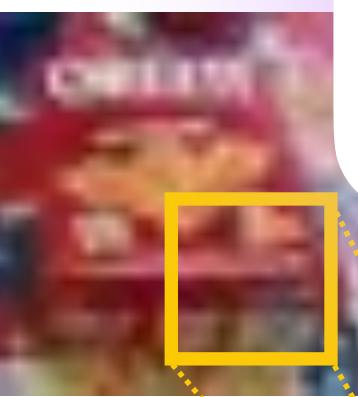


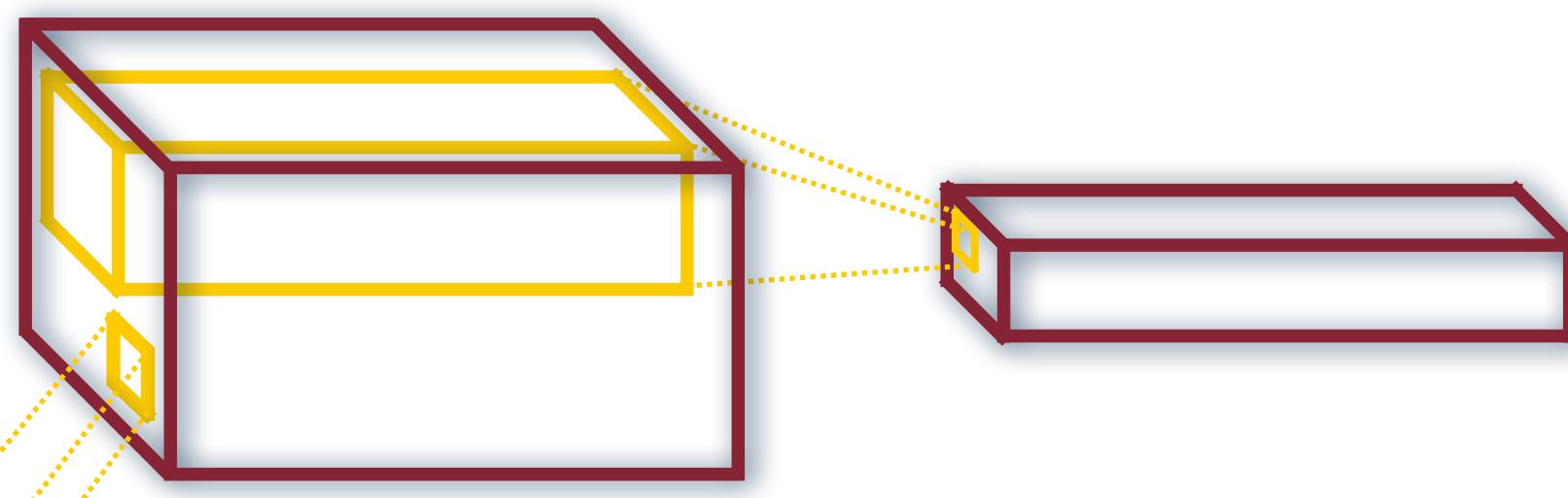
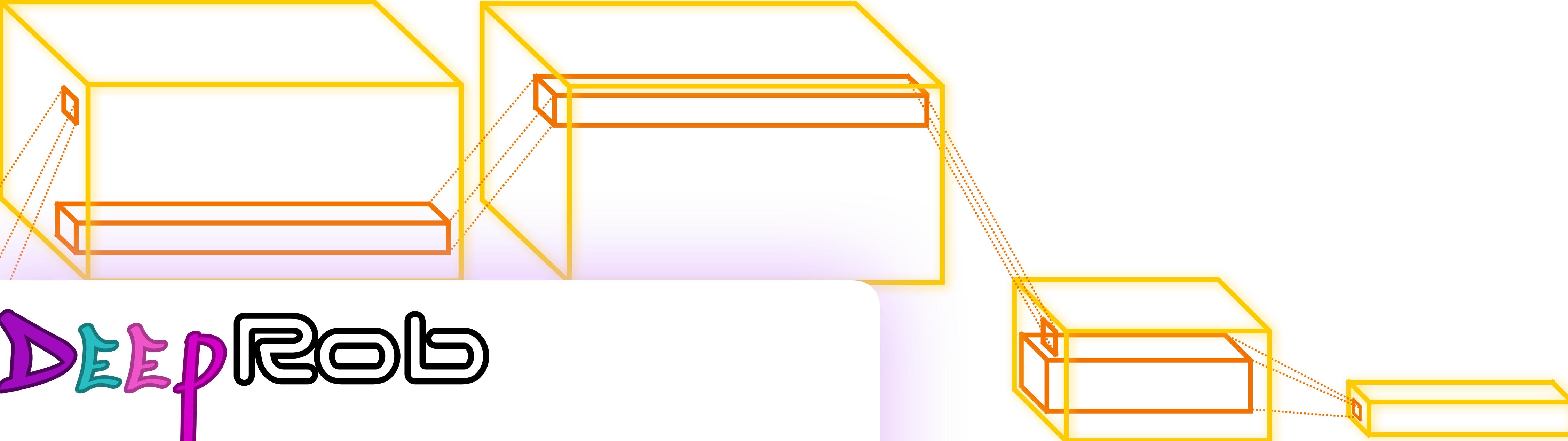


DEEPRob

Lecture 7
CNN Architectures
University of Michigan | Department of Robotics



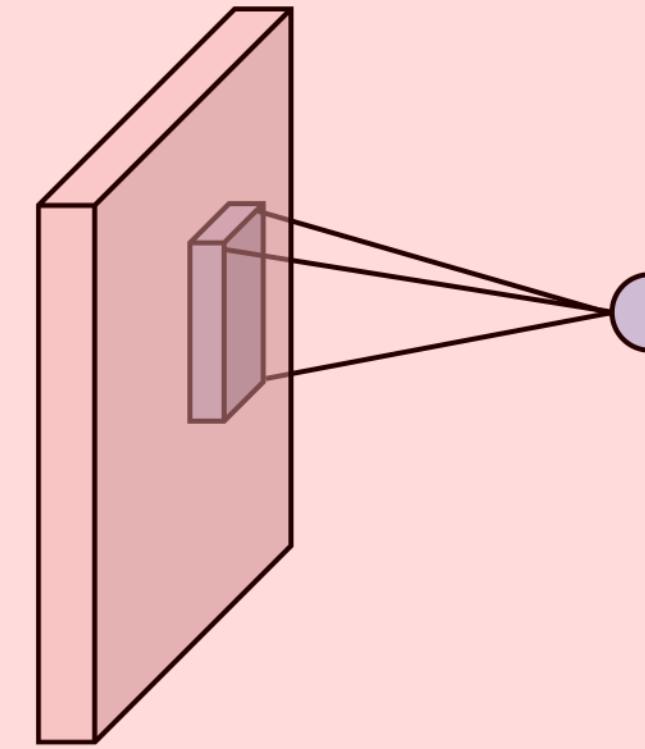
DEEPRob



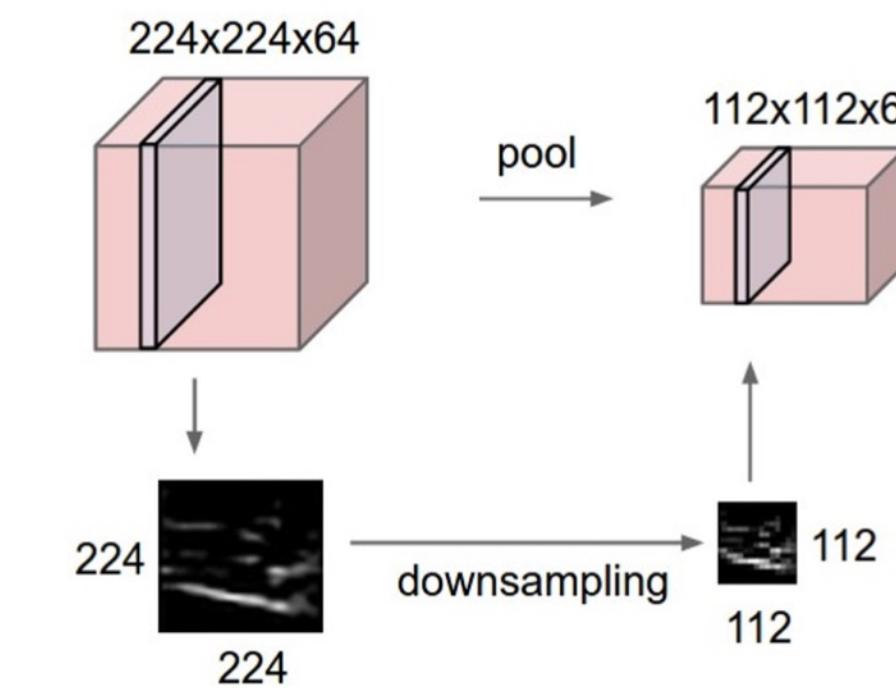


Components of Convolutional Networks

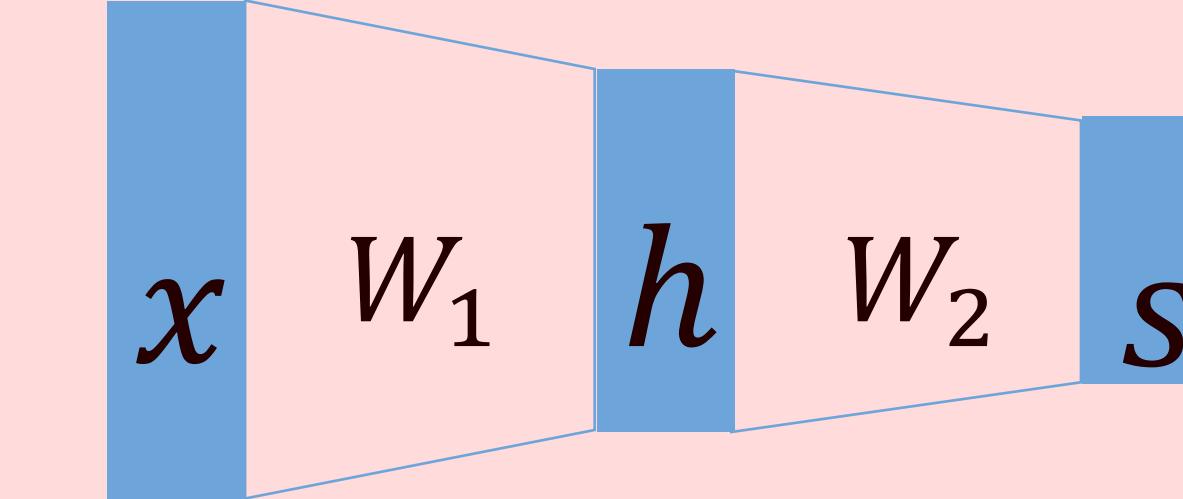
Convolution Layers



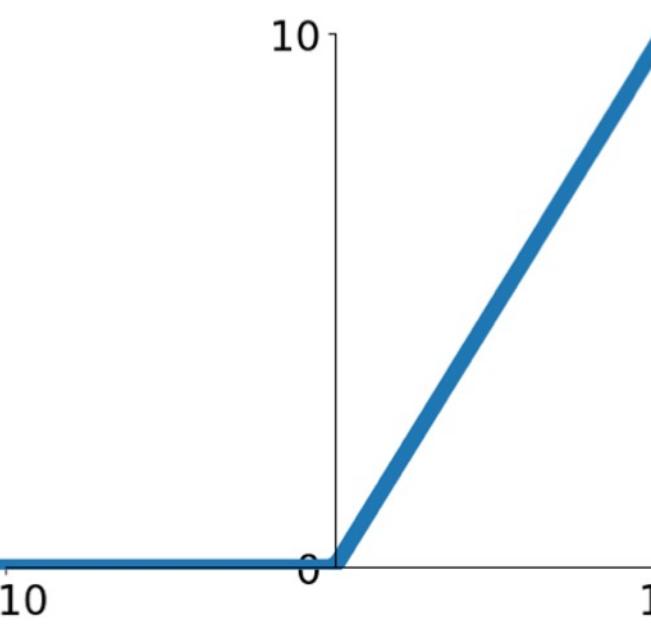
Pooling Layers



Fully-Connected Layers



Activation Function

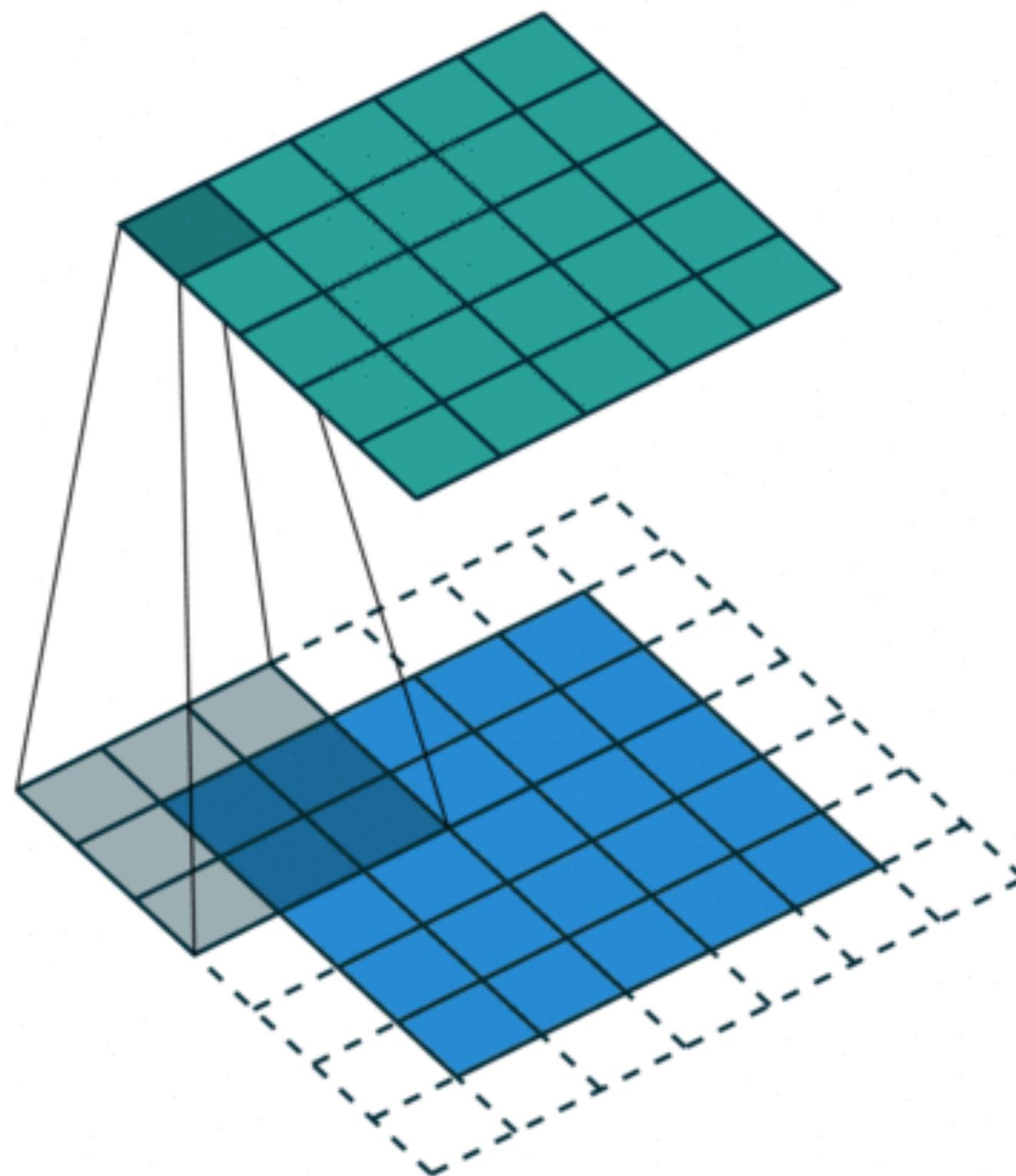


Normalization

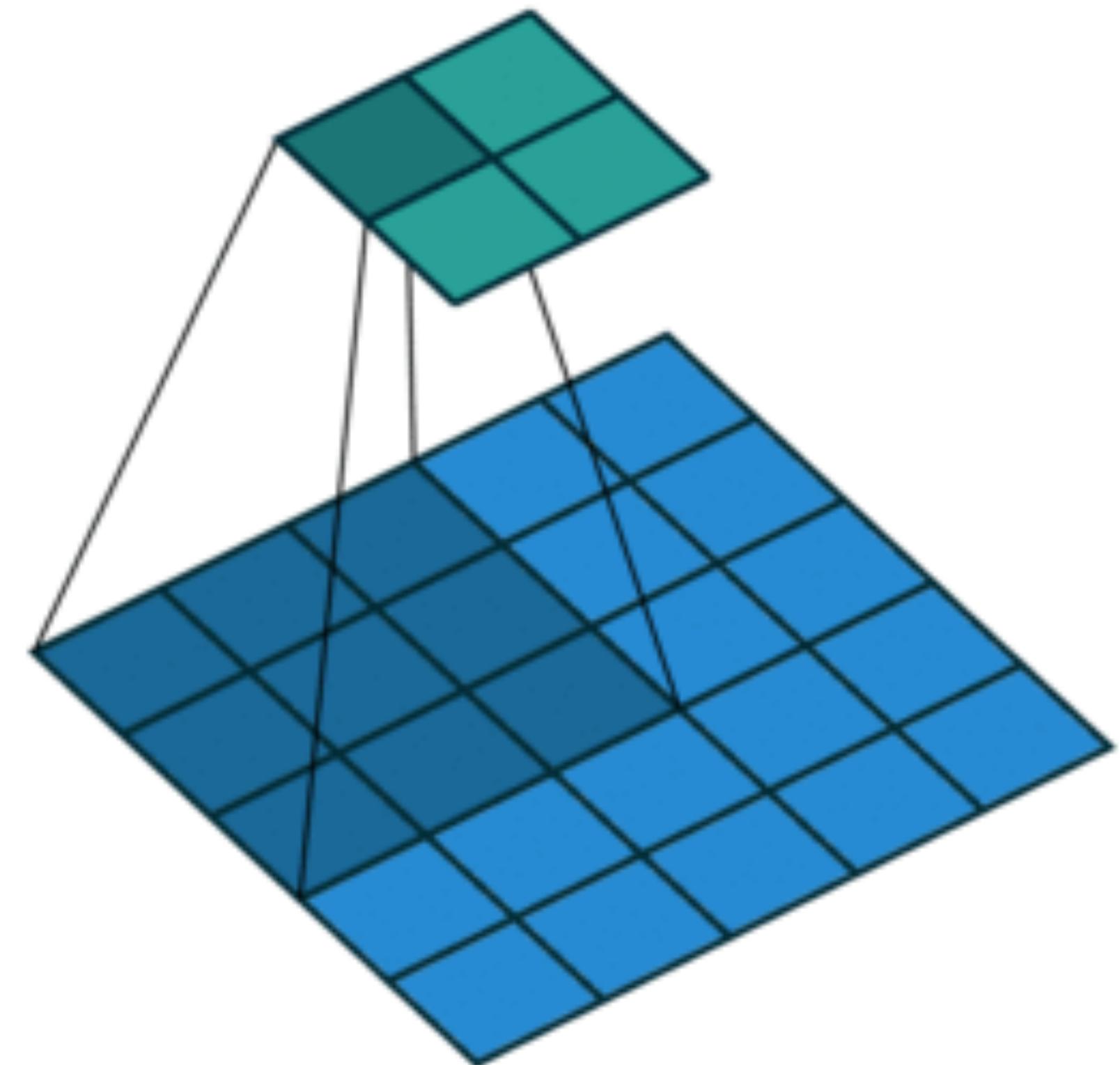
$$\hat{x}_{i,j} = \frac{x_{i,j} - \mu_j}{\sqrt{\sigma_j^2 + \epsilon}}$$



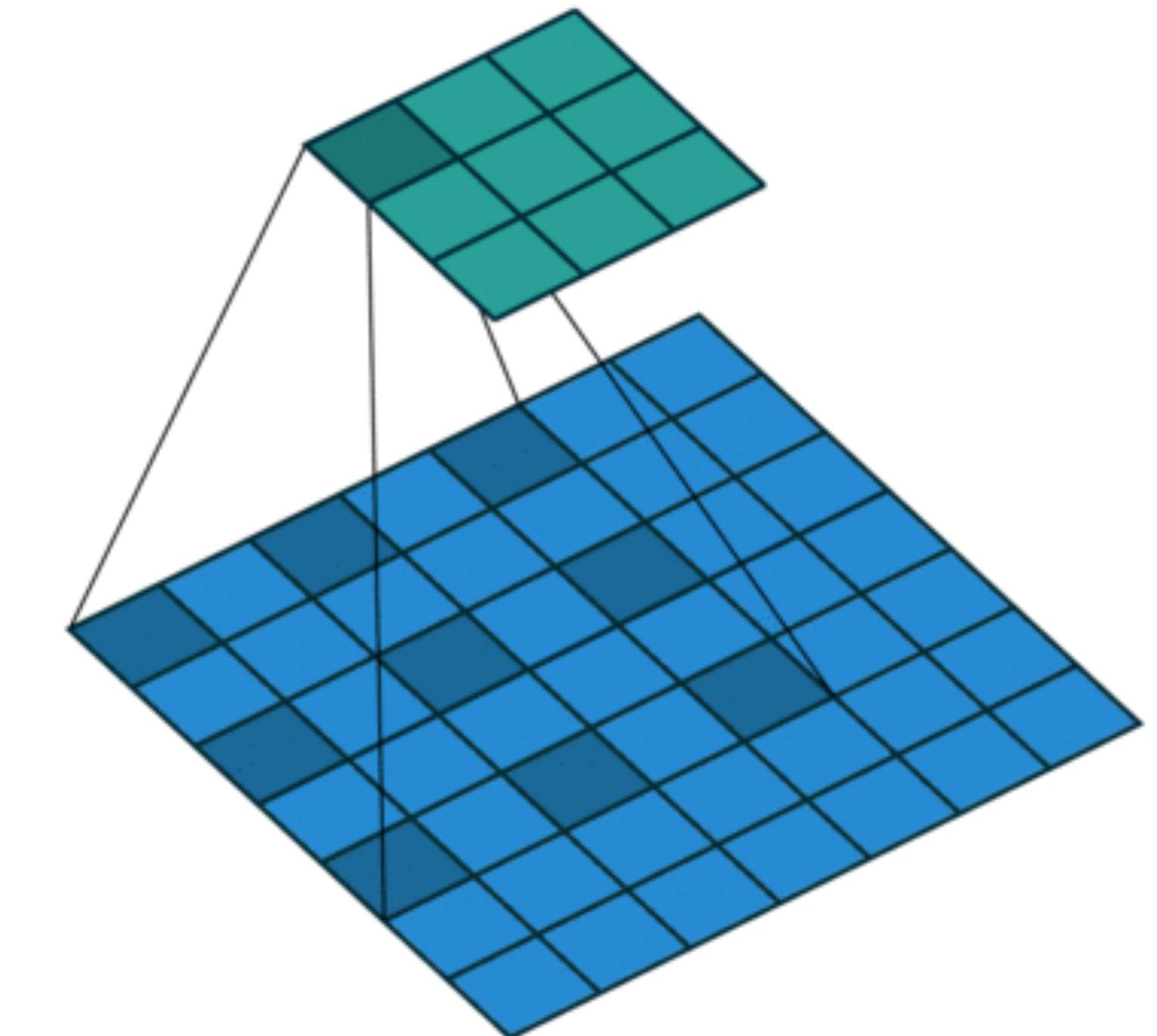
Recap: Convolution



Padding



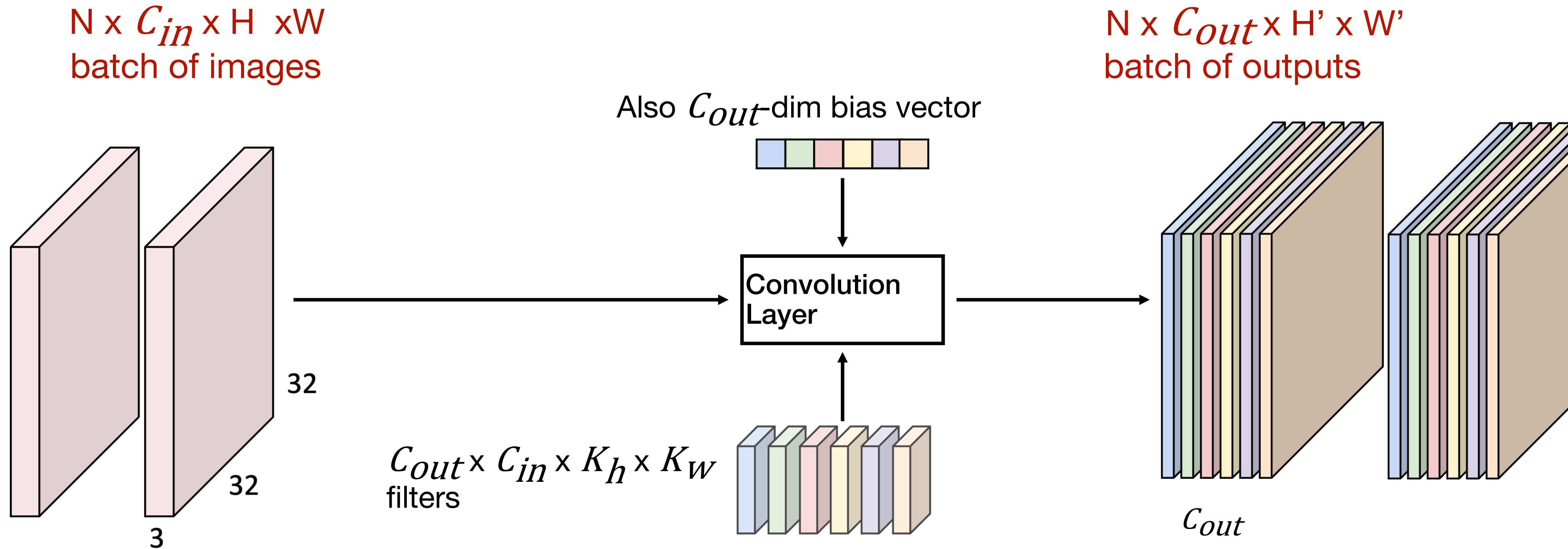
Stride = 2



dilation = 2



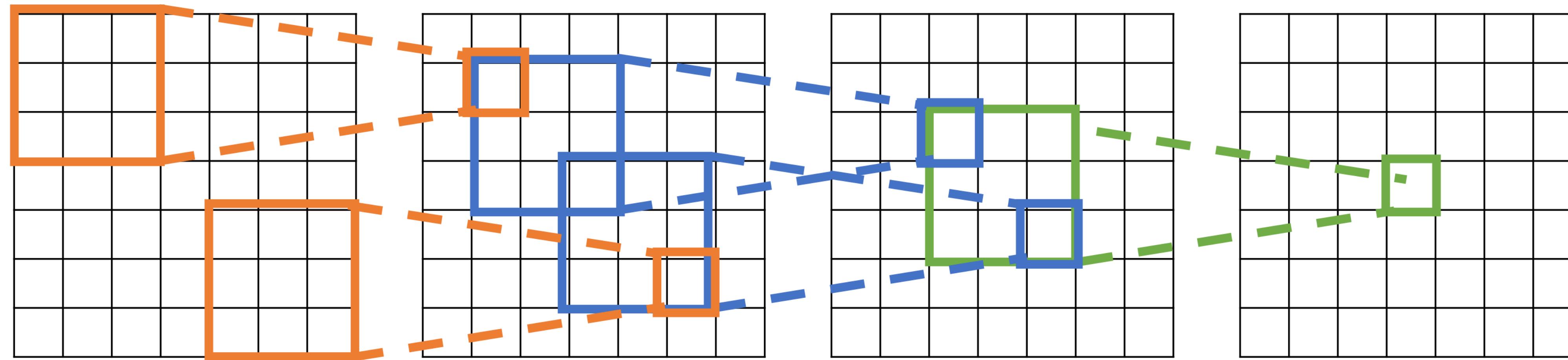
Recap: Convolution Layer Dimensions





Recap: Receptive Fields

Each successive convolution adds $K - 1$ to the receptive field size
With L layers the receptive field size is $1 + L * (K - 1)$



Input

Problem: For large images we need many layers
for each output to “see” the whole image

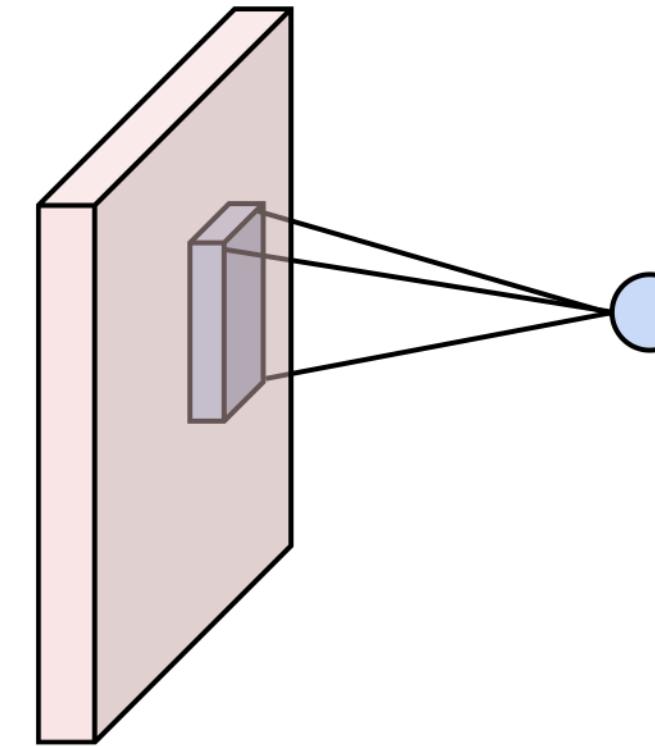
Output

Solution: Downsample inside the network

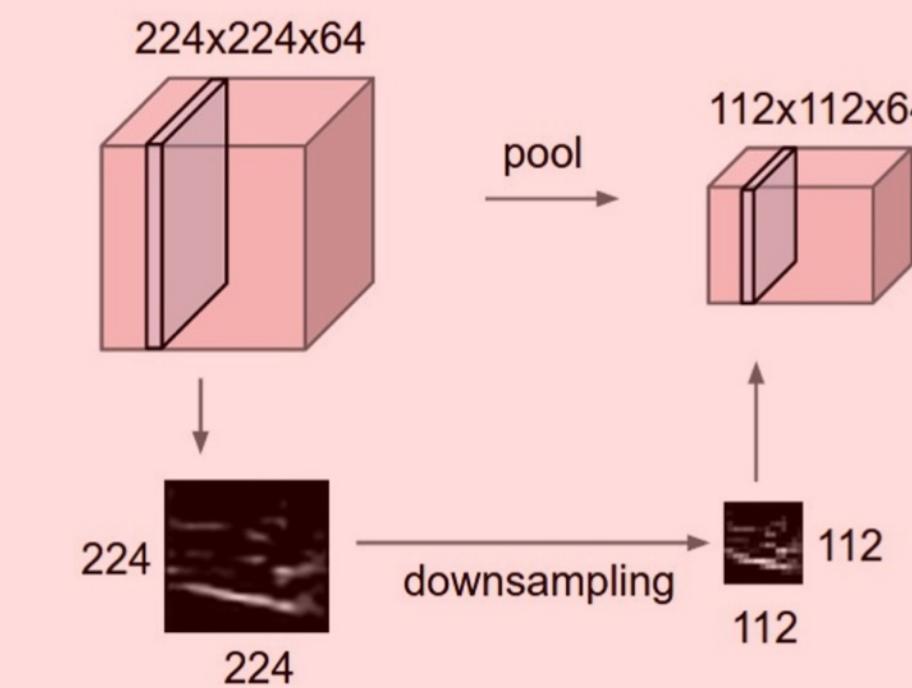


Components of Convolutional Networks

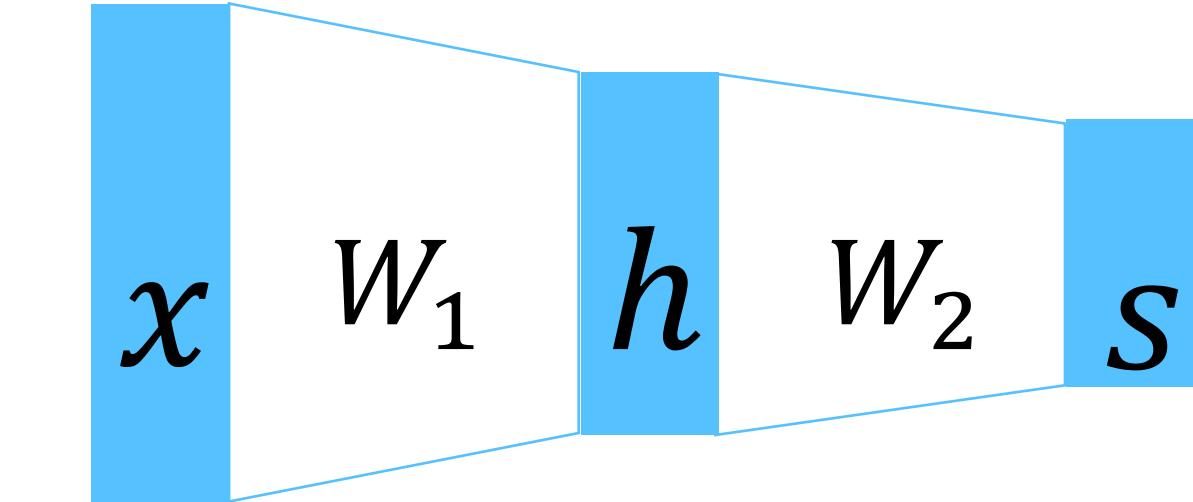
Convolution Layers



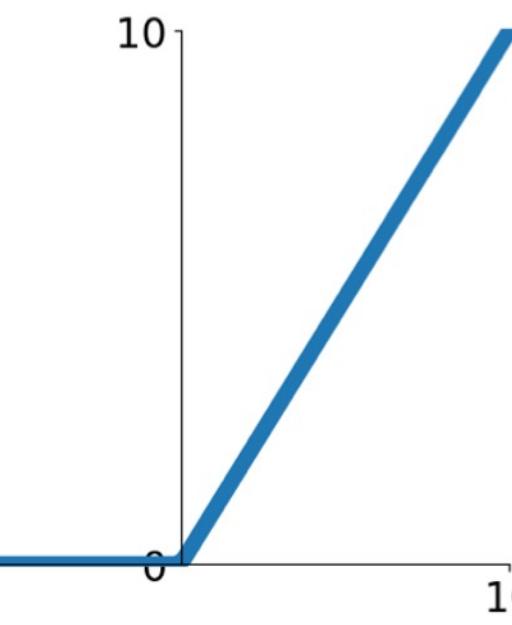
Pooling Layers



Fully-Connected Layers



Activation Function

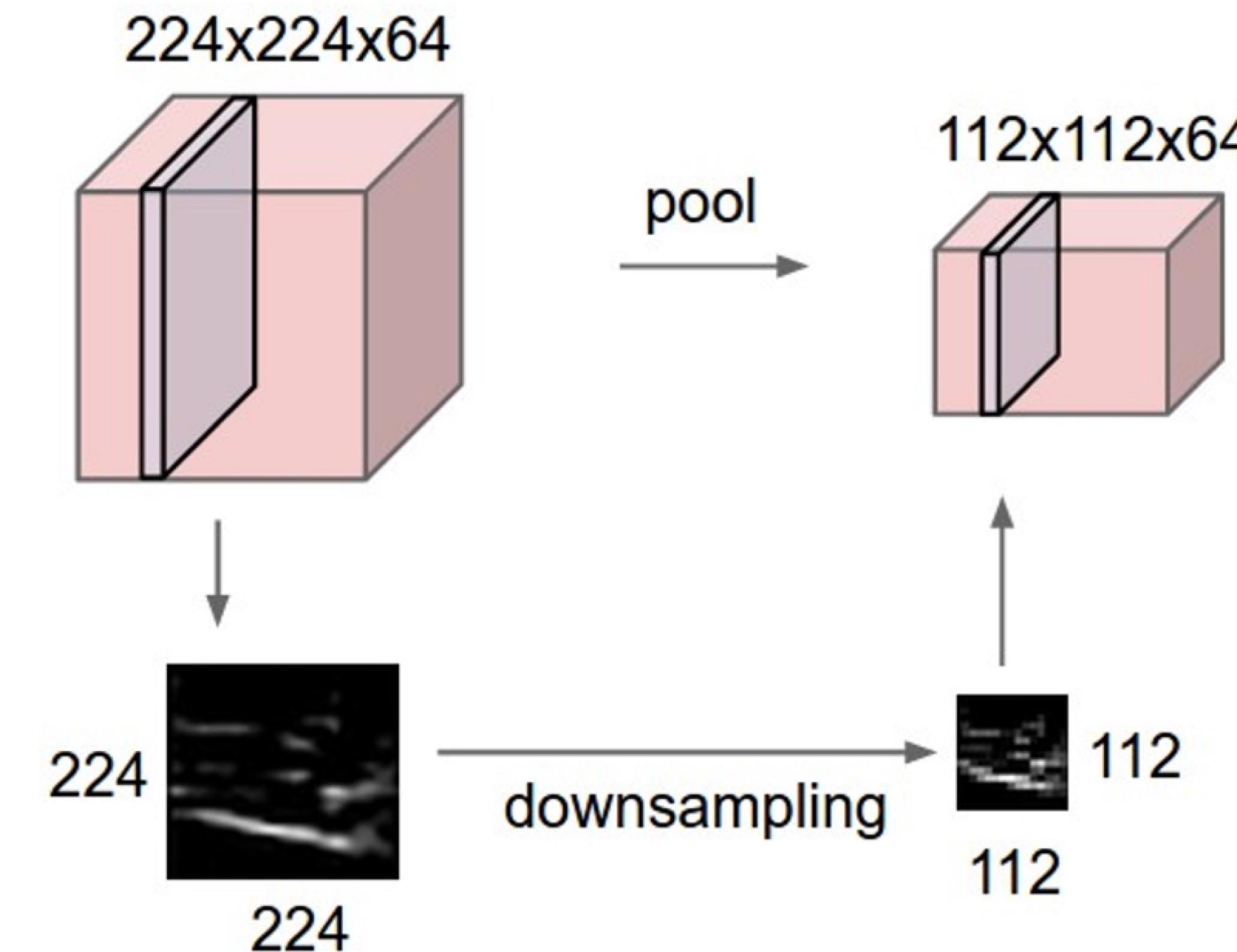


Normalization

$$\hat{x}_{i,j} = \frac{x_{i,j} - \mu_j}{\sqrt{\sigma_j^2 + \epsilon}}$$



Pooling Layers: Another way to downsample



Hyperparameters:

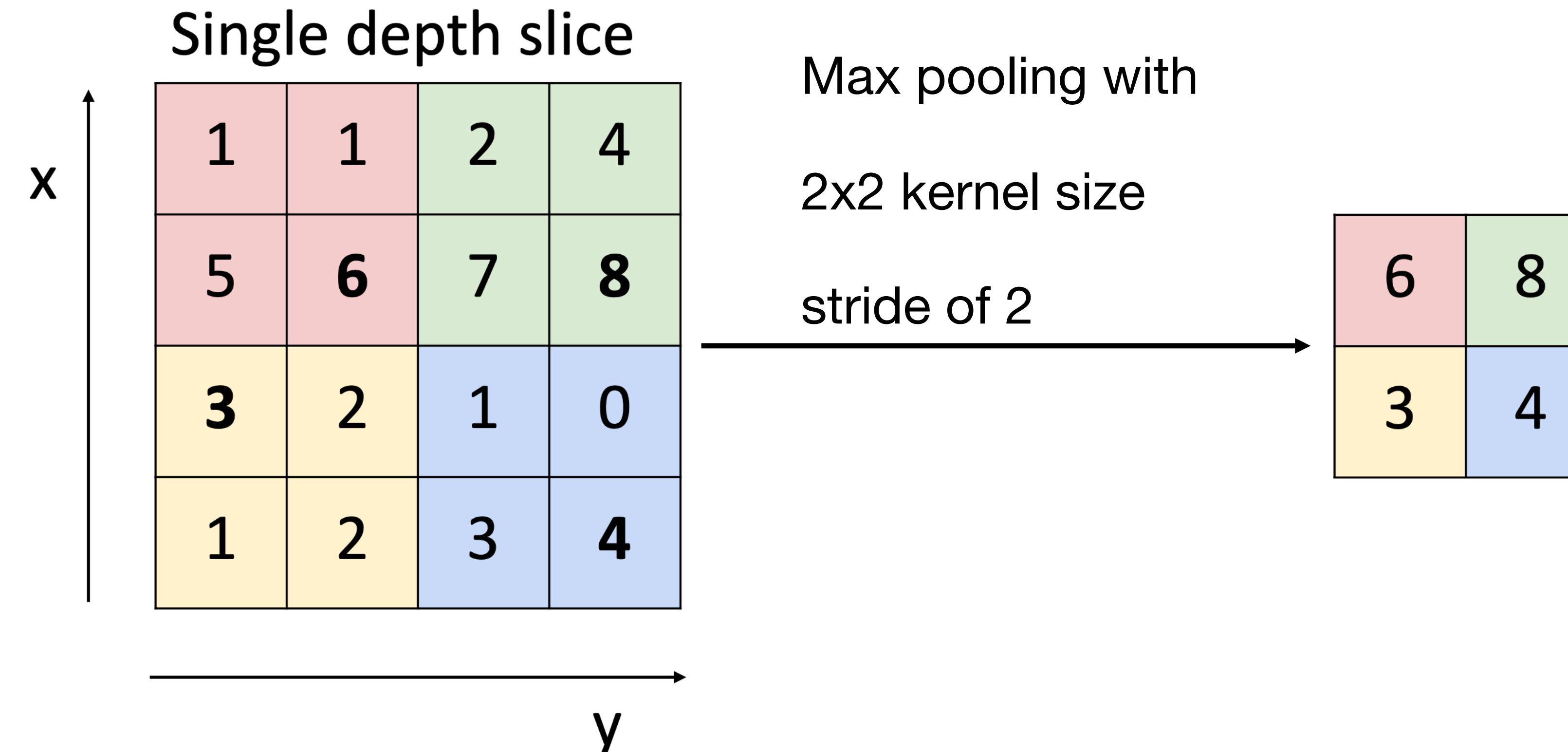
Kernel size

Stride

Pooling function

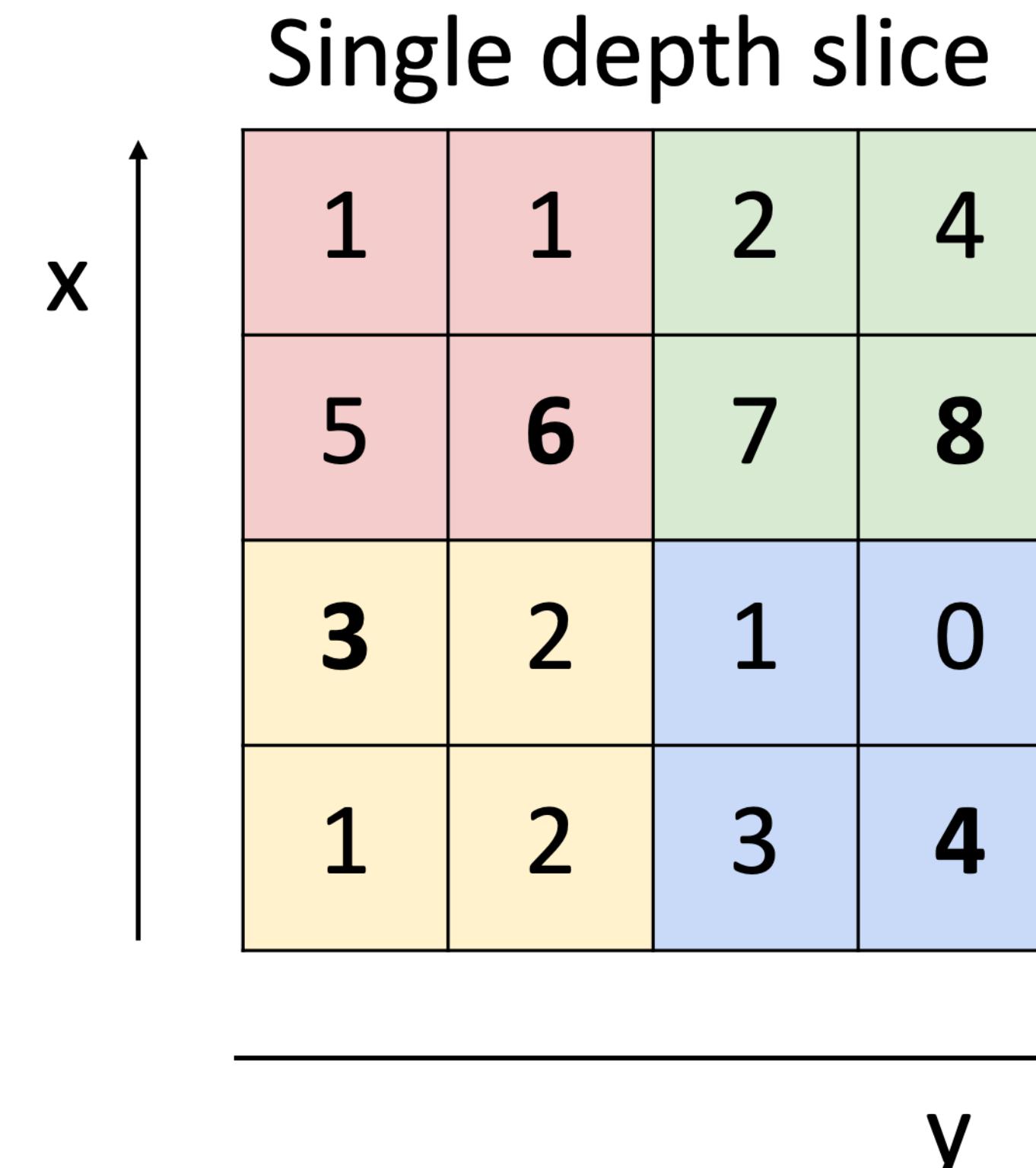


Max Pooling





Max Pooling



Max pooling with
2x2 kernel size
stride of 2

6	8
3	4

Introduces invariance to
small spatial shifts

No learnable parameters!



Pooling Summary

Input: $C \times H \times W$

Hyperparameters:

- Kernel size: K
- Stride: S
- Pooling function (max, avg)

Common settings:

max, $K = 2, S = 2$

max, $K = 3, S = 2$ (AlexNet)

Output: $C \times H' \times W'$ where

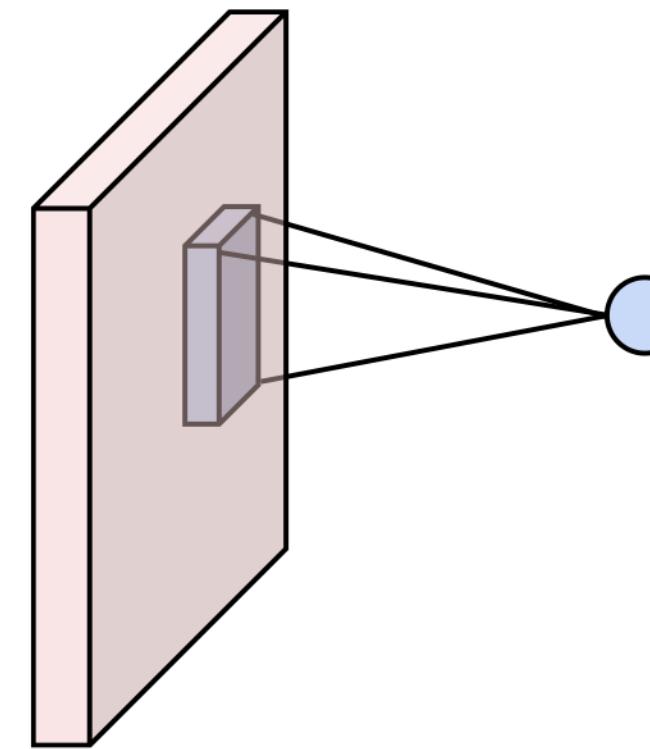
- $H' = (H - K) / S + 1$
- $W' = (W - K) / S + 1$

Learnable parameters: None!

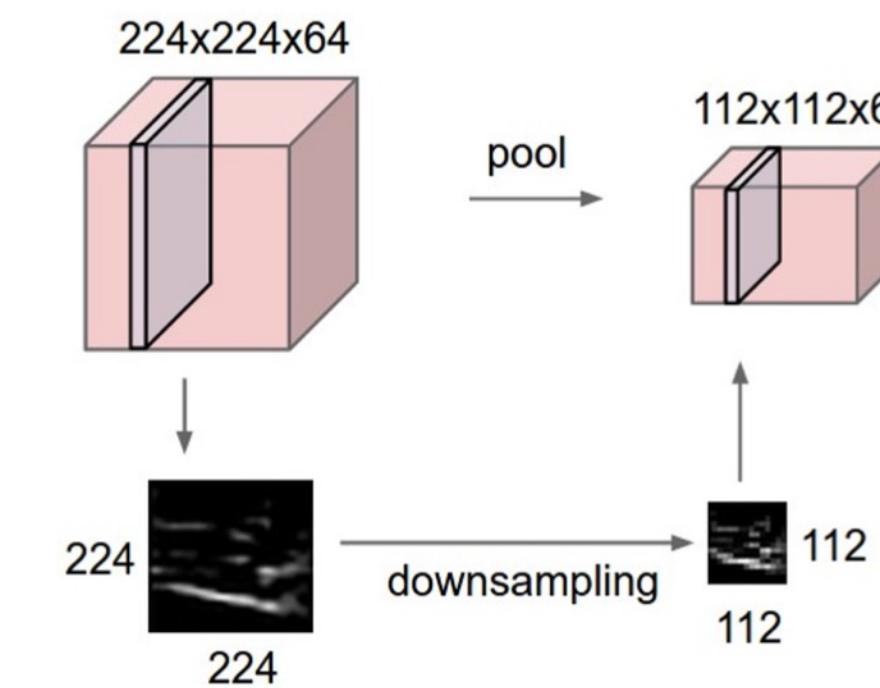


Components of Convolutional Networks

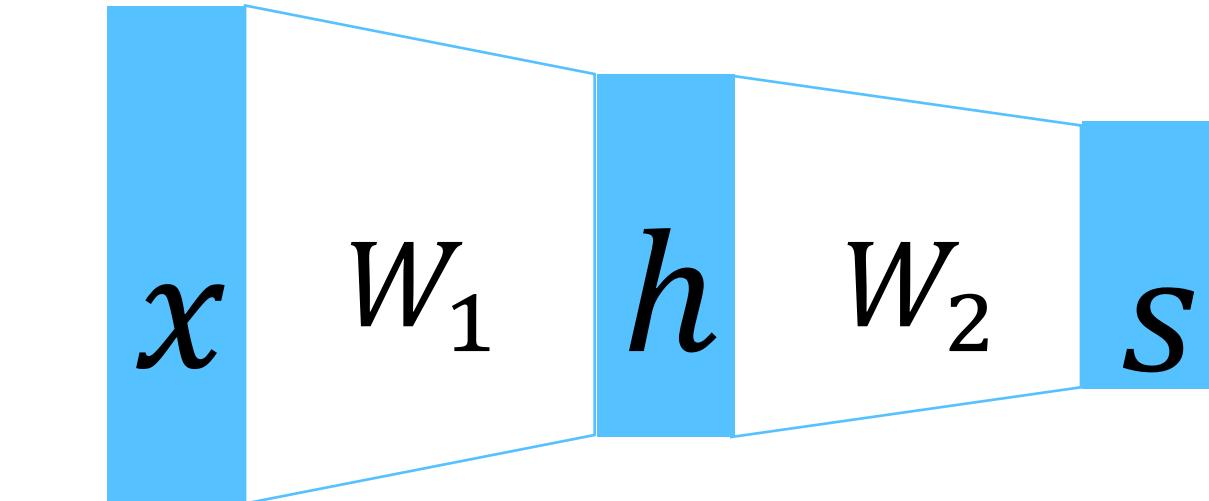
Convolution Layers



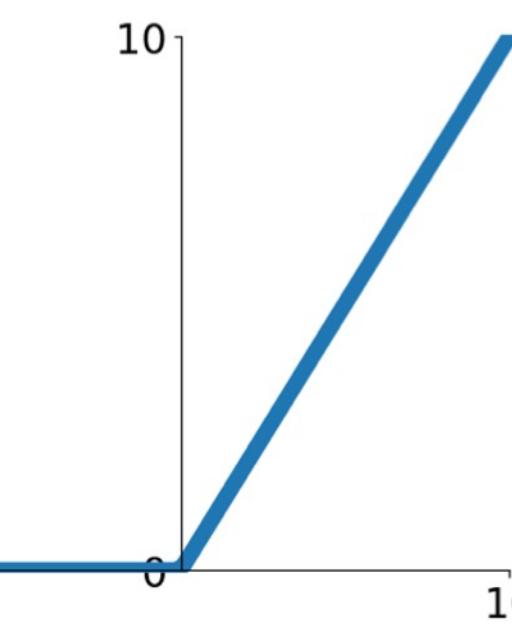
Pooling Layers



Fully-Connected Layers



Activation Function



Normalization

$$\hat{x}_{i,j} = \frac{x_{i,j} - \mu_j}{\sqrt{\sigma_j^2 + \epsilon}}$$

Problem:
Deep
Networks
very hard to
train



Batch Normalization

Consider a single layer $y = Wx$

The following could lead to tough optimization:

- Inputs x are not *centered around zero* (need large bias)
- Inputs x have different scaling per-element
(entries in W will need to vary a lot)

Idea: force inputs to be “nicely scaled” at each layer!



Batch Normalization

Idea: “Normalize” the outputs of a layer so they have zero mean and unit variance

Why? Helps reduce “internal covariate shift”, improves optimization results

We can normalize a batch of activations using:

$$\hat{x} = \frac{x - E[x]}{\sqrt{Var[x]}}$$

Ioffe and Szegedy, “Batch normalization: Accelerating deep network training by reducing internal covariate shift”, ICML 2015



Batch Normalization

Idea: “Normalize” the outputs of a layer so they have zero mean and unit variance

Why? Helps reduce “internal covariate shift”, improves optimization results

We can normalize a batch of activations using:

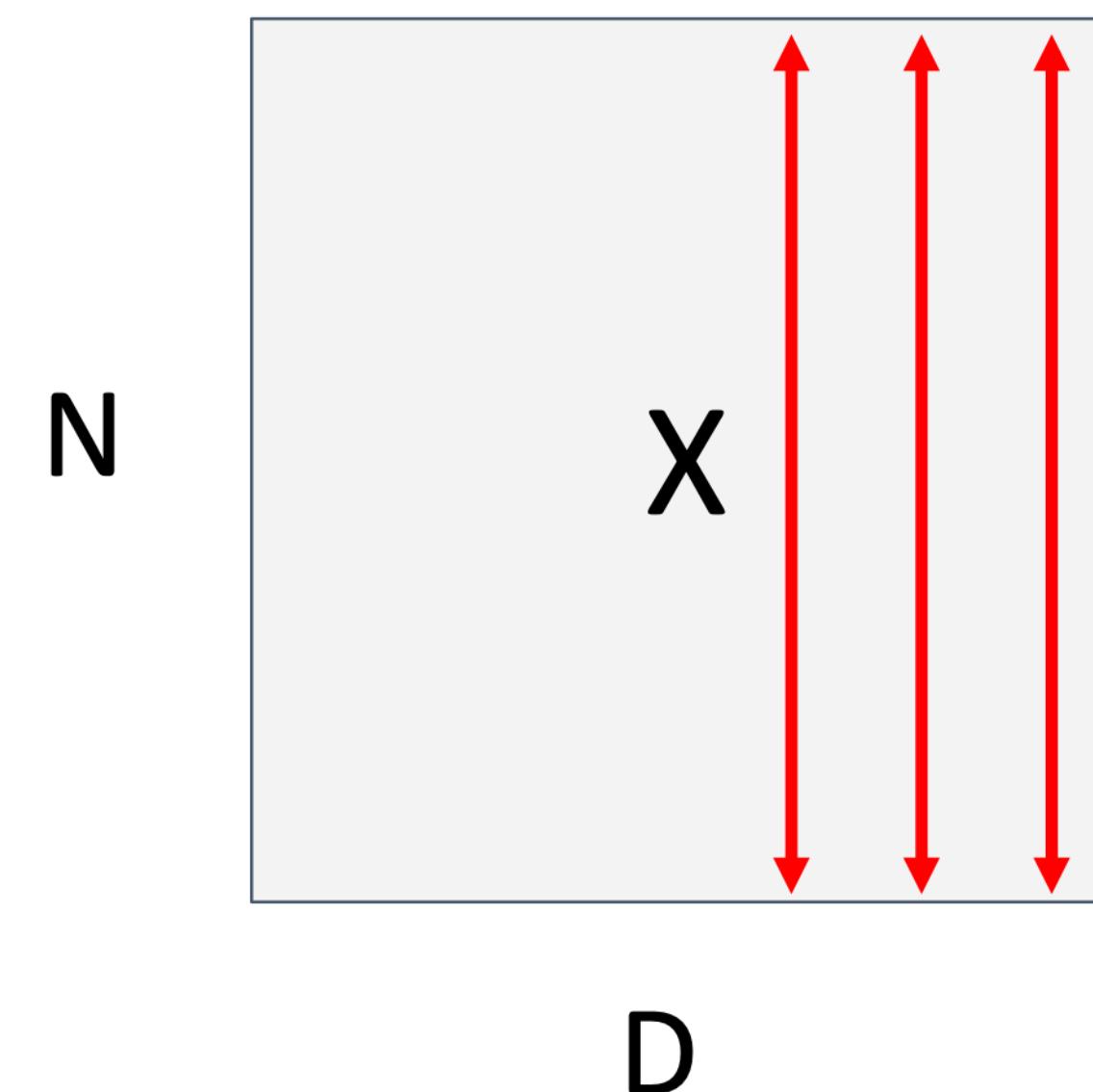
$$\hat{x} = \frac{x - E[x]}{\sqrt{Var[x]}}$$

This is a **differentiable function**, so we can use it as an operator in our networks and backdrop through it!



Batch Normalization

Input: $x \in \mathbb{R}^{N \times D}$



$$\mu_j = \frac{1}{N} \sum_{i=1}^N x_{i,j}$$

Per-channel
mean, shape is D

$$\sigma_j^2 = \frac{1}{N} \sum_{i=1}^N (x_{i,j} - \mu_j)^2$$

Per-channel
std, shape is D

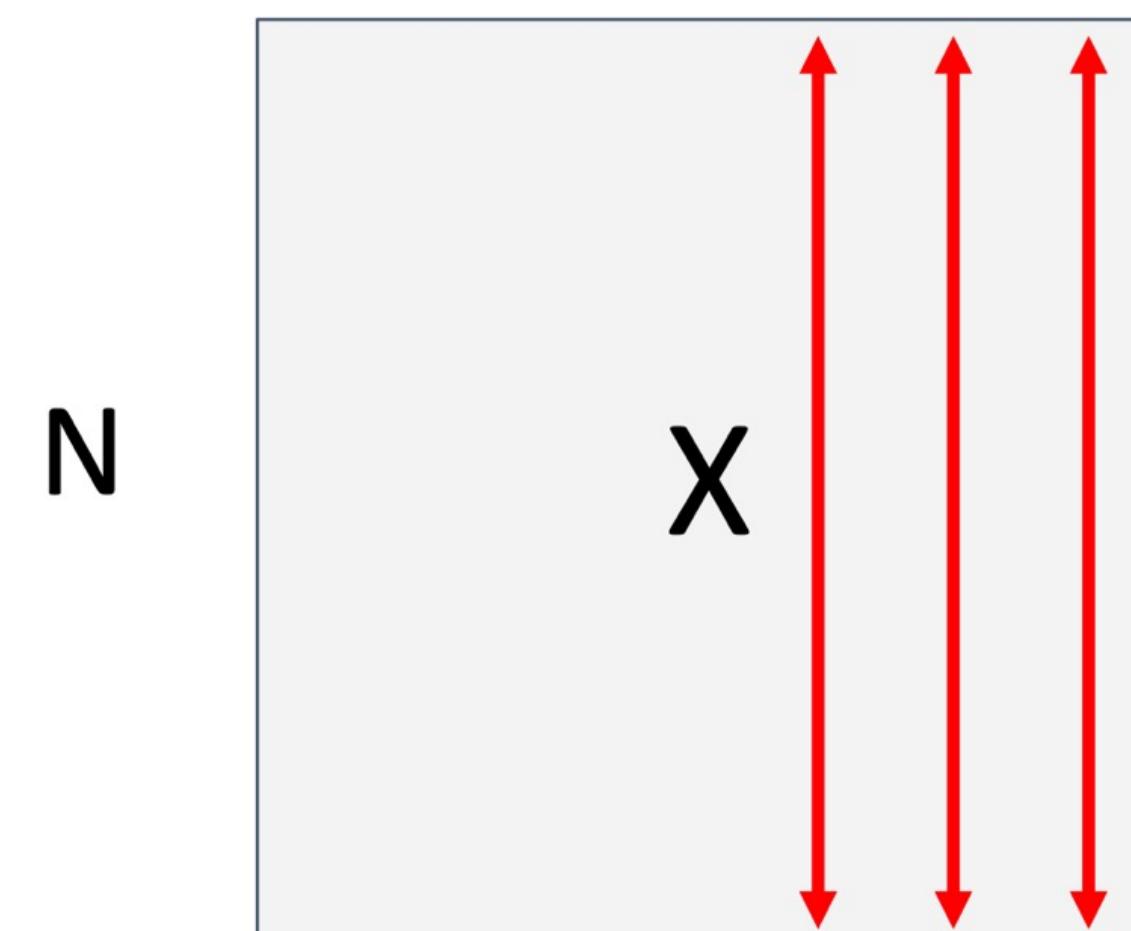
$$\hat{x}_{i,j} = \frac{x_{i,j} - \mu_j}{\sqrt{\sigma_j^2 + \epsilon}}$$

Normalized x,
Shape is N x D



Batch Normalization

Input: $x \in \mathbb{R}^{N \times D}$



$$\mu_j = \frac{1}{N} \sum_{i=1}^N x_{i,j}$$

Per-channel
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$$\sigma_j^2 = \frac{1}{N} \sum_{i=1}^N (x_{i,j} - \mu_j)^2$$

Per-channel
std, shape is D

$$\hat{x}_{i,j} = \frac{x_{i,j} - \mu_j}{\sqrt{\sigma_j^2 + \epsilon}}$$

Normalized x,
Shape is $N \times D$

Problem: What if zero-mean, unit variance is too hard of a constraint?



Batch Normalization

Input: $x \in \mathbb{R}^{N \times D}$

$$\mu_j = \frac{1}{N} \sum_{i=1}^N x_{i,j}$$

Per-channel
mean, shape is D

Add **Learnable scale and shift parameters:**

$$\gamma, \beta \in \mathbb{R}^D$$

Learning $\gamma = \sigma$, $\beta = \mu$ will recover the identity function (in expectation)

$$\sigma_j^2 = \frac{1}{N} \sum_{i=1}^N (x_{i,j} - \mu_j)^2$$

Per-channel
std, shape is D

$$\hat{x}_{i,j} = \frac{x_{i,j} - \mu_j}{\sqrt{\sigma_j^2 + \epsilon}}$$

Normalized x,
Shape is N x D

$$y_{i,j} = \gamma_j \hat{x}_{i,j} + \beta_j$$

Output,
Shape is N x D



Batch Normalization

Input: $x \in \mathbb{R}^{N \times D}$

Learnable scale and shift parameters:

$$\gamma, \beta \in \mathbb{R}^D$$

Learning $\gamma = \sigma$, $\beta = \mu$ will recover the identity function (in expectation)

$$\mu_j = \frac{1}{N} \sum_{i=1}^N x_{i,j}$$

Per-channel mean, shape is D

$$\sigma_j^2 = \frac{1}{N} \sum_{i=1}^N (x_{i,j} - \mu_j)^2$$

Per-channel std, shape is D

$$\hat{x}_{i,j} = \frac{x_{i,j} - \mu_j}{\sqrt{\sigma_j^2 + \epsilon}}$$

Normalized x,
Shape is N x D

$$y_{i,j} = \gamma_j \hat{x}_{i,j} + \beta_j$$

Output,
Shape is N x D

Problem: Estimates depend on minibatch; can't run layer at test-time!



Batch Normalization: Test-Time

Input: $x \in \mathbb{R}^{N \times D}$

Learnable scale and shift parameters:

$\gamma, \beta \in \mathbb{R}^D$

Learning $\gamma = \sigma, \beta = \mu$ will recover the identity function (in expectation)

$$\mu_j = \boxed{\text{(Running) average of values seen during training}}$$

Per-channel mean, shape is D

$$\sigma_j^2 = \boxed{\text{(Running) average of values seen during training}}$$

Per-channel std, shape is D

$$\hat{x}_{i,j} = \frac{x_{i,j} - \mu_j}{\sqrt{\sigma_j^2 + \epsilon}}$$

Normalized x,
Shape is N x D

$$y_{i,j} = \gamma_j \hat{x}_{i,j} + \beta_j$$

Output,
Shape is N x D



Batch Normalization: Test-Time

Input: $x \in \mathbb{R}^{N \times D}$

μ_j = (Running) average of
values seen during
training

Per-channel
mean, shape is D

**Learnable scale and
shift parameters:**

$\gamma, \beta \in \mathbb{R}^D$

In practice, usually momentum = 0.99

```
moving_mean = moving_mean * momentum + batch_mean * (1 - momentum)  
moving_var = moving_var * momentum + batch_var * (1 - momentum)
```



Batch Normalization: Test-Time

Input: $x \in \mathbb{R}^{N \times D}$

μ_j = (Running) average of values seen during training

Per-channel mean, shape is D

Learnable scale and shift parameters:

$$\gamma, \beta \in \mathbb{R}^D$$

Learning $\gamma = \sigma$, $\beta = \mu$ will recover the identity function (in expectation)

$$\mu_j^{test} = 0$$

For each training iteration:

$$\mu_j = \frac{1}{N} \sum_{i=1}^N x_{i,j}$$

$$\mu_j^{test} = 0.99 \mu_j^{test} + 0.01 \mu_j$$

(Similar for σ)



Batch Normalization: Test-Time

Input: $x \in \mathbb{R}^{N \times D}$

μ_j = (Running) average of values seen during training

Per-channel mean, shape is D

Learnable scale and shift parameters:

$\gamma, \beta \in \mathbb{R}^D$

σ_j^2 = (Running) average of values seen during training

Per-channel std, shape is D

During testing batchnorm becomes a linear operator!

