

MakeNoise<DI, MI, MO> for DiscreteLaplace

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This proof resides in “**contrib**” because it has not completed the vetting process.

Proves soundness of the implementation of **MakeNoise** for **DiscreteLaplace** in **mod.rs** at commit **f5bb719** (outdated¹).

This is an intermediary compile-time layer whose purpose is to dispatch to either the integer or floating-point variations of the mechanism, depending on the type of data in the input domain.

It does this through the use of the **Nature** trait, which has concrete implementations for each possible input type. This layer makes interior layers simpler to work with, and does not have privacy implications. It also makes **make_laplace** easier to call, by simplifying the type signature.

1 Hoare Triple

Precondition

Compiler-Verified

MakeNoise is parameterized as follows:

- DI implements trait **Domain**
- MI implements trait **Metric**
- MO implements trait **Measure**

The following trait bounds are also required:

- (DI, MI) implements trait **MetricSpace**
- **DI_Atom** implements trait **Nature**. This trait encodes the relationship between the atomic data type and the type of the noise distribution that is compatible with it: **DI_Atom_RV1**. In Rust, this corresponds to the (ugly) `<DI::Atom as Nature>::RV<1>` type.
- **DI_Atom_RV1** implements trait **MakeNoise**. That is, it must be possible to build the mechanism from this new equivalent distribution.

User-Verified

None

¹See new changes with `git diff f5bb719..18da8ea rust/src/measurements/noise/distribution/laplace/mod.rs`

Pseudocode

```
1 # analogous to impl MakeNoise<DI, MI, MO> for DiscreteLaplace in Rust
2 class DiscreteLaplace:
3     def make_noise(self, input_space: tuple[DI, MI]) -> Measurement[DI, DI_Carrier, MI, MO]:
4         # an equivalent random variable specific to the atom dtype
5         rv_nature = DI_Atom.new_distribution(self.scale, self.k) #
6         # build a measurement sampling from this equivalent distribution
7         return rv_nature.make_noise(input_space) #
```

Postcondition

Theorem 1.1. For every setting of the input parameters (`self`, `input_space`, `DI`, `MI`, `MO`) to `make_noise` such that the given preconditions hold, `make_noise` raises an error (at compile time or run time) or returns a valid measurement. A valid measurement has the following properties:

1. (Data-independent runtime errors). For every pair of members x and x' in `input_domain`, `invoke(x)` and `invoke(x')` either both return the same error or neither return an error.
2. (Privacy guarantee). For every pair of members x and x' in `input_domain` and for every pair (d_{in}, d_{out}) , where d_{in} has the associated type for `input_metric` and d_{out} has the associated type for `output_measure`, if x, x' are d_{in} -close under `input_metric`, `privacy_map(d_in)` does not raise an error, and `privacy_map(d_in) = d_out`, then `function(x)`, `function(x')` are d_{out} -close under `output_measure`.

Proof. On line 7, `make_noise` has no preconditions, so irregardless of any prior logic, the postcondition of `make_noise` follows that the output is a valid measurement. \square

The complexity in the type system here is designed to be free of privacy implications, to help simplify the core, privacy-sensitive implementation.