# fn match\_num\_groups\_predicate

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of match\_num\_groups\_predicate in mod.rs at commit f5bb719 (outdated1).

# 1 Hoare Triple

#### Precondition

## Compiler Verified

Types matching pseudocode.

## Precondition

None

#### **Function**

```
def match_num_groups_predicate(
      ranks: Expr,
      partition_by: Vec[Expr],
      identifier: Expr,
      threshold: u32,
  ) -> Optional[Bound]:
      # check if is a rank function
      if not isinstance(ranks, Expr.Function) or not isinstance(
          ranks.function, FunctionExpr.Rank
     ): #
10
          return None
11
12
      input = ranks.input
13
14
      options = ranks.function.options
15
16
      if partition_by != [identifier]: #
          raise "num_groups truncation must use the identifier in the over clause"
17
18
      if not isinstance(options.method, RankMethod.Dense): #
19
20
          raise "num_groups truncation's rank must be dense"
21
      if len(input) != 1: #
22
          raise "rank function must be applied to a single input"
23
```

 $<sup>^1\</sup>mathrm{See}$  new changes with git diff f5bb719..8a5d93c rust/src/transformations/make\_stable\_lazyframe/truncate/matching/mod.rs

```
input_item = input[0]
25
26
      # Treat as_struct as a special case that represents multiple columns.
27
28
      if isinstance(input_item, Expr.Function) and isinstance(
           \verb"input_item.function", FunctionExpr.AsStruct"
29
30
31
           # If the first field is a hash of the second field,
32
           # then interpret the grouping columns as the hash input.
33
           # The second field disambiguates hash collisions when ranking.
34
35
           if isinstance(input_item, Expr.Function) and isinstance(
               \verb"input_item.function", FunctionExpr.Hash"
36
37
               hash_input = input_item.input
38
39
               if hash_input.get(0) == input.get(1):
                   if not isinstance(hash_input.get(0), Expr.Function) or not isinstance(
40
                        hash_input.get(0).function, FunctionExpr.AsStruct
41
42
                        raise f"expected hash input to be a struct, found {hash_input}"
                   input = hash_input.get(0)
44
           by = set(input_item.input)
46
47
           by = {input_item}
48
      return Bound(by=by, per_group=None, num_groups=threshold)
```

#### Postcondition

**Theorem 1.1** (Postcondition). If ranks is a dense ranking of grouping columns, and partition\_by is a singleton of identifier, then returns the bound on per-identifier contributions, or an error if the truncation is mis-specified.

*Proof.* Due to the ambiguity between matching predicates that bound num\_groups or per\_group, an error is only raised if the predicate is unambiguously a per\_group truncation predicate.

The per\_group predicate is only unambiguously identified. This check happens on line 10.

Line 16 checks that partition\_by is a singleton of the identifier, meeting the conditions of the postcondition.

We now check whether the truncation predicate is well-defined, on lines 19 and 22.

Finally, line 30 extracts the grouping columns from the predicate. Special consideration is made for structs, which are considered multiple grouping columns.

Further consideration is made if the first field is a hash of the second field, on line 37. This effectively randomizes the ranking of the grouping columns, as the ranking is based on a lexicographic ordering. and gives in effect a random sample of grouping columns. The second field of grouping columns is kept in the ranker for the rare case that there are hash collisions, which prevents different combinations of grouping keys from being assigned the same rank, preventing more distinct groups being kept than is permitted.

This predicate corresponds to a num\_groups truncation predicate, because the over expression groups by the identifier column, and within each group, a dense ranking is applied to unique combinations of the grouping columns. If the only rows kept are those corresponding to grouping keys assigned dense ranks less than threshold, then each user identifier will have at most threshold unique combinations of the grouping columns after filtering by the predicate.

Therefore the bound on user contributions constructed on line 50 is valid.