

# fn make\_privacy\_filter

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This proof resides in “**contrib**” because it has not completed the vetting process.

Proves soundness of `fn make_privacy_filter`.

## 1 Hoare Triple

### Precondition

#### Compiler-verified

- Argument `odometer` of type `Odometer<DI, MI, MO, Q, A>`.
- Argument `d_in` of type `MI_Distance`, the associated distance type of `MI`.
- Argument `d_out` of type `MO_Distance`, the associated distance type of `MO`.
- Generic `DI` implements `Domain`.
- Generic `MI` implements `Metric`.
- Generic `MO` implements `Measure`.
- `MI_Distance` implements `ProductOrd`.
- `MO_Distance` implements `ProductOrd`.
- `(DI, MI)` implements `MetricSpace`.

#### User-verified

None

### Pseudocode

```
1 def make_privacy_filter(
2     odometer: Odometer[DI, MI, MO, Q, A],
3     d_in: MI_Distance,
4     d_out: MO_Distance,
5 ) -> Measurement[DI, MI, MO, OdometerQueryable[MI, MO, Q, A]]:
6     odo_function = odometer.function
7     continuation_rule = new_continuation_rule( #
8         d_in, d_out, Q, A, MI_Distance, MO_Distance
9     )
10
11     def function(arg: DI_Carrier) -> OdometerQueryable[MI, MO, Q, A]:
12         return wrap(continuation_rule, lambda: odo_function.eval(arg))  #
```

```

14     def privacy_map(d_in_p: MI_Distance) -> MO_Distance:
15         if d_in_p.total_gt(d_in):
16             raise "input distance must not be greater than d_in"
17
18         return d_out
19
20     return Measurement.new(
21         odometer.input_domain,
22         odometer.input_metric,
23         odometer.output_measure,
24         Function.new_interactive(function),
25         PrivacyMap.new_fallible(privacy_map),
26     )

```

### Postcondition

For every setting of the input parameters (`odometer`, `d_out`, `DI`, `MI`, `MO`, `Q`, `A`) to `make_privacy_filter` such that the given preconditions hold, `make_privacy_filter` raises an error (at compile time or run time) or returns a valid odometer. A valid odometer has the following properties:

1. (Data-independent runtime errors). For every pair of members  $x$  and  $x'$  in `input_domain`, `invoke(x)` and `invoke(x')` either both return the same error or neither return an error.
2. (Valid odometer queryable). For every member  $x$  in `input_domain`, where `function(x)` does not raise an error, `function(x)` returns a valid odometer queryable.

*Proof of data-independent errors.* `Function.eval` on line 12 has data-independent exceptions, because the function is from `odometer`, which is a valid odometer. Since this is the only location where an exception can be raised, the data-independent errors property holds.  $\square$

*Proof of privacy guarantee.* By the definition of a valid odometer queryable, the output of `make_privacy_filter` upholds the privacy guarantee.  $\square$