MakeNoiseThreshold<DI, MI, MO> for DiscreteLaplace

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of MakeNoiseThreshold for DiscreteLaplace in mod.rs at commit f5bb719 (outdated1).

This is an intermediary compile-time layer whose purpose is to dispatch to either the integer or floating-point variations of the mechanism, depending on the type of data in the input domain.

It does this through the use of the Nature trait, which has concrete implementations for each possible input type. This layer makes interior layers simpler to work with, and does not have privacy implications. It also makes make_laplace_threshold easier to call, by simplifying the type signature.

1 Hoare Triple

Precondition

Compiler-Verified

MakeNoiseThreshold is parameterized as follows:

- DI implements trait Domain
- MI implements trait Metric
- MO implements trait Measure

The following trait bounds are also required:

- (DI, MI) implements trait MetricSpace
- DI_Atom implements trait Nature. This trait encodes the relationship between the atomic data type and the type of the noise distribution that is compatible with it: DI_Atom_RV2. In Rust, this corresponds to the (ugly) <DI::Atom as Nature>::RV<2> type.
- DI_Atom_RV2 implements trait MakeNoiseThreshold. That is, it must be possible to build the mechanism from this new equivalent distribution.
- type (DI, MI) implements trait MetricSpace

User-Verified

None

 $^{^{1}} See \ new \ changes \ with \ \texttt{git} \ \ \texttt{diff} \ \ \texttt{f5bb719..ee8673a} \ \ rust/\texttt{src/measurements/noise_threshold/distribution/laplace/mod.rs}$ rs

Pseudocode

```
# analogous to impl MakeNoiseThreshold < DI, MI, MO > for DiscreteLaplace in Rust
class DiscreteLaplace:

def make_noise_threshold(self, input_space, threshold) -> Measurement[DI, DI_Carrier, MI, MO]:

# an equivalent random variable specific to the atom dtype
rv_nature = DI_Atom.new_distribution(self.scale, self.k) #
# build a measurement sampling from this equivalent distribution
return rv_nature.make_noise_threshold(input_space, threshold) #
```

Postcondition

Theorem 1.1. For every setting of the input parameters (self, input_space, threshold, DI, MI, MO) to make_noise_threshold such that the given preconditions hold, make_noise_threshold raises an exception (at compile time or run time) or returns a valid measurement. A valid measurement has the following properties:

- 1. (Data-independent runtime errors). For every pair of elements x, x' in input_domain, function(x) returns an error if and only if function(x') returns an error.
- 2. (Privacy guarantee). For every pair of elements x, x' in input_domain and for every pair (d_in, d_out) , where d_in has the associated type for input_metric and d_out has the associated type for output_measure, if x, x' are d_in-close under input_metric, privacy_map(d_in) does not raise an exception, and privacy_map(d_in) \leq d_out, then function(x), function(x') are d_out-close under output_measure.

Proof. On line 7, make_noise_threshold has no preconditions, so irregardless of any prior logic, the post-condition of make_noise_threshold follows that the output is a valid measurement.

The complexity in the type system here is designed to be free of privacy implications, to help simplify the core, privacy-sensitive implementation.