fn check_candidates

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of check_candidates in mod.rs at commit f5bb719 (outdated¹). check_candidates raises an error if the discrete quantile candidate set is invalid.

1 Hoare Triple

Precondition

None

Function

```
def validate_candidates(candidates: list[T]):
    if not candidates: #
        raise ValueError("candidates must not be empty")

i1 = iter(candidates)
    i2 = iter(candidates)
    next(i1)

for c1, c2 in zip(i1, i2): #
    cmp = c1.partial_cmp(c2)
    if cmp is None or cmp != Ordering.Less:
        raise ValueError("candidates must be non-null and strictly increasing")
```

Postcondition

Theorem 1.1. Candidates must be:

- 1. non-empty
- 2. strictly increasing
- 3. totally ordered

Otherwise the function errors.

Proof. The postconditions can be directly checked:

- 1. candidates is non-empty, by the check on line 2
- 2. candidates is strictly increasing, because there is no window where the left candidate is not less than the right candidate

¹See new changes with git diff f5bb719..08d9c49 rust/src/transformations/quantile_score_candidates/mod.rs

| Therefore the postcondition holds. | Ш |
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3. candidates is totally ordered, because no comparisons may fail