# CompositionMeasure for MaxDivergence

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of CompositionMeasure for MaxDivergence in mod.rs at commit f5bb719 (outdated1).

## 1 Hoare Triple

### Precondition

#### Compiler-Verified

Types matching pseudocode.

#### Caller-Verified

None

#### Pseudocode

#### Postcondition

Theorem 1.1. composability returns Ok(out) if the composition of a vector of privacy parameters d\_mids is bounded above by self.compose(d\_mids) under adaptivity adaptivity and out-composability. Otherwise returns an error.

*Proof.* By the postcondition of InfAdd we have that  $\sum_i d_{mids_i} \leq compose(d_{mids})$ .

Adaptivity	Sequential	Concurrent
Non-Adaptive	Theorem 1[DMNS06]	Theorem 1.8[VW21]
Adaptive	Theorem 1[DMNS06]	Theorem $1.8[VW21]$
Fully-Adaptive	None	None

<sup>&</sup>lt;sup>1</sup>See new changes with git diff f5bb719..556f302 rust/src/combinators/sequential\_composition/mod.rs

This table is reflected in the implementation of composability on line 2.

## References

[DMNS06] Cynthia Dwork, Frank McSherry, Kobbi Nissim, and Adam Smith. Calibrating noise to sensitivity in private data analysis. In Shai Halevi and Tal Rabin, editors, *Theory of Cryptography*, pages 265–284, Berlin, Heidelberg, 2006. Springer Berlin Heidelberg.

[VW21] Salil Vadhan and Tianhao Wang. Concurrent composition of differential privacy, 2021.