

# Safe Summer Stats Workshop 2020

The era of bad stuff, but also free virtual meetings.

Visit Erin Nishimura's lab at: [onishlab.colostate.edu](http://onishlab.colostate.edu)

Writing workshop – July 16th

Science communication workshop – August 6<sup>th</sup>

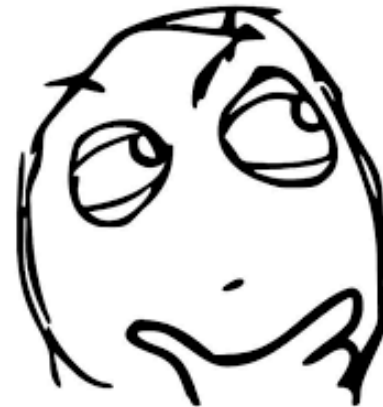
Show and Tell Style. Informal! Ask questions! Discuss!

Program:

1. Mikaela Elder – Regression
2. Rob Williams – Permutation Test
3. Adeline Williams – Chi-square
4. Adeline and David King – Equivalence Testing
5. Ben Prytherch – Effect Size and Power Analysis

# Equivalence testing: Statistical test for NO difference

We learned how to do this in  
undergrad stats.... right?

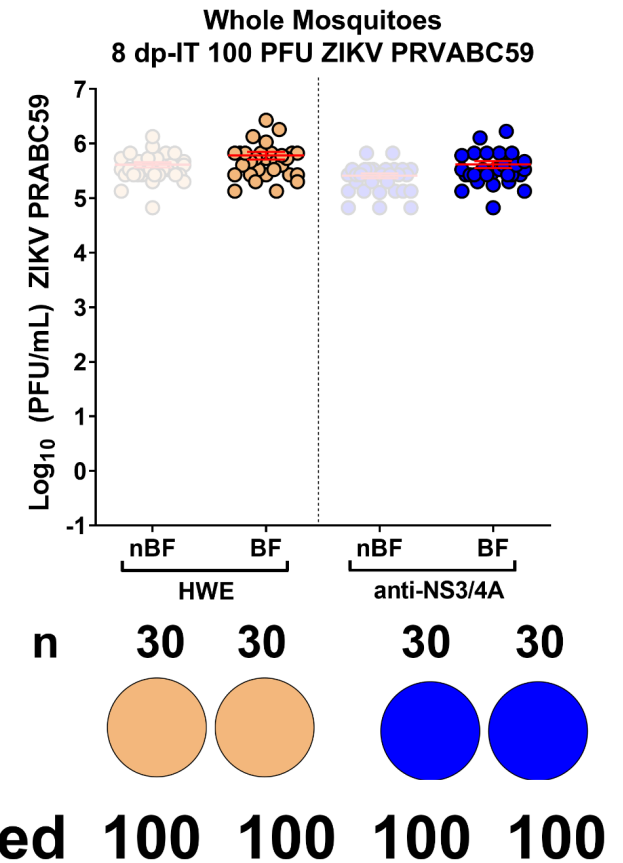
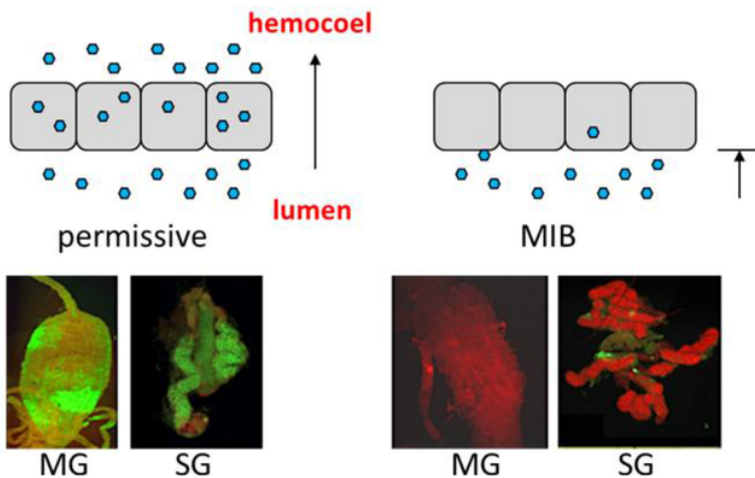


