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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of MakeNoise over scalars for ConstantTimeGeometric in mod.rs at commit f5bb719 (outdated<sup>1</sup>).

The intuition of this implementation is that a vector-valued mechanism can be used to privatize a scalarvalued input, by transforming the input into a singleton vector, applying the vector mechanism, and then unpacking the resulting singleton vector.

## 1 Hoare Triple

### Precondition

#### Compiler-Verified

MakeNoise is parameterized as follows:

- DI is of type AtomDomain<T>
- MI is of type AbsoluteDistance<T>
- MO implements trait Measure

The following trait bounds are also required:

- Generic T implements trait Integer
- Generic MO implements trait Measure
- Type usize implements trait ExactIntCast<T>
- Type RBig implements trait TryFrom<T>
- Type ZExpFamily<1> implements trait NoisePrivacyMap<L1Distance<RBig>, MO>. This bound requires that it must be possible to construct a privacy map for the combination of ZExpFamily<1> noise distribution, distance type and privacy measure. Since the ConstantTimeGeometric distribution is equivalent to ZExpFamily<1>, maps built for ZExpFamily<1> can be used for ConstantTimeGeometric.

#### **User-Verified**

None

 $<sup>^1\</sup>mathrm{See}$  new changes with git diff f5bb719..e47cc07 rust/src/measurements/noise/distribution/geometric/mod.rs

### Pseudocode

#### Postcondition

Theorem 1.1. For every setting of the input parameters (self, input\_space, T, MO) to make\_noise such that the given preconditions hold, make\_noise raises an error (at compile time or run time) or returns a valid measurement. A valid measurement has the following properties:

- 1. (Data-independent runtime errors). For every pair of members x and x' in input\_domain, invoke(x) and invoke(x') either both return the same error or neither return an error.
- 2. (Privacy guarantee). For every pair of members x and x' in input\_domain and for every pair (d\_in,d\_out), where d\_in has the associated type for input\_metric and d\_out has the associated type for

output\_measure, if x, x' are d\_in-close under input\_metric, privacy\_map(d\_in) does not raise an error, and privacy\_map(d\_in) = d\_out, then function(x), function(x') are d\_out-close under output\_measure.

*Proof.* Neither constructor make\_vec nor MakeNoise.make\_noise have manual preconditions, and the post-conditions guarantee a valid transformation and valid measurement, respectively. then\_index\_or\_default also does not have preconditions, and its postcondition guarantees that it returns a valid postprocessor.

The chain of a valid transformation, valid measurement and valid postprocessor is a valid measurement.

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