Can be fused with the previous fully-connected or conv layer

$$\hat{x}_{i,j} = \frac{x_{i,j} - \mu_j}{\sqrt{\sigma_j^2 + \epsilon}}$$

Normalized x,
Shape is N x D

$$y_{i,j} = \gamma_j \hat{x}_{i,j} + \beta_j$$

Output,
Shape is N x D



Batch Normalization for ConvNets

Batch Normalization for
fully-connected networks

$$x : N \times D$$

Normalize

$$\mu, \sigma : 1 \times D$$
$$\gamma, \beta : 1 \times D$$
$$y = \frac{(x - \mu)}{\sigma} \gamma + \beta$$

Batch Normalization for
convolutional networks
(Spatial Batchnorm, BatchNorm2D)

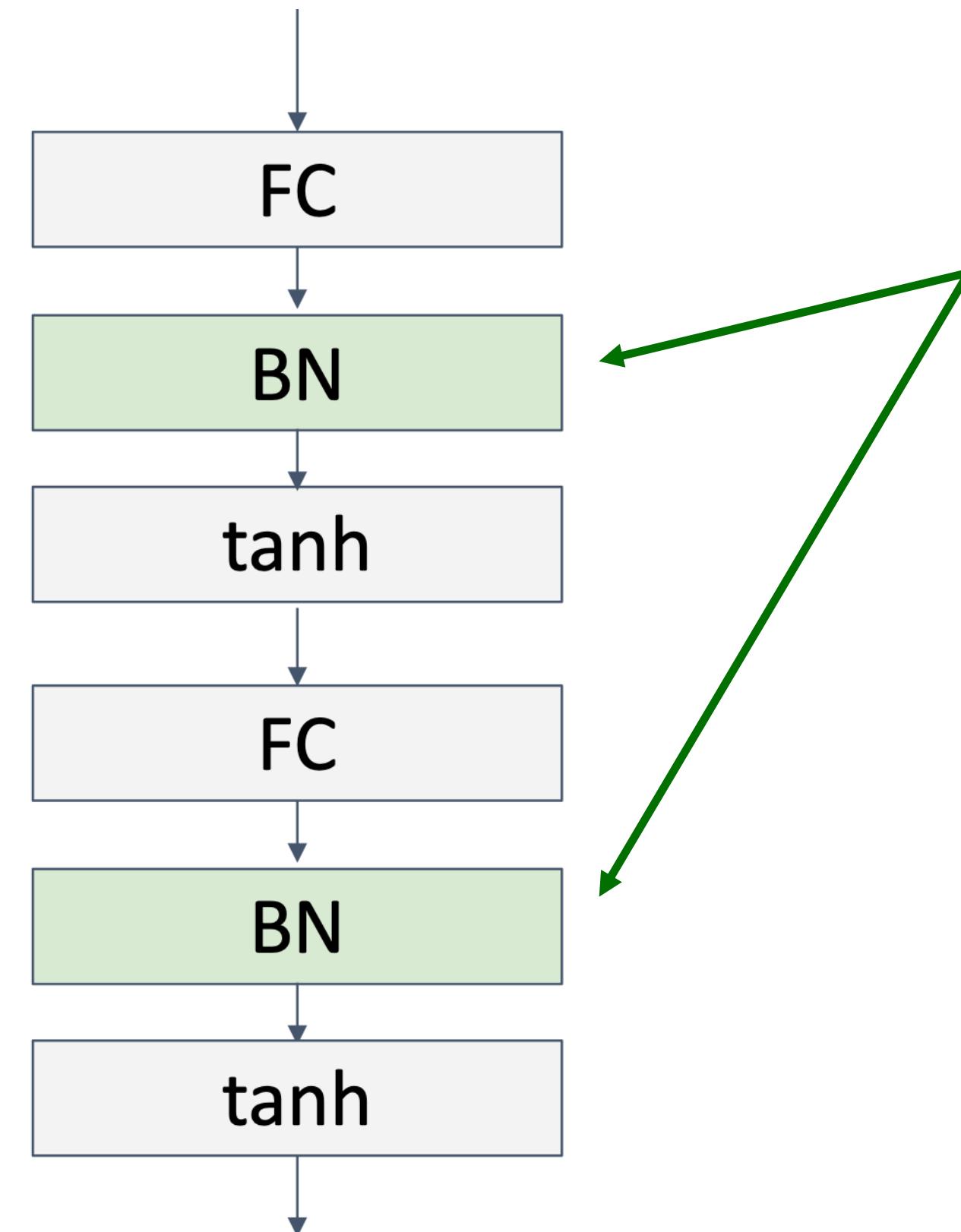
$$x : N \times C \times H \times W$$

Normalize

$$\mu, \sigma : 1 \times C \times 1 \times 1$$
$$\gamma, \beta : 1 \times C \times 1 \times 1$$
$$y = \frac{(x - \mu)}{\sigma} \gamma + \beta$$



Batch Normalization

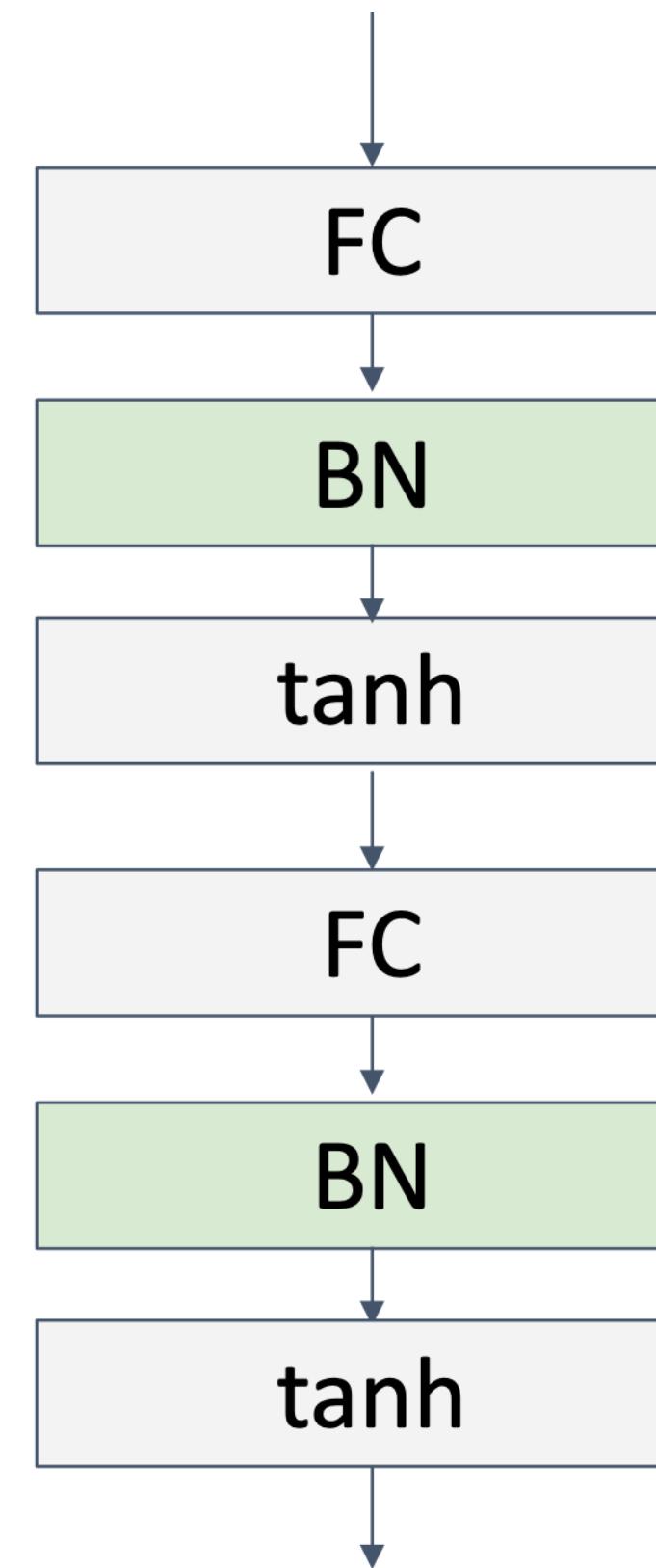


Usually inserted **after** Fully Connected or
Convolutional layers, and **before** nonlinearity

$$\hat{x} = \frac{x - E[x]}{\sqrt{Var[x]}}$$

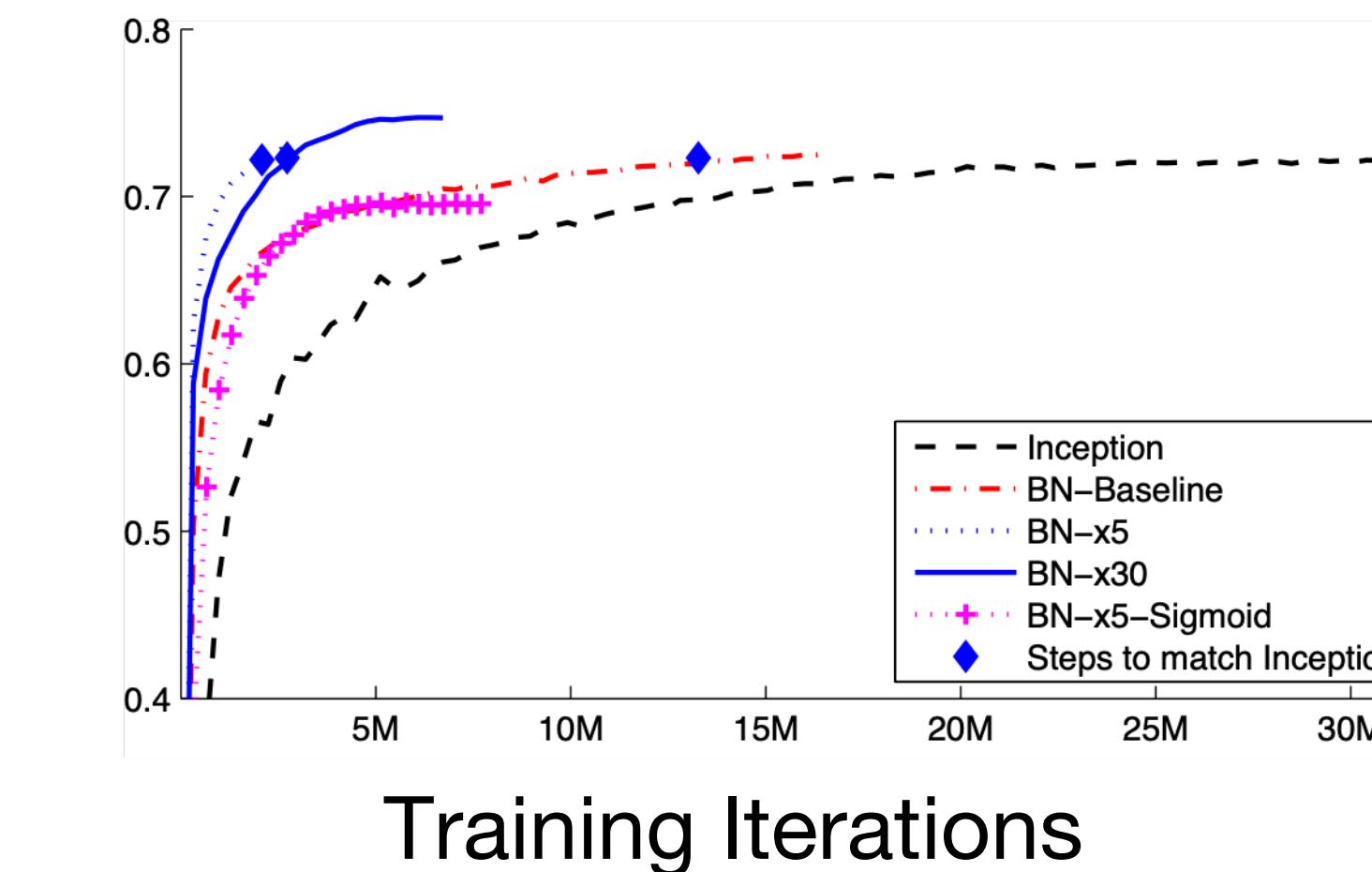


Batch Normalization



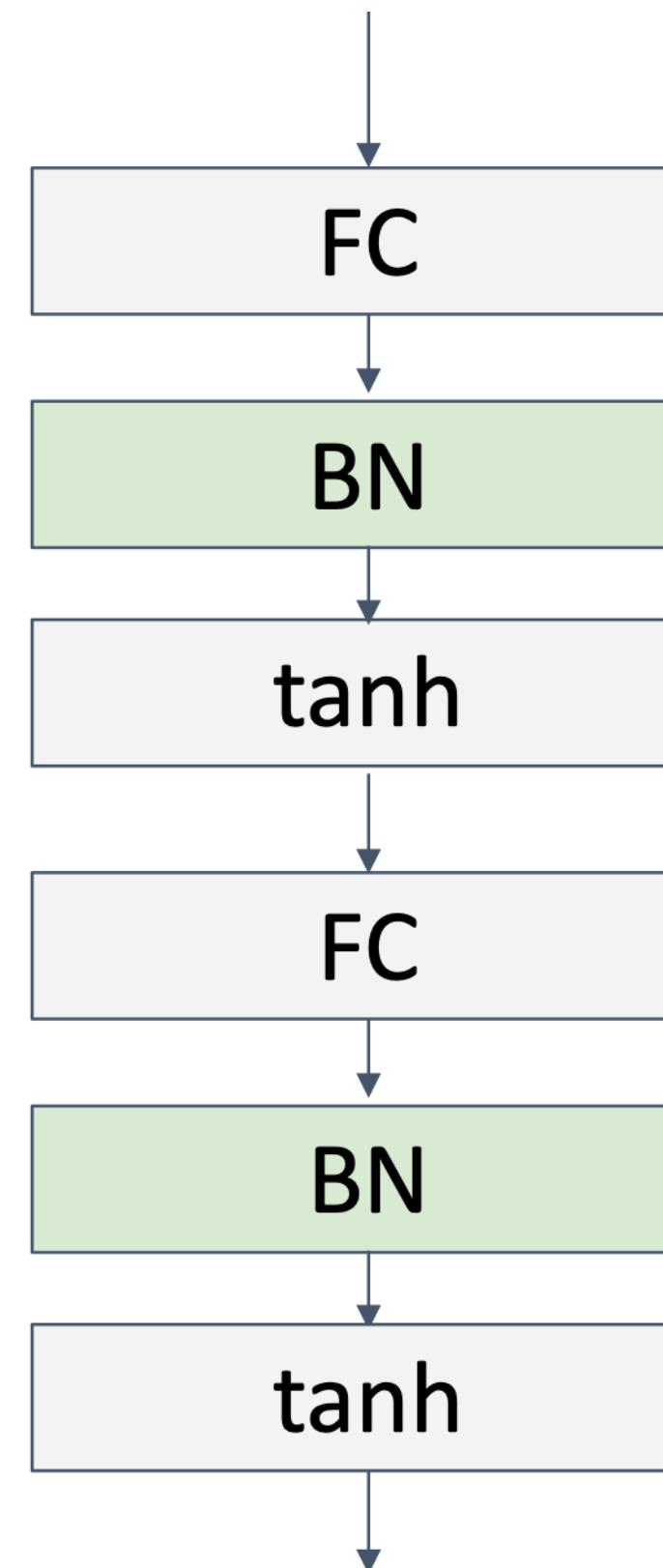
- Makes deep networks much easier to train!
- Allows higher learning rates, faster convergence
- Networks become more robust to initialization
- Acts as regularization during training
- Zero overhead at test-time: can be fused with conv

ImageNet
Classification
Accuracy





Batch Normalization



- Makes deep networks much easier to train!
- Allows higher learning rates, faster convergence
- Networks become more robust to initialization
- Acts as regularization during training
- Zero overhead at test-time: can be fused with conv
- Not well-understood theoretically (yet, still lots of debate!)
- Behaves differently during training and testing: very common source of bugs!



Layer Normalization

Batch Normalization for
fully-connected networks

Layer Normalization for fully-
connected networks
Same behavior at train and test!
Used in RNNs, Transformers

$$x : N \times D$$

Normalize

$$\mu, \sigma : 1 \times D$$

$$\gamma, \beta : 1 \times D$$
$$y = \frac{(x - \mu)}{\sigma} \gamma + \beta$$

$$x : N \times D$$

Normalize

$$\mu, \sigma : N \times 1$$

$$\gamma, \beta : 1 \times D$$
$$y = \frac{(x - \mu)}{\sigma} \gamma + \beta$$



Instance Normalization

Batch Normalization for convolutional networks

$$x : N \times C \times H \times W$$

Normalize

$$\mu, \sigma : 1 \times C \times 1 \times 1$$
$$\gamma, \beta : 1 \times C \times 1 \times 1$$

$$y = \frac{(x - \mu)}{\sigma} \gamma + \beta$$

Instance Normalization for convolutional networks

$$x : N \times C \times H \times W$$

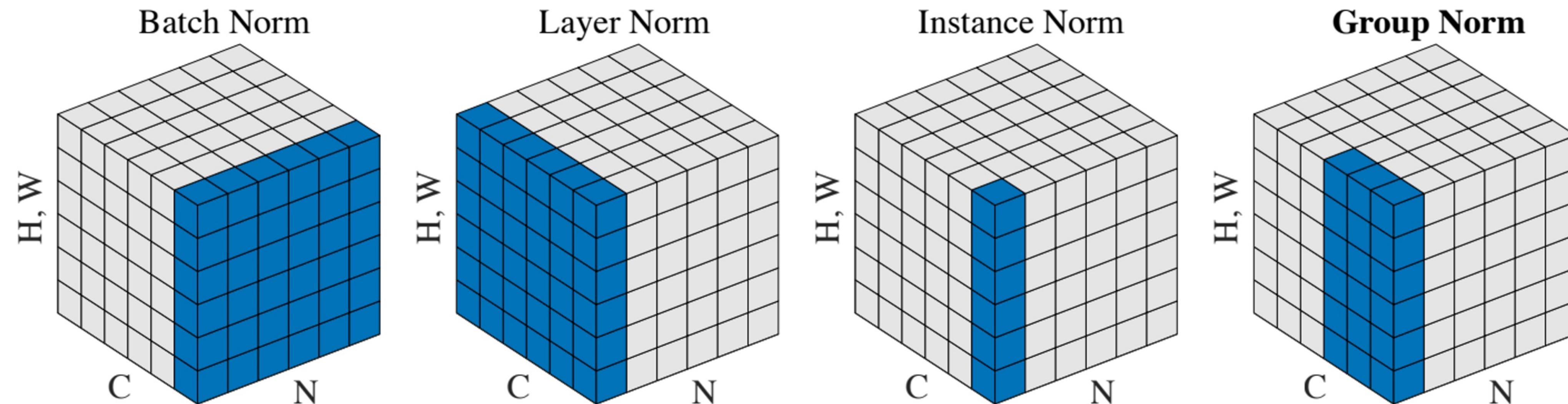
Normalize

$$\mu, \sigma : N \times C \times 1 \times 1$$
$$\gamma, \beta : 1 \times C \times 1 \times 1$$

$$y = \frac{(x - \mu)}{\sigma} \gamma + \beta$$

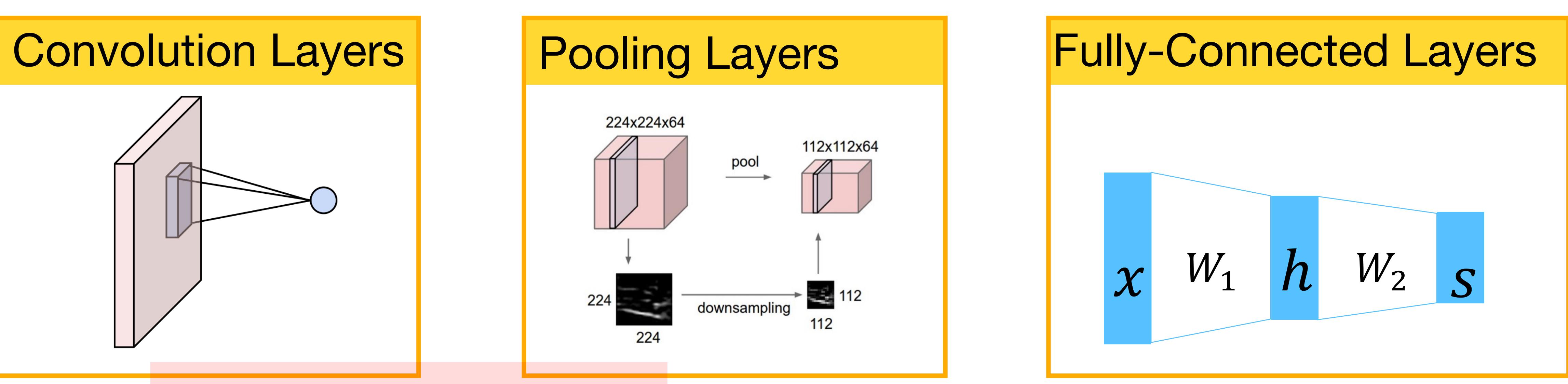


Group Normalization





Components of Convolutional Networks



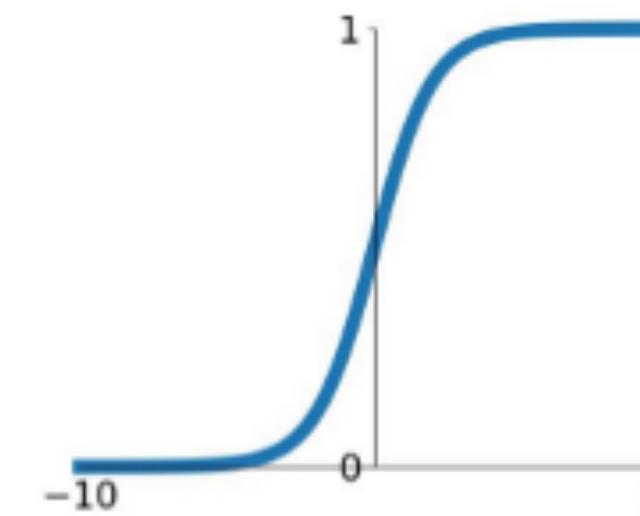
Problem:
Deep
Networks
very hard to
train



Activation Functions

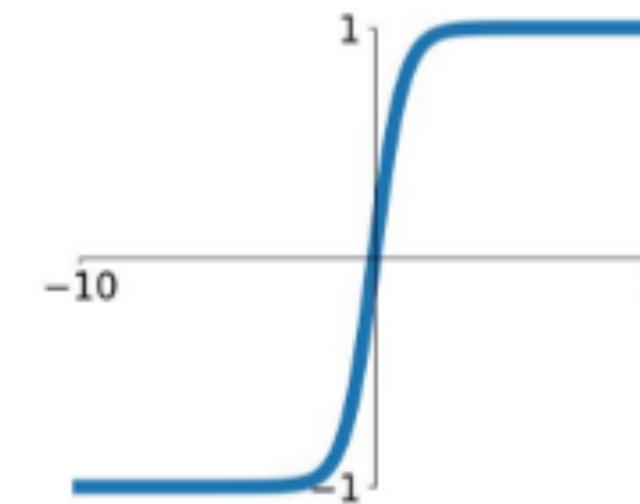
Sigmoid

$$\sigma(x) = \frac{1}{1+e^{-x}}$$



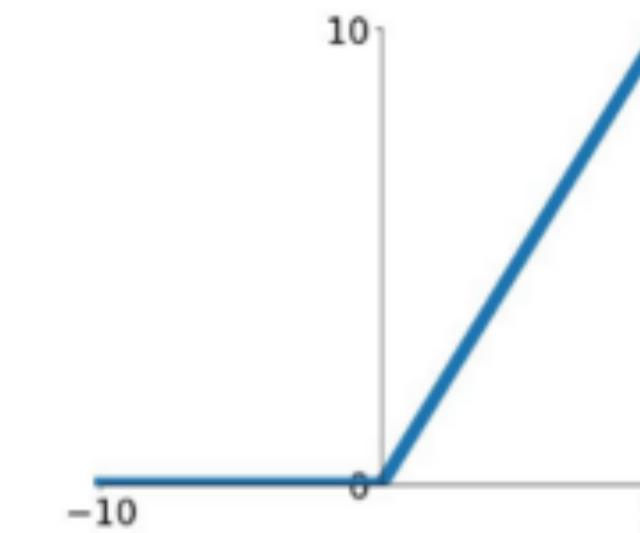
tanh

$$\tanh(x)$$



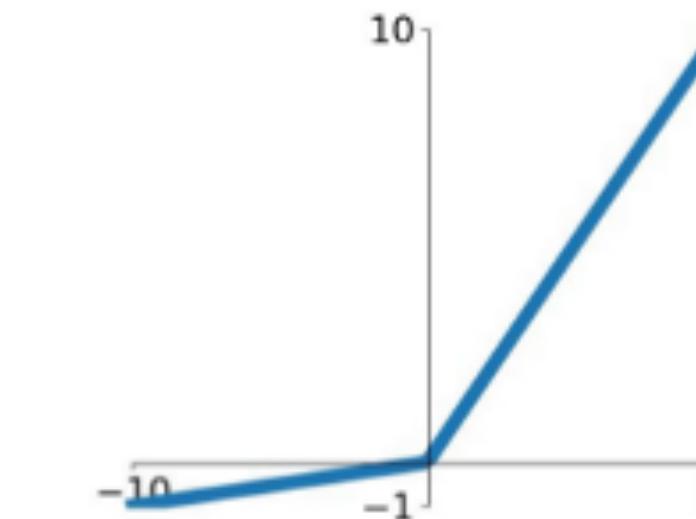
ReLU

$$\max(0, x)$$



Leaky ReLU

$$\max(0.1x, x)$$

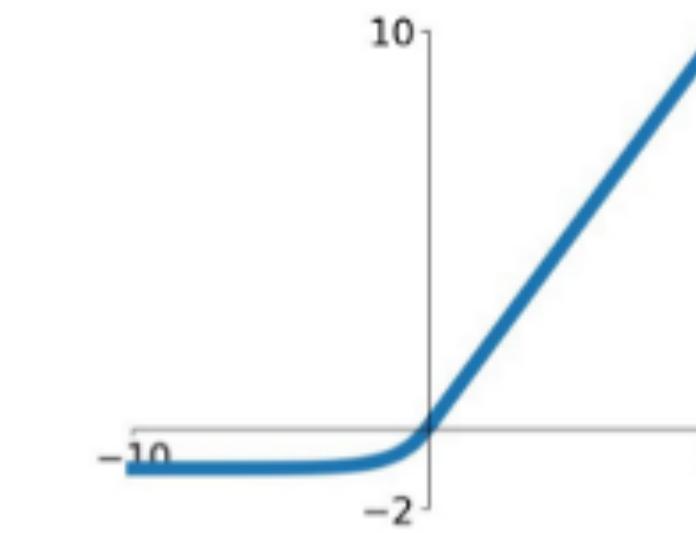


Maxout

$$\max(w_1^T x + b_1, w_2^T x + b_2)$$

ELU

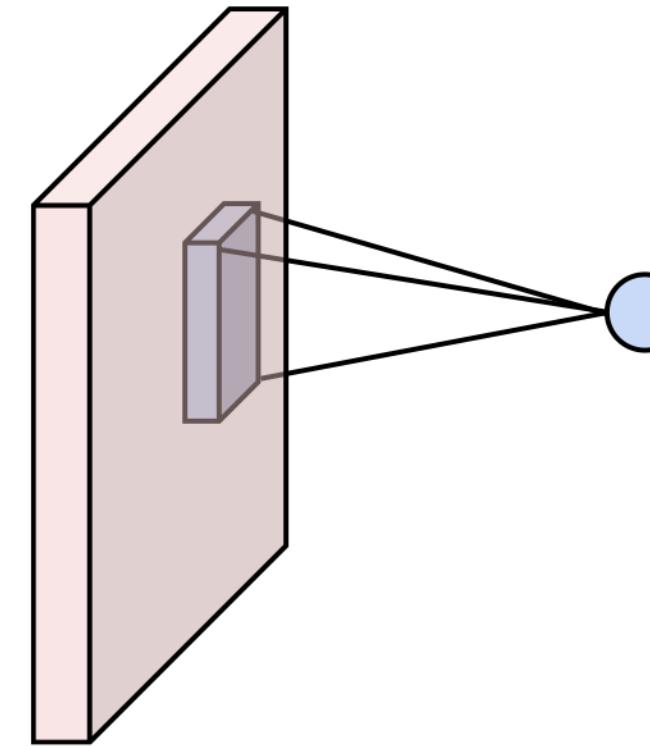
$$\begin{cases} x & x \geq 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$



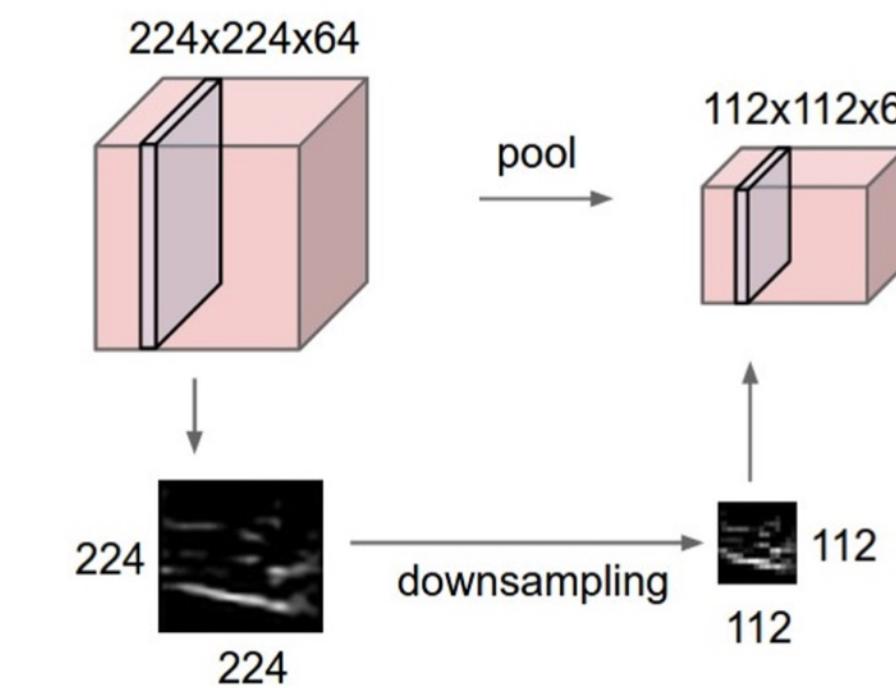


Summary: Components of Convolutional Networks

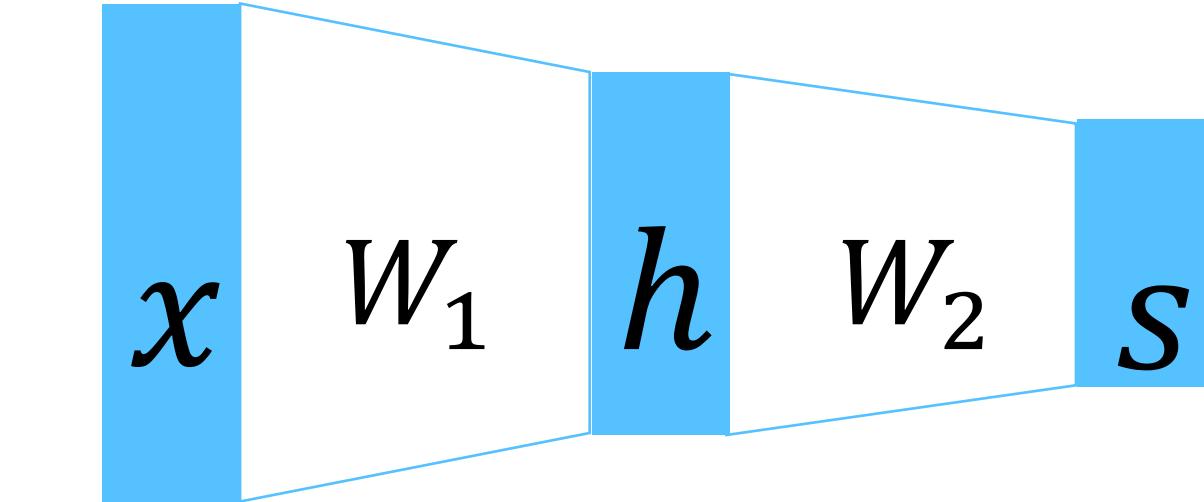
Convolution Layers



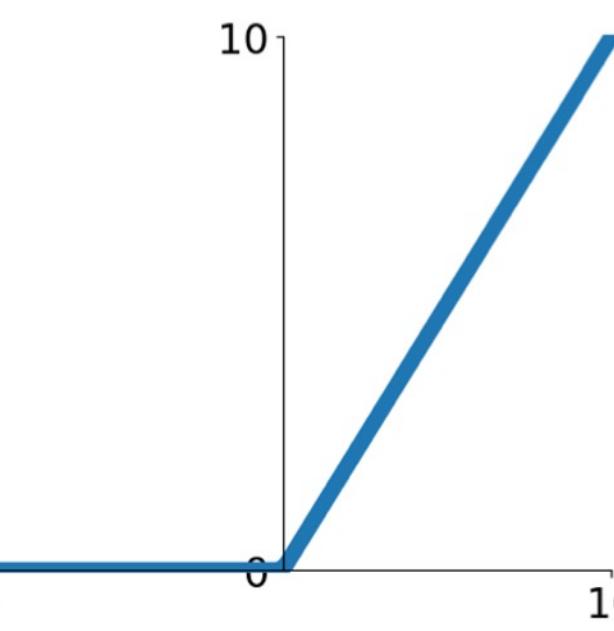
Pooling Layers



Fully-Connected Layers



Activation Function



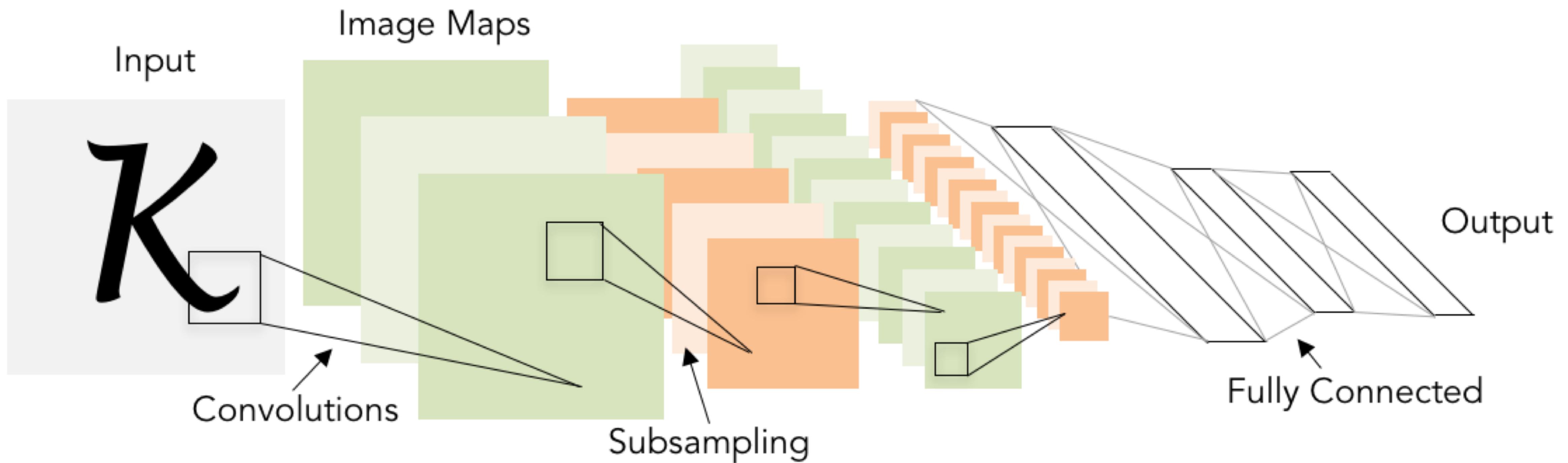
Normalization

$$\hat{x}_{i,j} = \frac{x_{i,j} - \mu_j}{\sqrt{\sigma_j^2 + \epsilon}}$$



Summary: Components of Convolutional Network

Problem: What is the right way to combine all these components?