Lakens, Daniël, et al. *"Equivalence Testing for Psychological Research: A Tutorial."*  
Advances in Methods and Practices in Psychological Science, vol. 1, no. 2, 2018  
(not really a tutorial)

Statistical test	Null hypothesis ( $H_0$ )	p-value	p-value < 0.05	p-value > .05
Two-sample t-test	No difference between the <b>means of the samples</b>	Probability of seeing observed $\Delta$ (or greater) if $H_0$ is true	Reject $H_0$ . Support $H_a$ : <b>means</b> are unequal.	Fail To Reject $H_0$

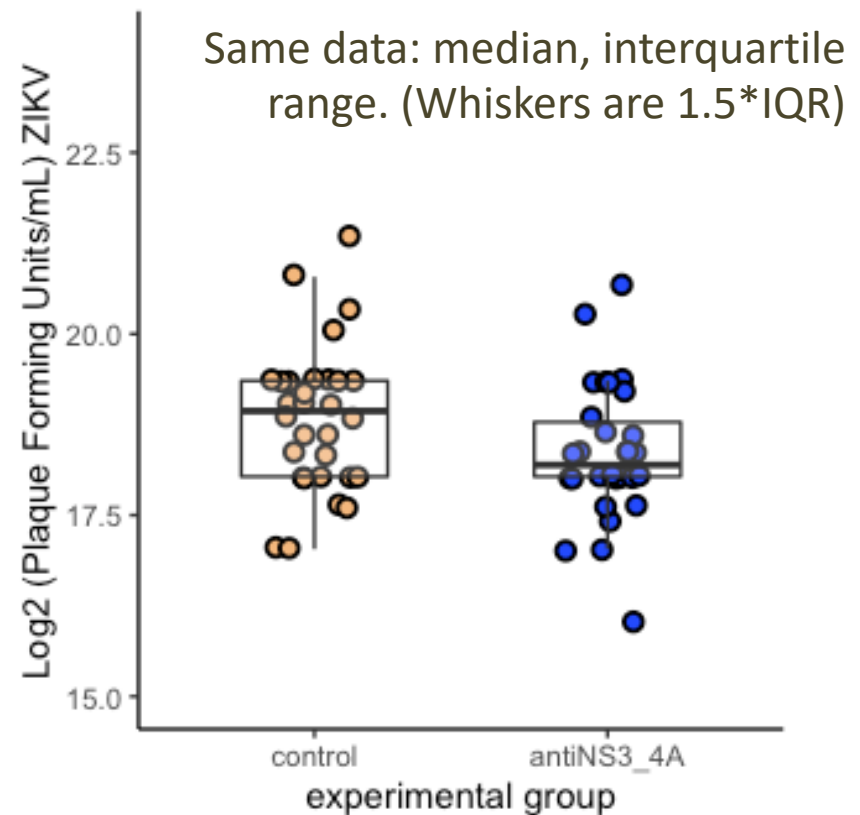
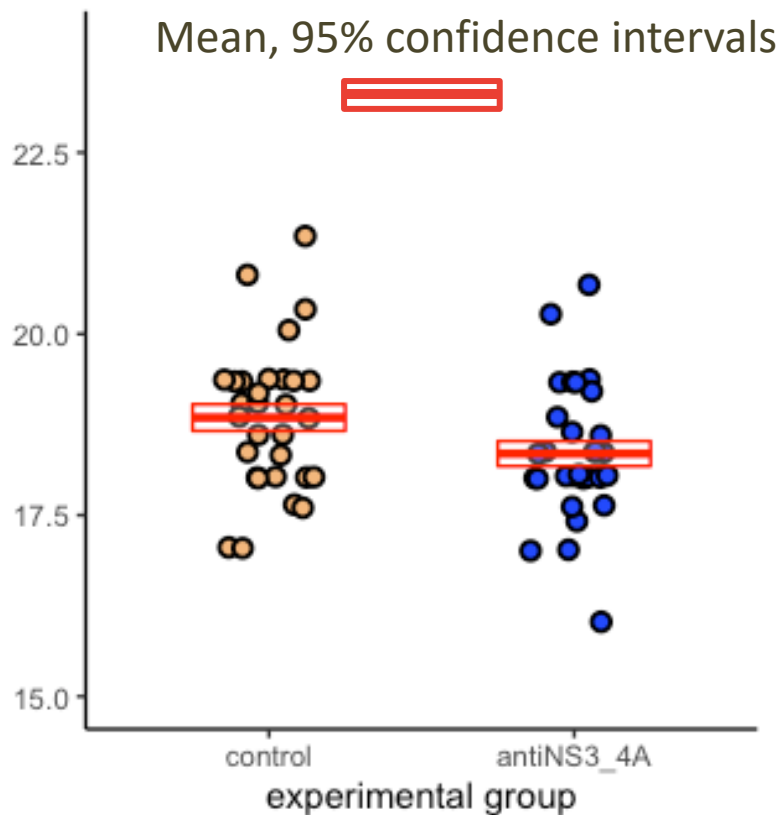
- How do we test the inverse? that the means are *not different*?
- Can't we just use a high p-value to *accept*  $H_0$ ? No? Why the H naught?
- What if  $p(H_a)$  is also high? We're only describing  $p(H_0)$
- Other methods compare probabilities, i.e.,  $p(H_1)/p(H_2)$  to see which is higher; Bayesian modeling, mixture models...
- How do we test, and get a p-value, for two things being equal?
- Example from Adeline's data.

