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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of MakeNoise over scalars for IntExpFamily in mod.rs at commit f5bb719 (outdated¹).

The intuition of this implementation is that a vector-valued mechanism can be used to privatize a scalar-valued input, by transforming the input into a singleton vector, applying the vector mechanism, and then unpacking the resulting singleton vector.

This matches the code and proof for the float case, MakeNoise<AtomDomain<T>, AbsoluteDistance<QI>, MO> for FloatExpFamily<P>, except for elementary data type.

1 Hoare Triple

Precondition

Compiler-Verified

- Generic T implements trait Integer and SaturatingCast<IBig> The saturating cast is for infallible postprocessing of big into back to type T.
- Const-generic P is of type usize
- Generic QI implements trait Integer
- Generic MO implements trait Measure
- Type IBig implements trait From<T>. This infallible exact cast is for converting integers to big ints in the preprocessing transformation.
- Type RBig implements trait TryFrom<QI>. This is for fallible casting from input sensitivity of type QI to a rational in the privacy map.
- Type ZExpFamily<P> implements trait NoisePrivacyMap<LpDistance<P, RBig>, MO>. This bound requires that it must be possible to construct a privacy map for this combination of noise distribution, distance type and privacy measure.

User-Verified

None

 $^{^1\}mathrm{See}$ new changes with git diff f5bb719..4aa6870 rust/src/measurements/noise/nature/integer/mod.rs

Pseudocode

Postcondition

Theorem 1.1. For every setting of the input parameters (self, input_space, MO, T, P, QI) to make_noise such that the given preconditions hold, make_noise raises an error (at compile time or run time) or returns a valid measurement. A valid measurement has the following properties:

- 1. (Data-independent runtime errors). For every pair of members x and x' in input_domain, invoke(x) and invoke(x') either both return the same error or neither return an error.
- 2. (Privacy guarantee). For every pair of members x and x' in input_domain and for every pair (d_in,d_out), where d_in has the associated type for input_metric and d_out has the associated type for output_measure, if x,x' are d_in-close under input_metric, privacy_map(d_in) does not raise an error, and privacy_map(d_in) = d_out, then function(x), function(x') are d_out-close under output_measure.

Proof. Neither constructor make_vec nor MakeNoise.make_noise have manual preconditions, and the post-conditions guarantee a valid transformation and valid measurement, respectively. then_index_or_default also does not have preconditions, and its postcondition guarantees that it returns a valid postprocessor.

The chain of a valid transformation, valid measurement and valid postprocessor is a valid measurement.