# CompositionMeasure for RenyiDivergence

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of the implementation of CompositionMeasure for RenyiDivergence in mod.rs at commit f5bb719 (outdated<sup>1</sup>).

# 1 Hoare Triple

### Precondition

## Compiler-Verified

Types matching pseudocode.

### Caller-Verified

None

### Pseudocode

```
class CompositionMeasure(RenyiDivergence):
      def composability( #
          self, adaptivity: Adaptivity
      ) -> Composability:
          return Composability.Concurrent
      def compose(self, d_mids: Vec[Self_Distance]) -> Self_Distance:
          def curve(alpha: float) -> float: #
              epsilons = [d_mid(alpha) for d_mid in d_mids]
              d_out = 0.0
11
              for d_mid in epsilons:
12
                  d_out = d_out.inf_add(d_mid)
              return d_out
14
15
          return Function.new_fallible(curve)
```

## Postcondition

Theorem 1.1. composability returns Ok(out) if the composition of a vector of privacy parameters d\_mids is bounded above by self.compose(d\_mids) under adaptivity adaptivity and out-composability. Otherwise returns an error.

*Proof.* The new curve constructed on line 8 composes all epsilon parameters at a given fixed alpha. By the postcondition of InfAdd we have that for any choice of alpha,  $\sum_i d_{mid_i}(alpha) \leq compose(d_{mids})(\alpha)$ .

 $<sup>^1\</sup>mathrm{See}$  new changes with git diff f5bb719..24be80d rust/src/combinators/sequential\_composition/mod.rs

	Adaptivity	Sequential	Concurrent
	Non-Adaptive	Proposition 1[Mir17]	Theorem 2[Lyu22]
	Adaptive	-	-
	Fully-Adaptive	Theorem $4.3[FZ22]$	Theorem $1.22[VW21]$
$\Gamma$ his	table is reflected	in the implementation	of composability on line 2.

# References

- [FZ22] Vitaly Feldman and Tijana Zrnic. Individual privacy accounting via a renyi filter, 2022.
- [Lyu22] Xin Lyu. Composition theorems for interactive differential privacy, 2022.
- [Mir17] Ilya Mironov. Rényi differential privacy. In 2017 IEEE 30th Computer Security Foundations Symposium (CSF), page 263–275. IEEE, August 2017.
- [VW21] Salil Vadhan and Tianhao Wang. Concurrent composition of differential privacy, 2021.