CompositionMeasure for RenyiDivergence

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of CompositionMeasure for RenyiDivergence in mod.rs at commit f5bb719 (outdated¹).

1 Hoare Triple

Precondition

Compiler-Verified

Types matching pseudocode.

Caller-Verified

None

Pseudocode

```
class CompositionMeasure(RenyiDivergence):
      def composability( #
          self, adaptivity: Adaptivity
      ) -> Composability:
          return Composability.Concurrent
      def compose(self, d_mids: Vec[Self_Distance]) -> Self_Distance:
          def curve(alpha: float) -> float: #
              epsilons = [d_mid(alpha) for d_mid in d_mids]
              d_out = 0.0
11
              for d_mid in epsilons:
12
                  d_out = d_out.inf_add(d_mid)
              return d_out
14
15
          return Function.new_fallible(curve)
```

Postcondition

Theorem 1.1. composability returns Ok(out) if the composition of a vector of privacy parameters d_mids is bounded above by self.compose(d_mids) under adaptivity adaptivity and out-composability. Otherwise returns an error.

Proof. The new curve constructed on line 8 composes all epsilon parameters at a given fixed alpha. By the postcondition of InfAdd we have that for any choice of alpha, $\sum_i d_{mid_i}(alpha) \leq compose(d_{mids})(\alpha)$.

 $^{^{1}\}mathrm{See}\ \mathrm{new}\ \mathrm{changes}\ \mathrm{with}\ \mathrm{git}\ \mathrm{diff}\ \mathrm{f5bb719..3e737bd9}\ \mathrm{rust/src/combinators/sequential_composition/mod.rs}$

Adaptivity	Sequential	Concurrent
Non-Adaptive	Proposition 1[Mir17]	Theorem 2[Lyu22]
Adaptive	-	-
Fully-Adaptive	Theorem 4.3[FZ22]	Theorem $1.21[VW21]$
This table is reflected	in the implementation	of composability on line 2 .

References

- [FZ22] Vitaly Feldman and Tijana Zrnic. Individual privacy accounting via a renyi filter, 2022.
- [Lyu22] Xin Lyu. Composition theorems for interactive differential privacy, 2022.
- [Mir17] Ilya Mironov. Rényi differential privacy. In 2017 IEEE 30th Computer Security Foundations Symposium (CSF), page 263–275. IEEE, August 2017.
- [VW21] Salil Vadhan and Tianhao Wang. Concurrent composition of differential privacy, 2021.