CompositionMeasure for RenyiDivergence

Michael Shoemate

This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of CompositionMeasure for RenyiDivergence in mod.rs at commit f5bb719 (outdated¹).

1 Hoare Triple

Precondition

Compiler-Verified

Types matching pseudocode.

Caller-Verified

None

Pseudocode

```
class CompositionMeasure(RenyiDivergence):
      def composability( #
          self, adaptivity: Adaptivity
      ) -> Composability:
          return Composability.Concurrent
      def compose(self, d_mids: Vec[Self_Distance]) -> Self_Distance:
          def curve(alpha: float) -> float: #
              epsilons = [d_mid(alpha) for d_mid in d_mids]
              d_out = 0.0
11
              for d_mid in epsilons:
12
                  d_out = d_out.inf_add(d_mid)
              return d_out
14
15
          return Function.new_fallible(curve)
```

Postcondition

Theorem 1.1. composability returns Ok(out) if the composition of a vector of privacy parameters d_mids is bounded above by self.compose(d_mids) under adaptivity adaptivity and out-composability. Otherwise returns an error.

Proof. The new curve constructed on line 8 composes all epsilon parameters at a given fixed alpha. By the postcondition of InfAdd we have that for any choice of alpha, $\sum_i d_{mid_i}(alpha) \leq compose(d_{mids})(\alpha)$.

 $^{^1\}mathrm{See}$ new changes with git diff f5bb719..556f302 rust/src/combinators/sequential_composition/mod.rs

| | Adaptivity | Sequential | Concurrent |
|--------------|--------------------|-----------------------|-----------------------------|
| | Non-Adaptive | Proposition 1[Mir17] | Theorem 2[Lyu22] |
| | Adaptive | - | - |
| | Fully-Adaptive | Theorem $4.3[FZ22]$ | Theorem $1.22[VW21]$ |
| Γ his | table is reflected | in the implementation | of composability on line 2. |

References

- [FZ22] Vitaly Feldman and Tijana Zrnic. Individual privacy accounting via a renyi filter, 2022.
- [Lyu22] Xin Lyu. Composition theorems for interactive differential privacy, 2022.
- [Mir17] Ilya Mironov. Rényi differential privacy. In 2017 IEEE 30th Computer Security Foundations Symposium (CSF), page 263–275. IEEE, August 2017.
- [VW21] Salil Vadhan and Tianhao Wang. Concurrent composition of differential privacy, 2021.