# MakeNoiseThreshold<DI, MI, MO> for DiscreteLaplace

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of MakeNoiseThreshold for DiscreteLaplace in mod.rs at commit f5bb719 (outdated1).

This is an intermediary compile-time layer whose purpose is to dispatch to either the integer or floating-point variations of the mechanism, depending on the type of data in the input domain.

It does this through the use of the Nature trait, which has concrete implementations for each possible input type. This layer makes interior layers simpler to work with, and does not have privacy implications. It also makes make\_laplace\_threshold easier to call, by simplifying the type signature.

# 1 Hoare Triple

#### Precondition

## Compiler-Verified

MakeNoiseThreshold is parameterized as follows:

- DI implements trait Domain
- MI implements trait Metric
- MO implements trait Measure

The following trait bounds are also required:

- (DI, MI) implements trait MetricSpace
- DI\_Atom implements trait Nature. This trait encodes the relationship between the atomic data type and the type of the noise distribution that is compatible with it: DI\_Atom\_RV2. In Rust, this corresponds to the (ugly) <DI::Atom as Nature>::RV<2> type.
- DI\_Atom\_RV2 implements trait MakeNoiseThreshold. That is, it must be possible to build the mechanism from this new equivalent distribution.
- type (DI, MI) implements trait MetricSpace

#### **User-Verified**

None

 $<sup>^{1}\</sup>mathrm{See}$  new changes with git diff f5bb719..0cdb8b9 rust/src/measurements/noise\_threshold/distribution/laplace/mod.rs

## Pseudocode

#### Postcondition

Theorem 1.1. For every setting of the input parameters (self, input\_space, threshold, DI, MI, MO) to make\_noise\_threshold such that the given preconditions hold, make\_noise\_threshold raises an error (at compile time or run time) or returns a valid measurement. A valid measurement has the following properties:

- 1. (Data-independent runtime errors). For every pair of members x and x' in input\_domain, invoke(x) and invoke(x') either both return the same error or neither return an error.
- 2. (Privacy guarantee). For every pair of members x and x' in input\_domain and for every pair (d\_in,d\_out), where d\_in has the associated type for input\_metric and d\_out has the associated type for
  - output\_measure, if x, x' are d\_in-close under input\_metric, privacy\_map(d\_in) does not raise an error, and privacy\_map(d\_in) = d\_out, then function(x), function(x') are d\_out-close under output\_measure.

*Proof.* On line 7, make\_noise\_threshold has no preconditions, so irregardless of any prior logic, the post-condition of make\_noise\_threshold follows that the output is a valid measurement.

The complexity in the type system here is designed to be free of privacy implications, to help simplify the core, privacy-sensitive implementation.