# fn make\_is\_equal

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of fn make\_is\_equal in mod.rs at commit 0db9c6036 (outdated<sup>1</sup>). The transformation checks if each element in a vector dataset is equivalent to a given value, returning a vector of booleans.

# Vetting History

• Pull Request #512

# 1 Hoare Triple

### Precondition

To ensure the correctness of the output, we require the following preconditions:

- Type TIA must have trait PartialEq.
- Type M must have trait DatasetMetric.
- MetricSpace is implemented for (VectorDomain<AtomDomain<TIA>>, M). Therefore M is a valid metric on VectorDomain<AtomDomain<TIA>>.
- MetricSpace is implemented for (VectorDomain<AtomDomain<bool>>, M).

### Pseudocode

```
def make_is_equal(
      input_domain: VectorDomain[AtomDomain[TIA]],
      input_metric: M,
      value: TIA
5
      output_row_domain = atom_domain(T=bool)
      def is_equal(arg: TA) -> TA: #
8
          return value == arg
10
      return make_row_by_row( #
11
12
          input_domain,
13
          input_metric,
14
          output_row_domain,
          is_equal
15
```

 $<sup>^{1}\</sup>mathrm{See}\ \mathrm{new}\ \mathrm{changes}\ \mathrm{with}\ \mathsf{git}\ \mathsf{diff}\ \mathsf{0db9c6036..303d3a1}\ \mathsf{rust/src/transformations/manipulation/mod.rs}$ 

#### Postconditions

Theorem 1.1. For every setting of the input parameters (input\_domain, input\_metric, value) to make\_is\_equal such that the given preconditions hold, make\_is\_equal raises an error (at compile time or run time) or returns a valid transformation. A valid transformation has the following properties:

- 1. (Data-independent runtime errors). For every pair of members x and x' in input\_domain, invoke(x) and invoke(x') either both return the same error or neither return an error.
- 2. (Appropriate output domain). For every member x in input\_domain, function(x) is in output\_domain or raises a data-independent runtime error.
- 3. (Stability guarantee). For every pair of members x and x' in input\_domain and for every pair  $(d_{in}, d_{out})$ , where  $d_{in}$  has the associated type for input\_metric and  $d_{out}$  has the associated type for output\_metric, if x, x' are  $d_{in}$ -close under input\_metric, stability\_map( $d_{in}$ ) does not raise an error, and stability\_map( $d_{in}$ ) =  $d_{out}$ , then function(x), function(x') are  $d_{out}$ -close under output\_metric.

# 2 Proof

Lemma 2.1. The invocation of make\_row\_by\_row (line 11) satisfies its preconditions.

*Proof.* The preconditions of make\_is\_equal and pseudocode definition (line 5) ensure that the type preconditions of make\_row\_by\_row are satisfied. The remaining preconditions of make\_row\_by\_row are:

- row\_function has no side-effects.
- If the input to row\_function is a member of input\_domain's row domain, then the output is a member of output\_row\_domain.

The first precondition is satisfied by the definition of is\_equal (line 8) in the pseudocode.

For the second precondition, assume the input is a member of input\_domain's row domain. By the definition of PartialEq, the output of is\_equal is boolean, and AtomDomain<br/>
Therefore, the output is a member of output\_row\_domain.

We now prove the postcondition of make\_is\_equal.

*Proof.* By 2, the preconditions of make\_row\_by\_row are satisfied. Thus, by the definition of make\_row\_by\_row, the output is a valid transformation.