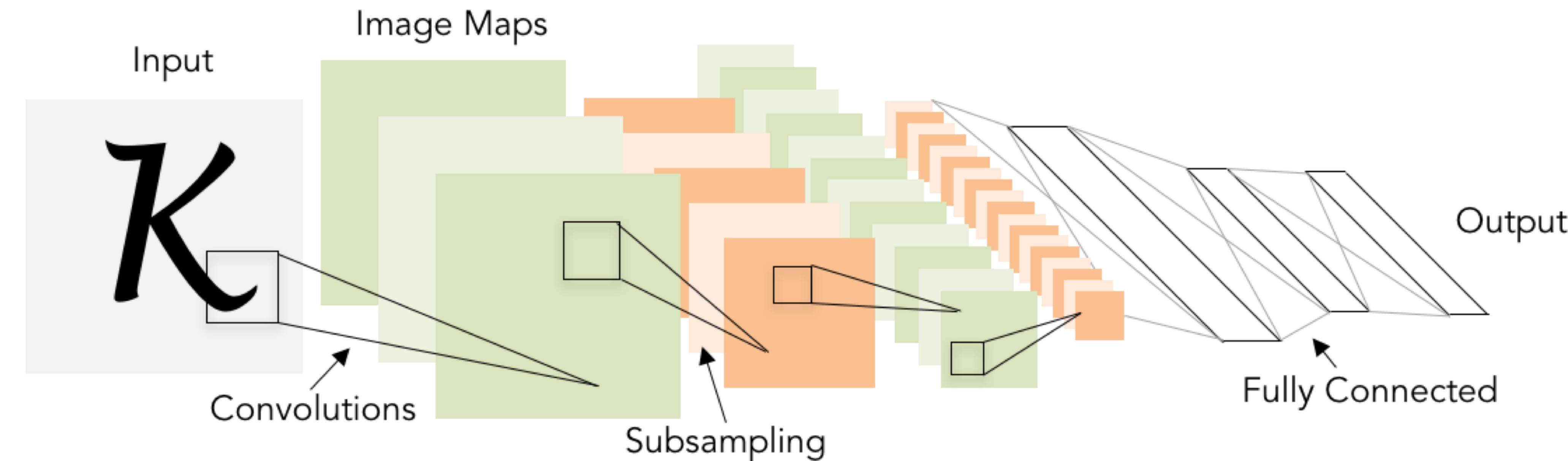




Convolutional Neural Networks

Classic architecture: [Conv, ReLU, Pool] x N, flatten, [FC, ReLU] x N, FC

Example: LeNet-5

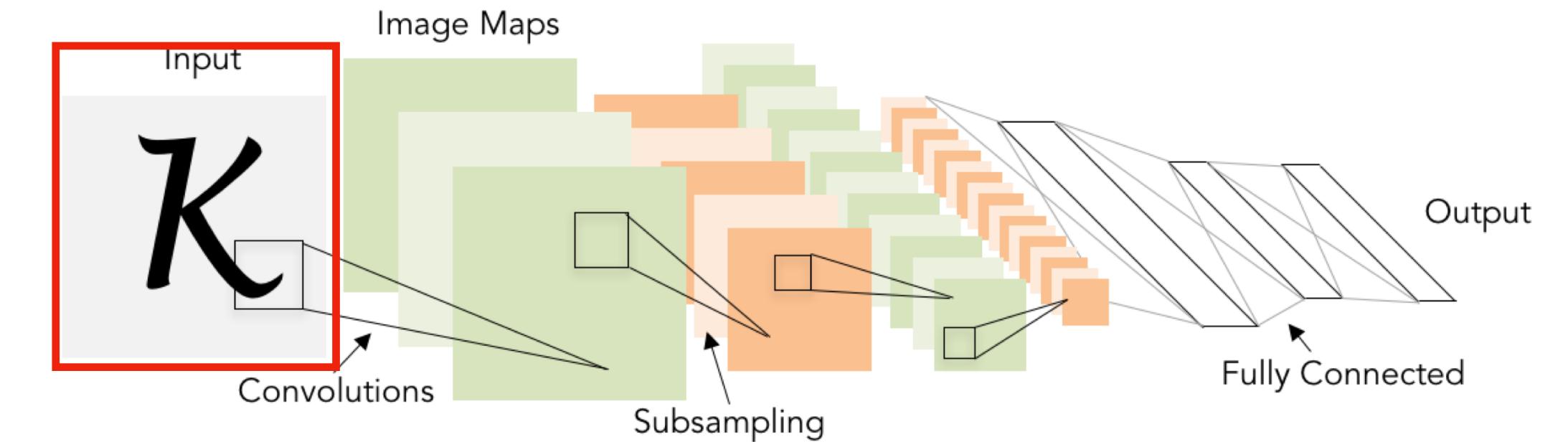


Lecun et al., "Gradient-based learning applied to document recognition", 1998



Example: LeNet-5

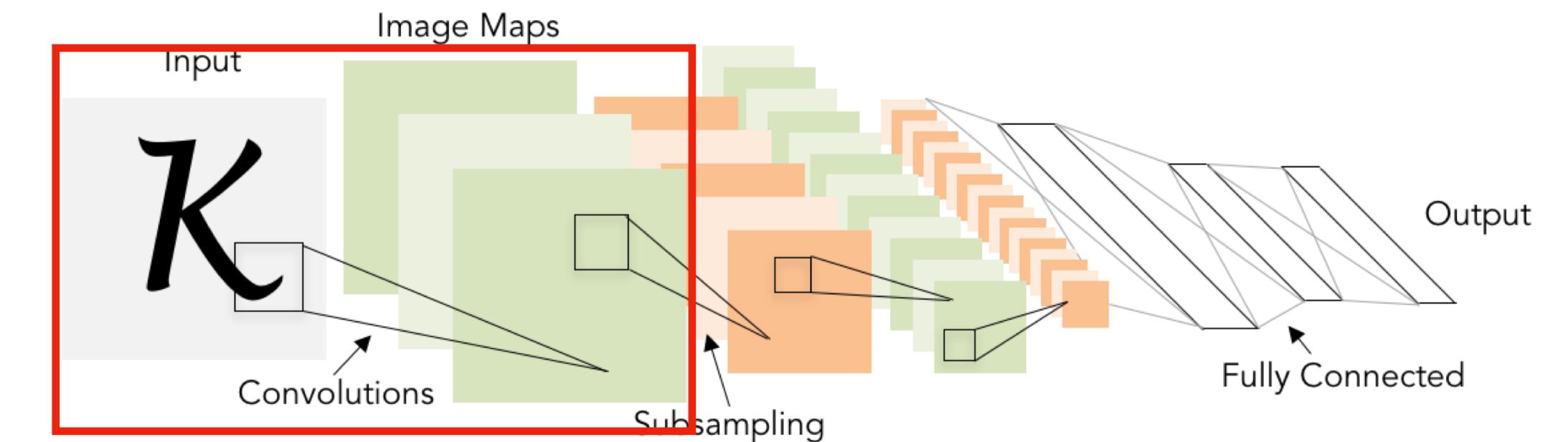
Layer	Output Size	Weight Size
Input	1 x 28 x 28	





Example: LeNet-5

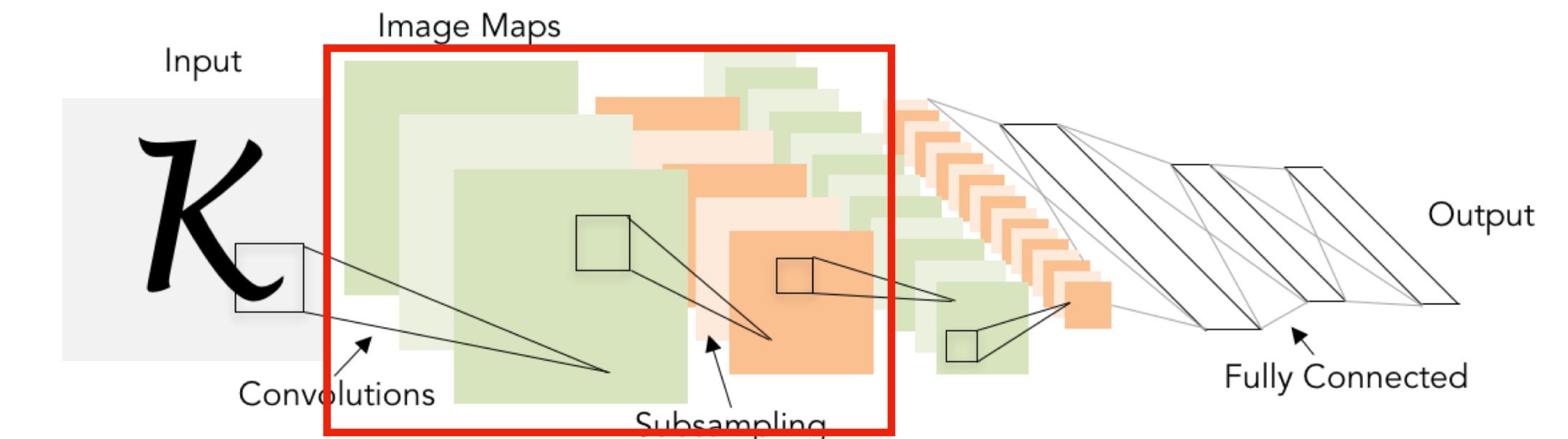
Layer	Output Size	Weight Size
Input	$1 \times 28 \times 28$	
Conv ($C_{out}=20, K=5, P=2, S=1$)	$20 \times 28 \times 28$	$20 \times 1 \times 5 \times 5$
ReLU	$20 \times 28 \times 28$	





Example: LeNet-5

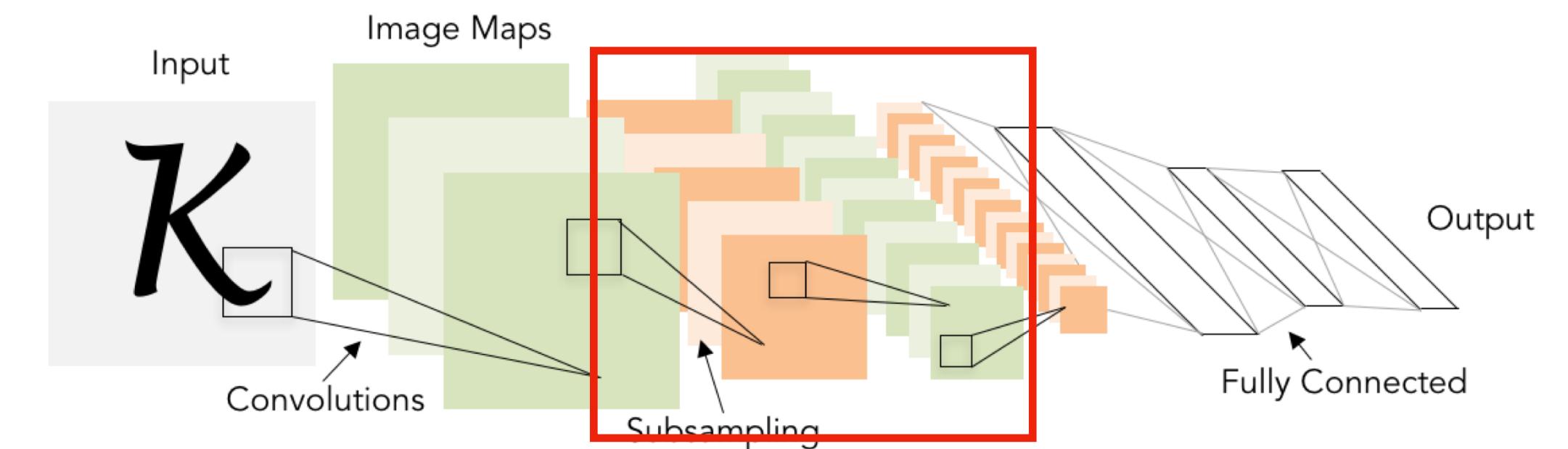
Layer	Output Size	Weight Size
Input	$1 \times 28 \times 28$	
Conv ($C_{out}=20, K=5, P=2, S=1$)	$20 \times 28 \times 28$	$20 \times 1 \times 5 \times 5$
ReLU	$20 \times 28 \times 28$	
MaxPool($K=2, S=2$)	$20 \times 14 \times 14$	





Example: LeNet-5

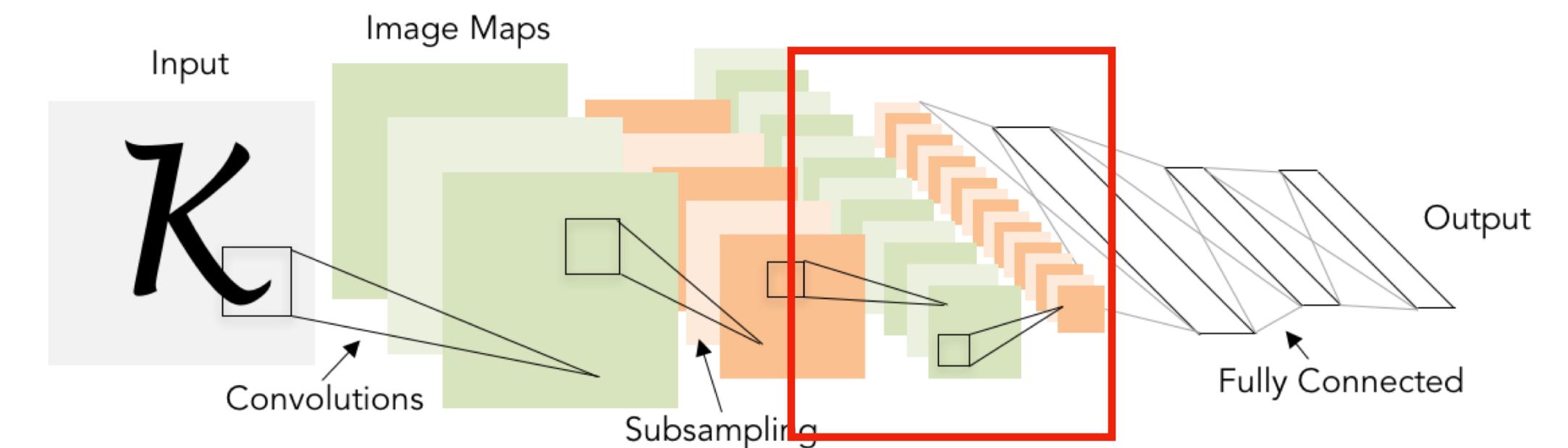
Layer	Output Size	Weight Size
Input	$1 \times 28 \times 28$	
Conv ($C_{out}=20, K=5, P=2, S=1$)	$20 \times 28 \times 28$	$20 \times 1 \times 5 \times 5$
ReLU	$20 \times 28 \times 28$	
MaxPool($K=2, S=2$)	$20 \times 14 \times 14$	
Conv ($C_{out}=50, K=5, P=2, S=1$)	$50 \times 14 \times 14$	$50 \times 20 \times 5 \times 5$
ReLU	$50 \times 14 \times 14$	





Example: LeNet-5

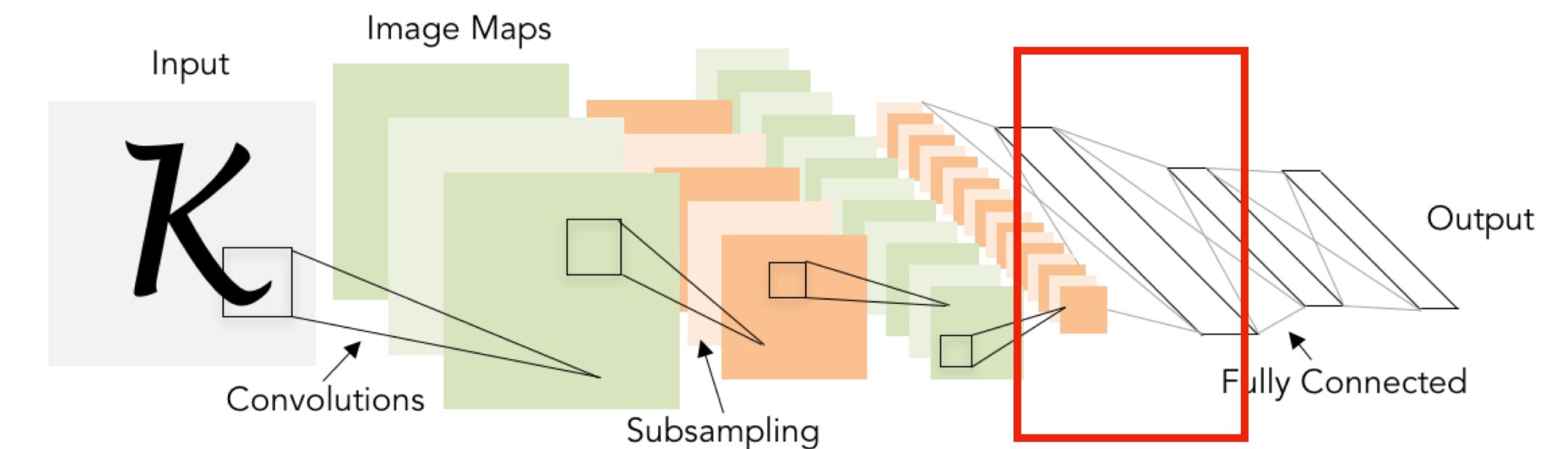
Layer	Output Size	Weight Size
Input	$1 \times 28 \times 28$	
Conv ($C_{out}=20, K=5, P=2, S=1$)	$20 \times 28 \times 28$	$20 \times 1 \times 5 \times 5$
ReLU	$20 \times 28 \times 28$	
MaxPool($K=2, S=2$)	$20 \times 14 \times 14$	
Conv ($C_{out}=50, K=5, P=2, S=1$)	$50 \times 14 \times 14$	$50 \times 20 \times 5 \times 5$
ReLU	$50 \times 14 \times 14$	
MaxPool($K=2, S=2$)	$50 \times 7 \times 7$	





Example: LeNet-5

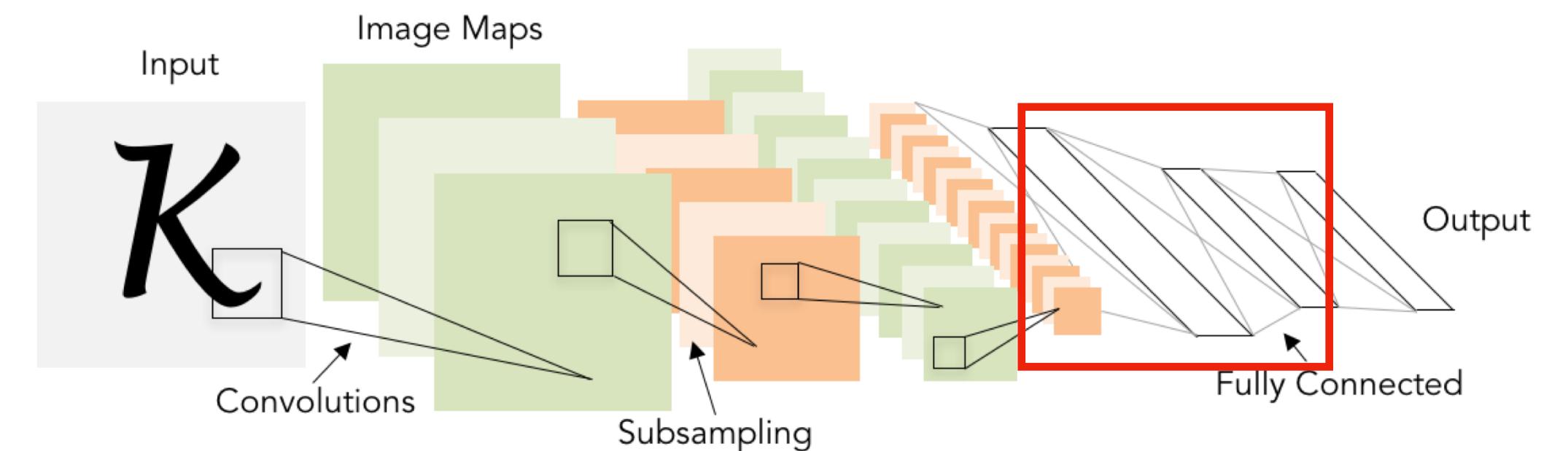
Layer	Output Size	Weight Size
Input	$1 \times 28 \times 28$	
Conv ($C_{out}=20$, $K=5$, $P=2$, $S=1$)	$20 \times 28 \times 28$	$20 \times 1 \times 5 \times 5$
ReLU	$20 \times 28 \times 28$	
MaxPool($K=2$, $S=2$)	$20 \times 14 \times 14$	
Conv ($C_{out}=50$, $K=5$, $P=2$, $S=1$)	$50 \times 14 \times 14$	$50 \times 20 \times 5 \times 5$
ReLU	$50 \times 14 \times 14$	
MaxPool($K=2$, $S=2$)	$50 \times 7 \times 7$	
Flatten	2450	





Example: LeNet-5

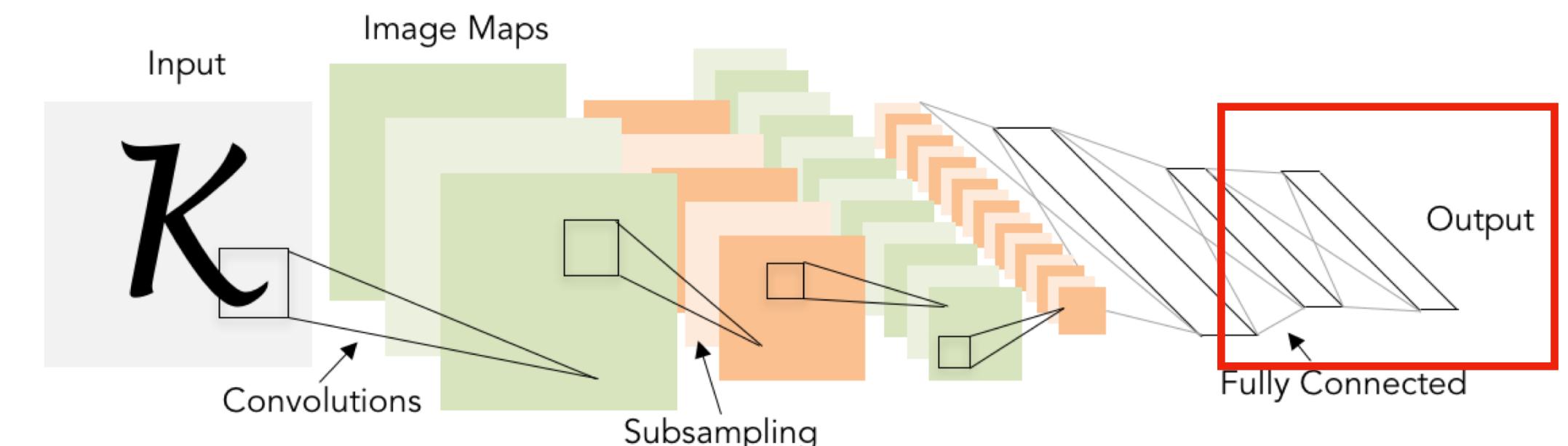
Layer	Output Size	Weight Size
Input	$1 \times 28 \times 28$	
Conv ($C_{out}=20, K=5, P=2, S=1$)	$20 \times 28 \times 28$	$20 \times 1 \times 5 \times 5$
ReLU	$20 \times 28 \times 28$	
MaxPool($K=2, S=2$)	$20 \times 14 \times 14$	
Conv ($C_{out}=50, K=5, P=2, S=1$)	$50 \times 14 \times 14$	$50 \times 20 \times 5 \times 5$
ReLU	$50 \times 14 \times 14$	
MaxPool($K=2, S=2$)	$50 \times 7 \times 7$	
Flatten	2450	
Linear ($2450 \rightarrow 500$)	500	2450×500
ReLU	500	





Example: LeNet-5

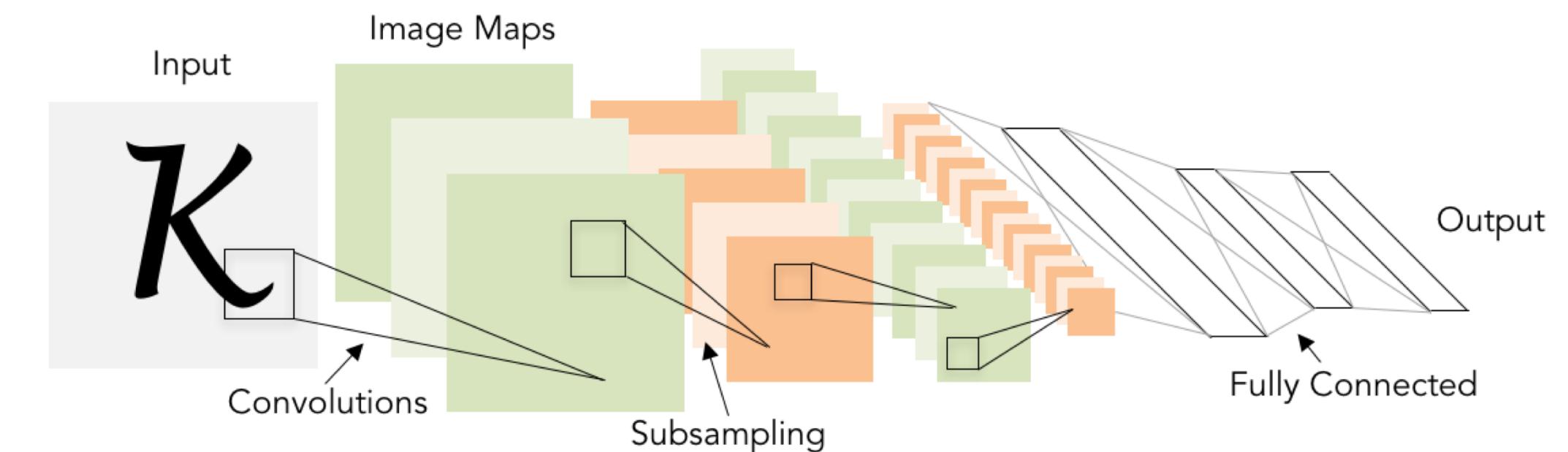
Layer	Output Size	Weight Size
Input	$1 \times 28 \times 28$	
Conv ($C_{out}=20, K=5, P=2, S=1$)	$20 \times 28 \times 28$	$20 \times 1 \times 5 \times 5$
ReLU	$20 \times 28 \times 28$	
MaxPool($K=2, S=2$)	$20 \times 14 \times 14$	
Conv ($C_{out}=50, K=5, P=2, S=1$)	$50 \times 14 \times 14$	$50 \times 20 \times 5 \times 5$
ReLU	$50 \times 14 \times 14$	
MaxPool($K=2, S=2$)	$50 \times 7 \times 7$	
Flatten	2450	
Linear ($2450 \rightarrow 500$)	500	2450×500
ReLU	500	
Linear ($500 \rightarrow 10$)	10	500×10





Example: LeNet-5

Layer	Output Size	Weight Size
Input	$1 \times 28 \times 28$	
Conv ($C_{out}=20, K=5, P=2, S=1$)	$20 \times 28 \times 28$	$20 \times 1 \times 5 \times 5$
ReLU	$20 \times 28 \times 28$	
MaxPool($K=2, S=2$)	$20 \times 14 \times 14$	
Conv ($C_{out}=50, K=5, P=2, S=1$)	$50 \times 14 \times 14$	$50 \times 20 \times 5 \times 5$
ReLU	$50 \times 14 \times 14$	
MaxPool($K=2, S=2$)	$50 \times 7 \times 7$	
Flatten	2450	
Linear (2450 -> 500)	500	2450×500
ReLU	500	
Linear (500 -> 10)	10	500×10



As we progress through the network:

Spatial size **decreases**

(using pooling or striped convolution)

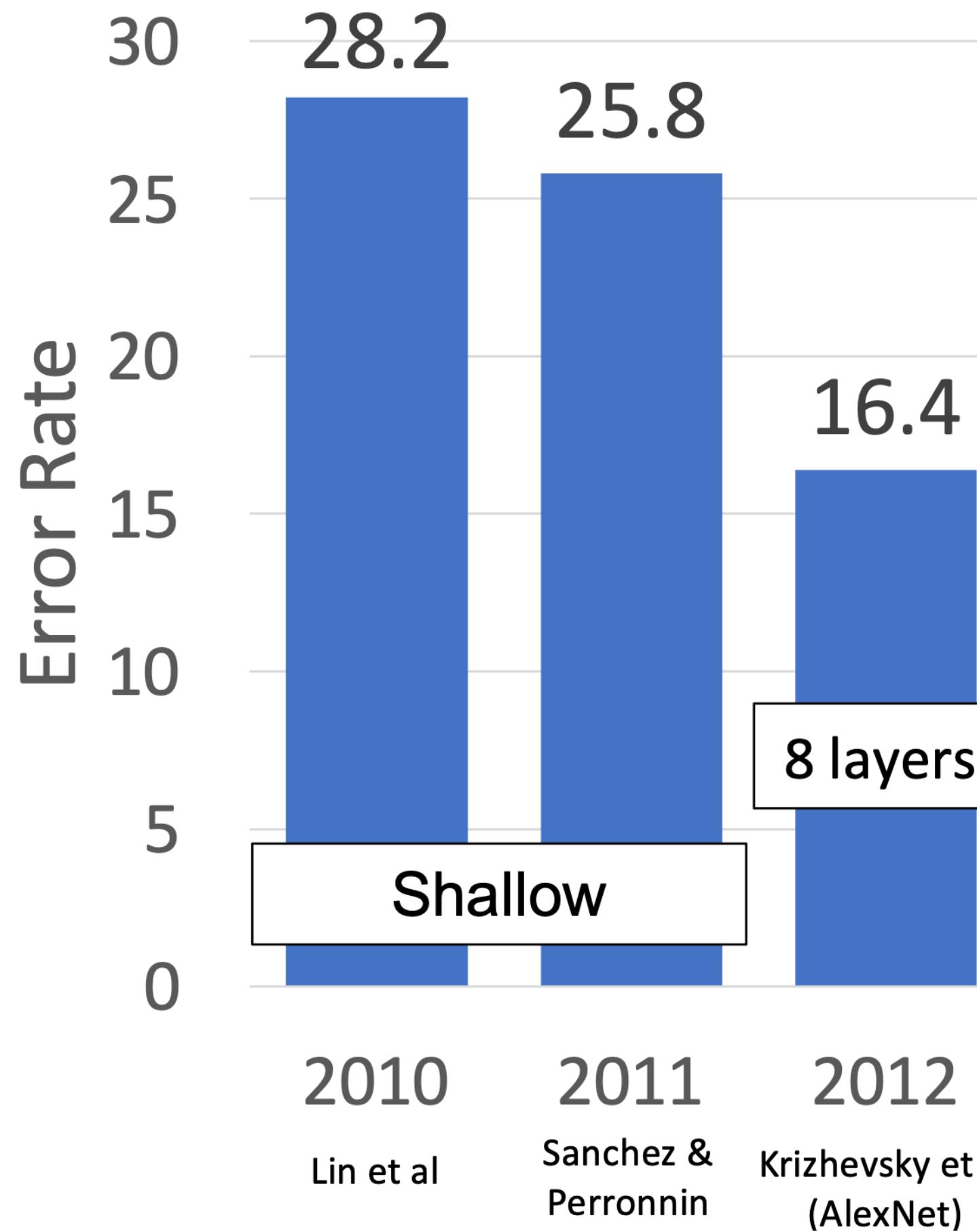
Number of channels **increases**

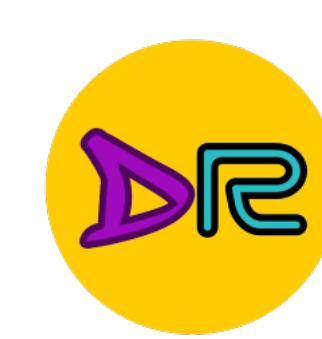
(total “volume” is preserved!)

Some modern architectures
break this trend—stay tuned!

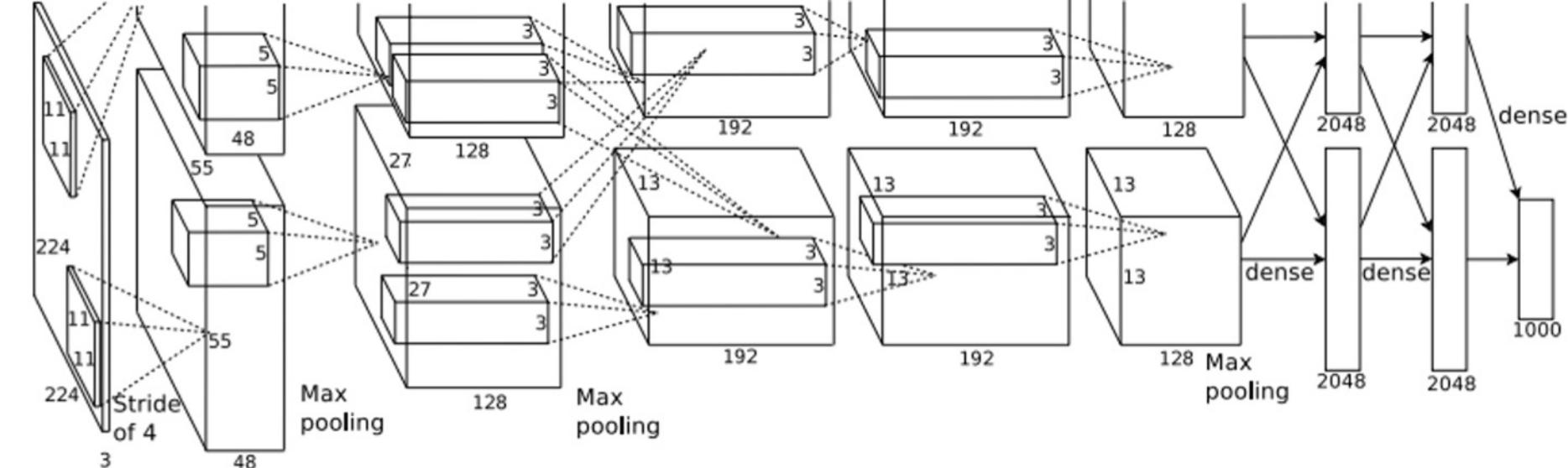


ImageNet Classification Challenge





AlexNet



- 227 x 227 inputs
- 5 Convolutional Layers
- Max pooling
- 3 Fully-connected Layers
- ReLU nonlinearities
- Used “Local response normalization”; *Not used anymore*
- Trained on two GTX 580 GPUs - only 3GB of memory each! Model split over two GPUs.



AlexNet

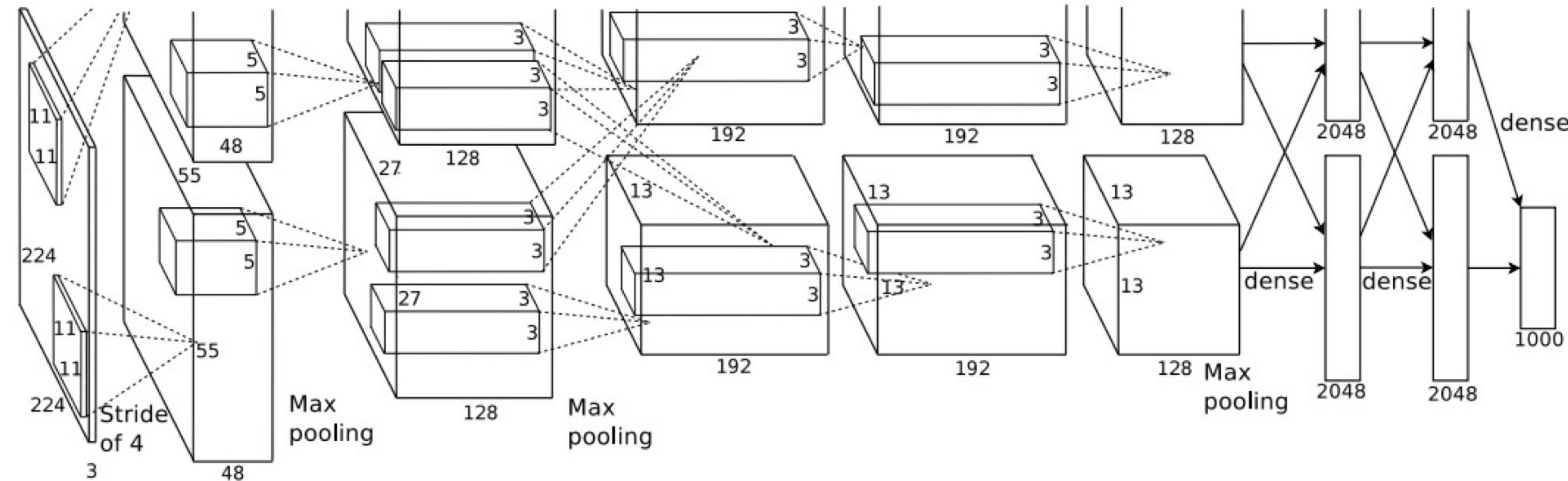
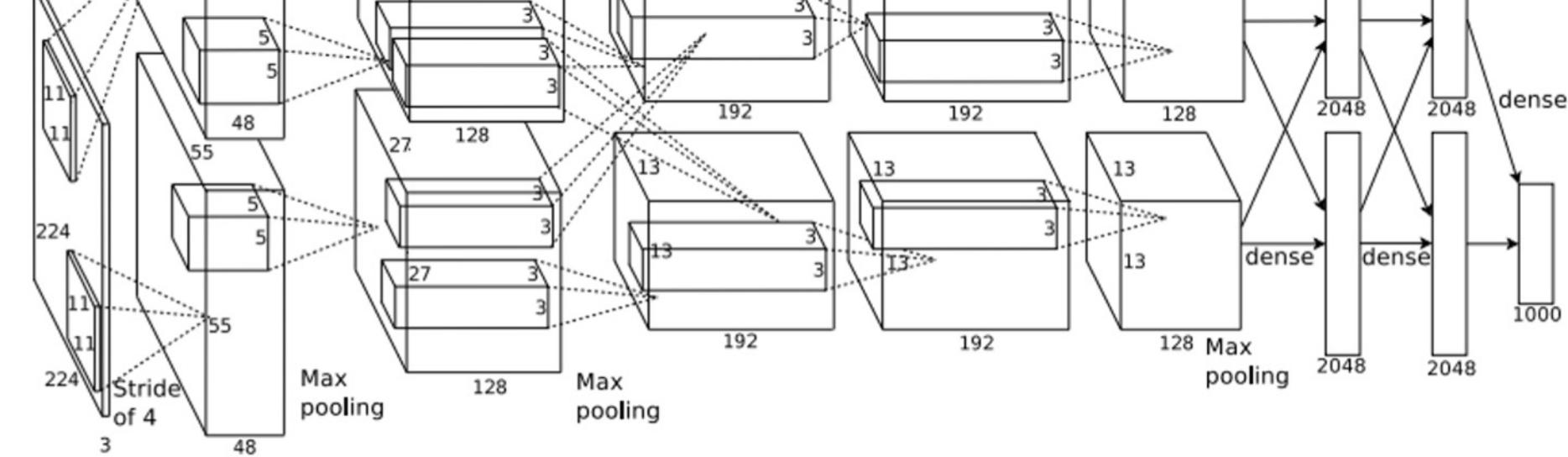


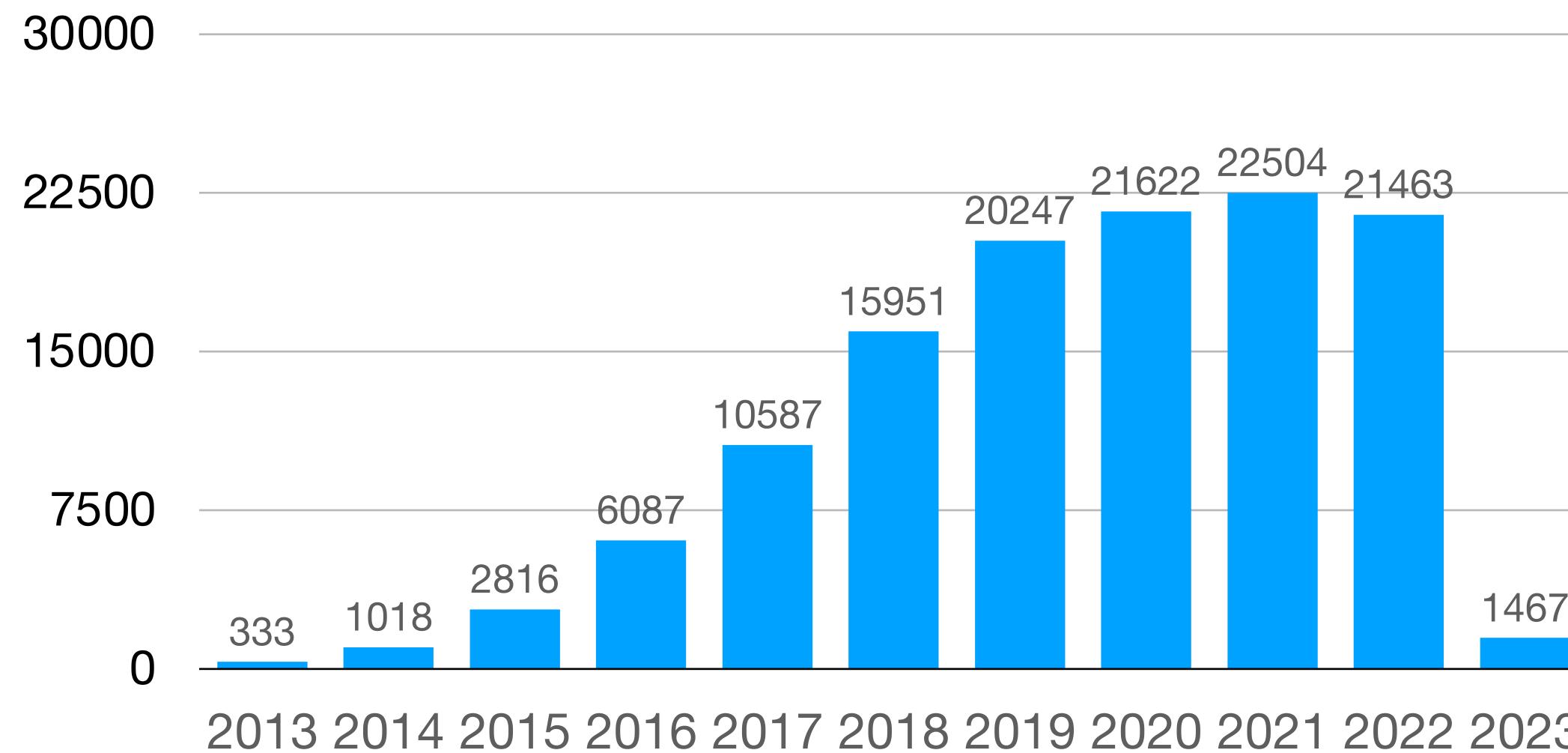
Figure 2: An illustration of the architecture of our CNN, explicitly showing the delineation of responsibilities between the two GPUs. One GPU runs the layer-parts at the top of the figure while the other runs the layer-parts at the bottom. The GPUs communicate only at certain layers. The network's input is 150,528-dimensional, and the number of neurons in the network's remaining layers is given by 253,440–186,624–64,896–64,896–43,264–4096–4096–1000.



