

fn make_laplace

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This proof resides in “**contrib**” because it has not completed the vetting process.

Proves soundness of the implementation of **make_laplace** in **mod.rs** at commit **f5bb719** (outdated¹).
Perturbative noise mechanisms may be parameterized along many different axes:

- domain: scalar or vector
- domain dtype: i8, i16, i32, i64, u8, u16, u32, u64, f32, f64, UBig, IBig, RBig
- metric: absolute distance, l1 distance, modular distance
- metric dtype: i8, i16, i32, i64, u8, u16, u32, u64, f32, f64, UBig, IBig, RBig
- measure: max divergence, zero concentrated divergence
- distribution: laplace, gaussian

All parameterizations reduce to a single core mechanism that perturbs a vector of signed big integers with noise sampled from the appropriate discrete distribution.

The implementation of this function constructs a random variable denoting the noise distribution to add, and then dispatches to the **MakeNoise**<DI, MI, MO> trait which constructs the core mechanism and wraps it in pre-processing transformations and post-processors to match the desired parameterization.

1 Hoare Triple

Precondition

Compiler-Verified

- generic DI implements trait **Domain**
- generic MI implements trait **Metric**
- generic MO implements trait **Measure**
- type **DiscreteLaplace** implements trait **MakeNoise**<DI, MI, MO> This trait bound constrains the choice of input domain, input metric and output measure to those that can form valid measurements.
- type (DI, MI) implements trait **MetricSpace**

User-Verified

None

¹See new changes with `git diff f5bb719..74d146e rust/src/measurements/noise/distribution/laplace/mod.rs`

Pseudocode

```
1 def make_laplace(  
2     input_domain: DI,  
3     input_metric: MI,  
4     scale: f64,  
5     k: Option[i32],  
6 ) -> Measurement[DI, DI_Carrier, MI, MO]:  
7     return DiscreteLaplace(scale, k).make_noise((input_domain, input_metric))
```

Postcondition

Theorem 1.1. For every setting of the input parameters (`input_domain`, `input_metric`, `scale`, `k`, `DI`, `MI`, `MO`) to `make_laplace` such that the given preconditions hold, `make_laplace` raises an error (at compile time or run time) or returns a valid measurement. A valid measurement has the following properties:

1. (Data-independent runtime errors). For every pair of members x and x' in `input_domain`, `invoke(x)` and `invoke(x')` either both return the same error or neither return an error.
2. (Privacy guarantee). For every pair of members x and x' in `input_domain` and for every pair (d_{in}, d_{out}) , where d_{in} has the associated type for `input_metric` and d_{out} has the associated type for `output_measure`, if x, x' are d_{in} -close under `input_metric`, `privacy_map(d_in)` does not raise an error, and `privacy_map(d_in) = d_out`, then `function(x), function(x')` are d_{out} -close under `output_measure`.

Proof. We first construct a random variable `DiscreteLaplace` representing the desired noise distribution. Since `MakeNoise.make_noise` has no preconditions, the postcondition follows, which matches the postcondition for this function. \square