# Anti-NS3/4A are resistant to ZIKV due to midgut infection barrier (MIB)

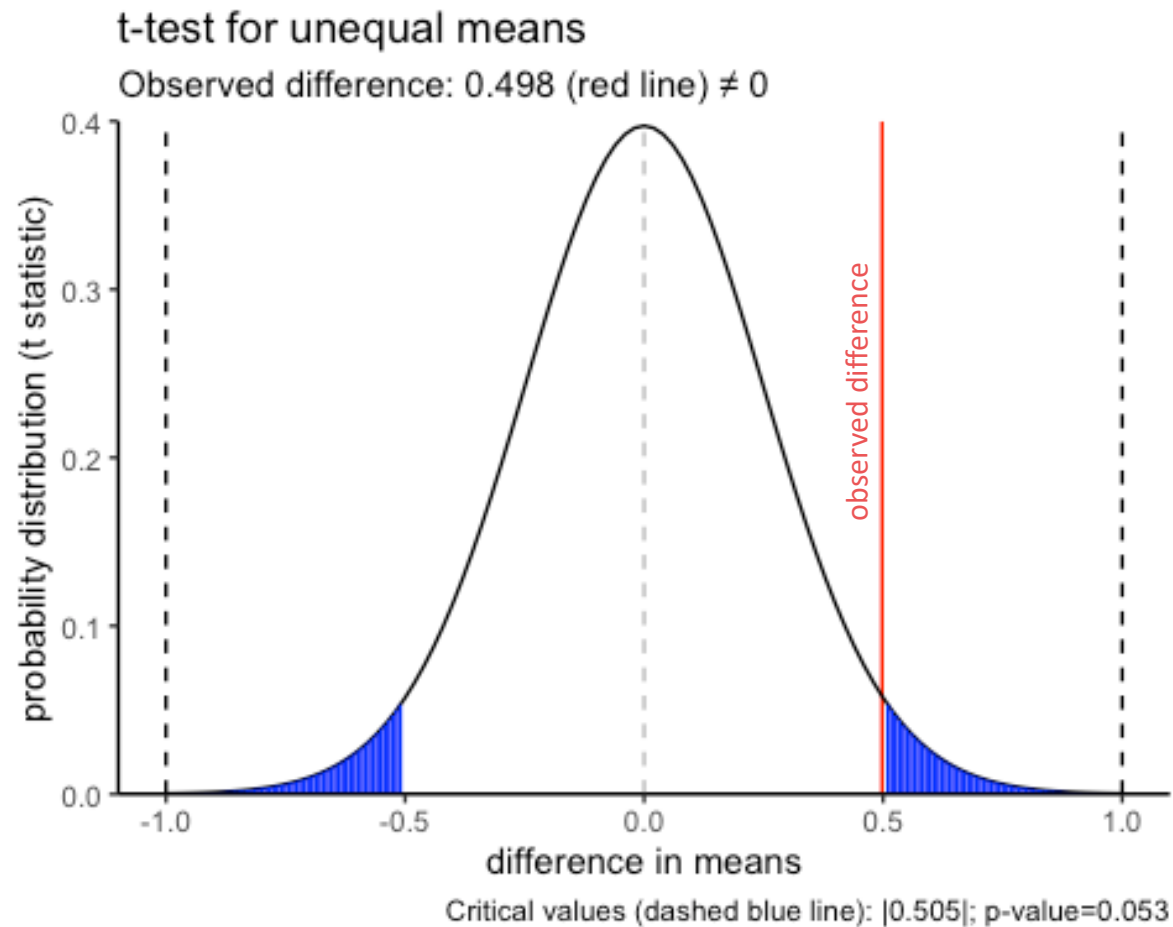


# Zooming in on the data: is there a difference between antiNS3/4A and the control?

Viral titre in infected mosquitos



# T-test (unequal means)



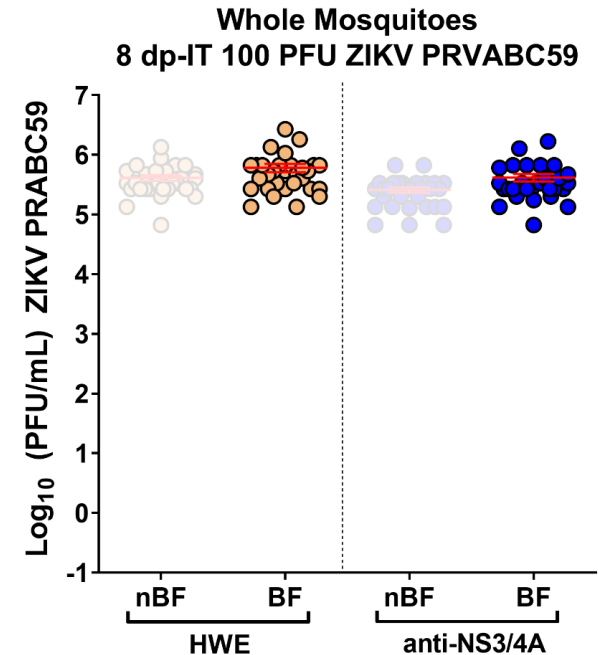
# Define an equivalence boundary

Question: When you present this to your peers, how far apart do they need to be before you say they are different?

