# fn make\_expr\_count

## Michael Shoemate

August 20, 2025

This document proves that the implementation of make\_expr\_count in mod.rs at commit f5bb719 (out-dated¹) satisfies its proof definition.

## 1 Hoare Triple

## Preconditions

### Compiler-verified

- Argument input\_domain of type ExprDomain
- Argument input\_metric of type PartitionDistance<MI>
- Argument expr of type Expr
- Generic MI must implement UnboundedMetric
- Const generic P must be of type usize
- (ExprDomain, PartitionDistance<MI>) implements MetricSpace
- (ExprDomain, LpDistance<P, f64>) implements MetricSpace
- Expr implements StableExpr<PartitionDistance<MI>, PartitionDistance<MI>

#### Caller-verified

None

#### Pseudocode

```
def make_expr_count(
    input_domain: ExprDomain, input_metric: PartitionDistance[MI], expr: Expr
) -> Transformation:
    match expr: #
    case Agg(Count(input, include_nulls)):
        if include_nulls:
            strategy = Strategy.Len
        else:
            strategy = Strategy.Count

case Function(inputs, function=FunctionExpr.NullCount):
    (input,) = inputs
    strategy = Strategy.NullCount
```

 $<sup>^1\</sup>mathrm{See}$  new changes with git diff f5bb719..7c4140b rust/src/transformations/make\_stable\_expr/expr\_count/mod.rs

```
14
           case Agg(NUnique(input)):
15
               strategy = Strategy.NUnique
16
17
18
           case _:
               raise ValueError ("expected count, null_count, len, or n_unique expression")
19
20
      # check if input is row-by-row
21
      is_row_by_row = input.make_stable(input_domain.as_row_by_row(), input_metric).is_ok() #
22
23
      # construct prior transformation
24
      t_prior = input.make_stable(input_domain, input_metric) #
25
      middle_domain, middle_metric = t_prior.output_space()
26
27
      by, margin = middle_domain.context.grouping("count") #
28
29
      output_domain = ExprDomain.new( #
30
31
           column=SeriesDomain.new( #
               middle_domain.column.name,
32
33
               AtomDomain.default(u32),
34
           context = Context . Grouping (
35
36
               by=by,
               margin=Margin(
37
                   max_partition_length=1,
38
                   max_num_partitions=margin.max_num_partitions,
39
                   max_partition_contributions=None,
40
41
                   \verb|max_influenced_partitions=margin.max_influenced_partitions|,
                   public_info=margin.public_info,
42
43
               ),
          )
44
      )
45
46
      match strategy: #
47
48
           case Strategy.Len:
               will_count_all = is_row_by_row
49
50
           case Strategy.Count:
               will_count_all = is_row_by_row and not middle_domain.column.nullable
51
52
           case _:
               will_count_all = False
53
54
      public_info = margin.public_info if will_count_all else None #
55
56
      def function(e: Expr) -> Expr: #
57
           match strategy:
58
59
               case Strategy.Count:
60
                   return e.count()
               case Strategy.NullCount:
61
                   return e.null_count()
62
63
               case Strategy.Len:
                  return e.len()
64
65
               case Strategy.NUnique:
                   return e.n_unique()
66
67
      return t_prior >> Transformation.new( #
68
           middle_domain,
69
70
           output_domain,
           Function.then_expr(function),
71
72
           middle_metric,
           LpDistance.default(),
73
           counting_query_stability_map(public_info), #
74
75
```

#### Postcondition

**Theorem 1.1.** For every setting of the input parameters (input\_domain, input\_metric, expr, MI, P) to make\_expr\_count such that the given preconditions hold, make\_expr\_count raises an error (at compile time or run time) or returns a valid transformation. A valid transformation has the following properties:

- 1. (Data-independent runtime errors). For every pair of members x and x' in input\_domain, invoke(x) and invoke(x') either both return the same error or neither return an error.
- 2. (Appropriate output domain). For every member x in input\_domain, function(x) is in output\_domain or raises a data-independent runtime error.
- 3. (Stability guarantee). For every pair of members x and x' in input\_domain and for every pair  $(d_in, d_out)$ , where  $d_in$  has the associated type for input\_metric and  $d_out$  has the associated type for output\_metric, if x, x' are  $d_in$ -close under input\_metric, stability\_map $(d_in)$  does not raise an error, and stability\_map $(d_in)$  =  $d_out$ , then function(x), function(x') are  $d_out$ -close under

## 2 Proof

output\_metric.

Starting from line 4, expr is analyzed to determine the type of counting query strategy and input to the counting query input.

All preconditions for make\_stable on line 25 are compiler-verified, therefore by the postcondition t\_prior is a valid transformation.

To prove that the output is a valid transformation, we must first prove that the transformation on line 68 is valid.

*Proof.* Appropriate Output Domain Since the count transformation is not row-by-row, line 28 disallows this count transformation from being constructed in a row-by-row context, satisfying the requirements of ExprDomain.

By the definition of each of the allowed counting expressions in 4, the resulting output will always contain one series whose name matches the active series' name, and the data type of elements in the series is u32, which is consistent with 31. This series is then part of a dataframe and and operations are continued to be applied with the same context, on line 30. This domain is then used on line 70 to construct the count transformation.

#### Proof. Stability Guarantee

To determine if input is row-by-row, line 22 checks if input can be parsed into a row-by-row transformation.

Line 47 uses domain descriptors to determine if the counting query will count all rows. This is the case if the counting query is Len, or if the counting query counts all non-null values in data that doesn't contain nulls.

If all rows are to be counted, then the public\_info domain descriptor about the partitioning applies to this count query strategy, on line 55.

The function defined on line 57 applies the counting query to the input expression with the given query strategy. The stability of this function is governed by the stability map returned by counting\_query\_stability\_map, as the Len, Count and NullCount strategies can be expressed as arbitrary predicates, and the NUnique strategy can be considered as a 1-stable (non-row-by-row) "unique" transformation chained with a counting query with the Len strategy.

Since it has been shown that both t\_prior and the count transformation are valid transformations, then the preconditions for make\_chain\_tt are met (invoked via the right-shift operator shorthand).