fn make_odomter_to_filter

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This proof resides in "contrib" because it has not completed the vetting process.

Proves soundness of fn make_odomter_to_filter.

1 Hoare Triple

Precondition

Compiler-verified

- Argument odometer of type Odometer <DI, MI, MO, Q, A>.
- Argument d_in of type MI_Distance, the associated distance type of MI.
- Argument d_out of type MO_Distance, the associated distance type of MO.
- Generic DI implements Domain.
- Generic MI implements Metric.
- Generic MO implements Measure.
- MI_Distance implements ProductOrd.
- MO_Distance implements ProductOrd.
- (DI, MI) implements MetricSpace.

User-verified

Pseudocode

```
def make_odometer_to_filter(
      odometer: Odometer[DI, MI, MO, Q, A],
      d_in: MI_Distance,
      d_out: MO_Distance,
  ) -> Measurement[DI, OdometerQueryable[MI, MO, Q, A], MI, MO]:
      odo_function = odometer.function
      def function(
         arg: DI_Carrier, query_wrapper: Wrapper | None
      ) -> OdometerQueryable[MI, MO, Q, A]:
          continuation_rule = new_continuation_rule(d_in, d_out, MI, MO) #
11
12
          wrapper = compose_wrappers(continuation_rule, query_wrapper) #
13
          return odo_function.eval_wrap(arg, wrapper) #
14
      def privacy_map(d_in_p: MI_Distance) -> MO_Distance:
```

```
if d_in_p.total_gt(d_in):
17
               raise "input distance must not be greater than d_in"
18
19
20
           return d_out
21
       return Measurement.new(
22
23
           odometer.input_domain,
           Function.new_interactive(function),
24
           odometer.input_metric,
25
           odometer.output_measure
26
27
           PrivacyMap.new_fallible(privacy_map),
```

Postcondition

For every setting of the input parameters (odometer, d_in, d_out, DI, MI, MO, Q, A) to make_odometer_to_filter such that the given preconditions hold, make_odometer_to_filter raises an exception (at compile time or run time) or returns a valid odometer. A valid odometer has the following properties:

- 1. (Data-independent exceptions). For every pair of elements x, x' in input_domain, function(x) and function(x') either both raise an exception, or neither raise an exception.
- 2. (Wrapping guarantee). Interactive measurement queryables spawned while evaluating external queries are wrapped by the wrapper function accompanying the external query.
- 3. (Valid odometer queryable). For every element x in input_domain, where function(x) does not raise an exception, function(x) returns a valid odometer queryable.

Proof. Data-independent exceptions Function.eval_wrap on line 14 has data-independent exceptions, because the function is from odometer, which is a valid odometer. Since this is the only location where an exception can be raised, the data-independent exceptions guarantee holds.

Proof. Wrapping Guarantee The query wrapper is labeled query_wrapper on line 9. wrapper on line 13 includes query_wrapper by the postcondition on compose_wrappers.

Function.eval_wrap on line 14 guarantees to wrap all spawned IM queryables with the provided wrapper, satisfying the wrapping guarantee. Since this is the only location where interactive mechanism queryables can be spawned, the wrapping guarantee holds.

Proof. (Privacy Guarantee). TODO