fn make_laplace

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of make_laplace in mod.rs at commit f5bb719 (outdated¹). Perturbative noise mechanisms may be parameterized along many different axes:

- domain: scalar or vector
- domain dtype: i8, i16, i32, i64, u8, u16, u32, u64, f32, f64, UBig, IBig, RBig
- metric: absolute distance, 11 distance, modular distance
- metric dtype: i8, i16, i32, i64, u8, u16, u32, u64, f32, f64, UBig, IBig, RBig
- measure: max divergence, zero concentrated divergence
- distribution: laplace, gaussian

All parameterizations reduce to a single core mechanism that perturbs a vector of signed big integers with noise sampled from the appropriate discrete distribution.

The implementation of this function constructs a random variable denoting the noise distribution to add, and then dispatches to the MakeNoise<DI, MI, MO> trait which constructs the core mechanism and wraps it in pre-processing transformations and post-processors to match the desired parameterization.

1 Hoare Triple

Precondition

Compiler-Verified

- generic DI implements trait Domain
- generic MI implements trait Metric
- generic MO implements trait Measure
- type DiscreteLaplace implements trait MakeNoise<DI, MI, MO> This trait bound constrains the choice of input domain, input metric and output measure to those that can form valid measurements.
- type (DI, MI) implements trait MetricSpace

User-Verified

None

 $^{^1\}mathrm{See}$ new changes with git diff f5bb719..7495ff0 rust/src/measurements/noise/distribution/laplace/mod.rs

Pseudocode

```
def make_laplace(
input_domain: DI,
input_metric: MI,
scale: f64,
k: Option[i32],
) -> Measurement[DI, DI_Carrier, MI, M0]:
return DiscreteLaplace(scale, k).make_noise((input_domain, input_metric))
```

Postcondition

Theorem 1.1. For every setting of the input parameters (input_domain, input_metric, scale, k, DI, MI, MO) to make_laplace such that the given preconditions hold, make_laplace raises an exception (at compile time or run time) or returns a valid measurement. A valid measurement has the following properties:

- 1. (Data-independent runtime errors). For every pair of elements x, x' in input_domain, function(x) returns an error if and only if function(x') returns an error.
- 2. (Privacy guarantee). For every pair of elements x, x' in input_domain and for every pair (d_in,d_out), where d_in has the associated type for input_metric and d_out has the associated type for output_measure, if x, x' are d_in-close under input_metric, privacy_map(d_in) does not raise an exception, and privacy_map(d_in) \leq d_out, then function(x), function(x') are d_out-close under output_measure.

Proof. We first construct a random variable <code>DiscreteLaplace</code> representing the desired noise distribution. Since <code>MakeNoise.make_noise</code> has no preconditions, the postcondition follows, which matches the postcondition for this function.