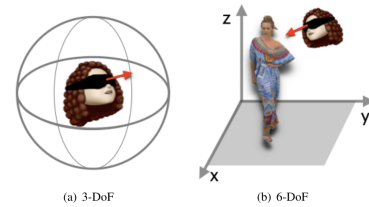


Figure 2: Viewing paradigm in 3- and 6-DoF VR. Source: [20]

2.3 Motion-to-photon latency

VR Application are deployed to the end-user with a goal to create an immersion of a physical presence in a non-physical world. In the real world there is no time delay between action taken and reaction observed. However, in AR/VR/MR Applications the difference between the user's head movement (action) and its corresponding display output reflections (reaction) is defined as motion-to-photon (M2P) latency. The presence of a delay between the physical movement and the display output worsens HMD user experience. In worst case even sense of physical presence in a virtual world would be lost. MTP latencies of more than 20 ms are experienced and cause spatial disorientation and dizziness, referred to as VR sickness or motion sickness [2, 12]. Display lag can produce a range of other perceptual effects include degraded vision, compromised visuo-motor performance and motion sickness [2]. Different components of the HMD, such as the sensors, SOC, display and software can affect M2P latency. Reducing the M2P latency is the key to proving the best VR experience. Not only improving the device parameters, such a usage of more

powerful HMD processor, need to be taken in account. VR Application developers must consider how to deploy more light-weighted applications. If the VR Application need to pull some data from the network or remote server, the network round-trip time and the added processing delays will increase the M2P latency compared to a system that only performs the processing locally [12].

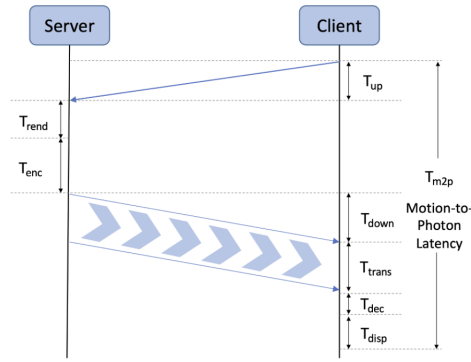


Figure 3: M2P latency for a remote rendering system. Source: [13]

As this thesis evaluates the reducing the M2P latency for VV streaming from remote cloud server, the Fig. 3 illustrates the different components of the M2P latency for a remote rendering system. Total M2P latency is equal to sum of the time taken by a bit of data to travel across the network from HMD to a server, server delay involved in computing the future user position and render a 2D view and a HMD delay during sensor measurements. If the user's future head pose for a look-ahead time (LAT) equal to or larger than

the M2P latency of the system could be predicted, it can eliminate M2P latency and improve the quality of the VR Applications. Studies showed that display lags of greater than 40 ms cause errors in tracking and following a target with the head [2]. This thesis evaluates the performance of RNN Models for LAT 100 ms that is higher than the measured M2P latency of a cloud-based volumetric streaming system described in the next section.

2.4 Cloud-based volumetric video streaming

Volumetric video (VV) is a young technology and is used to build a content for AR and VR Applications. Real-life video from cameras surrounding the 3D object is stored as point clouds or 3D textured mesh sequences and builds a dynamic 3D scene of a real 3D object. In VR Application user can walk through VR environment with a HMD and thus VV can be looked at from any viewpoint. In almost all cases today, the VVs objects stored and rendered locally on a users device. Photo-realistic modelling, real-time rendering and animation of VVs is still computationally difficult. The long sequence VV can even exceed the HMD memory capacity and could not be deployed as a VR Application even on high-cost VR HMD as HoloLens 2. There are still no efficient hardware decoders for point clouds or meshes and software decoding can be prohibitively expensive in terms of battery usage [12]. Thus in the

research field there is a growing interest in VV compression and adaptive streaming, as real-time streaming is necessary for some applications, e.g., telepresence and remote collaboration [25]. The processing and memory load on the user's HMD can be decreased by sending a 2D precomputed rendered view instead of the volumetric 3D content. Some previous studies reveal that participants preferred to stay in front of static point clouds and 1 metre away from them and spent more time looking at the frontal view and faces of human models [25]. VVs are not transparent and provide a feeling of a real 3D object with a mass and a weight thus as a real 3D object they can be looked at only from one viewpoint at one time step. Thus if the sending unneeded information (for example, a back view of a human model when the user looks at model's front view) can be avoided, it decreases the computational load on the user's HMD.