AlexNet



AlexNet citations per year



Total citations: >120,000

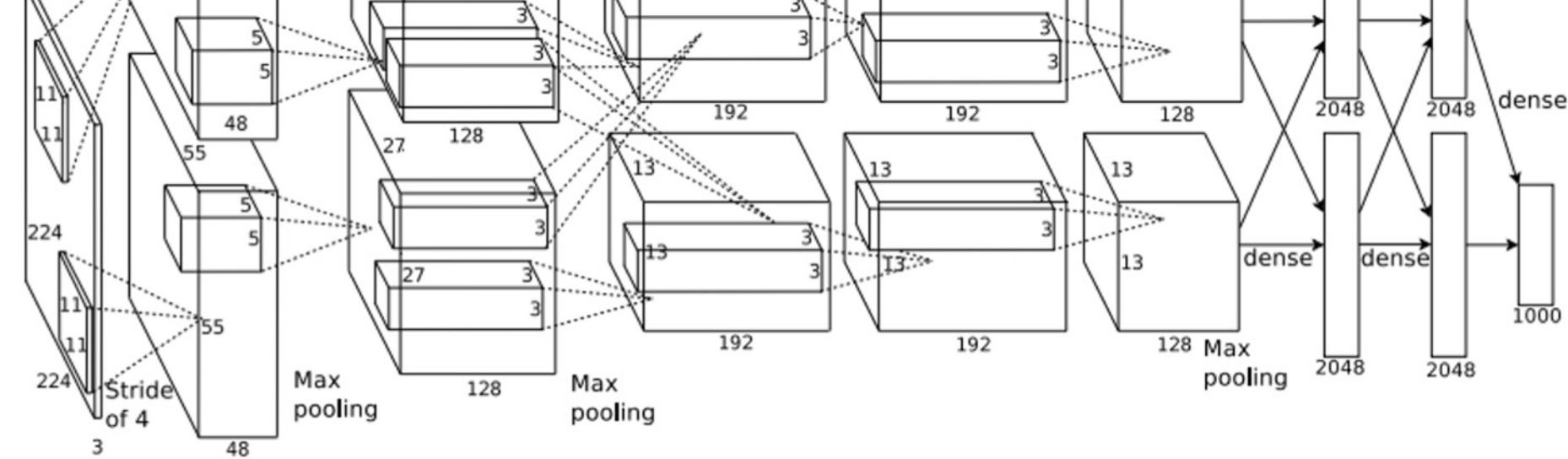
Citation as of 1/31/2024: 124,651

Citation Counts:

- Darwin, “On the origin of species”, 1859: **60,117**
- Shannon, “A mathematical theory of communication,” 1948: **140,459**
- Watson and Crick, “Molecular Structure of Nucleic Acids,” 1953: **16,298**



AlexNet

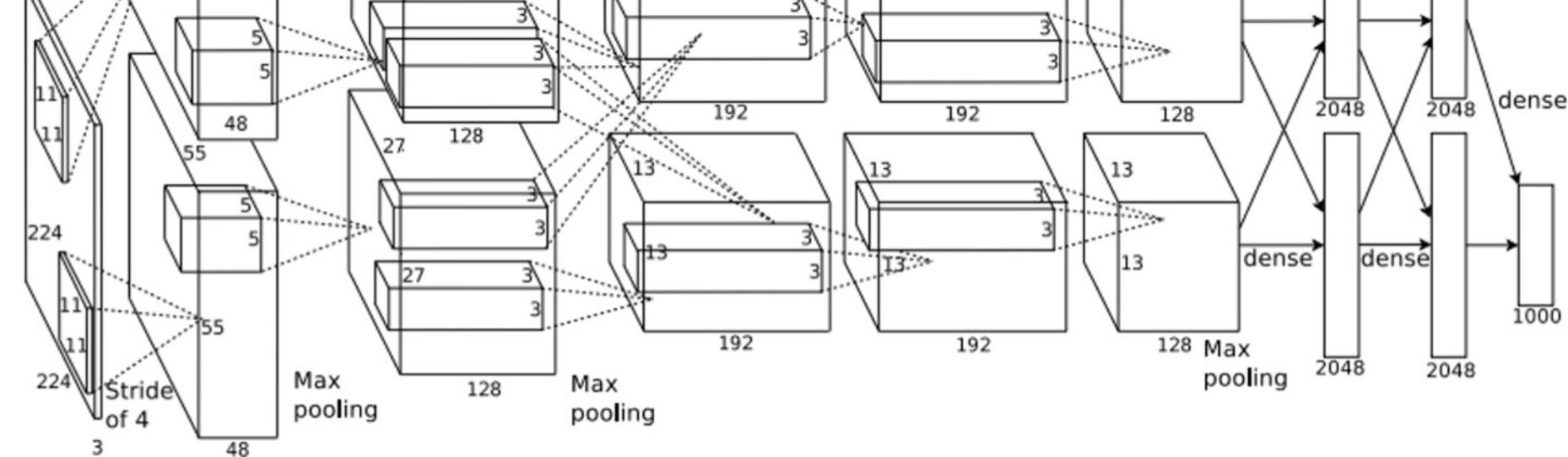


	Input size		Layer				Output size	
Layer	C	H/W	Filters	Kernel	Stride	Pad	C	H/W
Conv1	3	227	64	11	4	2		?

Recall: Output channels = number of filters



AlexNet

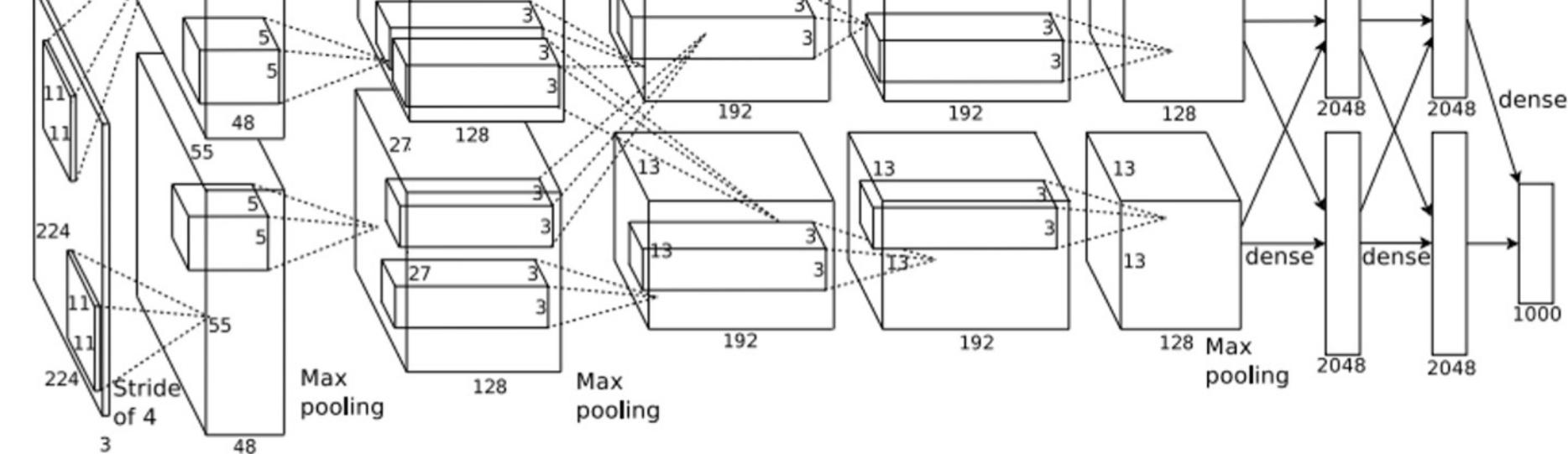


	Input size		Layer				Output size	
Layer	C	H/W	Filters	Kernel	Stride	Pad	C	H/W
Conv1	3	227	64	11	4	2	64	56

$$\begin{aligned} \text{Recall: } W' &= (W - K + 2P) / S + 1 \\ &= (227 - 11 + 2 \times 2) / 4 + 1 \\ &= 220 / 4 + 1 = 56 \end{aligned}$$



AlexNet



	Input size		Layer				Output size		Memory (KB)
Layer	C	H/W	Filters	Kernel	Stride	Pad	C	H/W	
Conv1	3	227	64	11	4	2	64	56	784

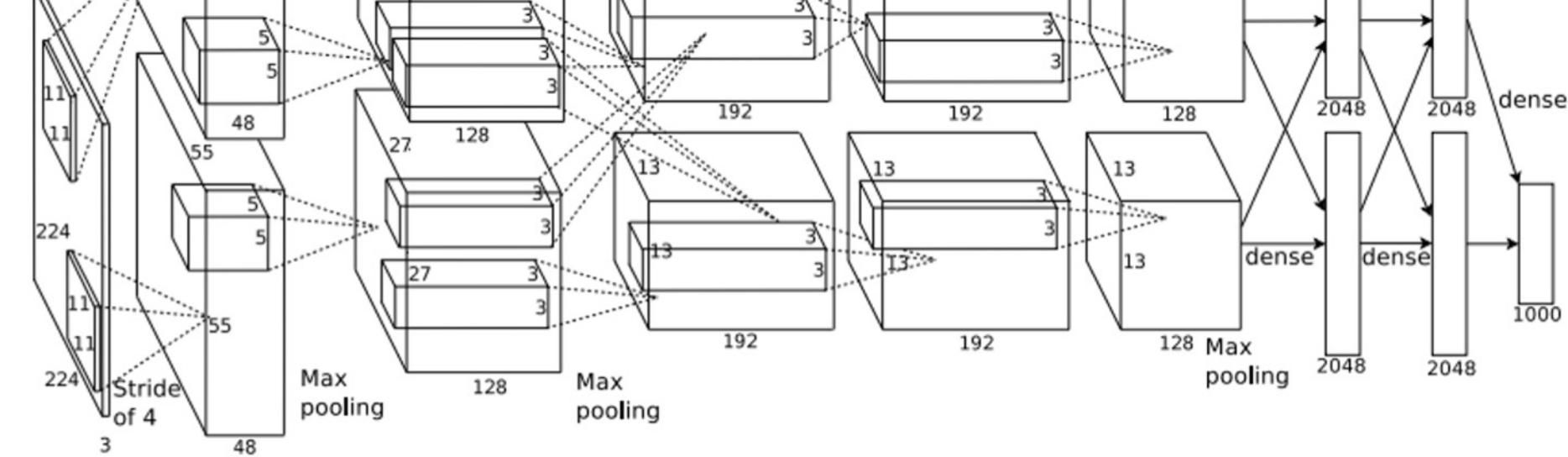
Number of output elements = $C \times H' \times W'$
 $= 64 \times 56 \times 56 = 200,704$

Bytes per element = 4 (for 32-bit floating point)

$KB = (\text{number of elements}) \times (\text{bytes per elem}) / 1024$
 $= 200704 \times 4 / 1024$
 $= 784$



AlexNet



Layer	Input size		Layer				Output size		Memory (KB)	Params (k)
	C	H/W	Filters	Kernel	Stride	Pad	C	H/W		
Conv1	3	227	64	11	4	2	64	56	784	23

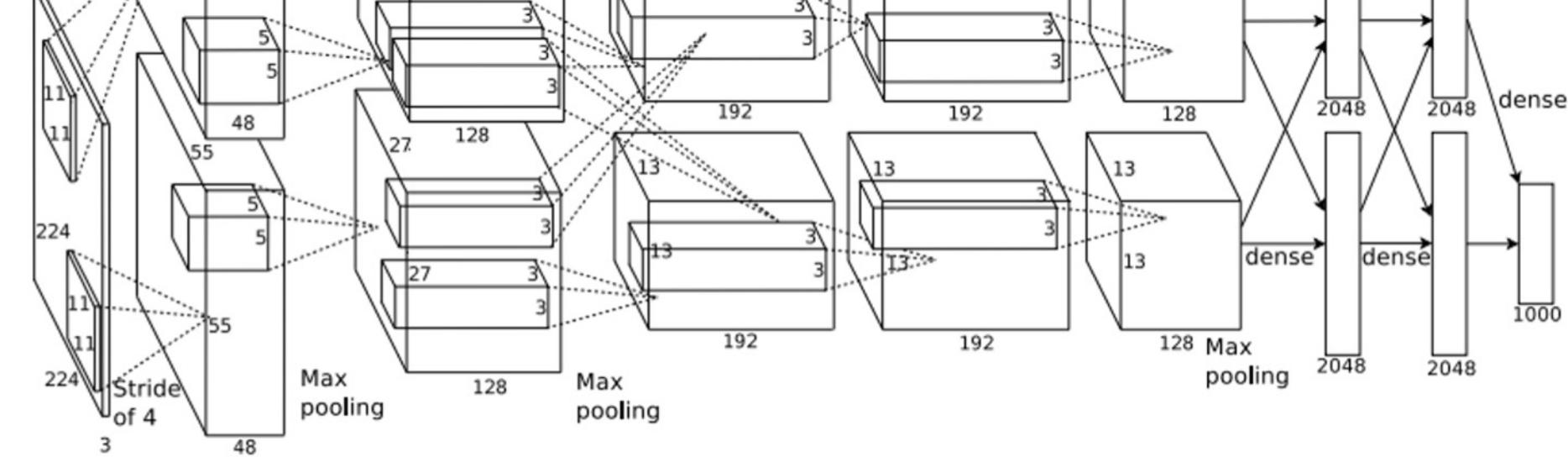
Weight shape = $C_{out} \times C_{in} \times K \times K$
 $= 64 \times 3 \times 11 \times 11$

Bias shape = $C_{out} = 64$

Number of weights = $64 \times 3 \times 11 \times 11 + 64$
 $= 23,296$



AlexNet

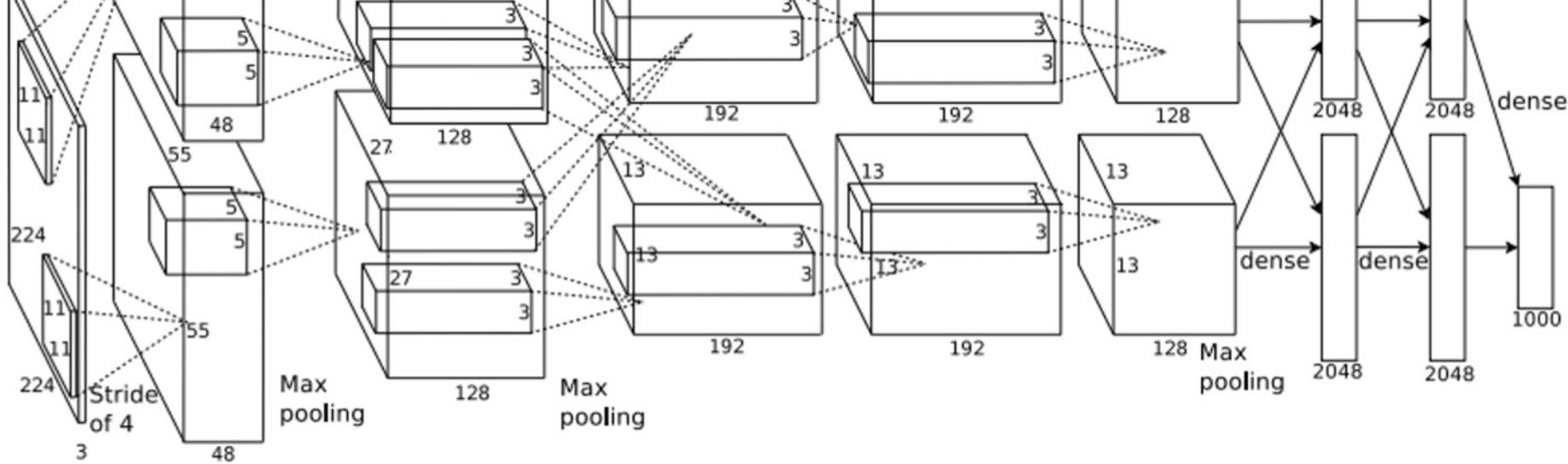


	Input size		Layer				Output size				
Layer	C	H/W	Filters	Kernel	Stride	Pad	C	H/W	Memory (KB)	Params (k)	Flop (M)
Conv1	3	227	64	11	4	2	64	56	784	23	73

Number of floating point operations (multiply + add)
= (number of output elements) * (ops per output elem)
= ($C_{out} \times H' \times W'$) * ($C_{in} \times K \times K$)
= $(64 \times 56 \times 56) \times (3 \times 11 \times 11)$
= $200,704 \times 363$
= 72,855,552



AlexNet



	Input size		Layer				Output size				
Layer	C	H/W	Filters	Kernel	Stride	Pad	C	H/W	Memory (KB)	Params (k)	Flop (M)
Conv1	3	227	64	11	4	2	64	56	784	23	73
Pool1	64	56		3	2	0	64	27			

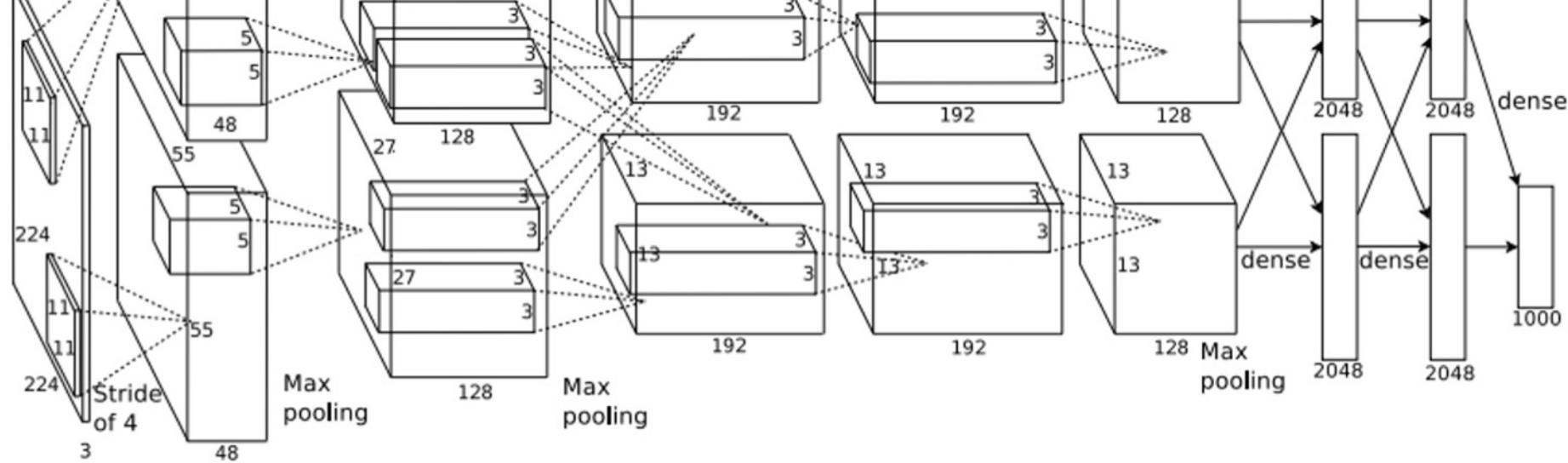
For pooling layer:

#output channels = #input channels = 64

$$\begin{aligned} W' &= \text{floor}(W-K)/S+1 \\ &= \text{floor}(53/2 + 1) = \text{floor}(27.5) = 27 \end{aligned}$$



AlexNet



	Input size		Layer				Output size				
Layer	C	H/W	Filters	Kernel	Stride	Pad	C	H/W	Memory (KB)	Params (k)	Flop (M)
Conv1	3	227	64	11	4	2	64	56	784	23	73
Pool1	64	56		3	2	0	64	27	182	?	

#output elms = $C_{out} \times H' \times W'$

Bytes per elem = 4

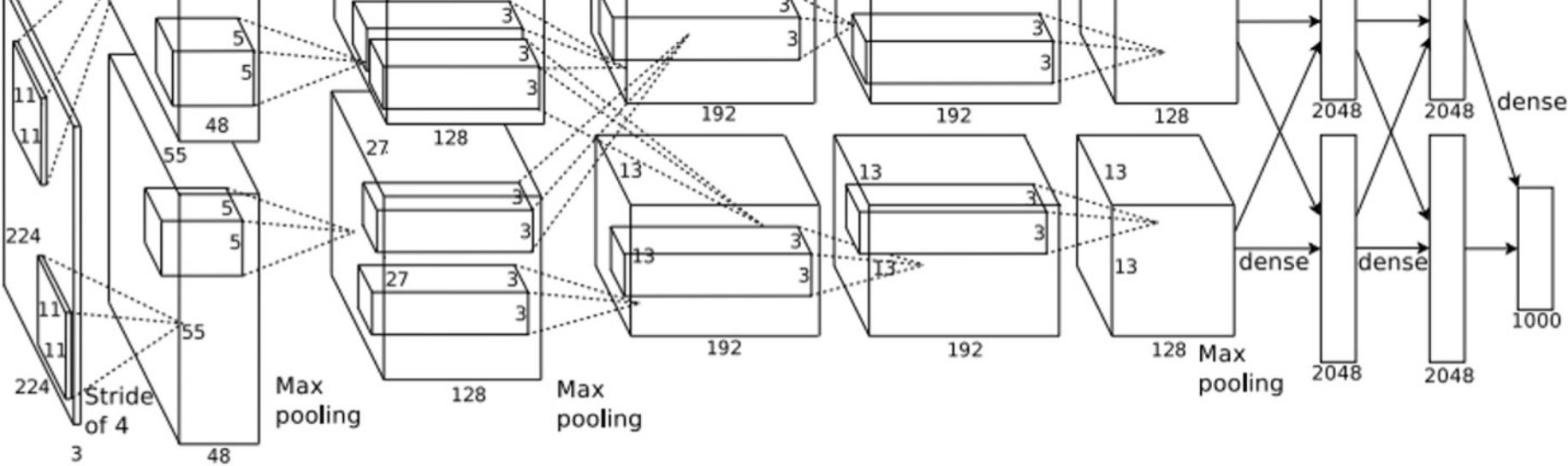
$$KB = C_{out} \times H' \times W' \times 4 / 1024$$

$$= 64 * 27 * 27 * 4 / 1024$$

$$= 182.25$$



AlexNet



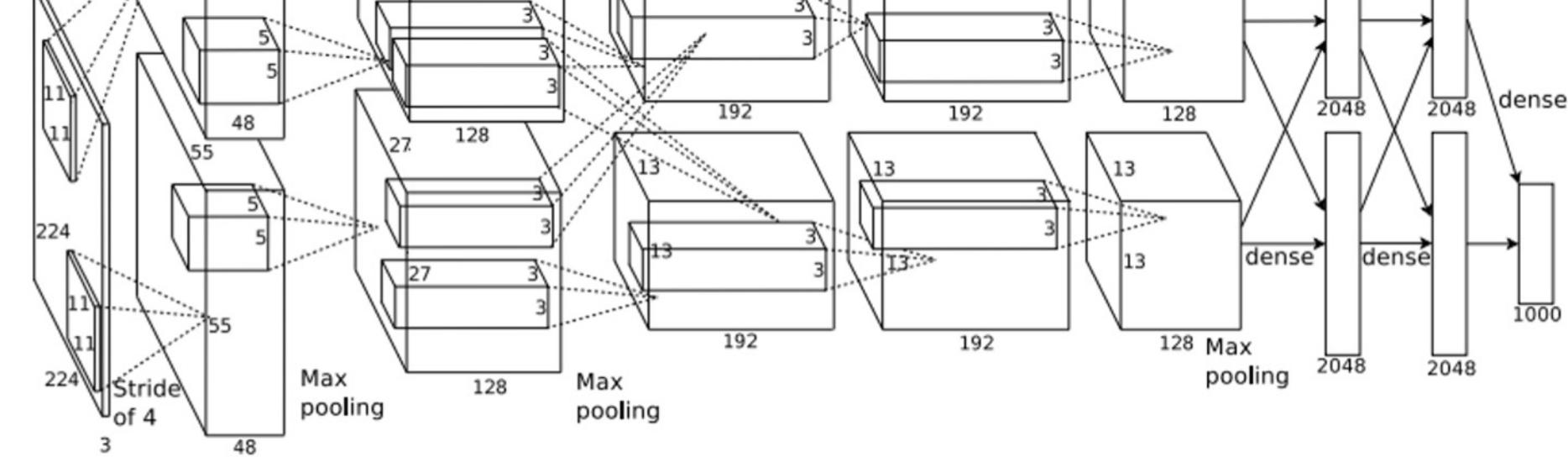
	Input size		Layer				Output size				
Layer	C	H/W	Filters	Kernel	Stride	Pad	C	H/W	Memory (KB)	Params (k)	Flop (M)
Conv1	3	227	64	11	4	2	64	56	784	23	73
Pool1	64	56		3	2	0	64	27	182	0	0



Pooling layers have no learnable parameters!



AlexNet

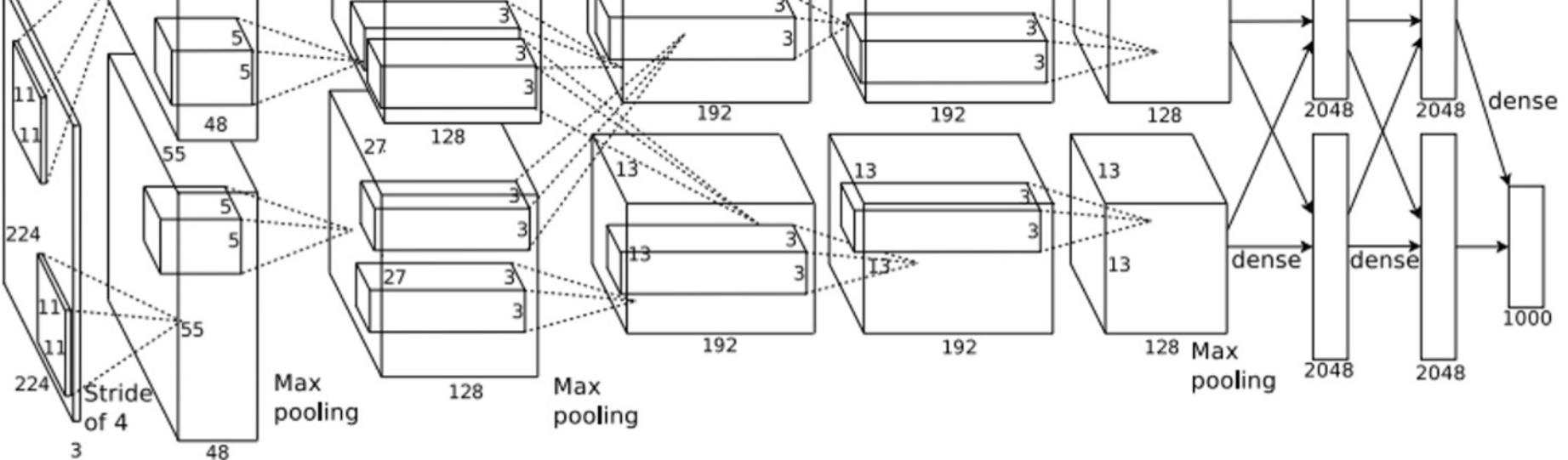


	Input size		Layer				Output size				
Layer	C	H/W	Filters	Kernel	Stride	Pad	C	H/W	Memory (KB)	Params (k)	Flop (M)
Conv1	3	227	64	11	4	2	64	56	784	23	73
Pool1	64	56		3	2	0	64	27	182	0	0

Floating-point ops for pooling layer
= (numer of output positions) * (flops per output position)
= ($C_{out} \times H' \times W'$) $\times (K \times K)$
= $(64 \times 27 \times 27) \times (3 \times 3)$
= 419,904
= **0.4 MFLOP**



AlexNet

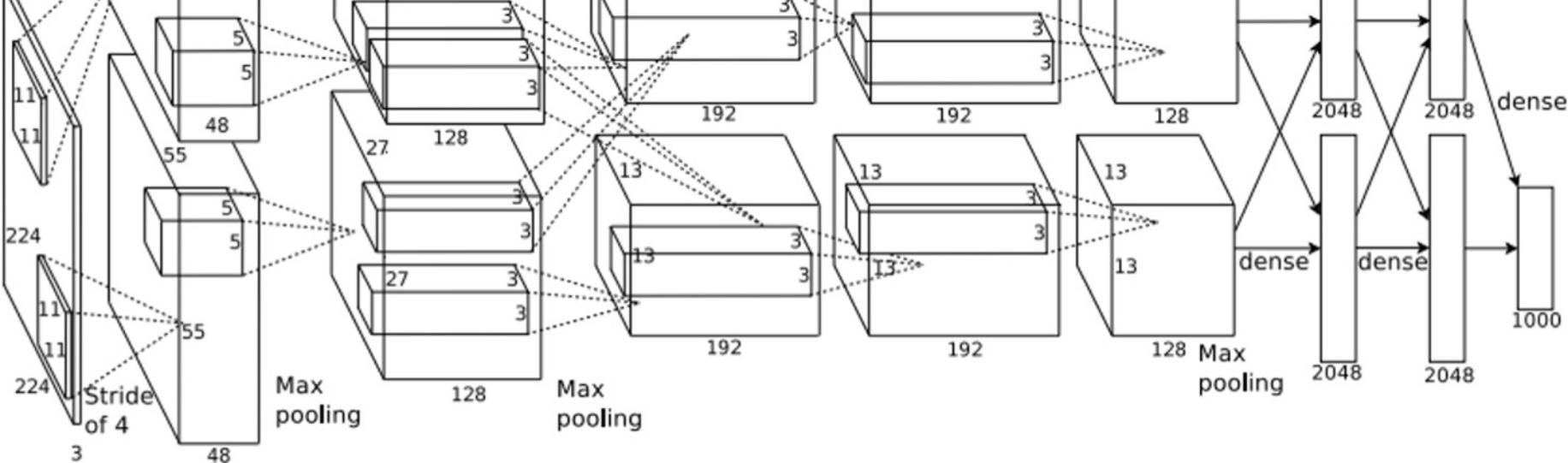


	Input size		Layer				Output size				
Layer	C	H/W	Filters	Kernel	Stride	Pad	C	H/W	Memory (KB)	Params (k)	Flop (M)
Conv1	3	227	64	11	4	2	64	56	784	23	73
Pool1	64	56		3	2	0	64	27	182	0	0
Conv2	64	27	192	5	1	2	192	27	547	307	224
Pool2	192	27		3	2	0	192	13	127	0	0
Conv3	192	13	384	3	1	1	384	13	254	664	112
Conv4	384	13	256	3	1	1	256	13	169	885	145
Conv5	256	13	256	3	1	1	256	13	169	590	100
Pool5	256	13		3	2	0	256	6	36	0	0
Flatten	256	6					9216		36	0	0

$$\begin{aligned}\text{Flatten output size} &= C_{in} \times H \times W \\ &= 256 * 6 * 6 \\ &= 9216\end{aligned}$$



AlexNet



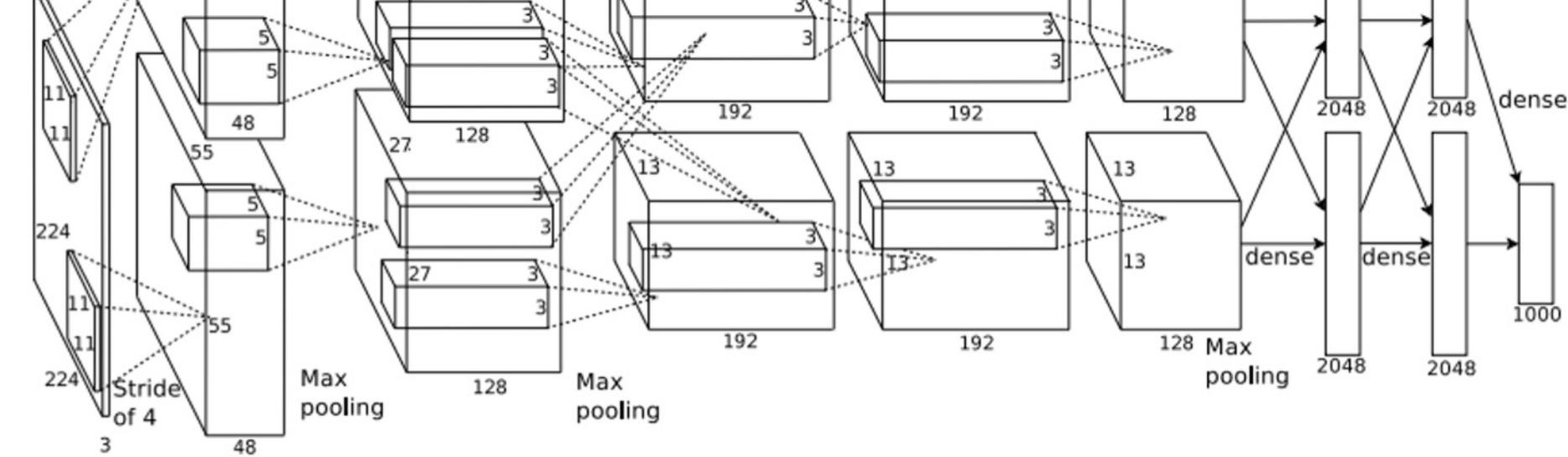
	Input size		Layer				Output size				
Layer	C	H/W	Filters	Kernel	Stride	Pad	C	H/W	Memory (KB)	Params (k)	Flop (M)
Conv1	3	227	64	11	4	2	64	56	784	23	73
Pool1	64	56		3	2	0	64	27	182	0	0
Conv2	64	27	192	5	1	2	192	27	547	307	224
Pool2	192	27		3	2	0	192	13	127	0	0
Conv3	192	13	384	3	1	1	384	13	254	664	112
Conv4	384	13	256	3	1	1	256	13	169	885	145
Conv5	256	13	256	3	1	1	256	13	169	590	100
Pool5	256	13		3	2	0	256	6	36	0	0
Flatten	256	6					9216		36	0	0
FC6	9216		4096				4096		16	37749	38

$$\begin{aligned}
 \text{FC params} &= C_{\text{in}} * C_{\text{out}} + C_{\text{out}} \\
 &= 9216 * 4096 + 4096 \\
 &= 37.725.832
 \end{aligned}$$

$$\begin{aligned}
 \text{FC flops} &= C_{\text{in}} * C_{\text{out}} \\
 &= 9216 * 4096 \\
 &= 37.748.736
 \end{aligned}$$



