## fn x\_mul\_2k

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of x\_mul\_2k in mod.rs at commit f5bb719 (outdated1).

# 1 Hoare Triple

#### Precondition

Compiler-Verified

None

**User-Verified** 

 $k \neq \texttt{i32.MIN}$ 

#### Pseudocode

```
def x_mul_2k(x: RBig, k: i32) -> RBig:
    num, den = x.into_parts() #
    if k < 0:
        den <<= cast(-k, usize)
    else:
        num <<= cast(k, usize)

return RBig.from_parts(num, den)</pre>
```

## Postcondition

**Theorem 1.1.** Return  $x \cdot 2^k$ .

*Proof.* Since x is a fraction, line 2 splits x into its numerator and denominator. Consider two cases:

- If k < 0, then multiplying the denominator by  $2^-k$  is equivalent to multiplying by  $2^k$ . Since k is negative, then -k is positive, meaning the cast to usize is valid. Shifting -k zeros to the left is equivalent to multiplying the denominator by  $2^k$ . Negation of k is well-defined for all values of i32, except for i32.MIN, which is not allowed by the precondition. Therefore, the result is  $x \cdot 2^k$ .
- If  $k \ge 0$ , then we multiply the numerator by  $2^k$ . Since k is positive, the cast to usize is valid. Shifting k zeros to the left is equivalent to multipying the numerator by  $2^k$ . Therefore, the result is  $x \cdot 2^k$ .

In both cases, the result is  $x \cdot 2^k$ .

<sup>&</sup>lt;sup>1</sup>See new changes with git diff f5bb719..303d3a1 rust/src/measurements/noise/nature/float/utilities/mod.rs