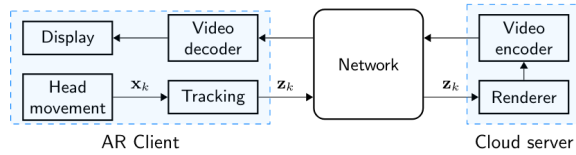


Figure 4: High level operation of a cloud-based volumetric streaming system. Source [12]

A remote rendering system takes complex graphics computational and rendering tasks and delivers the result over a network to a less-powerful client device. Fig. 4 shows an overview of a cloud-based volumetric streaming system proposed by *Gül et al., 2020*.

This thesis evaluates RNN Models and the trained model with the best performance is intended to be used as a part of prediction system of a remote system. A detailed software architecture of a system is described in [13]. In this system a compressed volumetric video is stored as a single MP4 file containing video and mesh tracks [12]. The game engine (Unity) runs at a server and decodes the compressed mesh and texture data. The tracking system of the HMD measures the user position and orientation and sends over a network to the cloud server. Based on the actual user's spatial attributes, cloud server calculates the future position and orientation and renders the corresponding view from the volumetric content. The rendered view is encoded as a video stream and sent to the client over the network. The time period between the head movement and display of the decoded video frame to the viewer is the M2P latency of the system which can be compensated by applying prediction algorithm [12].

2.5 Challenges of head motion prediction

All modern HMD has a position tracker, a device or a system of devices, that is responsible for reporting the position and orientation of HMD to the computational unit that generates the virtual environment images displayed in the HMD. These

images represent the view that a wearer of HMD would have seen if user was present in VR at the position and orientation reported by position tracker [6]. While the task of position tracking is performed by HMD hardware, the task of position prediction of the movement of human body in the virtual reality remains challenging, and it is still complicate to achieve high-precision estimation.

Understanding how users interact and behave in AR or VR is important when working with HMD's sensors. The experiment done by *Zerman et al., 2021* found out that users preferred to stay in front of static point clouds and 1-1.5 meter away from them and spent more time looking at the faces of human models [25]. The navigation trajectories of users within a 6-Degrees-of-Freedom (DoF) should be additionally investigated since an extra level of interaction between user and content is available in 6-DoF environment. The user has now the freedom to change the viewing direction (rotating and translating the head as in 3DoF) but also to change position inside the VR environment [19]. In a 6-DoF environment, users are not being positioned at the centre of the spherical content any longer and the distance changes over time when user moves due to the added degrees of freedom. Thus viewport's center position is not sufficient for tracking the trajectories, the additional metrics such the spatial coordinates and user orientation are needed to obtain the point of origin. Following [19] *Rossi et al, 2021* authored same year another work [20] dedicated 6-DoF metrics. Researchers experimented with different metrics to perform clustering in order to detect group of users with similar behavior in VR. The most promising metric seems to be based on the user position on the virtual floor. Metrics based only on viewport center, as it was used in 3-DoF, and distance failed in detecting the group of similar users [20]. For the trajectory detection best performed a metrics based on user position, orientation on the virtual floor and distance [20]. The analysis above leads to the conclusions that prediction of the user's position and orientation on 6-DoF requires new metrics and approaches to be investigated and implemented.

2.6 Related works

This section presents the overview of previous research in the field of the prediction of user position and focuses on time series methods using different RNN architectures such as LSTM and GRU.

2.6.1 Traditional prediction algorithms

A lot of previous approaches uses basic processing of head movement history to predict the future movement, such as simple average, linear regression, and weighted linear regression [17]. Work of *Corbillon et al., 2017* determines the distance to the

center of viewpoint with simple average and calculates the region that receives from server the video data with a better quality than the remaining of part the video [9]. The work of *Duanmu et al., 2017* proposes prediction of the viewing direction for segment $n + 1$ through linear regression based on the past view segments [11]. Approach of *Xie et al., 2017* uses user's orientation in Euler angle and leverage Linear Regression model to apply Least Square Method and to calculate the trends of head movements [24]. The work [21] proposes to receive from a server only the data of covered by user's viewport. At each point of time, the client requests data which would be played in the future. *Taghavi et al., 2017* use Weighted Linear Regression to predict the next viewport based on window with the latest viewport samples. Researchers mentioned that a client can continue playback of at least a low-quality version of the video when the download time of next video portion varies [21]. Analysis done by *Qian et al., 2016* indicates that at least in the short term, viewers' head movement can be predicted with accuracy $> 90\%$ by even using simple methods such as linear regression [18]. The different approaches were compared such as computing the average value, using the linear regression with all samples and with weighted linear regression with recent samples. With weighted linear regression the average prediction accuracy for short-term values was higher than 90% across all users. However in the longer term it is more difficult to achieve the good result and the average accuracy drops to about 70% [18].

