fn match_datetime_component

Michael Shoemate

This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of match_datetime_component in mod.rs at commit f5bb719 (outdated¹).

match_datetime_component returns the data type and number of possible unique values of a compute operation that retrieves a datetime component.

1 Hoare Triple

Precondition

Compiler-verified

• Argument temporal_function of type TemporalFunction

Human-verified

None

Pseudocode

```
def match_datetime_component(
      temporal_function: TemporalFunction,
    -> tuple[DataType, u32 | None] | None:
          Millennium: (DataType.UInt32, None),
          Century: (DataType.Int32, None),
          Year: (DataType.Int32, None),
          IsoYear: (DataType.Int32, None),
          Quarter: (DataType.Int8, 4),
          Month: (DataType.Int8, 12),
          Week: (DataType.Int8, 53),
11
          WeekDay: (DataType.Int8, 7),
12
          Day: (DataType.Int8, 31),
13
          OrdinalDay: (DataType.Int16, 366),
14
          Hour: (DataType.Int8, 24),
15
          Minute: (DataType.Int8, 60),
16
          Second: (DataType.Int8, 60),
17
          Millisecond: (DataType.Int32, 1_000),
18
          Microsecond: (DataType.Int32, 1_000_000),
19
20
          Nanosecond: (DataType.Int32, 1_000_000_000),
      }).get(temporal_function)
```

¹See new changes with git diff f5bb719..ab057864 rust/src/transformations/make_stable_expr/namespace_dt/expr_datetime_component

Postcondition

Theorem 1.1. For every setting of the input parameters (temporal_function) to match_datetime_component such that the given preconditions hold, match_datetime_component raises an exception (at compile time or run time) or returns a valid transformation. A valid transformation has the following properties:

- 1. (Appropriate output domain). For every element x in input_domain, function(x) is in output_domain or raises a data-independent runtime exception.
- 2. (Stability guarantee). For every pair of elements x, x' in input_domain and for every pair (d_in, d_out), where d_in has the associated type for input_metric and d_out has the associated type for output_metric, if x, x' are d_in-close under input_metric, stability_map(d_in) does not raise an exception, and stability_map(d_in) \leq d_out, then function(x), function(x') are d_out-close under output_metric.

2 Proof

Proof. For each compute operation, the data type is automatically tested and verified to be correct. Only output cardinalities that are specified must be proven. Of note:

- there may be up to 53 weeks in a year, due to partial weeks overlapping the end of the year.
- There are up to 366 ordinal days due to leap years.
- Polars does not account for leap seconds, so there are at most 60 seconds in a minute.
- Milliseconds, microseconds and nanoseconds are computed modulo seconds.