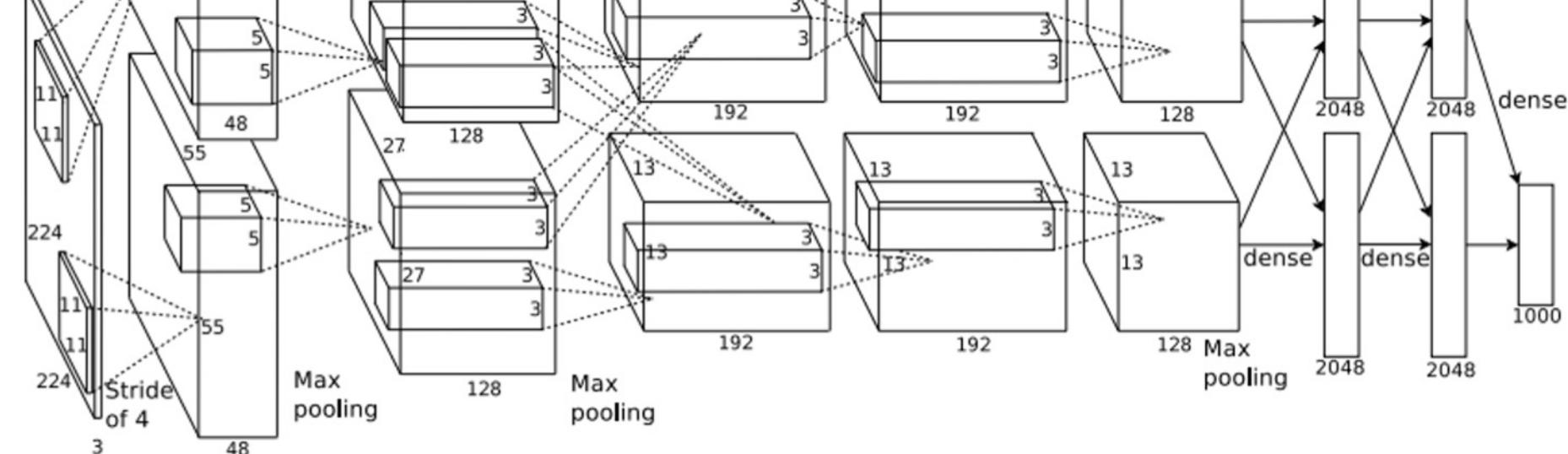
AlexNet



	Input size		Layer				Output size				
Layer	C	H/W	Filters	Kernel	Stride	Pad	C	H/W	Memory (KB)	Params (k)	Flop (M)
Conv1	3	227	64	11	4	2	64	56	784	23	73
Pool1	64	56		3	2	0	64	27	182	0	0
Conv2	64	27	192	5	1	2	192	27	547	307	224
Pool2	192	27		3	2	0	192	13	127	0	0
Conv3	192	13	384	3	1	1	384	13	254	664	112
Conv4	384	13	256	3	1	1	256	13	169	885	145
Conv5	256	13	256	3	1	1	256	13	169	590	100
Pool5	256	13		3	2	0	256	6	36	0	0
Flatten	256	6					9216		36	0	0
FC6	9216		4096				4096		16	37749	38
FC7	4096		4096				4096		16	16777	17
FC8	4096		1000				1000		4	4096	4



AlexNet

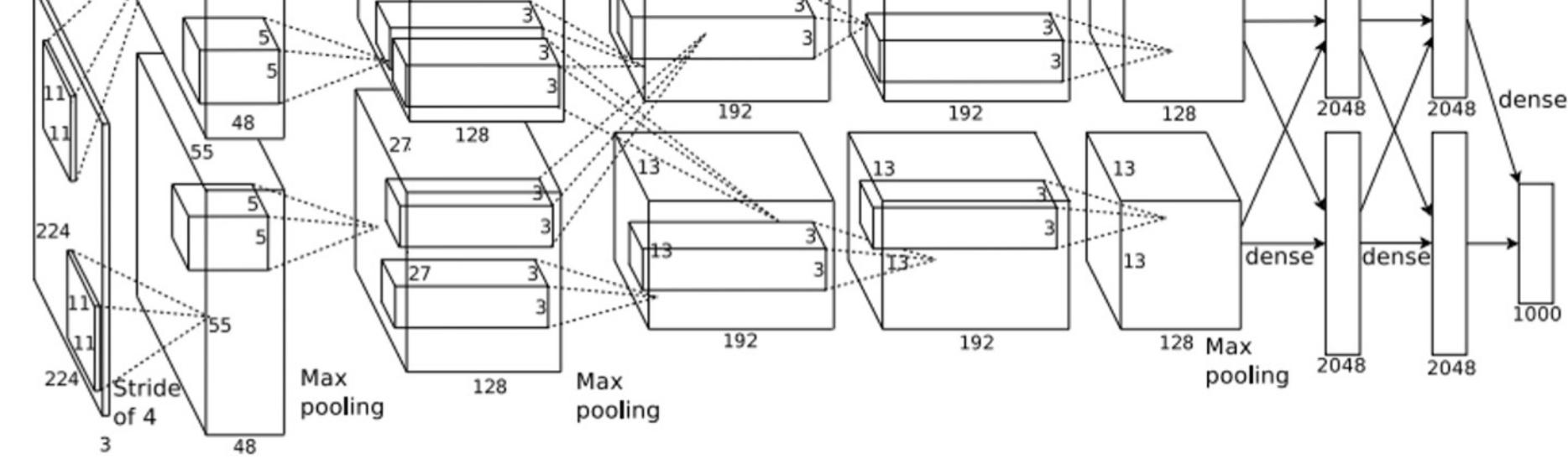


How to choose this? Trial and error :(

Layer	Input size		Layer				Output size				
	C	H/W	Filters	Kernel	Stride	Pad	C	H/W	Memory (KB)	Params (k)	Flop (M)
Conv1	3	227	64	11	4	2	64	56	784	23	73
Pool1	64	56		3	2	0	64	27	182	0	0
Conv2	64	27	192	5	1	2	192	27	547	307	224
Pool2	192	27		3	2	0	192	13	127	0	0
Conv3	192	13	384	3	1	1	384	13	254	664	112
Conv4	384	13	256	3	1	1	256	13	169	885	145
Conv5	256	13	256	3	1	1	256	13	169	590	100
Pool5	256	13		3	2	0	256	6	36	0	0
Flatten	256	6					9216		36	0	0
FC6	9216		4096				4096		16	37749	38
FC7	4096		4096				4096		16	16777	17
FC8	4096		1000				1000		4	4096	4



AlexNet

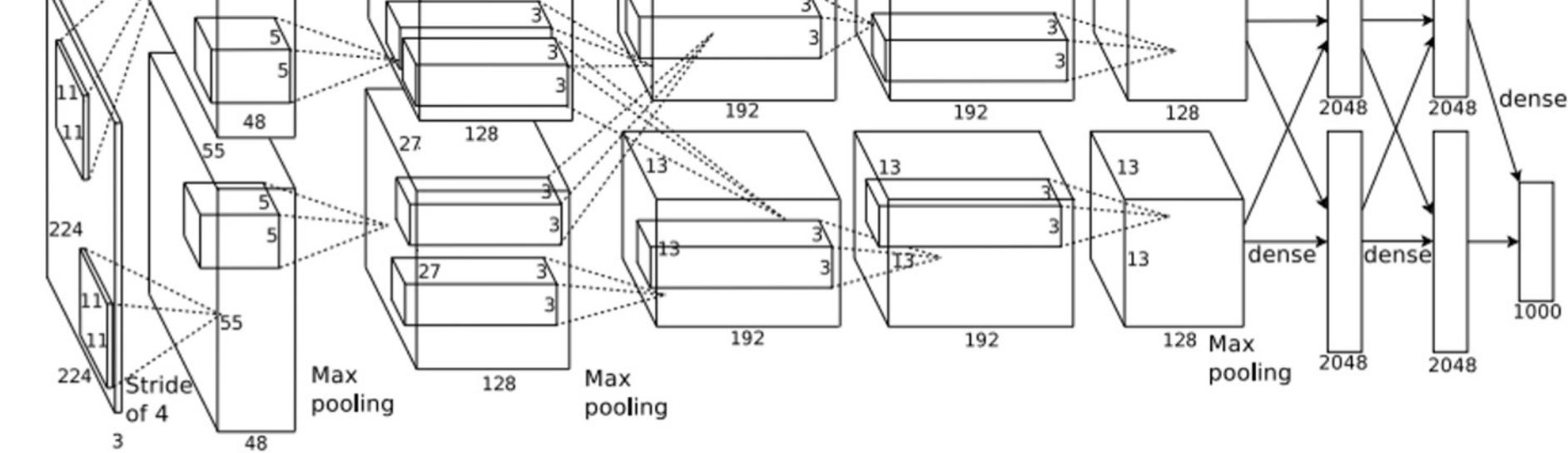


	Input size		Layer					Output size		Memory (KB)	Params (k)	Flop (M)
Layer	C	H/W	Filters	Kernel	Stride	Pad	C	H/W				
Conv1	3	227	64	11	4	2	64	56	784	23	73	
Pool1	64	56		3	2	0	64	27	182	0	0	
Conv2	64	27	192	5	1	2	192	27	547	307	224	
Pool2	192	27		3	2	0	192	13	127	0	0	
Conv3	192	13	384	3	1	1	384	13	254	664	112	
Conv4	384	13	256	3	1	1	256	13	169	885	145	
Conv5	256	13	256	3	1	1	256	13	169	590	100	
Pool5	256	13		3	2	0	256	6	36	0	0	
Flatten	256	6					9216		36	0	0	
FC6	9216		4096				4096		16	37749	38	
FC7	4096		4096				4096		16	16777	17	
FC8	4096		1000				1000		4	4096	4	

Interesting trends here!



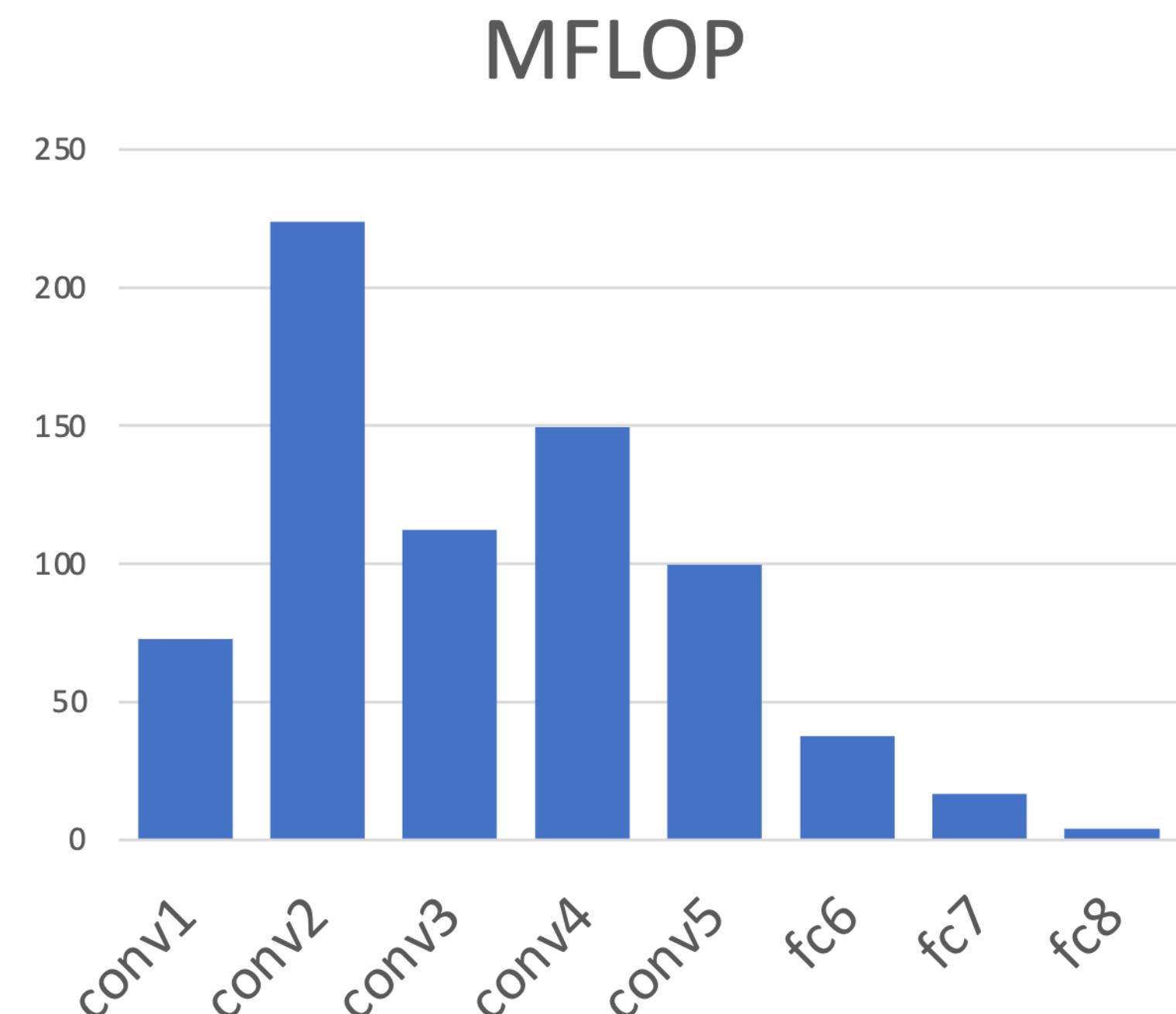
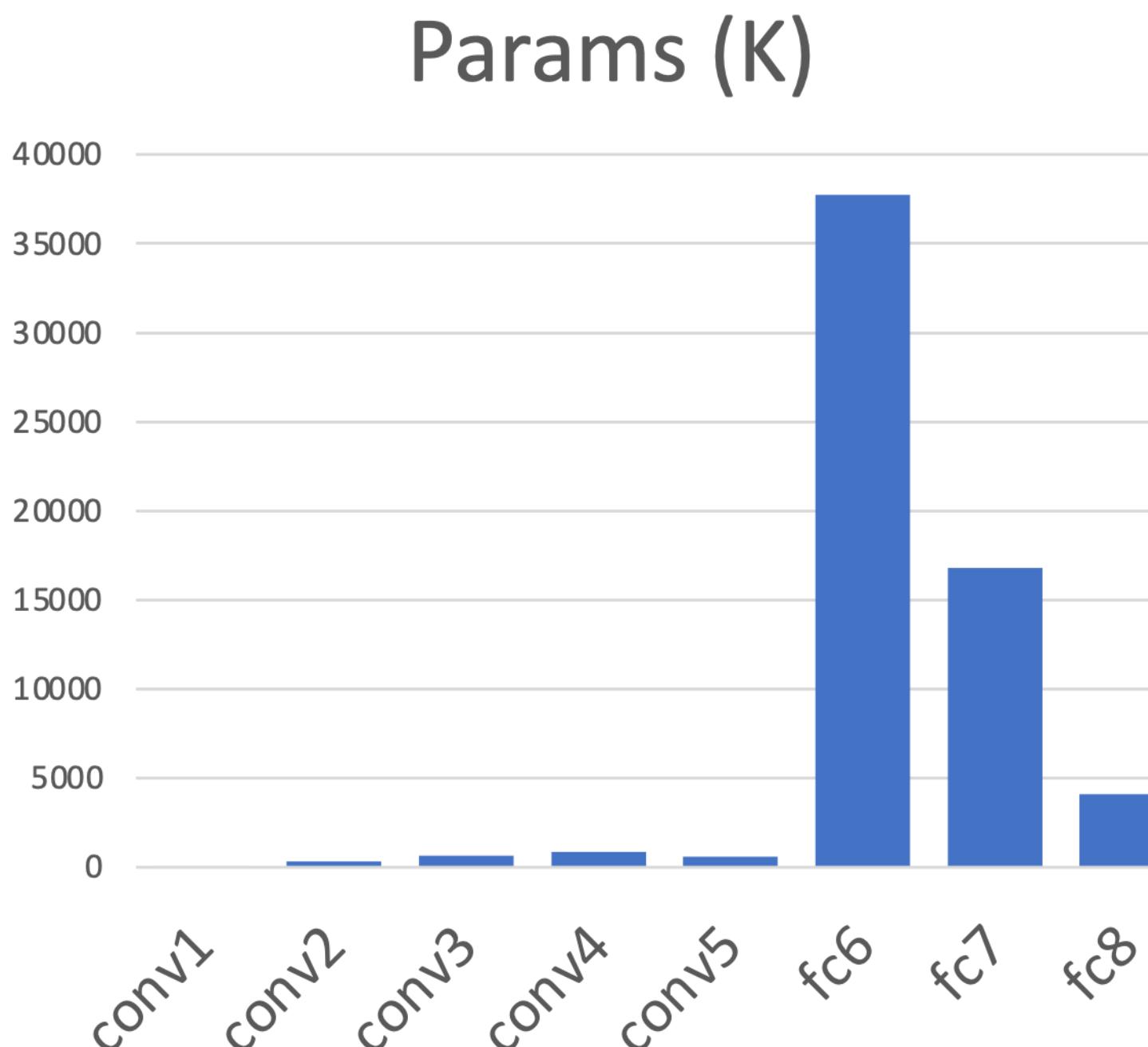
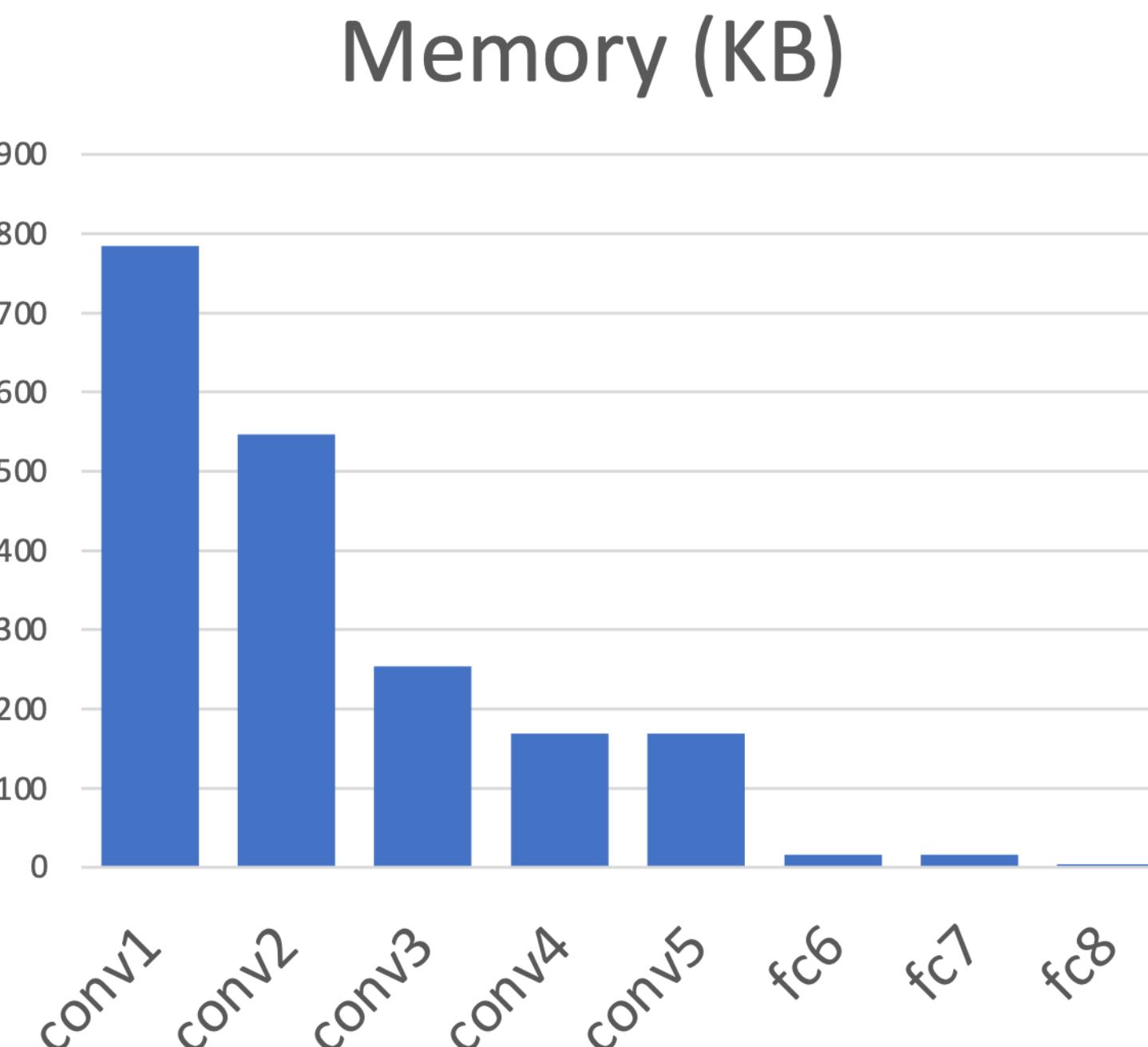
AlexNet



Most of the **memory usage** in the early convolution layers

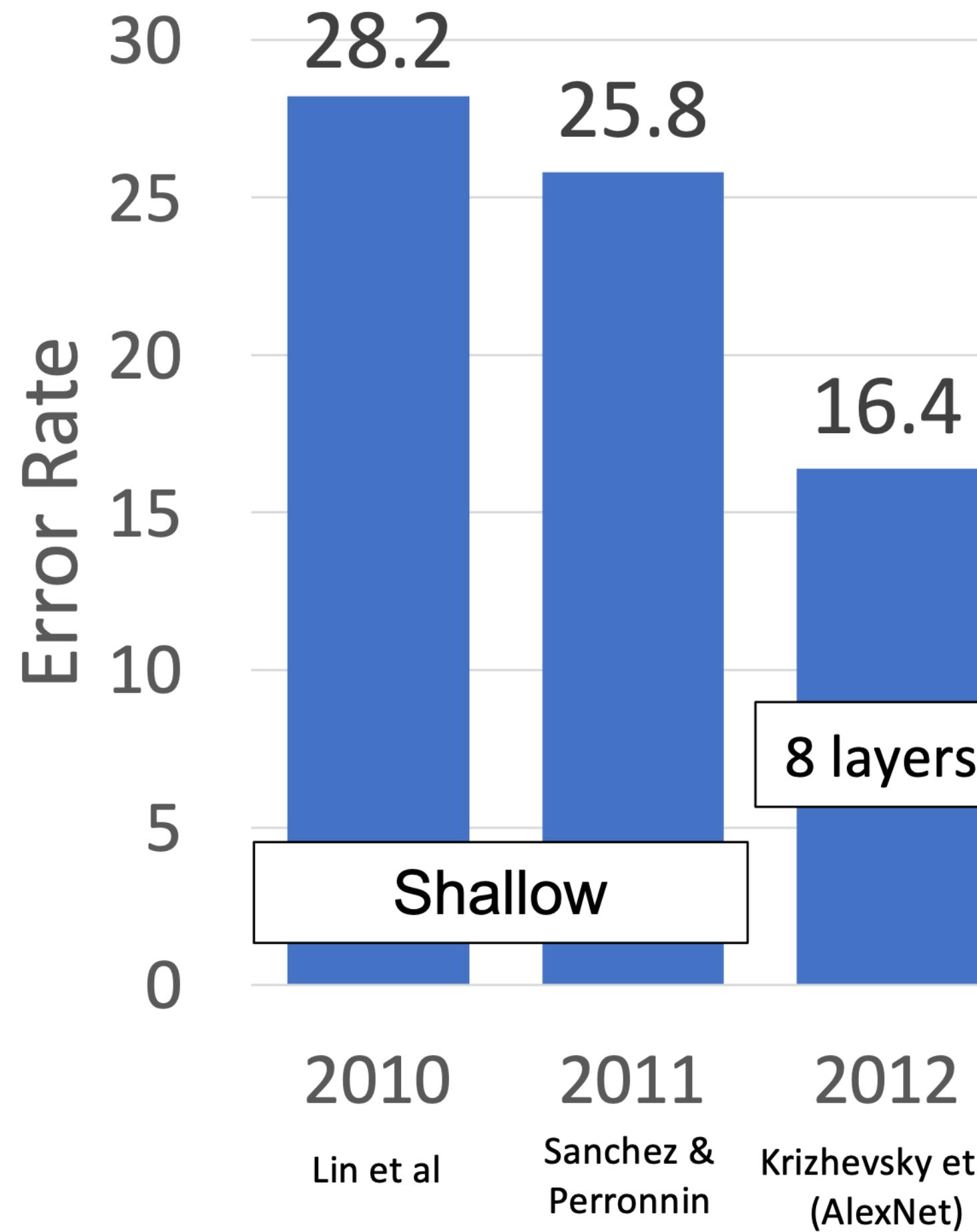
Nearly all **parameters** are in the fully-connected layers

Most **floating-point ops** occur in the convolution layers



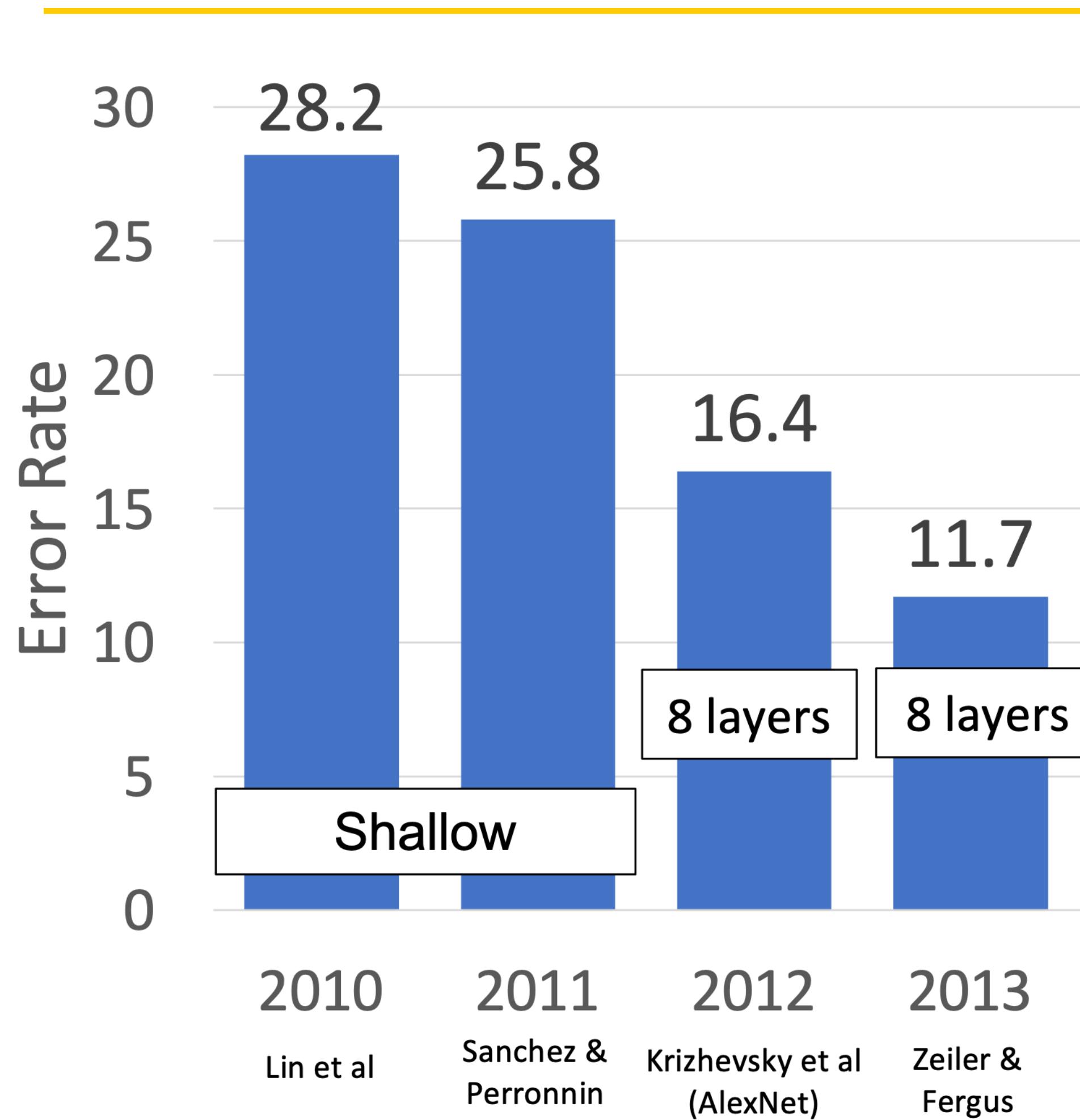


ImageNet Classification Challenge





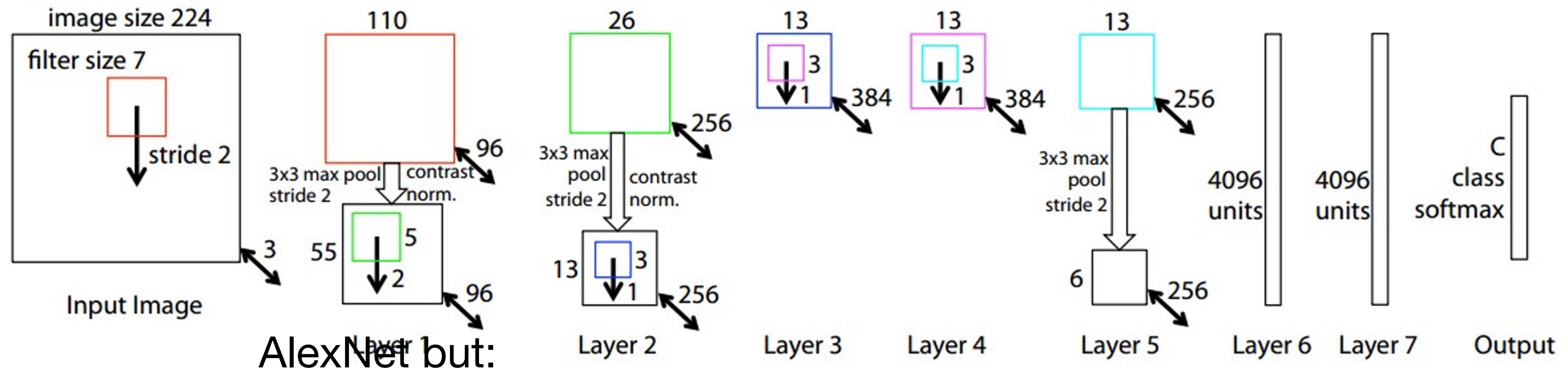
ImageNet Classification Challenge





ZFNet: A Bigger AlexNet

ImageNet top 5 error: 16.4% → 11.7%



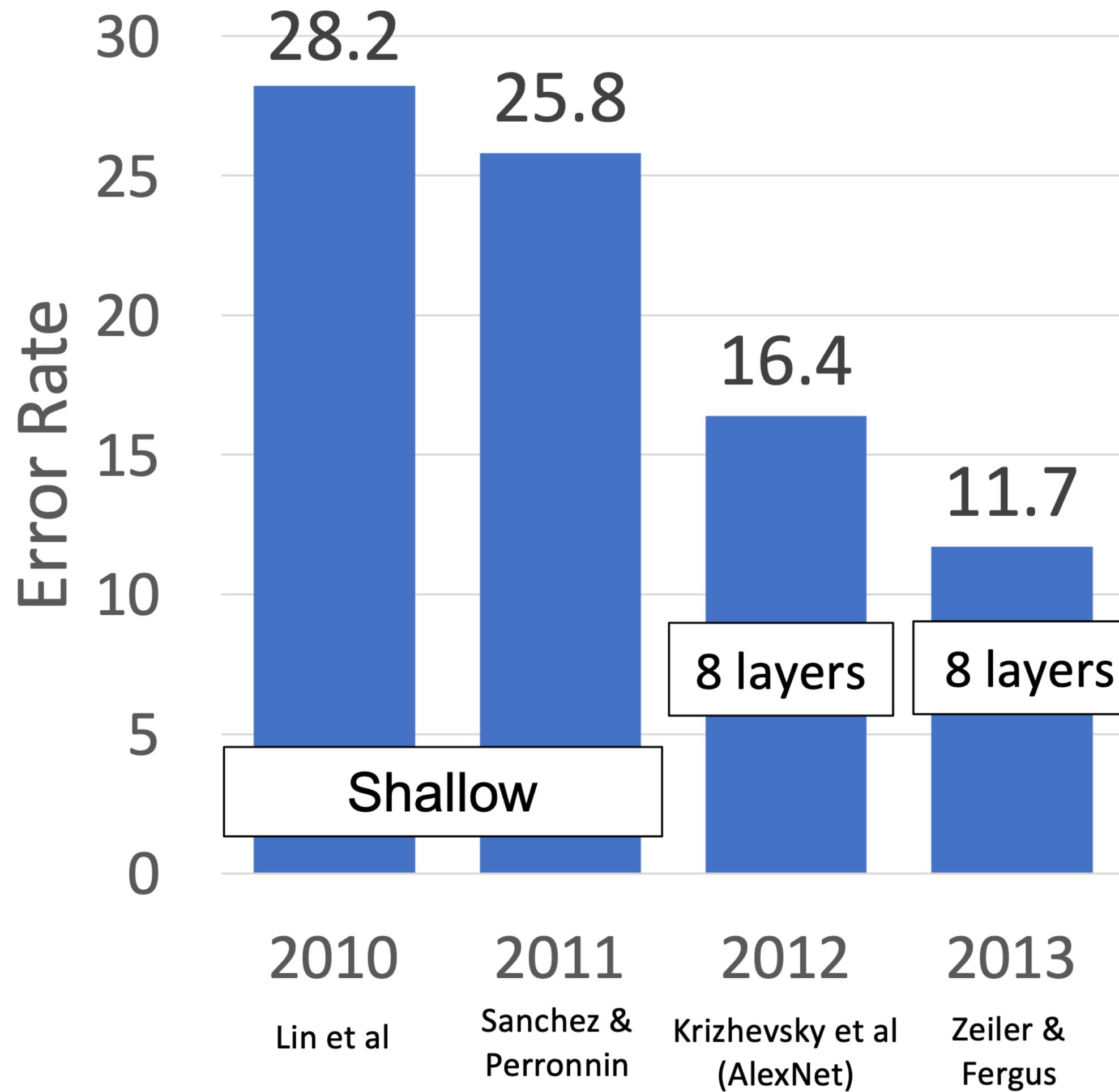
Conv1: change from (11x11 stride 4) to (7x7 stride 2)