A method to apply saliency algorithms to VR video viewings was presented by *Aladagli et al., 2017* in work [1]. Cross-correlation analysis used for measuring the relationship between the predicted fixation sequences and the recorded head movements [1]. Based on works mentioned above, *Nguyen et al., 2018* proposed panoramic saliency algorithm in order to learn the dependence of head tracking logs and saliency maps from the past video frames.

2.6.2 Recurrent Neuronal Networks

As was explained above, traditional prediction algorithms can not be used straightforward on a new media content in 6-DoF VR Applications. The user position and rotation data is coming as time series with a sequential order that is crucial to be followed in order to predict correctly the next future step for a look-ahead time. A sequence of inputs can be processed with Artificial Neural Network (ANN) called Recurrent Neural Network (RNN). Moreover, RNN can processes input with remembering its state while processing the next sequence of inputs. It is known that standard RNN has difficulties to learn long-term dependencies with gradient descent [5]. Though RNN can robustly store information, it yields a problem of vanishing gradient that make leaning difficult [5]. In the last decade, RNN algorithms have been adopted for motion prediction of 3D sequences with long-term dependencies

taken into account. For example, the work of *Crivellari et al., 2020* targets traces of tourists in a foreign country and tries to predict the motion of people in the environment they never seen before. LSTM-based model is used thus for analyzing the tourists' mobility patterns [10].

The authors *Aykut et al., 2018* claims their research to be first work that applies deep learning for head motion prediction. The authors experimentally confirmed that Feed-forward Neural Network (FFN) indeed had difficulties to learn for different delays. The decision to use LSTM-based architectures *Aykut et al., 2018* reasoned with feedback loop and ability to establish a way of memory and share weights over time [3]. Conducted by researchers experiments showed that the LSTM-based architecture leads to a significant improvement of the MAE and RMSE metrics [3]. The LSTM-based methods were compared also to widely used approaches like the Linear Regression and a Kalman Filter based optimal state estimate. Thus *Aykut et al., 2018* demonstrated a substantial improvement of the deep predictor for latencies in the range of 0.1–0.9 s [3].

Next year *Aykut et al., 2019* experimented in their work [4] with GRU model that belongs to the group of recurrent neural networks (RNN). Authors considered GRU usage because it is computationally more efficient, as it has fewer parameters and states than LSTM units [4]. Proposed in the research GRU-based network is able to improve the MAE and RMSE compared to mentioned above LSTM model, especially for larger delays [4].

Researchers *Karim et al., 2018* developed long short term memory fully convolutional network (LSTM-FCN). In the proposed models, LSTM block is augmented by an fully convolutional block [15] identical to the convolution block in the CNN architecture proposed by *Wang et al., 2018* in their work [23]. *Karim et al., 2018* tried to reduce the rapid model's overfitting by transformation of input to have N variables with a single time step [15].

In work of *Chang et al., 2020* used in addition to standard LSTM networks also bidirectional LSTM (Bi-LSTM) networks, which is stacked two LSTM networks in forward and backward directions. Standard LSTM networks can only consider the past information and Bi-LSTM networks can capture both past and future information by two opposite temporal order in hidden layers [7]. Experimentally, authors found that the basic LSTM performs the best comparing to Bi-LSTM and Temporal Convolutional Network [7]. GRU Model and additionally a bidirectional LSTM (Bi-LSTM) network are used for action recognition based on sensor signals from HMD in work [16]. Similar as in work [7] the LSTM model performed better compared to Bi-LSTM and a GRU outperformed both models. Authors said that the possible reason could be the short-term correlation of human actions in their dataset and that Bi-LSTM with its complicated model structure is rather suitable for long-term actions [16]. The experiments provided in these works clearly indicate that GRU unit can outperform LSTM unit. However, researches suggested that the choice of the RNN model can depend heavily on the dataset and corresponding task [8].

Implementation

This chapter presents the steps of development and implementation of the proposed approach. The Unity Application for HoloLens was deployed on HMD and a raw data with measures and dimension columns was obtained. This data than was analysed and preprocessed to ensure that the captured data can be used in corresponding machine learning models. The model architecture was implemented and experimentally improved during training and evaluation steps.

3.1 6-DoF Dataset

This section describes how the dataset was obtained, analysed and presents the visualization of user's head position and rotation. Almost all machine learning approaches require not only raw data collection but also data exploration and preprocessing steps to be done before training begins.