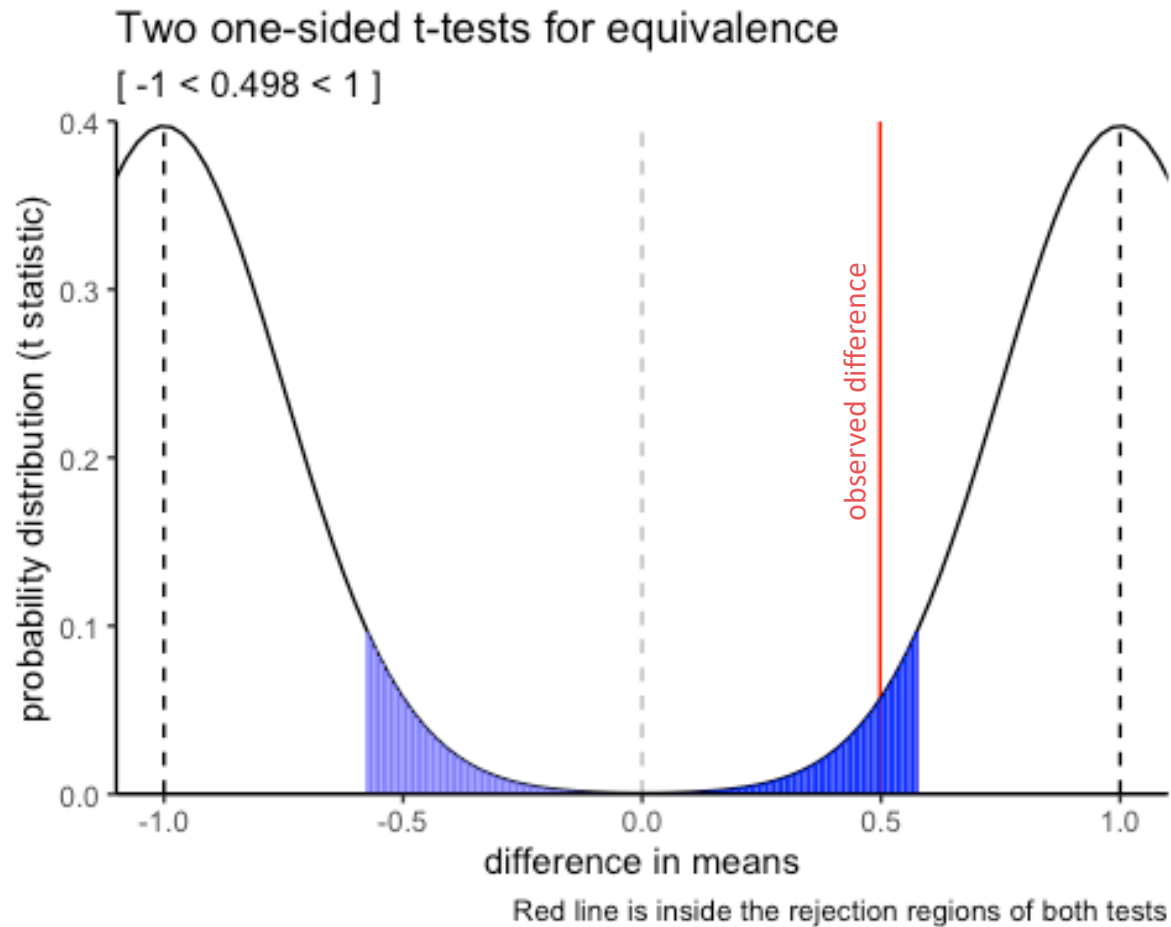
Answer: A 2-fold difference

Equivalence bounds:  $\pm 1$  in  $\log_2$  space.

We'll discuss different choices for this at the end.



# Equivalence test: Two One-Sided Tests (TOST).



