

# fn make\_privacy\_filter

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This proof resides in “**contrib**” because it has not completed the vetting process.

Proves soundness of `fn make_privacy_filter`.

## 1 Hoare Triple

### Precondition

#### Compiler-verified

- Argument `odometer` of type `Odometer<DI, MI, MO, Q, A>`.
- Argument `d_out` of type `MO_Distance`, the associated distance type of `MO`.
- Generic `DI` implements `Domain`.
- Generic `MI` implements `Metric`.
- Generic `MO` implements `FilterMeasure`.
- `MI_Distance` implements `ProductOrd`.
- `MO_Distance` implements `ProductOrd`.
- `(DI, MI)` implements `MetricSpace`.

#### User-verified

### Pseudocode

```
1 def make_privacy_filter(  
2     odometer: Odometer[DI, MI, MO, Q, A],  
3     d_out: MO_Distance,  
4 ) -> Measurement[DI, OdometerQueryable[MI, MO, Q, A], MI, MO]:  
5     odo_function = odometer.function  
6     d_in = odometer.d_in  
7  
8     def function(arg: DI_Carrier) -> OdometerQueryable[MI, MO, Q, A]:  
9         #  
10        continuation_rule = new_continuation_rule(d_out, MO)  
11        return wrap(continuation_rule, lambda: odo_function.eval(arg)) #  
12  
13    def privacy_map(d_in_p: MI_Distance) -> MO_Distance:  
14        if d_in_p.total_gt(d_in):  
15            raise "input distance must not be greater than d_in"  
16  
17        return d_out  
18
```

```

19     return Measurement.new(
20         odometer.input_domain,
21         Function.new_interactive(function),
22         odometer.input_metric,
23         odometer.output_measure,
24         PrivacyMap.new_fallible(privacy_map),
25     )

```

## Postcondition

For every setting of the input parameters (`odometer`, `d_out`, `DI`, `MI`, `MO`, `Q`, `A`) to `make_privacy_filter` such that the given preconditions hold, `make_privacy_filter` raises an exception (at compile time or run time) or returns a valid odometer. A valid odometer has the following properties:

1. (Data-independent exceptions). For every pair of elements  $x, x'$  in `input_domain`, `function(x)` and `function(x')` either both raise an exception, or neither raise an exception.
2. (Wrapping guarantee). Interactive measurement queryables spawned while evaluating external queries are wrapped by the wrapper function accompanying the external query.
3. (Valid odometer queryable). For every element  $x$  in `input_domain`, where `function(x)` does not raise an exception, `function(x)` returns a valid odometer queryable.

*Proof of data-independent errors.* `Function.eval` on line 11 has data-independent exceptions, because the function is from `odometer`, which is a valid odometer. Since this is the only location where an exception can be raised, the data-independent errors property holds.  $\square$

*Proof of wrapping guarantee.* `wrap` on line 11 guarantees to wrap all spawned IM queryables with the provided wrapper, satisfying the wrapping guarantee.  $\square$

*Proof of privacy guarantee.* By the definition of a valid odometer queryable, and by the definition of `FilterMeasure`, the output of `make_privacy_filter` upholds the privacy guarantee.  $\square$