3.1.1 Data collection from HMD

The real 6-DoF dataset must be used as training data from which the model can learn the spacial and time dependences. In this master thesis HoloLens 2, the second iteration of Microsoft's head-mounted mixed reality device, was used for data collection. The user position and orientation were obtained with Unity application developed for this purpose. Main Camera in Unity is automatically configured to track head movements. More details about Unity application can be found in section 3.2.3. Using the Main Camera, a user position (x, y, z) and orientation in quaternion (qx, qy, qz, qw) were logged in a *csv*-file. Quaternions obtained from HMD will be used to define a rotation by four numbers. Quaternions representations are very convenient for operations such as composition or rotations and coordinate transformation [22]. For these reasons quaternions are chosen for the representation of user head's rotation in three dimensions. Comparing to dataset in [12], the additional parameters were recorded from the Main Camera in order to add more information during training processes. Thus the world-space speed of the camera in meters per second was recorded. Unity velocity has the speed in (x, y, z) defining the direction. The obtained 6-DoF dataset has 10 features used in training process: position (x, y, z) , orientation (qx, qy, qz, qw) and velocity (x, y, z) .

The datasets were recorded in the laboratory space. HMD was presented to users and the basic functions were explained. During data recording, users freely walked wearing HMD in laboratory space. The Unity application, running on HMD, not only recorded the mentioned before parameters but also had a volumetric animated object placed 3 meters ahead of the user in the Mixed Reality environment. No personal data was recorded during these sessions and all traces are obtained anonymously. Thus, after an Unity application was launched, user could immediately see the animated object. The several traces were recorded at least for 10 minutes each. It allows to have enough data after splitting the dataset into training, test and validation partitions. Table 3.1 show the first 20 rows from raw dataset obtained from HoloLens 2 and used in training. Although dataset has 10 columns, the table 3.1 presents only *timestamp* and position (x, y, z) columns.

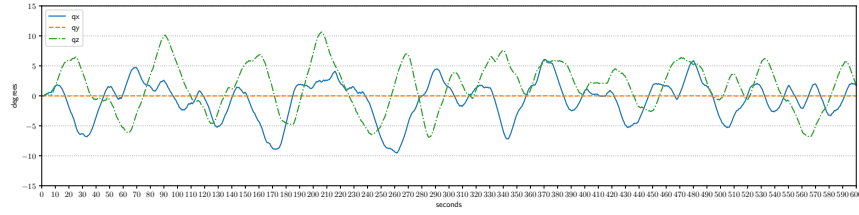
timestamp	x	y	z
2.649431	0.004954389	0.003402365	0.01010712
2.66943	0.00459053	0.003120769	0.01130438
2.698009	0.003960807	0.002990472	0.01276976
2.719285	0.003730714	0.003037783	0.01305151
2.746641	0.003252693	0.003489003	0.01368421
2.764094	0.003153284	0.003518121	0.01400959
2.780033	0.003087142	0.003409061	0.01435899
2.802086	0.003021815	0.00314023	0.01473305
2.815575	0.002789935	0.003551113	0.01506916
2.832602	0.002527435	0.003542757	0.01534094
2.848514	0.002212256	0.003605011	0.01565307
2.863769	0.001921757	0.003369405	0.01590317
2.879648	0.001668522	0.00348538	0.01607716
2.89686	0.001501704	0.003624826	0.01627397
2.913541	0.001487849	0.00359472	0.01643924
2.930006	0.001501501	0.003769569	0.01669565
2.948201	0.001617525	0.004252479	0.01697758
2.964302	0.001755987	0.004224311	0.01721937
2.97978	0.001838901	0.004487753	0.01747578
2.997117	0.002005509	0.005007531	0.01782864

Table 3.1: Raw data from HoloLens 2

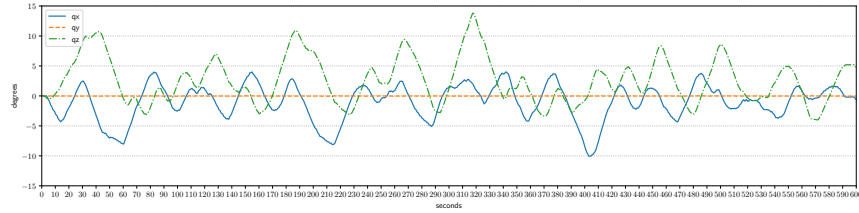
The first column in dataset is *timestamp*. It is obviously, that timestamp appears in row dataset not linearly and comes with different pauses. Even the high-cost HMD, like used in this research HoloLens 2, is sometimes unstable in frame rate during collecting data. Due to signal processing and propagation delays, distance in time between two consecutive samples was either increased or decreased. In the Unity Application, the frame rate is 60 Hz which means that data is expected to be collected every 0.016(6) seconds. Data on some expected timestamps seemed to be unavailable in HMS for recording. Between two sequences with bigger time gap, some records may be considered to be missed. To deal with above situation, the preprocessing steps must be done. They are described in a section 3.1.3 below.

