fn make_clamp

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of fn make_clamp in mod.rs at commit 0db9c6036 (outdated¹).

Vetting History

• Pull Request #512

1 Hoare Triple

Precondition

To ensure the correctness of the output, we require the following preconditions:

- Type TA must have trait ProductOrd.
- Type M must have trait DatasetMetric.

Pseudocode

```
def make_clamp(
      input_domain: VectorDomain[AtomDomain[TA]],
      input_metric: M,
      bounds: tuple[TA, TA]
  ): #
      input_domain.element_domain.assert_non_null() #
      # clone to make it explicit that we are not mutating the input domain
      output_row_domain = input_domain.element_domain.clone()
9
      output_row_domain.bounds = Bounds.new_closed(bounds)
10
11
      def clamper(value: TA) -> TA: #
          return value.total_clamp(bounds[0], bounds[1])
13
14
15
      return make_row_by_row_fallible( #
          input_domain,
16
17
          input_metric,
          output_row_domain,
18
          clamper
```

Postconditions

Theorem 1.1. For every setting of the input parameters (input_domain, input_metric, bounds) to make_clamp such that the given preconditions hold, make_clamp raises an exception (at compile time or run time) or returns a valid transformation. A valid transformation has the following properties:

¹See new changes with git diff 0db9c6036..380194c rust/src/transformations/clamp/mod.rs

- 1. (Appropriate output domain). For every element x in input_domain, function(x) is in output_domain or raises a data-independent runtime exception.
- 2. (Stability guarantee). For every pair of elements x, x' in input_domain and for every pair (d_in,d_out), where d_in has the associated type for input_metric and d_out has the associated type for output_metric, if x, x' are d_in-close under input_metric, stability_map(d_in) does not raise an exception, and stability_map(d_in) \leq d_out, then function(x), function(x') are d_out-close under output_metric.

2 Proof

Lemma 2.1. The invocation of make_row_by_row_fallible (line 15) satisfies its preconditions.

Proof. The preconditions of make_clamp and pseudocode definition (line 5) ensure that the type preconditions of make_row_by_row_fallible are satisfied. The remaining preconditions of make_row_by_row_fallible are:

- row_function has no side-effects.
- If the input to row_function is a member of input_domain's row domain, then the output is a member of output_row_domain.

The first precondition is satisfied by the definition of clamper (line 12) in the pseudocode.

For the second precondition, assume the input is a member of input_domain's row domain. Therefore, by 6, the input is non-null. In addition, since Bounds.new_closed did not raise an exception, then by the definition of Bounds.new_closed, the bounds are non-null. Thus, by the definition of ProductOrd, the preconditions of total_clamp are satisfied, so the output is within the bounds. Therefore, the output is a member of output_row_domain.

We now prove the postcondition of make_clamp.

Proof. By 2, the preconditions of make_row_by_row_fallible are satisfied. Thus, by the definition of make_row_by_row_fallible, the output is a valid transformation.