CompositionMeasure for ZeroConcentratedDivergence

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of CompositionMeasure for ZeroConcentratedDivergence in mod.rs at commit f5bb719 (outdated1).

1 Hoare Triple

Precondition

Compiler-Verified

Types matching pseudocode.

Caller-Verified

None

Pseudocode

```
class CompositionMeasure(ZeroConcentratedDivergence):
      def composability( #
          self, adaptivity: Adaptivity
      ) -> Composability:
          match adaptivity:
              case Adaptivity.FullyAdaptive:
                  return Composability. Sequential
                  return Composability.Concurrent
11
      def compose(self, d_mids: Vec[Self_Distance]) -> Self_Distance:
          d_out = 0.0
12
          for d_mid in d_mids:
              d_out = d_out.inf_add(d_mid)
14
          return d_out
```

Postcondition

Theorem 1.1. composability returns Ok(out) if the composition of a vector of privacy parameters d_mids is bounded above by self.compose(d_mids) under adaptivity adaptivity and out-composability. Otherwise returns an error.

Proof. By the postcondition of InfAdd we have that $\sum_i d_{mids_i} \leq compose(d_{mids})$.

¹See new changes with git diff f5bb719..d47ae9ad rust/src/combinators/sequential_composition/mod.rs

Adaptivity	Sequential	Concurrent
Non-Adaptive	Lemma 1.7[BS16]	Corollary 1[Lyu22]
Adaptive	Lemma 1.7[BS16]	Corollary 1[Lyu22]
Fully-Adaptive	Remark 4.4[FZ22]	None

This table is reflected in the implementation of composability on line 2.

References

[BS16] Mark Bun and Thomas Steinke. Concentrated differential privacy: Simplifications, extensions, and lower bounds, 2016.

[FZ22] Vitaly Feldman and Tijana Zrnic. Individual privacy accounting via a renyi filter, 2022.

[Lyu22] Xin Lyu. Composition theorems for interactive differential privacy, 2022.