3.1.2 Data Exploration

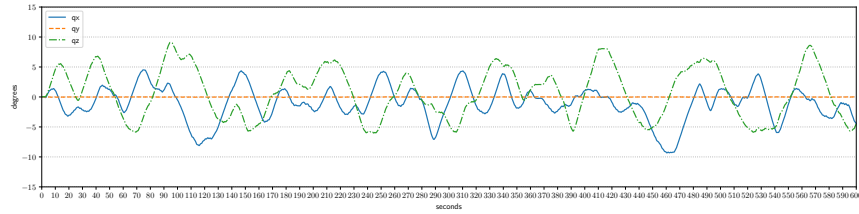
The next step after looking at raw data, gathered for machine learning, is a data exploration. The goal of this initial step is, firstly, a data visualization for understanding of dataset characterizations. As already stated in section 3.1.1, a user position (x, y, z) , orientation in quaternion (qx, qy, qz, qw) and the world-space speed of the camera for each direction in (x, y, z) was obtained from Main Camera in Unity application launched on HMD.



(a) Dataset 1556



(b) Dataset 1623



(c) Dataset 1703

Figure 5: User position plots from obtained datasets (a, b, c)

First, let's start with the analysis of user position data. The figures 5a, 5b, 5c show dataset named 1556, 1623 and 1703 correspondently. As a matter of fact, plotted dataset were already interpolated on the preprocessing step. Although interpolation was done before data exploration, the details about interpolation can be found in section 3.1.3. The names of datasets means only a *timestamp* in form *HH : MM* when a dataset was obtained from HMD in laboratory space. Thus the unique name of *csv*-files on HMD system was guaranteed for the day of experiment. In this thesis the names will be used to identify each of all three datasets. Fig. 5 shows only 3 chosen datasets from those obtained in laboratory space. All datasets indicates the

same behaviour of VR users with HMD looking on the VV projected in VR space as was found out in works [12, 25]. The MAE and RMSE metric results are tend to be similar for every dataset during training and testing.

All traces were recorded over 10 minutes long on average 12 minutes. All traces were then shortened to a precise length of 10 minutes to ensure equal data length for the purpose of visualization and analysis. The observations based on the sample traces can be made similar as it done by *Gül et al., 2020* in their work [12]. The user rarely moves along the y-axis. The y-axis shows the vertical movement that the users could make if they sit down or stand up. Based on the data obtained, users walked around a volumetric object in virtual reality and did not make particularly noticeable and prolonged attempts to examine the object at the lower point of the projection on a laboratory's floor since vertical movement requires more effort to crouch down and stand up. The laboratory space where the dataset was obtained was not cluttered with furniture thus users could walk around the volumetric object projected into their HMD. The figure 6 shows an enlarged y-axis in the range from 400ms to 500ms and thus proves there is no significant change in the vertical position of the user.

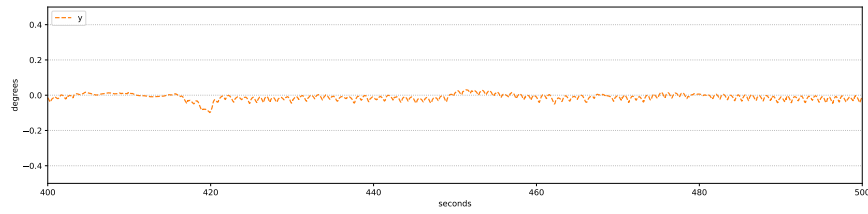


Figure 6: Changes in the user's position along the Y axis in the range from 400ms to 500ms

3.1.3 Data preprocessing

As was mentioned in section ??, the raw sensor data obtained from the HoloLens was unevenly sampled at 60 Hz and had different temporal distances between consecutive samples. *Gül et al., 2020* obtained the similar raw dataset from same HMD and interpolated it to obtain temporally equidistant samples. Same as it was done in work [12], the position and velocity data were upsampled using linear interpolation and for quaternions SLEP was used. During preprocessing step Euler angles (yaw, pitch, roll) were calculated from quaternions and these parameters are used for visualization purposes. Although the interpolated *csv*-file contains additional Euler angles columns, only described in section ?? parameters were used for training and prediction. The table 3.2 lists first 20 rows for columns *timestamp* and position (x, y, z) from interpolated dataset. This interpolated dataset is created with linear interpolation and SLEP mathematical methods from raw dataset shown in table 3.1.