Conv3,4,5: instead of 384, 384, 256 filters use 512, 1024, 512

More trial and error :(

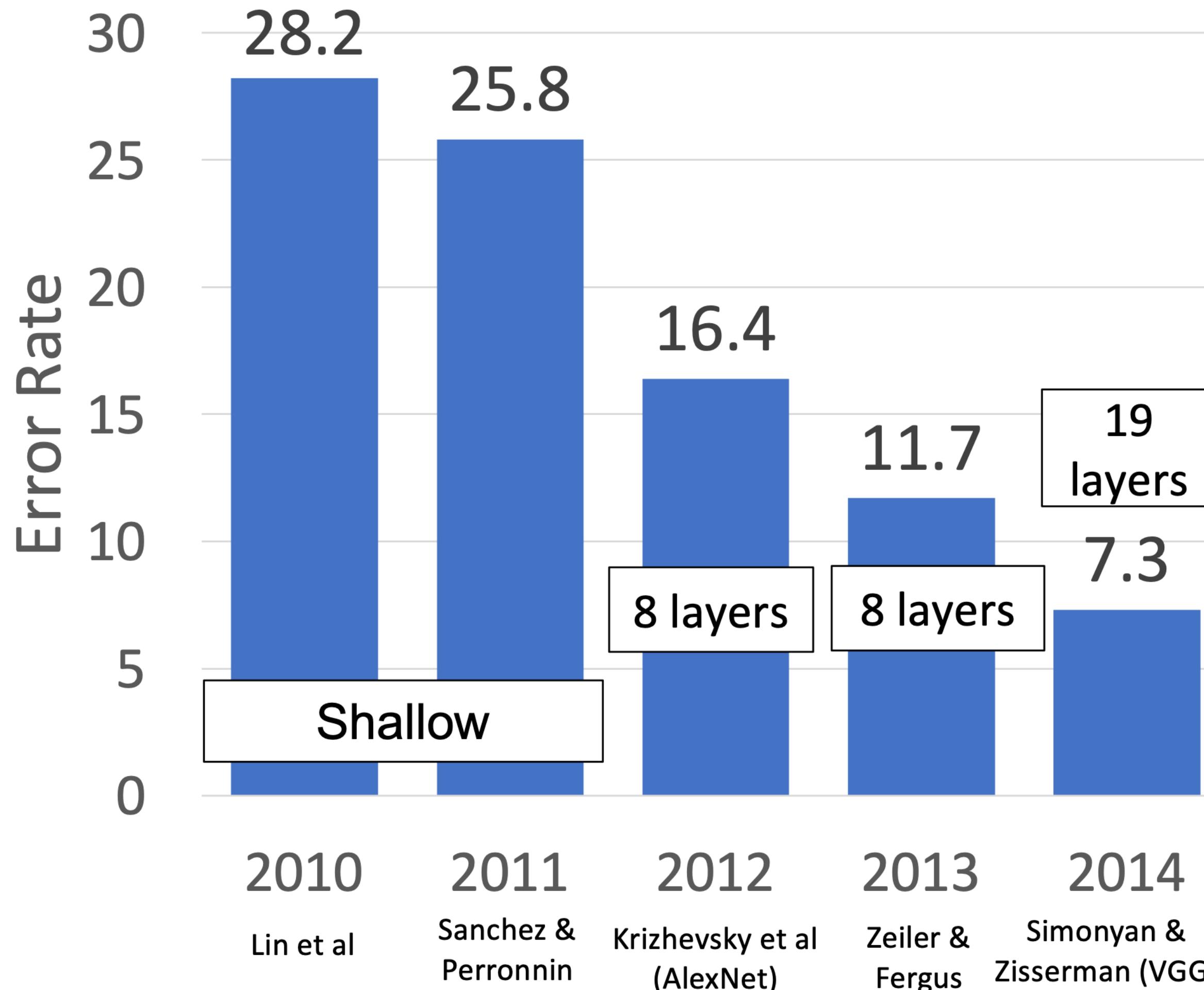


ImageNet Classification Challenge





ImageNet Classification Challenge





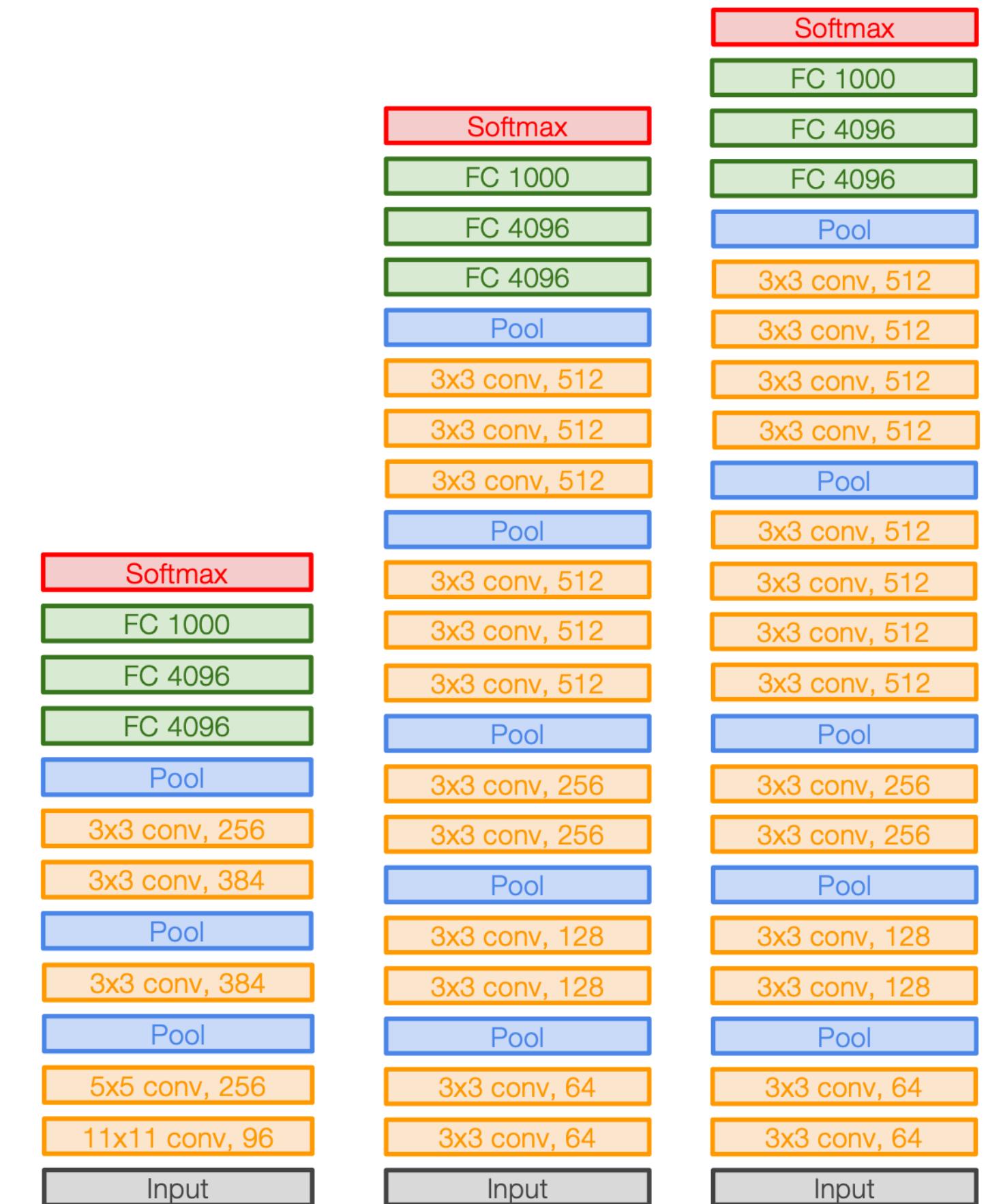
VGG: Deeper Networks, Regular Design

VGG Design rules:

All conv are 3x3 stride 1 pad 1

All max pool are 2x2 stride 2

After pool, double #channels



AlexNet

VGG16

VGG19



VGG: Deeper Networks, Regular Design

VGG Design rules:

All conv are 3x3 stride 1 pad 1

All max pool are 2x2 stride 2

After pool, double #channels

Network has 5 convolution **stages**:

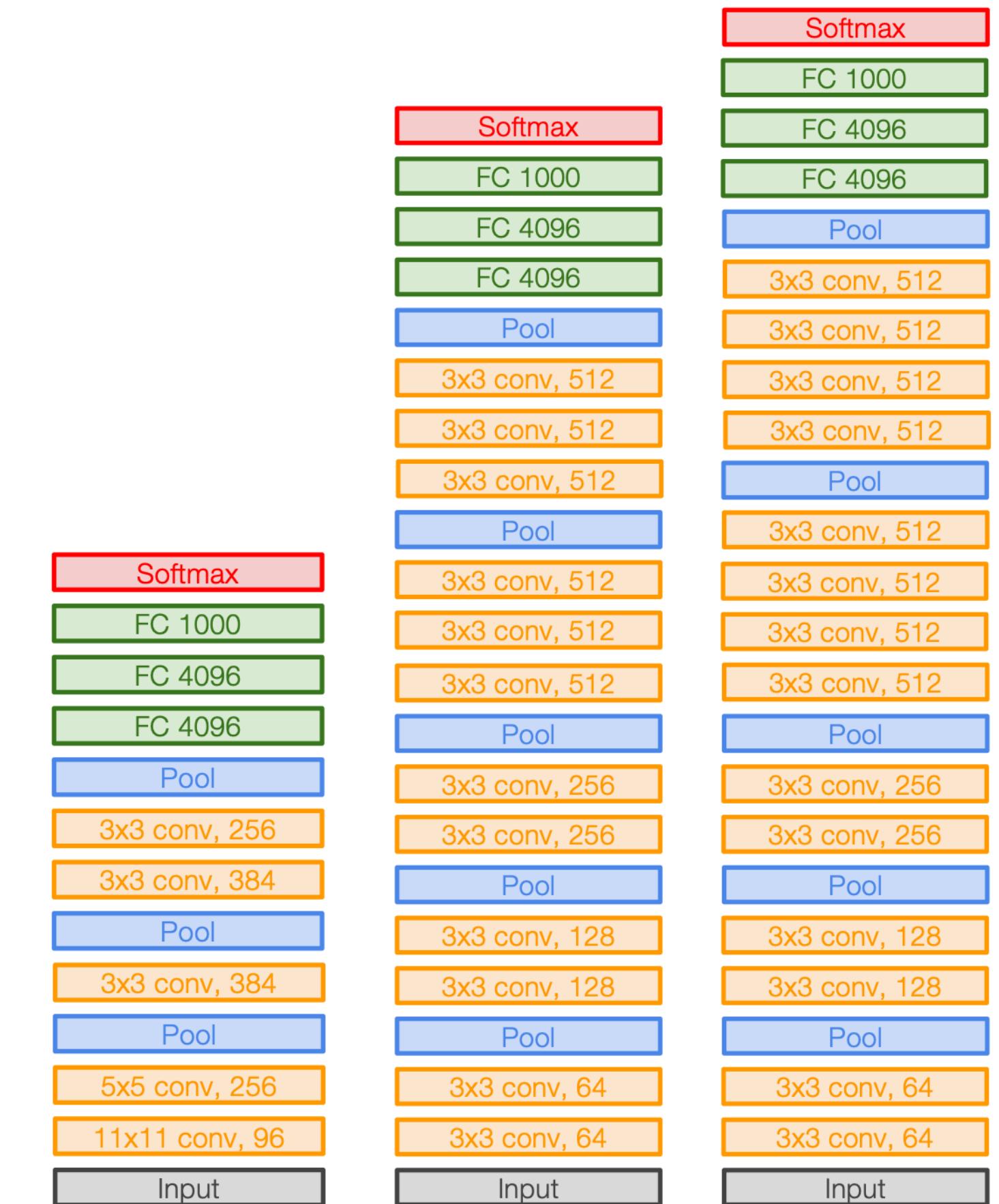
Stage 1: conv-conv-pool

Stage 2: conv-conv-pool

Stage 3: conv-conv-pool

Stage 4: conv-conv-conv-[conv]-pool

Stage 5: conv-conv-conv-[conv]-pool



AlexNet

VGG16

VGG19



VGG: Deeper Networks, Regular Design

VGG Design rules:

All conv are 3x3 stride 1 pad 1

All max pool are 2x2 stride 2

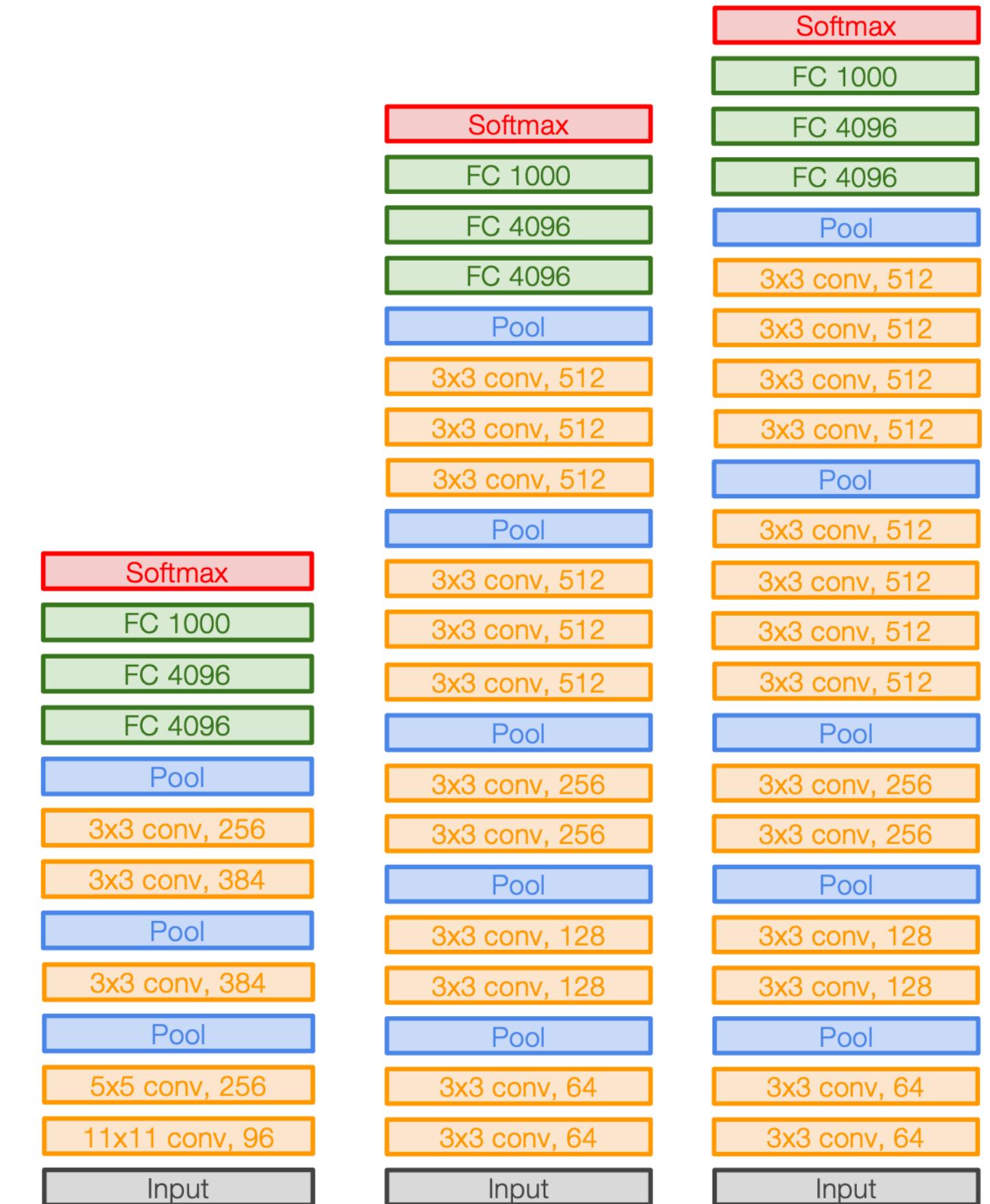
After pool, double #channels

Option 1:

Conv(5x5, C->C)

Params: $25C^2$

FLOPs: $25C^2HW$



AlexNet

VGG16

VGG19



VGG: Deeper Networks, Regular Design

VGG Design rules:

All conv are 3x3 stride 1 pad 1

All max pool are 2x2 stride 2

After pool, double #channels

Option 1:

Conv(5x5, C->C)

Params: $25C^2$

FLOPs: $25C^2HW$

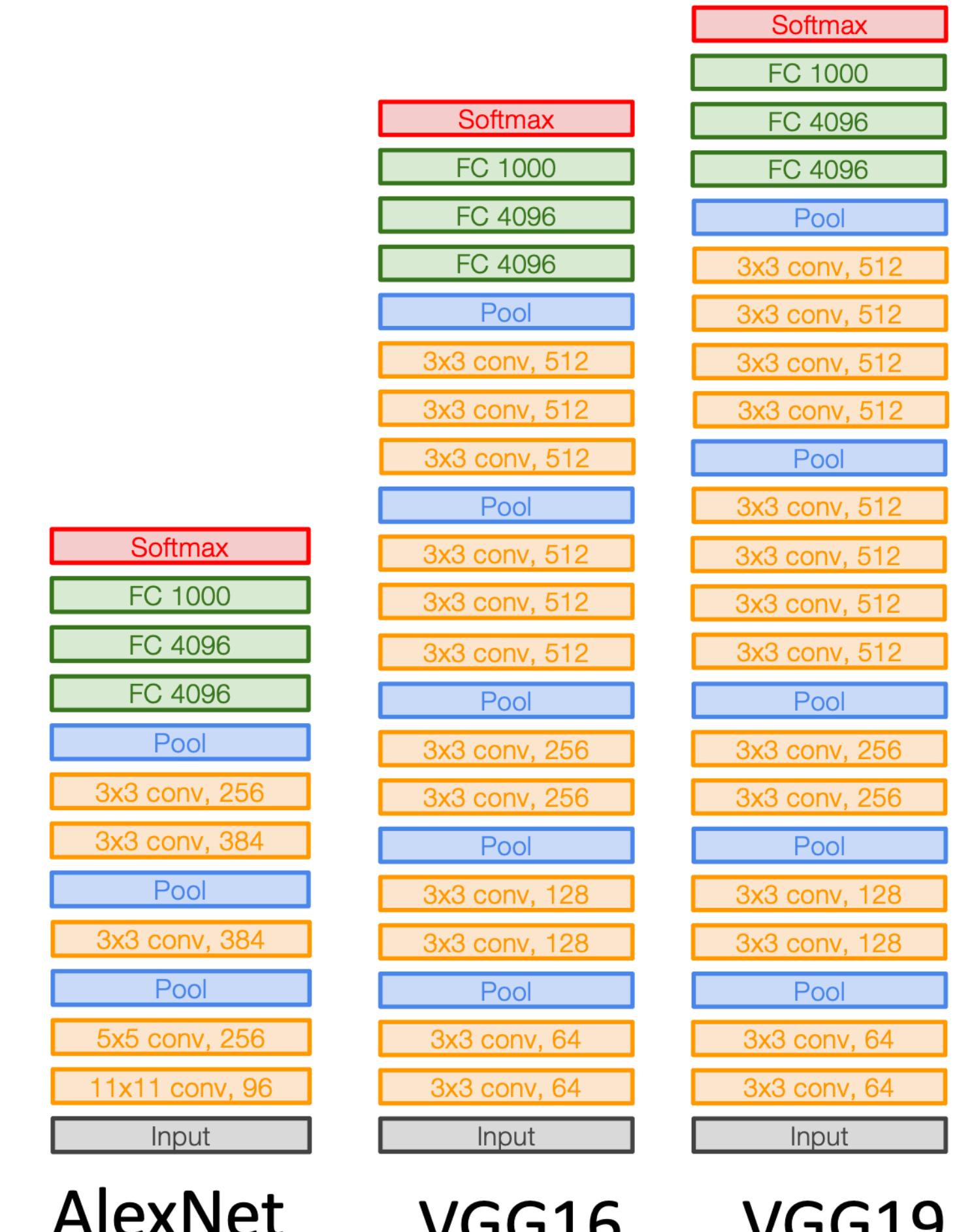
Option 2:

Conv(3x3, C->C)

Conv(3x3, C->C)

Params: $18C^2$

FLOPs: $18C^2HW$



AlexNet

VGG16

VGG19



VGG: Deeper Networks, Regular Design

VGG Design rules:

All conv are 3x3 stride 1 pad 1

All max pool are 2x2 stride 2

After pool, double #channels

Option 1:

Conv(5x5, C->C)

Params: $25C^2$

FLOPs: $25C^2HW$

Option 2:

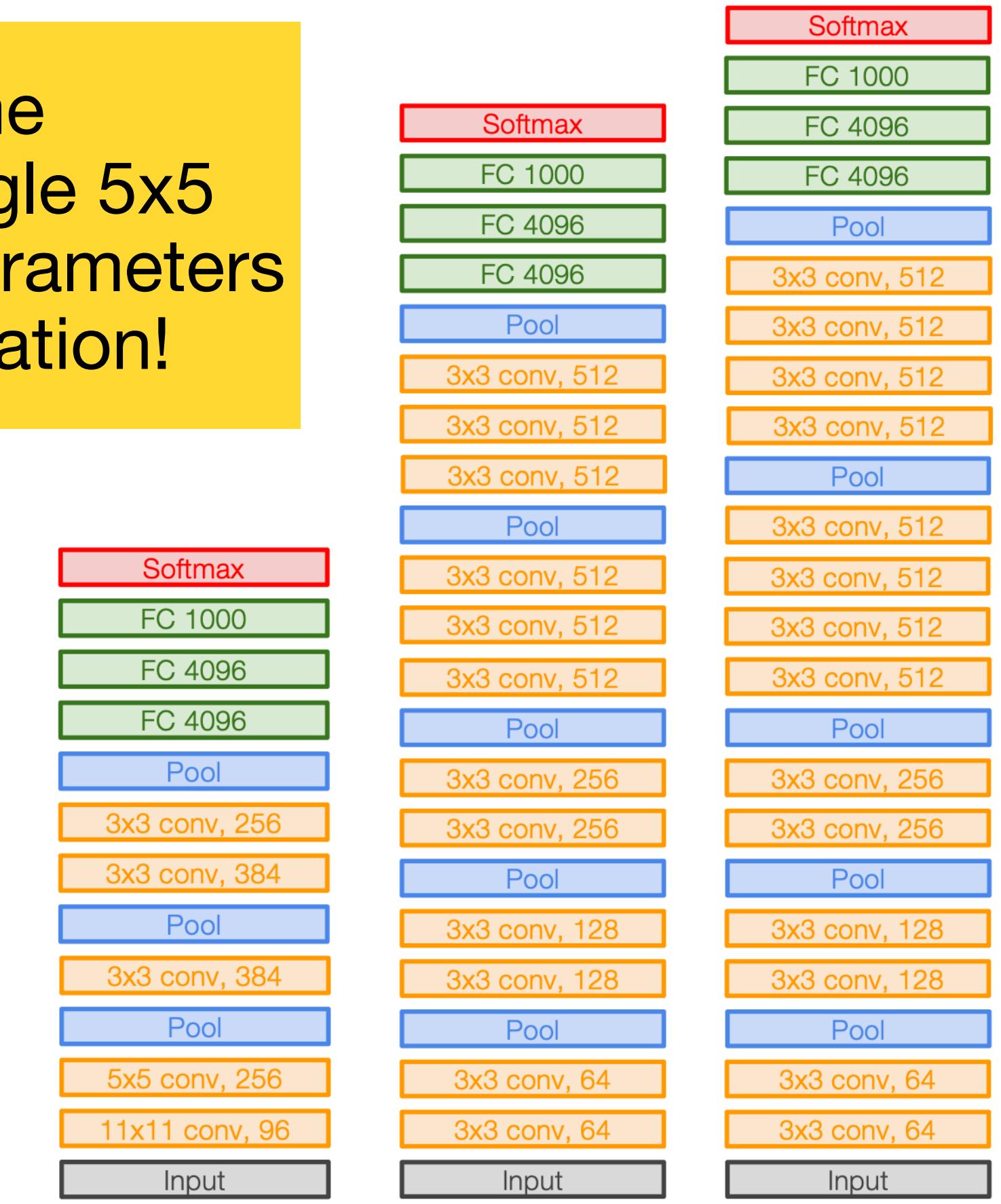
Conv(3x3, C->C)

Conv(3x3, C->C)

Params: $18C^2$

FLOPs: $18C^2HW$

Two 3x3 conv has same receptive field as a single 5x5 conv, but has fewer parameters and takes less computation!



AlexNet

VGG16

VGG19



VGG: Deeper Networks, Regular Design

VGG Design rules:

All conv are 3x3 stride 1 pad 1

All max pool are 2x2 stride 2

After pool, double #channels

Option 1:

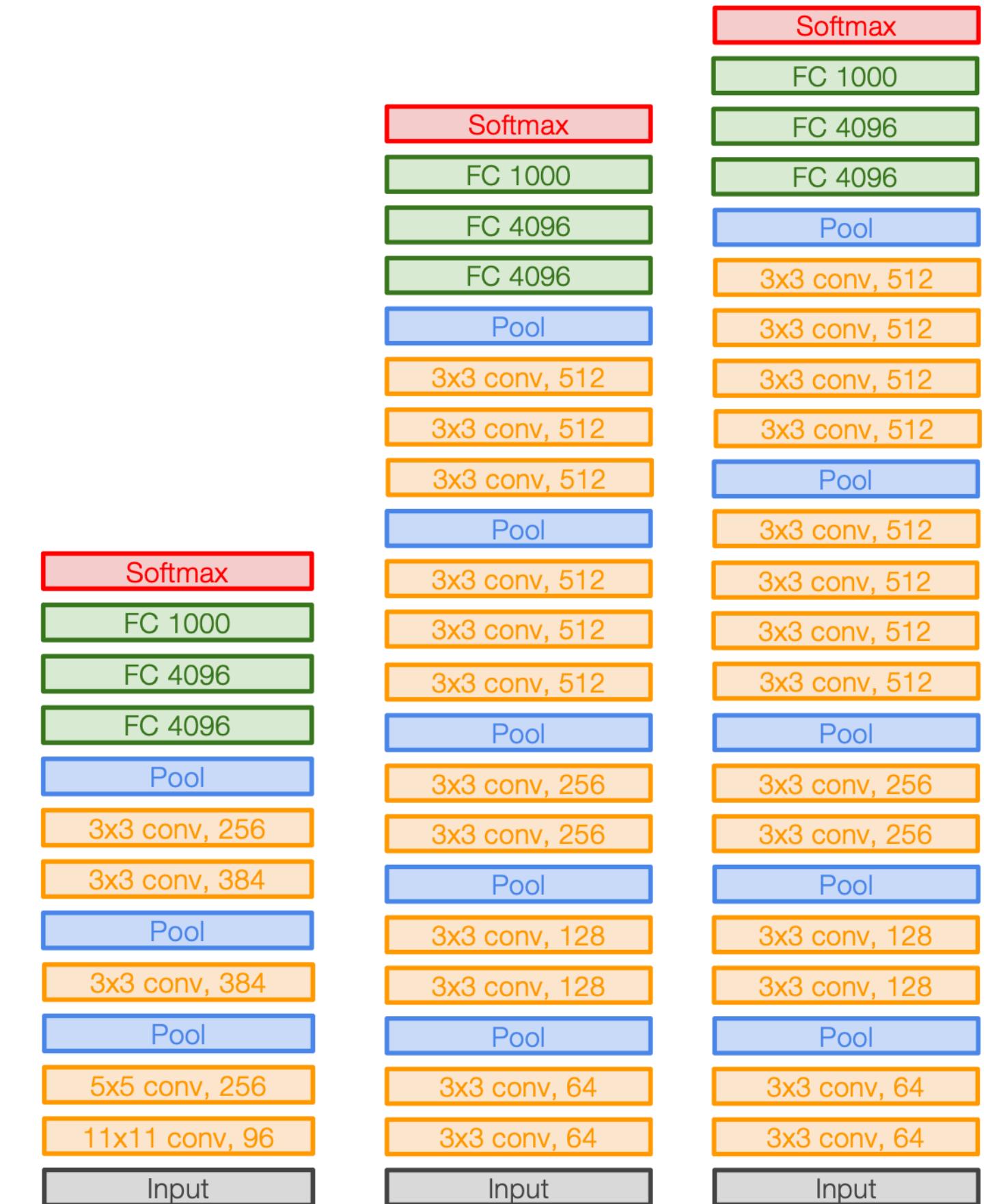
Input: $C \times 2H \times 2W$

Layer: Conv(3x3, $C \rightarrow C$)

Memory: 4HWC

Params: $9C^2$

FLOPs: $36HWC^2$



AlexNet

VGG16

VGG19



VGG: Deeper Networks, Regular Design

VGG Design rules:

All conv are 3x3 stride 1 pad 1

All max pool are 2x2 stride 2

After pool, double #channels

Option 1:

Input: $C \times 2H \times 2W$

Layer: Conv(3x3, $C \rightarrow C$)

Memory: 4HWC

Params: $9C^2$

FLOPs: $36HWC^2$

Option 2:

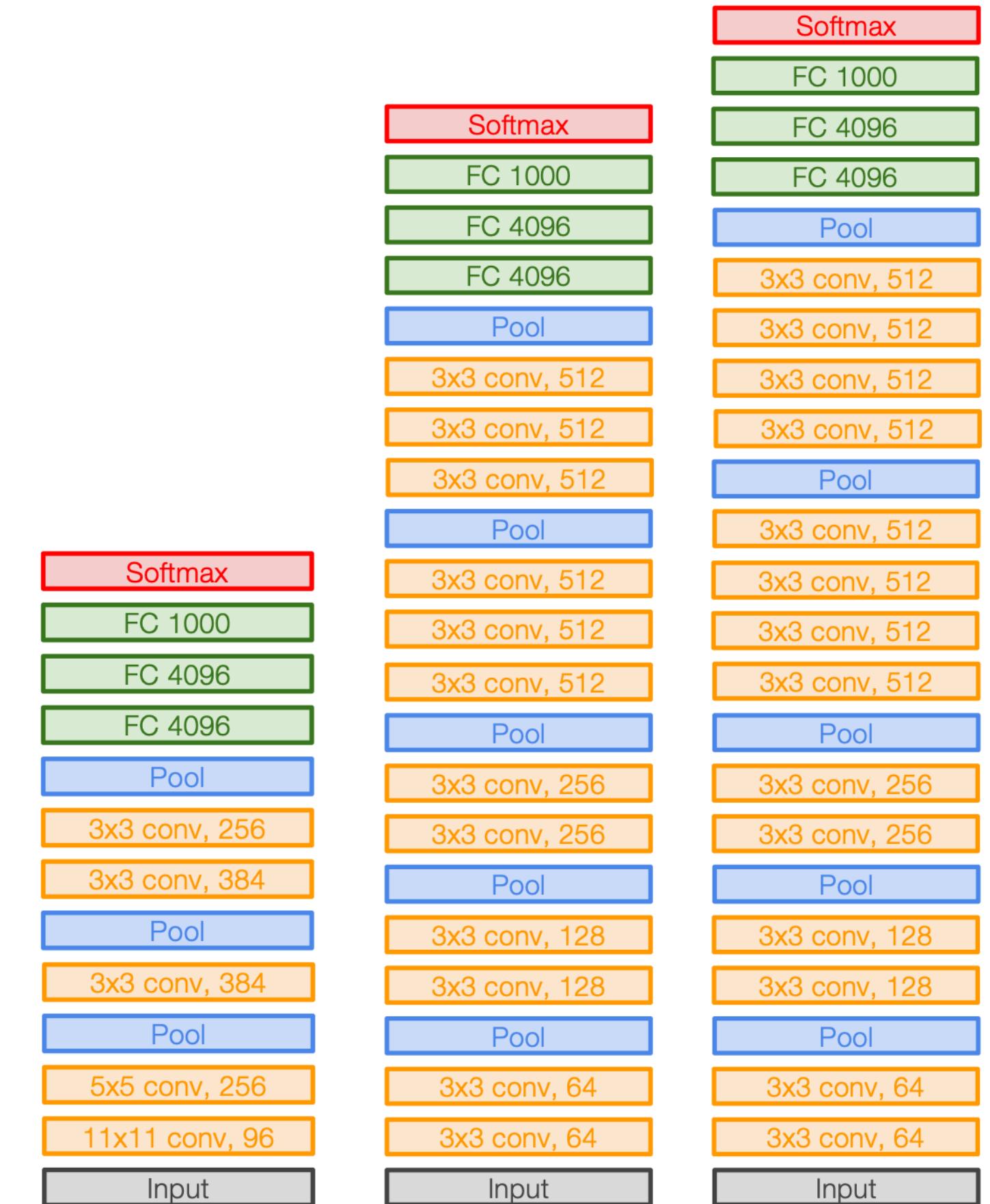
Input: $2C \times H \times W$

Layer: Conv(3x3, $2C \rightarrow 2C$)

Memory: 2HWC

Params: $36C^2$

FLOPs: $36HWC^2$



AlexNet

VGG16

VGG19



VGG: Deeper Networks, Regular Design

VGG Design rules:

All conv are 3x3 stride 1 pad 1

All max pool are 2x2 stride 2

After pool, double #channels

Option 1:

Input: $C \times 2H \times 2W$

Layer: Conv(3x3, $C \rightarrow C$)

Memory: 4HWC

Params: $9C^2$

FLOPs: $36HWC^2$

Option 2:

Input: $2C \times H \times W$

Layer: Conv(3x3, $2C \rightarrow 2C$)

Memory: 2HWC

Params: $36C^2$

FLOPs: $36HWC^2$

Conv layers at each spatial resolution take the same amount of computation!



