fn then_deintegerize_vec

Michael Shoemate

This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of then_deintegerize_vec in mod.rs at commit f5bb719 (out-dated¹).

1 Hoare Triple

Precondition

Compiler-Verified

• Generic TO implements trait CastInternalRational

User-Verified

None

Pseudocode

```
def then_deintegerize_vec(k: i32) -> Function[Vec[IBig], Vec[T0]]:

if k == i32.MIN: #
    raise ValueError("k must be greater than i32.MIN")

def element_function(x_i):
    return TO.from_rational(x_mul_2k(RBig.from_(x_i), k))

return Function.new(lambda x: [element_function(x_i) for x_i in x])
```

Postcondition

Theorem 1.1. For every setting of the input parameters (k, T0) to then_deintegerize_vec such that the given preconditions hold, then_deintegerize_vec raises an exception (at compile time or run time) or returns a valid postprocessor. A valid postprocessor has the following property:

1. (Data-independent errors). For every pair of elements x, x' in input_domain, function(x), function(x') either neither or both raise an error. If both raise an error, then they both raise the same error.

Proof. By the postcondition of TO.from_rational, the outcome of the function is the nearest representable float, and may saturate to positive or negative infinity. The precondition of x_mul_2k that k is not i32.MIN is satisfied on line 3. Since TO.from_rational and x_mul_2k are both infallible, the function is infallible, meaning that the function cannot raise data-dependent errors. Therefore the function is a valid postprocessor.

¹See new changes with git diff f5bb719..5369e78 rust/src/measurements/noise/nature/float/mod.rs