timestamp	x	y	z
0.0	0.004954389	0.003402365	0.01010712
5000000.0	0.004833102666666667	0.003308499666666667	0.010506206666666667
10000000.0	0.004711816333333333	0.003214634333333332	0.010905293333333333
15000000.0	0.00459053	0.003120769	0.01130438
20000000.0	0.004485576166666666	0.003099052833333333	0.011548609999999999
25000000.0	0.004380622333333333	0.003077336666666667	0.011792839999999999
30000000.0	0.0042756685	0.0030556205	0.01203707
35000000.0	0.004170714666666667	0.003033904333333333	0.0122813
40000000.0	0.004065760833333334	0.003012188166666667	0.01252553
45000000.0	0.003960807	0.002990472	0.01276976
50000000.0	0.00390328375	0.00300229975	0.0128401975
55000000.0	0.0038457605	0.0030141275	0.012910635
60000000.0	0.00378823725	0.00302595525	0.0129810725
65000000.0	0.003730714	0.003037783	0.01305151
70000000.0	0.003651043833333334	0.003112986333333335	0.01315696
75000000.0	0.003571373666666667	0.003188189666666667	0.01326241
80000000.0	0.0034917035000000003	0.003263393	0.01336786
85000000.0	0.003412033333333332	0.003338596333333333	0.01347331
90000000.0	0.003332363166666667	0.003413799666666667	0.01357876
95000000.0	0.003252693	0.003489003	0.01368421

Table 3.2: Interpolated data from HoloLens 2

After the interpolated dataset was plotted as figure 7, the important observations based on the sample trace could be done. While the user position data plots look appropriate for machine learning algorithms, the two graphs with orientation show data that is not the perfect case for usage with machine learning technologies and could decrease the prediction rate. The real part qw and the component qy of quaternion and yaw of Euler angles have obviously discontinuous (sharp change of sign) making it hard for a predictor to learn. A orientation on quaternions is used in training, thus this data requires a few additionally preprocessing steps. Usually, when doing calculation with quaternions, quaternions must be normalized to a unit length in order to represent valid rotations [22]. The normalized quaternion can be calculated using formula:

$$U_g = \frac{q}{||q||} = \frac{w}{||q||} + i \cdot \frac{x}{||q||} + j \cdot \frac{y}{||q||} + k \cdot \frac{z}{||q||} \quad (3.1)$$

where $||q||$ is a magnitude and can be found with formula:

$$||q|| = \sqrt{w^2 + x^2 + y^2 + z^2} \quad (3.2)$$

During experiments with quaternions in dataset obtained from HoloLens was found that quaternion magnitudes $||q||$ in HoloLens dataset are equal to 1. Thus data came from HMD already normalized, so that a quaternion in dataset kept the same orientation as it was during user's movement but its magnitude is 1.0.

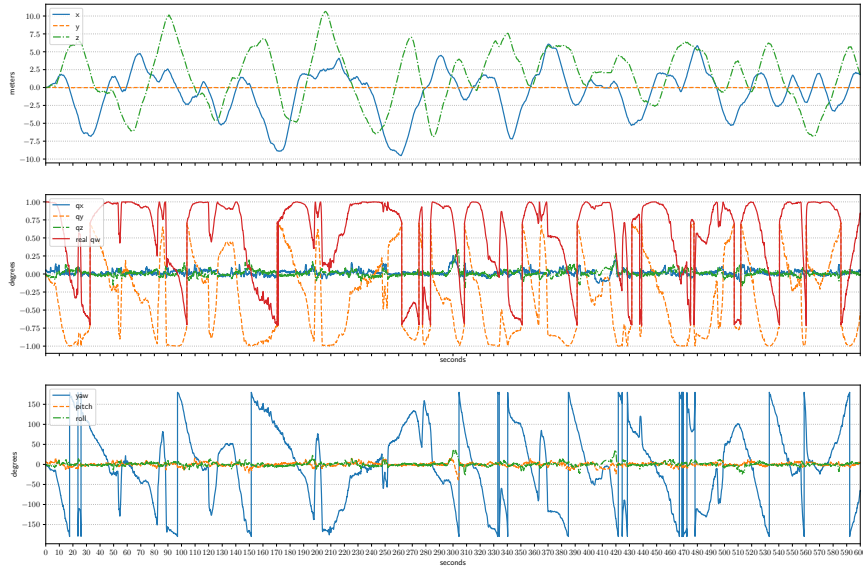


Figure 7: Interpolated 6-DoF dataset's user position and orientation in quaternions and Euler angles.

