fn make_gaussian_threshold

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of make_gaussian_threshold in mod.rs at commit f5bb719 (outdated1).

Thresholded noise mechanisms may be parameterized along many different axes:

- key dtype: i8, i16, i32, i64, u8, u16, u32, u64, f32, f64, UBig, IBig, RBig
- metric dtype: i8, i16, i32, i64, u8, u16, u32, u64, f32, f64, UBig, IBig, RBig
- measure: max divergence, zero concentrated divergence
- distribution: laplace, gaussian

All parameterizations reduce to a single core mechanism that perturbs a signed big integers with noise sampled from the appropriate discrete distribution, and then thresholds and shuffles the result.

The implementation of this function constructs a random variable denoting the noise distribution to add, and then dispatches to the MakeNoiseThreshold<DI, MI, MO> trait which constructs the core mechanism and wraps it in pre-processing transformations and post-processors to match the desired parameterization.

1 Hoare Triple

Precondition

Compiler-Verified

- generic DI implements trait NoiseDomain
- generic MI implements trait Metric
- generic MO implements trait Measure
- generic DiscreteGaussian implements trait MakeNoiseThreshold
- type (DI, MI) implements trait MetricSpace

User-Verified

None

 $^{^{1}\}mathrm{See}$ new changes with git diff f5bb719..33f2250 rust/src/measurements/noise_threshold/distribution/gaussian/mod.rs

Pseudocode

Postcondition

output_measure.

Theorem 1.1. For every setting of the input parameters (input_domain, input_metric, scale, threshold, k, DI, MI, MO) to make_gaussian_threshold such that the given preconditions hold, make_gaussian_threshold raises an error (at compile time or run time) or returns a valid measurement. A valid measurement has the following properties:

- 1. (Data-independent runtime errors). For every pair of members x and x' in input_domain, invoke(x) and invoke(x') either both return the same error or neither return an error.
- 2. (Privacy guarantee). For every pair of members x and x' in input_domain and for every pair (d_in,d_out), where d_in has the associated type for input_metric and d_out has the associated type for output_measure, if x, x' are d_in-close under input_metric, privacy_map(d_in) does not raise an error, and privacy_map(d_in) = d_out, then function(x), function(x') are d_out-close under

Proof. We first construct a random variable DiscreteGaussian representing the desired noise distribution. Since MakeNoiseThreshold.make_noise_threshold has no preconditions, the postcondition follows, which matches the postcondition for this function.