MakeNoise<VectorDomain<AtomDomain<T>, LpDistance<P, QI>, MO> for FloatExpFamily<P>

Michael Shoemate

This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of MakeNoise over vectors for FloatExpFamily in mod.rs at commit f5bb719 (outdated¹).

This mechanism samples from the FloatExpFamily distribution, where the tails saturate to the positive and negative infinity floats in the native float type. This is done by rounding floats to a fractional grid, adding noise from from the ZExpFamily distribution (supported on all integers) to the numerator of the fraction (with noise scale multiplied by the denominator), and then converting back to the nearest float, or saturating to positive or negative infinity.

1 Hoare Triple

Precondition

Compiler-Verified

- Generic T implements trait Float
- Const-generic P is of type usize
- Generic QI implements trait Number
- Generic MO implements trait Measure
- Type i32 implements trait ExactIntCast«T as FloatBits>::Bits>, This requirement means that the raw bits of T can be exactly cast to an i32.
- Type RBig implements traits TryFrom<T> and TryFrom<QI>. This is for fallible exact casting from input sensitivity to a rational in the privacy map.
- Type ZExpFamily<P> implements traits NoisePrivacyMap<LpDistance<P, RBig>, MO> This bound requires that it must be possible to construct a privacy map for this combination of noise distribution, distance type and privacy measure.

User-Verified

None

¹See new changes with git diff f5bb719..78358cc rust/src/measurements/noise/nature/float/mod.rs

Pseudocode

Postcondition

Theorem 1.1. For every setting of the input parameters (self, input_space, MO, T, P, QI) to make_noise such that the given preconditions hold, make_noise raises an exception (at compile time or run time) or returns a valid measurement. A valid measurement has the following properties:

- 1. (Data-independent runtime errors). For every pair of elements x, x' in input_domain, function(x) returns an error if and only if function(x') returns an error.
- 2. (Privacy guarantee). For every pair of elements x, x' in input_domain and for every pair (d_in, d_out), where d_in has the associated type for input_metric and d_out has the associated type for output_measure, if x, x' are d_in-close under input_metric, privacy_map(d_in) does not raise an exception, and privacy_map(d_in) \leq d_out, then function(x), function(x') are d_out-close under output_measure.

Proof. Line 4 constructs a new random variable following a distribution equivalent to FloatExpFamily, but without tails that saturate to infinity, and with gaps between adjacent point on the grid adjusted to one.

Neither constructor make_float_to_bigint nor MakeNoise.make_noise have manual preconditions, and the postconditions guarantee a valid transformation and valid measurement, respectively. then_deintegerize_vec also does not have preconditions, and its postcondition guarantees that it returns a valid postprocessor.

The chain of a valid transformation, valid measurement and valid postprocessor is a valid measurement.