Next, quaternions between neighboring points in obtained dataset represent the very similar orientation made by user wearing HMD step by step. The middle plot on figure 8 has discontinuities that can be seen on qw line. As a consequence of the discontinuity (sharp change of line from negative to positive area with the same amplitude) the two neighboring quaternions with similar rotation have significant 4D vector space between them. It makes prediction worse what can be proved by RMSE and MSE rotation metrics. Flipping the sign will not affect the rotation, but it will ensure that there are no large jumps in 4D vector space when the rotation difference in rotation space ($SO(3)$) is small. If negative component of quaternions will be flipped into positive then the dataset representing same rotation without creating an artificial discontinuity in the space will be available for model training.

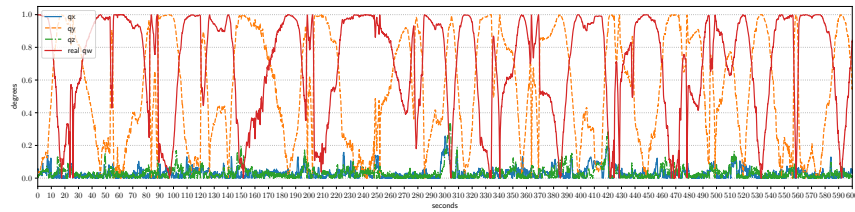


Figure 8: Quaternions from 6-DoF dataset's flipped if their real part is negative

Thus after normalization step, the two representations of quaternions are blended into one data set, omitting to discontinuities in the time series as can be seen

presented on Figure 8. Indeed, the RMSE and MSE rotation metrics were improved when model was trained with dataset with quaternions without sharp sign changes. More information can be found in sections ?? and ?. The figure 9 represents quaternions of the original interpolated dataset on the upper part of the plot and the normalized flipped quaternions on the lower part of the plot. The quaternion's components were flipped only if the if their real part became negative. Different to figure 8 the limit of y-axis is set to $[-1, 1]$ on figure 9 so that the result of inverting of quaternion is easy to compare to original data. Figure 8 shows plotted data with length of 20 seconds in range 162 - 182 s from both datasets.

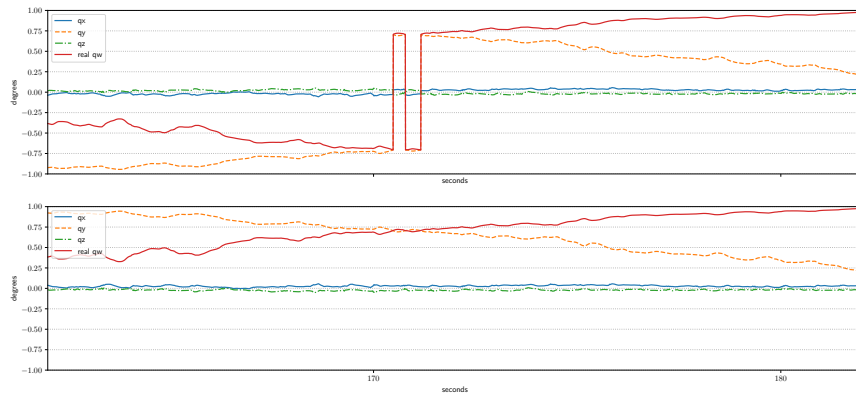


Figure 9: Quaternions from 6-DoF dataset's flipped if their real part is negative

3.2 Model

3.2.1 Model inputs

3.2.2 Architecture

Analysis done by *Qian et al., 2016* indicates that at least in the short term, viewers' head movement can be predicted with accuracy $> 90\%$ by even using simple methods such as linear regression [18]. However in the longer term it is more difficult to achieve the good result and the average accuracy drops to about 70% [18]. !!!!!

Researchers used Adam optimization algorithm, the maximum number of epochs was set to 1000, early stopping technique (patience = 2, min. delta = 0) was used to avoid overfitting. Additionally, the learning rate was decreased by 70% from initial value of 0.001 every 30 epochs. The batch size B was set to 2^{11} . Rectified Linear Unit (ReLU) as activation function for the FFN layers used with LSTM

!!! Recurrent neural networks have recently shown promising results in many machine learning tasks, especially when input and/or output are of variable length and are coming as time series with a sequential order. Unfortunately, the known problem of RNN that was observed many years ago by e.g., *Bengio et al., 1994* that it is difficult to train RNNs to capture long-term dependencies because the gradients tend to either vanish (most of the time) or explode (rarely, but with severe effects) [5]. New approaches are needed to be implemented to reduce the negative impacts of this issue. Since traditional recurrent unit overwrites its content at each time-step, a LSTM unit is able to decide whether to keep the existing memory via the introduced gates. The Long Short-Term Memory (LSTM) has a number of minor modifications [8] since it was initially proposed in work [14]. Another approach called a gated recurrent unit (GRU) can adaptively capture dependencies of different time scales without having a separate memory cells [8]. These two approaches can help to find the long-term dependencies in the data obtained from HMD that are otherwise are hidden by the effect of short-term dependencies from the standard RNN models.

