fn then_deintegerize_hashmap

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of then_deintegerize_hashmap in mod.rs at commit f5bb719 (outdated¹).

1 Hoare Triple

Precondition

Compiler-Verified

• Generic TV implements trait CastInternalRational

User-Verified

None

Pseudocode

```
def then_deintegerize_hashmap(k: i32) -> Function[HashMap[TK, IBig], HashMap[TK, TV]]:
    if k == i32.MIN: #
        raise ValueError("k must not be i32.MIN")

def value_function(v_i):
        return TV.from_rational(x_mul_2k(RBig.from_(v_i), k))

return Function.new(lambda x: {k_i: value_function(v_i) for k_i, v_i in x.items()})
```

Postcondition

Theorem 1.1. For every setting of the input parameters (k, TK, TV) to then_deintegerize_hashmap such that the given preconditions hold, then_deintegerize_hashmap raises an exception (at compile time or run time) or returns a valid postprocessor. A valid postprocessor has the following property:

1. (Data-independent errors). For every pair of elements x, x' in input_domain, function(x), function(x') either neither or both raise an error. If both raise an error, then they both raise the same error.

Proof. By the postcondition of TV.from_rational, the outcome of the function is the nearest representable float, and may saturate to positive or negative infinity. The precondition of x_mul_2k that k is not i32.MIN is satisfied on line 2. Since TV.from_rational and x_mul_2k are both infallible, the function is infallible, meaning that the function cannot raise data-dependent errors. Therefore the function is a valid postprocessor.

¹See new changes with git diff f5bb719..0bd3ea93 rust/src/measurements/noise_threshold/nature/float/mod.rs