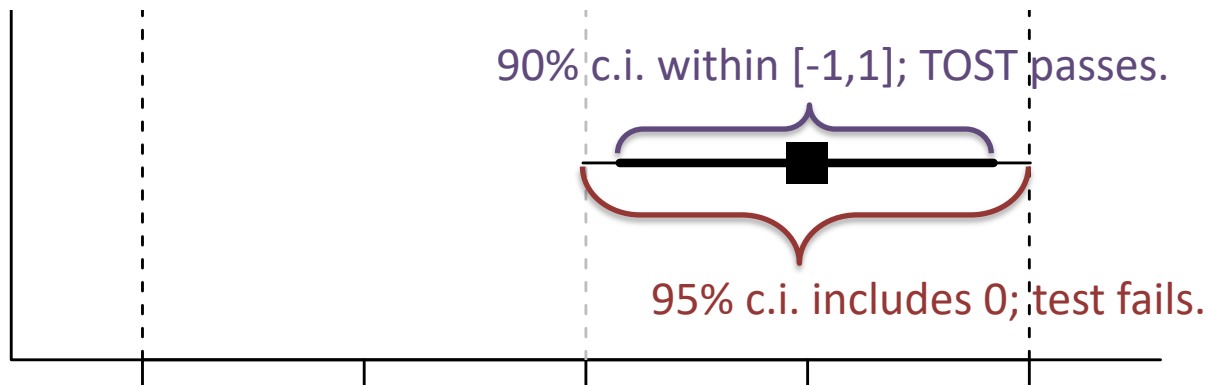




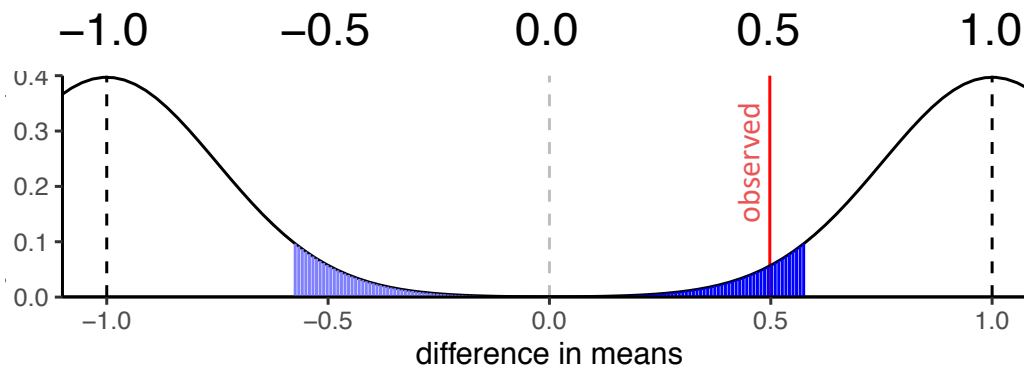
Confused about the switch from 90% confidence intervals to conclusions with 95% certainty? Good. That means you are paying attention. It **is** confusing!