LSTM Model

GRU Model

Bidirectional GRU Model

3.2.3 Development

This section presents the developments of the Unity application for obtaining the dataset and development of LSTM and GRU models with Python and PyTorch.

Unity application

An application was developed in Unity with the Mixed Reality Toolkit and deployed on HoloLens 2. The goal of the application is to obtain the user position and orientation during the time a user wears a HMD. As this research aims to find an approach to reduce the M2P latency during rendering and delivering the volumetric content to end-user device, the volumetric animated object was placed three meters ahead of the user in Unity application. Users wearing HMD thus were asked to look on animated volumetric object and to move freely inside the laboratory space. In Unity, the Main Camera is always the primary stereo rendering component

attached to HMD and it is rendering everything the user sees ¹. The starting position of the user is set to (0, 0, 0) during the application launch and the Main Camera tracks movement of the user's head. Although HoloLens allows to build a world-scale application, the room-scale experience was selected for spatial coordinate system. This lets users to walk around within the 10-meter boundary what is quite enough for user's movements inside the laboratory space and simultaneously watching the volumetric video object.

User position and rotation data were logged in csv-file. This raw data has been converted into datasets on the preprocessing step and thus original interpolated dataset, the transformed with flipped negative quaternions and several normalised datasets were used in experiments during model development and hyperparameters search.

Training and evaluation

The LSTM and GRU models development and implementation are done using Python and PyTorch.

Hyperparameter search

The hyperparameters search is done using VCA GPU cluster which is installed with the SLURM resource manager/scheduler and Singularity container is used to containerize the application.

¹<https://docs.microsoft.com/en-us/windows/mixed-reality/develop/unity/camera-in-unity>

Evaluation

4.1 Baseline model

4.2 Goal of evaluation

The paper of *Chung et al., 2014* also provides an interesting comparison and evaluation of the performance of recurrent units LSTM and GRU on sequence modeling. Authors mentioned the ability of LSTM to keep the existing memory via the introduced gates and thus to detect an important feature from an input sequence at early stage, to easily carry this information (the existence of the feature) over a long distance, hence, capturing potential long-distance dependencies [8]. The GRU takes linear sum between the existing state and the newly computed state similar to the LSTM but does not have any mechanism to control the degree to which its state is exposed, but exposes the whole state each time [8]. *Chung et al., 2014* emphasize the fact that any important feature, decided by either the forget gate of the LSTM unit or the update gate of the GRU, will not be overwritten but be maintained as it is [8]. LSTM unit controls the amount of the new memory content and does not have any separate control of the amount of information flowing from the previous time step. The GRU differs and controls the information flow from the previous activation when computing the new and does not independently control the amount of the candidate activation being added via update gate [8].

4.3 Evaluation metrics

4.4 Experiments

4.4.1 First experiments

Datasets

As already stated in section ??

Batch size

A high impact on the performance e.g. the prediction accuracy has a batch size used in LSTM or GRU Model. The batch-size helps to learn the common patterns as important features by providing a fixed number of samples at one time. So that the model thus can distinguish the common features by looking at all the introduced samples of the batch. In most cases, an optimal batch size is set to 64. When this batch size was initially used with LSTM model, it gave significant high MSE, RMSE, train and validation errors. Based on the performance observation during experiments with LSTM parameters, batch size fine-tuning was done. The experiments done by *Aykut et al* in their works [3] and [4] proved that appropriate batch size can be found in range $2^9 - 2^{11}$ (512 - 2048). Notice that a power of 2 is used as a batch size. The overall idea is to fit a batch of samples entirely in the the CPU/GPU. Since, all the CPU/GPU comes with a storage capacity in power of two, it is advised to keep a batch size a power of two. Using a number different from a power of 2 could lead to poor performance.

Learning rate

4.4.2 Prediction with LSTM

4.4.3 Prediction with GRU

4.4.4 Prediction with Bidirectional GRU

Conclusion

The Python application *UserPrediction6DOF* is a result of this work and can be used for future preprocessing of the new obtained datasets, training routine and prediction of user position and rotation in 6-DoF virtual environment.

5.1 Analysis

5.2 Limitations

5.3 Suggestions for future work

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