

fn check_candidates

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This proof resides in “`contrib`” because it has not completed the vetting process.

Proves soundness of `check_candidates` in `mod.rs` at commit f5bb719 (outdated¹). `check_candidates` raises an error if the discrete quantile candidate set is invalid.

1 Hoare Triple

Precondition

None

Function

```
1 def validate_candidates(candidates: list[T]): 
2     if not candidates: #
3         raise ValueError("candidates must not be empty")
4
5     i1 = iter(candidates)
6     i2 = iter(candidates)
7     next(i1)
8
9     for c1, c2 in zip(i1, i2): #
10        cmp = c1.partial_cmp(c2)
11        if cmp is None or cmp != Ordering.Less:
12            raise ValueError("candidates must be non-null and strictly increasing")
```

Postcondition

Theorem 1.1. Candidates must be:

1. non-empty
2. strictly increasing
3. totally ordered

Otherwise the function errors.

Proof. The postconditions can be directly checked:

1. `candidates` is non-empty, by the check on line 2
2. `candidates` is strictly increasing, because there is no window where the left candidate is not less than the right candidate

¹See new changes with `git diff f5bb719..f99639a rust/src/transformations/quantile_score_candidates/mod.rs`

3. `candidates` is totally ordered, because no comparisons may fail

Therefore the postcondition holds. □