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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of MakeNoise over scalars for IntExpFamily in mod.rs at commit f5bb719 (outdated1).

The intuition of this implementation is that a vector-valued mechanism can be used to privatize a scalarvalued input, by transforming the input into a singleton vector, applying the vector mechanism, and then unpacking the resulting singleton vector.

This matches the code and proof for the float case, MakeNoise<AtomDomain<T>, AbsoluteDistance<QI>, MO> for FloatExpFamily<P>, except for elementary data type.

## 1 Hoare Triple

#### Precondition

#### Compiler-Verified

- Generic MO implements trait Measure
- Generic T implements trait Integer and SaturatingCast<IBig> The saturating cast is for infallible postprocessing of big ints back to type T.
- Const-generic P is of type usize
- Generic QI implements trait Integer
- Type IBig implements trait From<T>. This infallible exact cast is for converting integers to big ints in the preprocessing transformation.
- Type RBig implements trait TryFrom<QI>. This is for fallible casting from input sensitivity of type QI to a rational in the privacy map.
- Type ZExpFamily<P> implements trait NoisePrivacyMap<LpDistance<P, RBig>, MO>. This bound requires that it must be possible to construct a privacy map for this combination of noise distribution, distance type and privacy measure.

### **User-Verified**

None

 $<sup>^1\</sup>mathrm{See}$  new changes with git diff f5bb719..92ee78b9 rust/src/measurements/noise/nature/integer/mod.rs

#### Pseudocode

#### Postcondition

#### Theorem 1.1.

Theorem 1.2. For every setting of the input parameters (self, input\_space, MO, T, P, QI) to make\_noise such that the given preconditions hold, make\_noise raises an exception (at compile time or run time) or returns a valid measurement. A valid measurement has the following property:

1. (Privacy guarantee). For every pair of elements x, x' in input\_domain and for every pair (d\_in, d\_out), where d\_in has the associated type for input\_metric and d\_out has the associated type for output\_measure, if x, x' are d\_in-close under input\_metric, privacy\_map(d\_in) does not raise an exception, and privacy\_map(d\_in)  $\leq$  d\_out, then function(x), function(x') are d\_out-close under output\_measure.

*Proof.* Neither constructor make\_vec nor MakeNoise.make\_noise have manual preconditions, and the post-conditions guarantee a valid transformation and valid measurement, respectively. then\_index\_or\_default also does not have preconditions, and its postcondition guarantees that it returns a valid postprocessor.

The chain of a valid transformation, valid measurement and valid postprocessor is a valid measurement.

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