# fn make\_fully\_adaptive\_composition

### Michael Shoemate

This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of fn make\_fully\_adaptive\_composition.

## 1 Hoare Triple

#### Precondition

#### Compiler-verified

- Argument input\_domain of type DI.
- Argument input\_metric of type MI.
- Argument output\_measure of type MO.
- Argument d\_in of type MI\_Distance.
- Generic DI implements Domain.
- Generic MI implements Metric.
- Generic MO implements Measure.
- (DI, MI) implements MetricSpace.

#### **User-verified**

#### Pseudocode

```
def make_fully_adaptive_composition(
      input_domain: DI,
      input_metric: MI,
      output_measure: MO,
  ) -> Odometer[DI, MI, MO, Measurement[DI, TO, MI, MO], TO]:
      sequential = matches(
          \verb"output_measure.theorem"(Adaptivity.FullyAdaptive)",
          Sequentiality. Sequential
9
10
      def fully_adaptive_composition(arg: DI_Carrier):
11
          return new_fully_adaptive_composition_queryable(
              input_domain,
13
14
               input_metric,
               output_measure,
15
               arg,
16
17
               sequential)
```

```
return Odometer.new(
    input_domain,
    input_metric,
    output_measure,
    Function.new_fallible(fully_adaptive_composition))
```

#### Postcondition

For every setting of the input parameters (input\_domain, input\_metric, output\_measure, d\_in, DI, TO, MI, MO) to make\_fully\_adaptive\_composition such that the given preconditions hold, make\_fully\_adaptive\_compositions are exception (at compile time or run time) or returns a valid odometer. A valid odometer has the following properties:

- 1. (Data-independent exceptions). For every pair of elements x, x' in input\_domain, function(x) and function(x') either both raise an exception, or neither raise an exception.
- 2. (Wrapping guarantee). Interactive measurement queryables spawned while evaluating external queries are wrapped by the wrapper function accompanying the external query.
- 3. (Valid odometer queryable). For every element x in input\_domain, where function(x) does not raise an exception, function(x) returns a valid odometer queryable.

*Proof.* (Data-independent exceptions). The only function called, new\_sequential\_odometer\_queryable, does not raise an exception, as verified by the compiler. Therefore all invocations of function do not raise an exception.

*Proof.* (Valid odometer queryable). Under the assumption that the input data is a member of the input domain, the precondition of new\_fully\_adaptive\_composition\_queryable is met, so by its postcondition the return is a valid odometer queryable.