Help doc from Prism/GraphPad

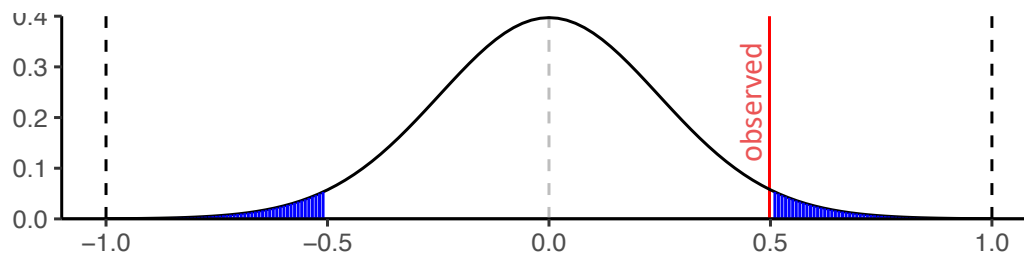
TOSTER package (R)  
output:  
confidence intervals



Two one-sided t-  
test distributions



Original two-sided  
t-test against 0:  
distribution



```

## TOST results:
## t-value lower bound: 5.94      p-value lower bound: 0.00000009
## t-value upper bound: -1.99    p-value upper bound: 0.026
## degrees of freedom : 57.8
##
## Equivalence bounds (raw scores):
## low eqbound: -1
## high eqbound: 1
##
## TOST confidence interval:
## lower bound 90% CI: 0.076
## upper bound 90% CI: 0.919
##
## NHST confidence interval:
## lower bound 95% CI: -0.007
## upper bound 95% CI: 1.002
##
## Equivalence Test Result:
## The equivalence test was significant,  $t(57.8) = -1.992$ ,  $p = 0.0255$ ,
given equivalence bounds of -1.000 and 1.000 (on a raw scale) and an
alpha of 0.05.
##
## Null Hypothesis Test Result:
## The null hypothesis test was non-significant,  $t(57.8) = 1.975$ ,  $p =$ 
0.053, given an alpha of 0.05.
##
## Based on the equivalence test and the null-hypothesis test combined,
we can conclude that the observed effect is statistically not different
from zero and statistically equivalent to zero.

```

# Possible outcomes

## t-test

TOST

	t-test for difference Reject null	t-test for difference Fail to Reject null
Two one-sided tests: both tests reject null	Different, but within equivalence bounds.	Equivalent (what we saw).
Two one-sided tests either test Fails To Reject	Different and exceeding equivalence bounds.	Inconclusive.

# Choice of smallest effect size of interest (SESOI)

Tutorial (Lakens et al., 2018) discussion.

## **Just-noticeable difference. Burriss et al., 2015:**

Research question: Do ovulating women signal men by becoming more flush in the face?

- NIH funded research?
- Maybelline?

Just-noticeable difference = min.  $\Delta$  in face redness perceptible by men.

Authors' conclusions: women do become more flush, but not enough to be discernable by the naked eye. (Maybelline cancels rouge ad project)

## **Statistical Power, no laughing matter**

- What **effect size** can we detect at  $\alpha=.05$ , sample size  $n$ , power=.8?
- **Effect size** in units of *Cohen's d*.
- Run TOST using **effect size**, rather than raw value.

**Inform your choice from prior research.**

# One more thing

- I will forever look at the 95% confidence interval as the TOST equivalence boundary at  $\alpha = .025$
- Predefining an equivalence bound *a priori* is a specific test of a hypothesis. A succinct framing of the question.
- TOSTER has functions for:
  - one-sample t-test
  - two-sample t-test
  - proportion test
  - correlation (r)