# fn make\_privacy\_filter

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of fn make\_privacy\_filter.

## 1 Hoare Triple

#### Precondition

#### Compiler-verified

- Argument odometer of type Odometer<DI, MI, MO, Q, A>.
- Argument d\_out of type MO\_Distance, the associated distance type of MO.
- Generic DI implements Domain.
- Generic MI implements Metric.
- Generic MO implements Measure.
- MI\_Distance implements ProductOrd.
- MO\_Distance implements ProductOrd.
- (DI, MI) implements MetricSpace.

#### **User-verified**

None

### Pseudocode

```
def make_privacy_filter(
      odometer: Odometer[DI, MI, MO, Q, A],
      d_out: MO_Distance,
  ) -> Measurement[DI, OdometerQueryable[MI, MO, Q, A], MI, MO]:
      odo_function = odometer.function
      d_in = odometer.d_in
      def function(arg: DI_Carrier) -> OdometerQueryable[MI, MO, Q, A]:
          continuation_rule = new_continuation_rule(d_out, MO_Distance)
10
11
          return wrap(continuation_rule, lambda: odo_function.eval(arg))
12
      def privacy_map(d_in_p: MI_Distance) -> MO_Distance:
13
          if d_in_p.total_gt(d_in):
14
              raise "input distance must not be greater than d_in"
```

```
return d_out

return Measurement.new(
    odometer.input_domain,
    Function.new_interactive(function),
    odometer.input_metric,
    odometer.output_measure,
    PrivacyMap.new_fallible(privacy_map),

privacyMap.new_fallible(privacy_map),
```

#### Postcondition

For every setting of the input parameters (odometer, d\_out, DI, MI, MO, Q, A) to make\_privacy\_filter such that the given preconditions hold, make\_privacy\_filter raises an exception (at compile time or run time) or returns a valid odometer. A valid odometer has the following properties:

- 1. (Data-independent exceptions). For every pair of elements x, x' in input\_domain, function(x) and function(x') either both raise an exception, or neither raise an exception.
- 2. (Wrapping guarantee). Interactive measurement queryables spawned while evaluating external queries are wrapped by the wrapper function accompanying the external query.
- 3. (Valid odometer queryable). For every element x in input\_domain, where function(x) does not raise an exception, function(x) returns a valid odometer queryable.

Proof of data-independent errors. Function.eval on line 11 has data-independent exceptions, because the function is from odometer, which is a valid odometer. Since this is the only location where an exception can be raised, the data-independent errors property holds.

*Proof of wrapping guarantee.* wrap on line 11 guarantees to wrap all spawned IM queryables with the provided wrapper, satisfying the wrapping guarantee.

*Proof of privacy guarantee.* By the definition of a valid odometer queryable, the output of make\_privacy\_filter upholds the privacy guarantee.