AlexNet

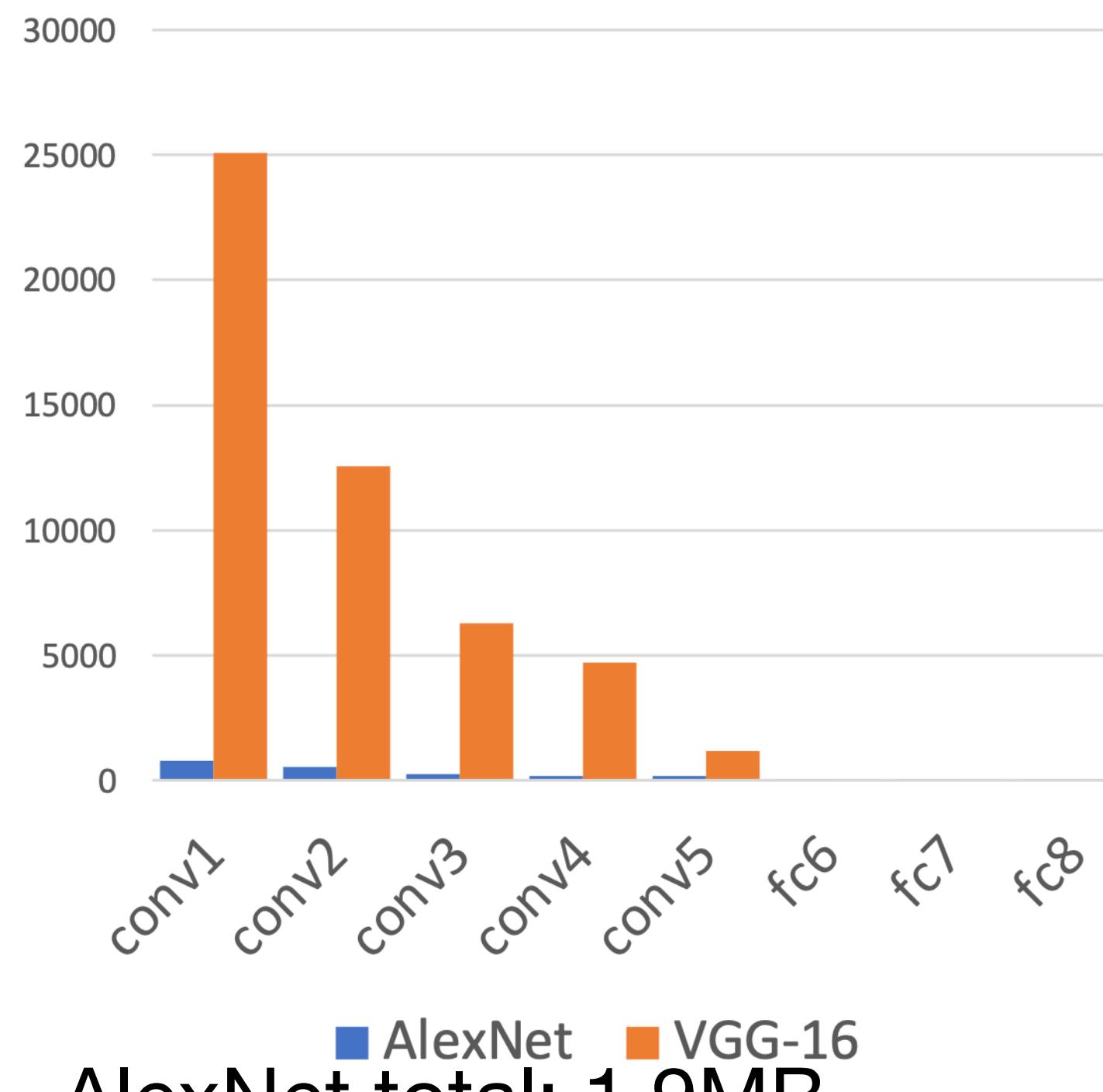
VGG16

VGG19



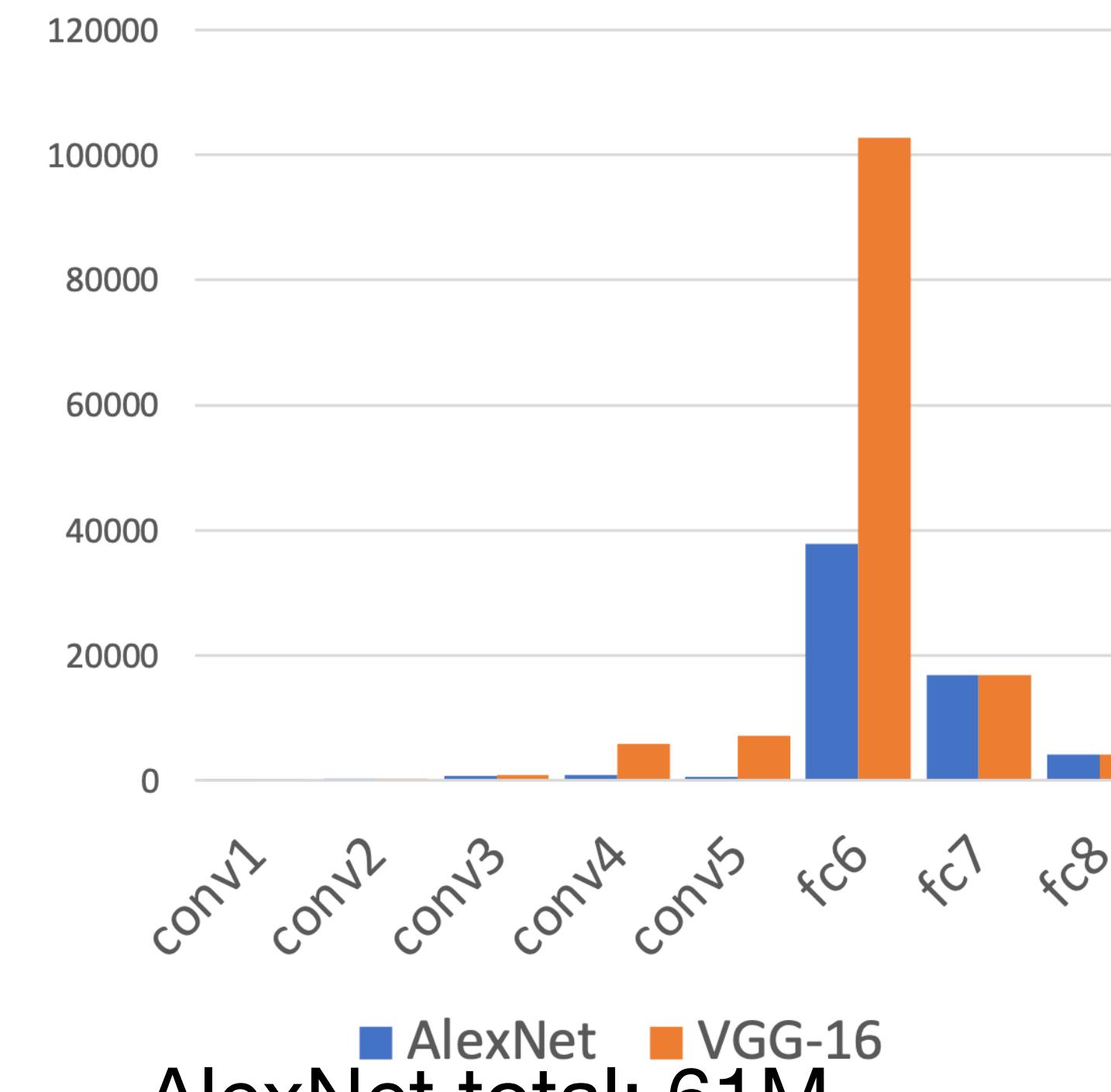
AlexNet vs VGG-16: Much bigger network!

AlexNet vs VGG-16
(Memory, KB)



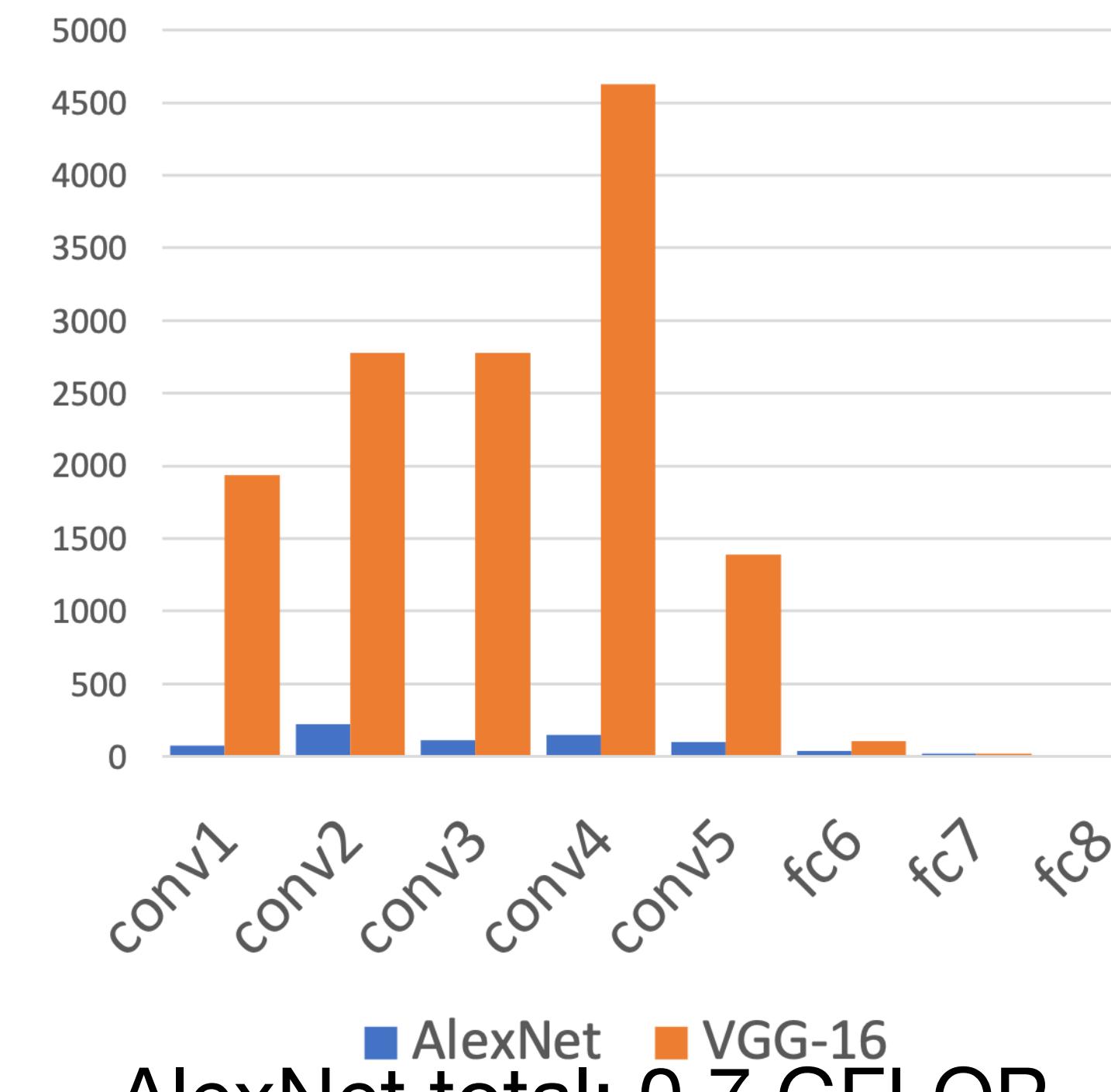
VGG-16 total: 48.6MB (25x)

AlexNet vs VGG-16
(Params, M)



VGG-16 total: 138M (2.3x)

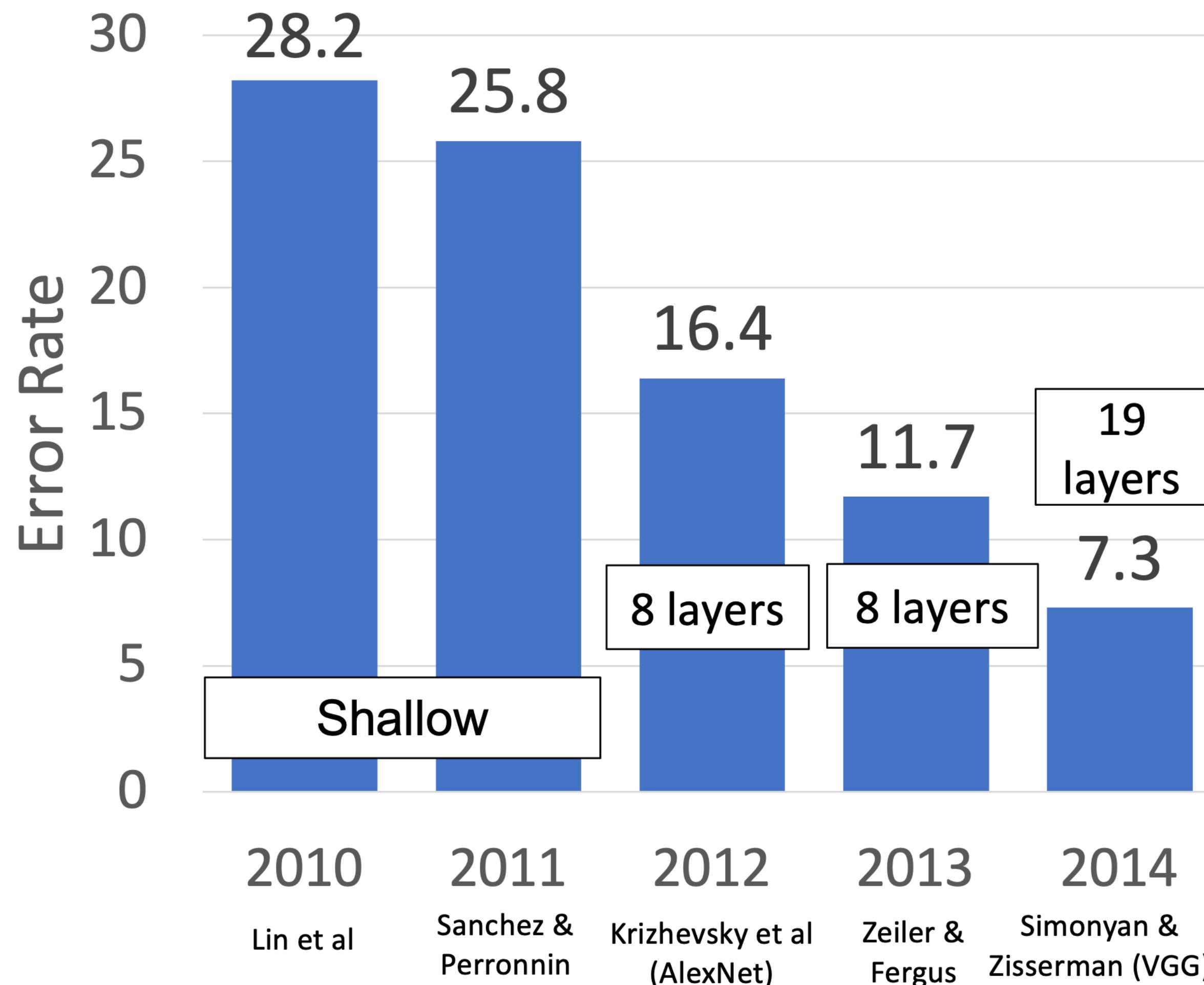
AlexNet vs VGG-16
(MFLOPs)



VGG-16 total: 13.6 GFLOP (19.4x)

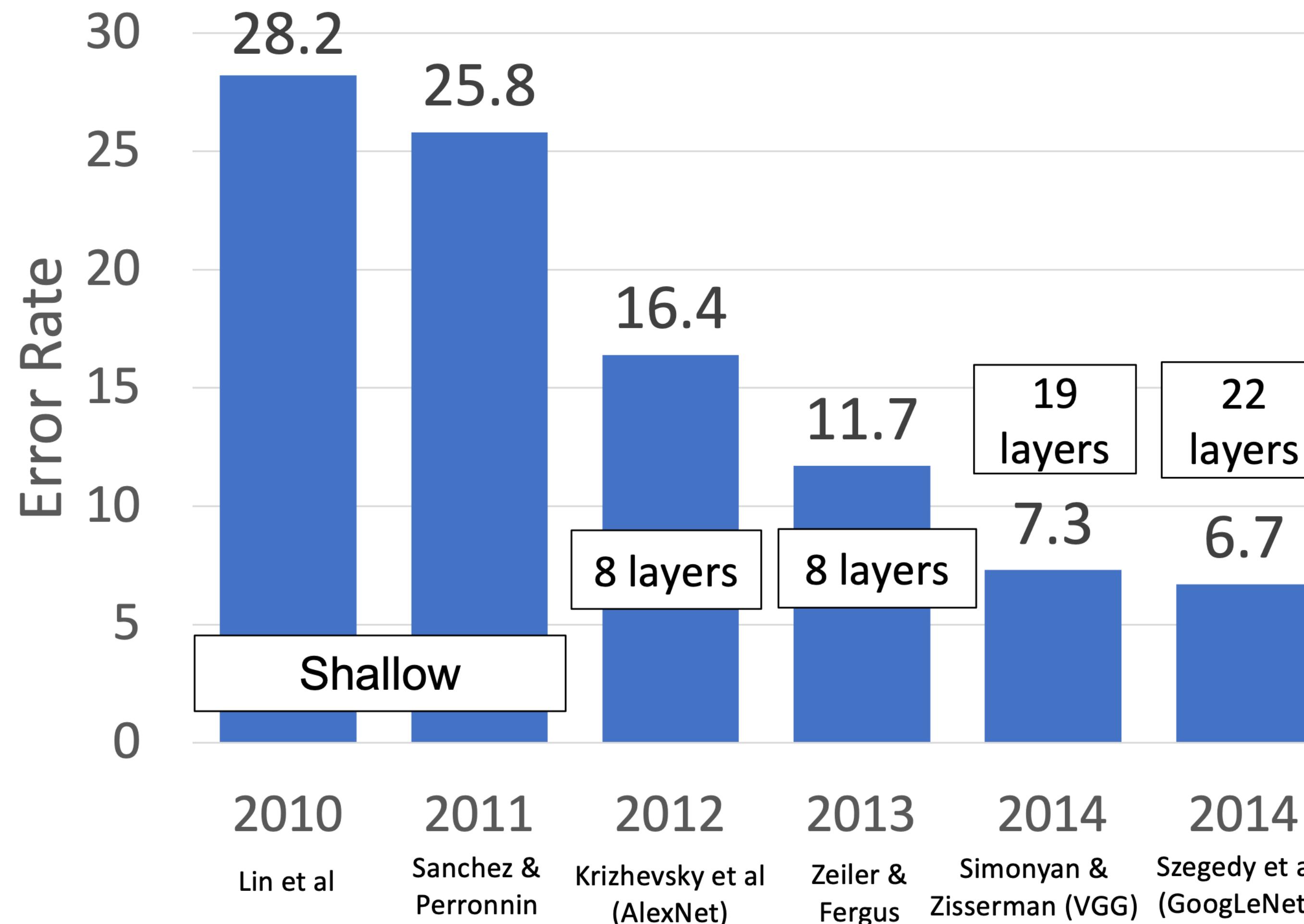


ImageNet Classification Challenge





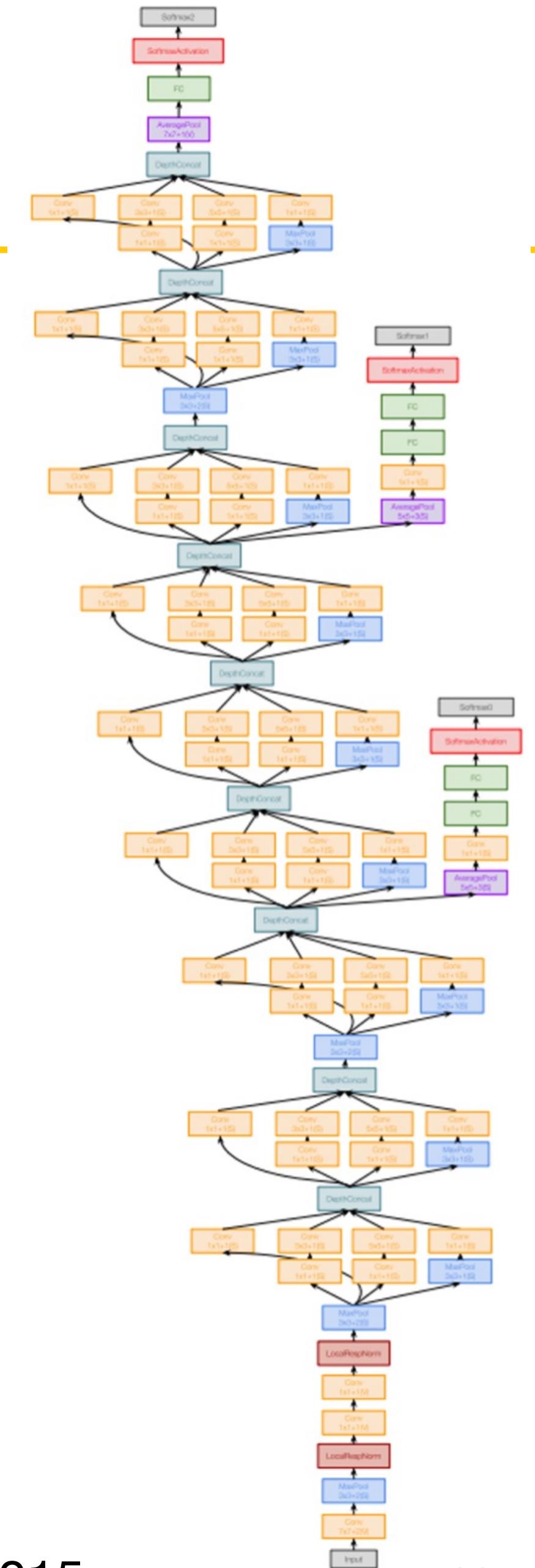
ImageNet Classification Challenge





GoogLeNet: Focus on Efficiency

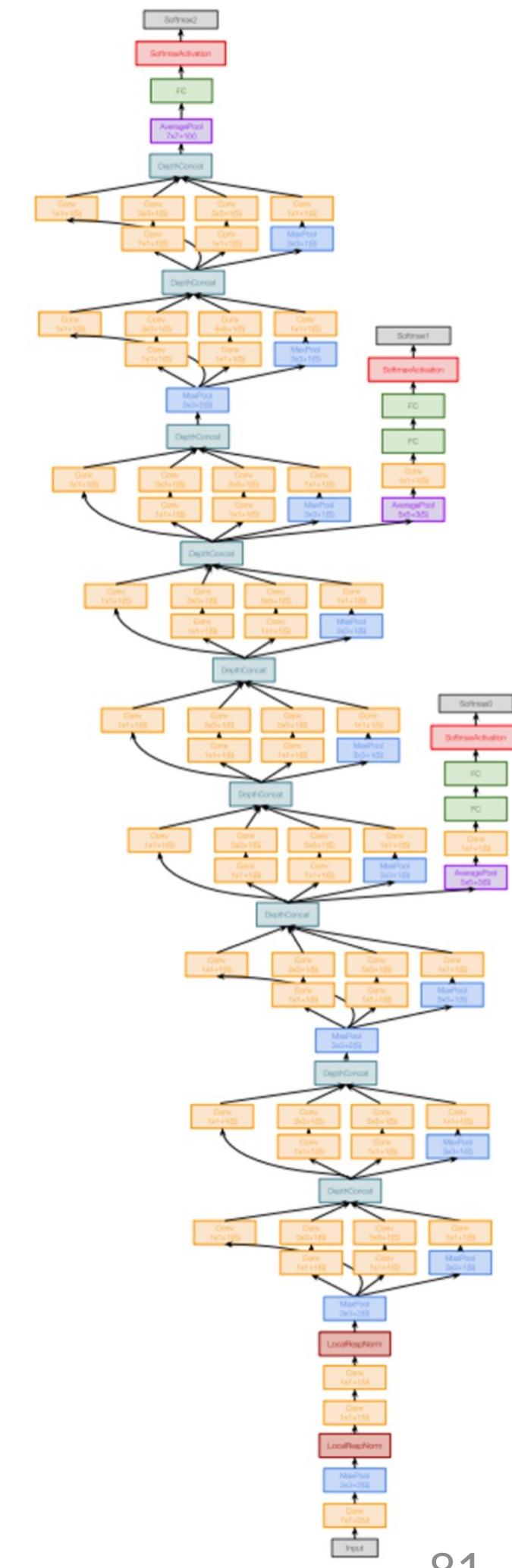
Many innovations for efficiency: reduce parameter count, memory usage, and computation





GoogLeNet: Aggressive Stem

Stem network at the start aggressively downsamples input
(Recall in VGG-16: Most of the compute was at the start)

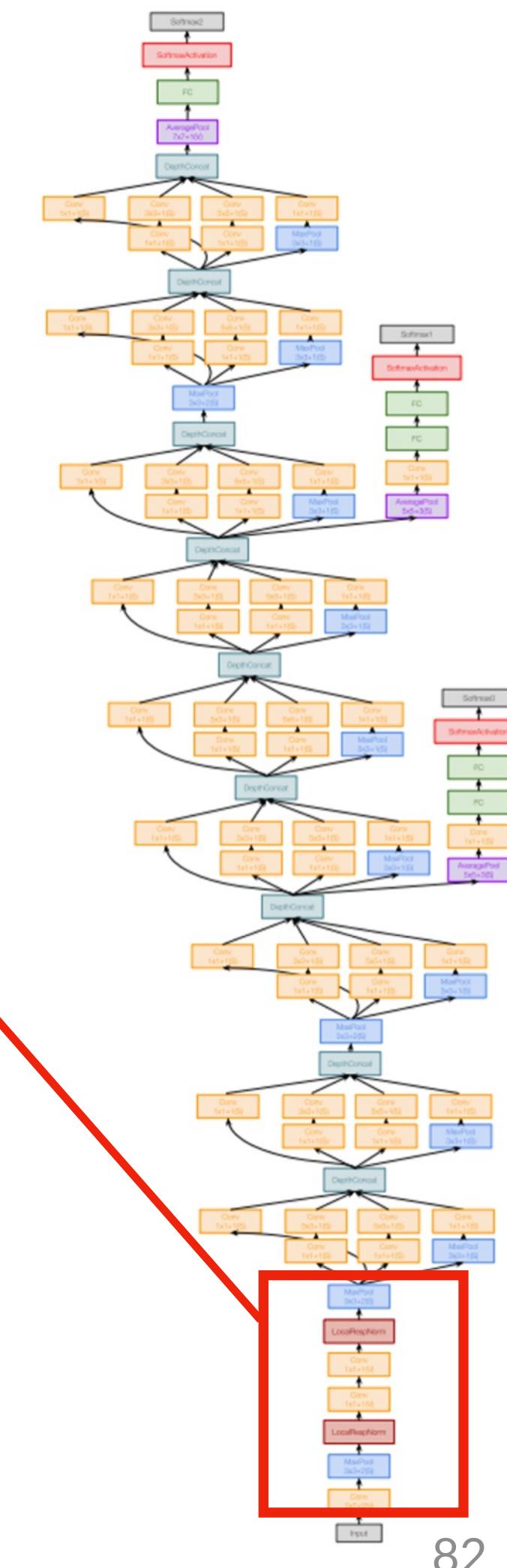




GoogLeNet: Aggressive Stem

Stem network at the start aggressively downsamples input
(Recall in VGG-16: Most of the compute was at the start)

Layer	Input size		Layer				Output size		Memory (KB)	Params (k)	Flop (M)
	C	H/W	Filters	Kernel	Stride	Pad	C	H/W			
Conv Poo	3	224	64	7	2	3	64	112	3136	9	118
Max-pool	64	112		3	2	1	64	56	784	0	2
Conv Poo	64	56	64	1	1	0	64	56	784	4	13
Conv Poo	64	56	192	3	1	1	192	56	2352	111	347
Max-pool	192	56		3	2	1	192	28	588	0	1





GoogLeNet: Aggressive Stem

Stem network at the start aggressively downsamples input
(Recall in VGG-16: Most of the compute was at the start)

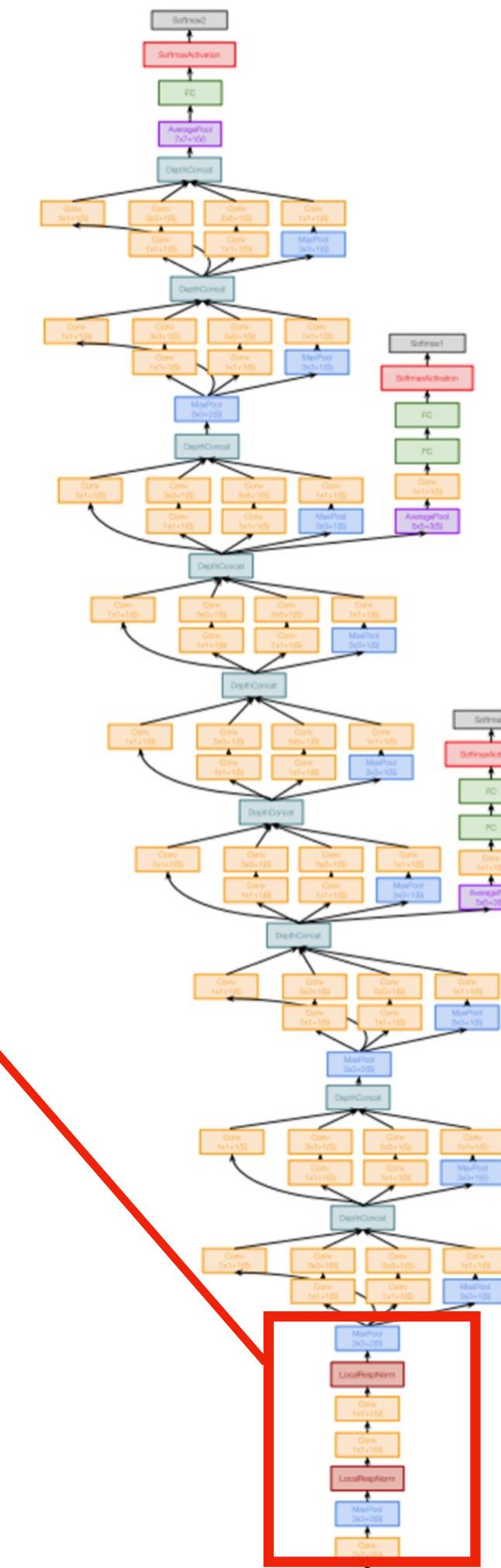
	Input size		Layer				Output size				
Layer	C	H/W	Filters	Kernel	Strid	Pad	C	H/W	Memory	Params	Flop (M)
Conv	3	224	64	7	2	3	64	112	3136	9	118
Max-pool	64	112		3	2	1	64	56	784	0	2
Conv	64	56	64	1	1	0	64	56	784	4	13
Conv	64	56	192	3	1	1	192	56	2352	111	347
Max-pool	192	56		3	2	1	192	28	588	0	1

Total from 224 to 28 spatial resolution:

Memory: 7.5 MB
Params: 124K
MFLOP: 418

Compare VGG-16:

Memory: 42.9 MB (5.7x)
Params: 1.1M (8.9x)
MFLOP: 7485 (17.8x)

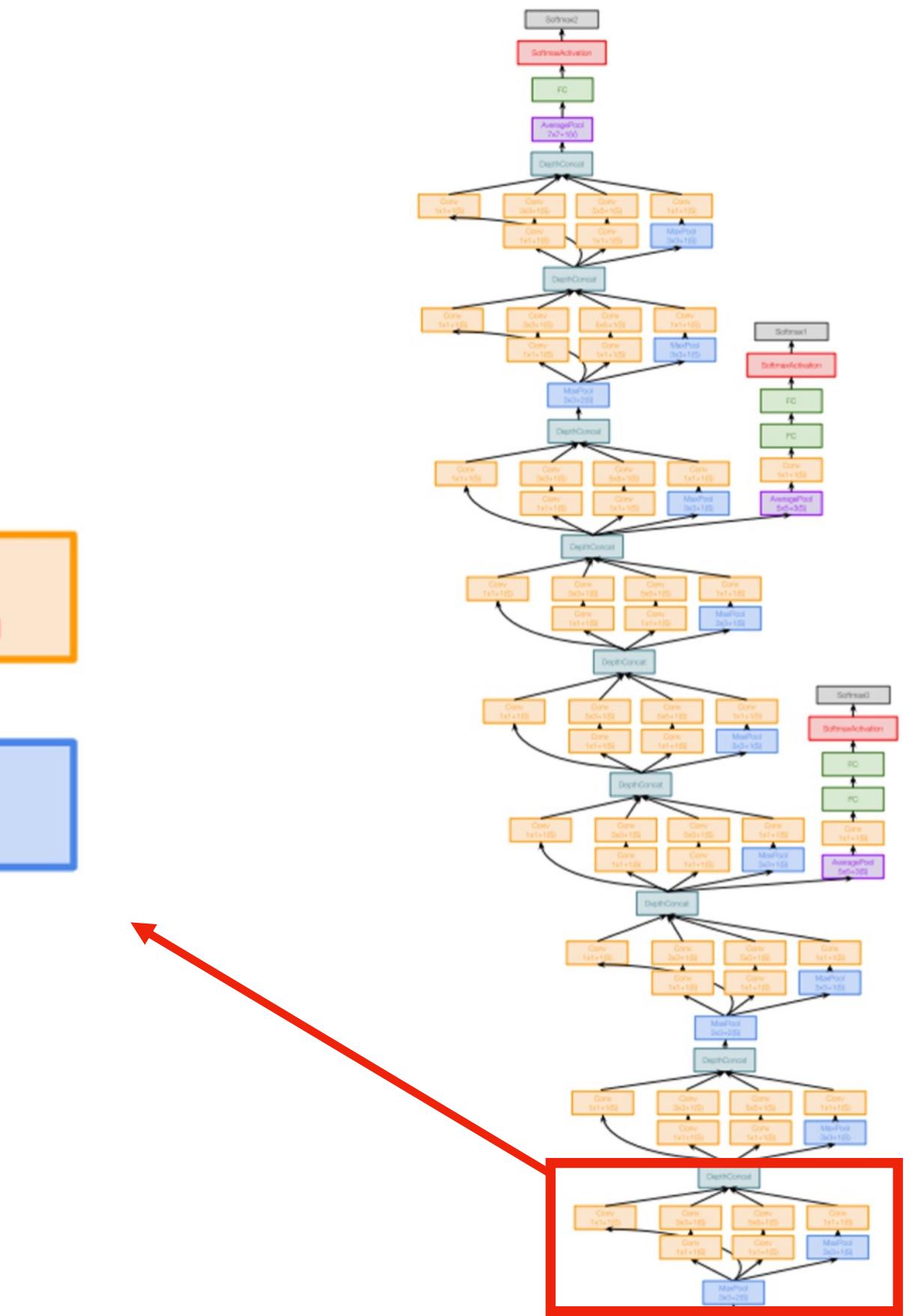
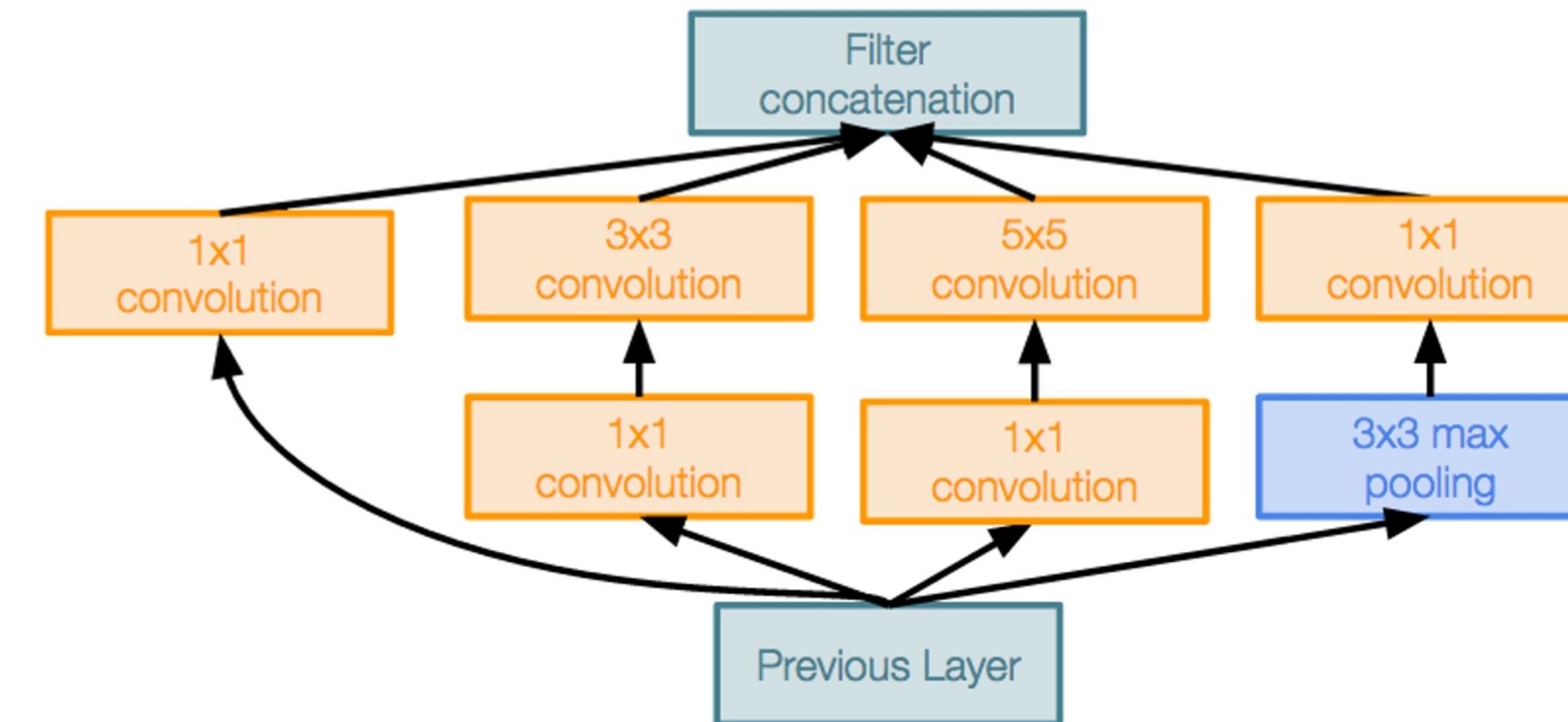




GoogLeNet: Inception Module

Inception module: Local unit with parallel branches

Local structure repeated many times throughout the network



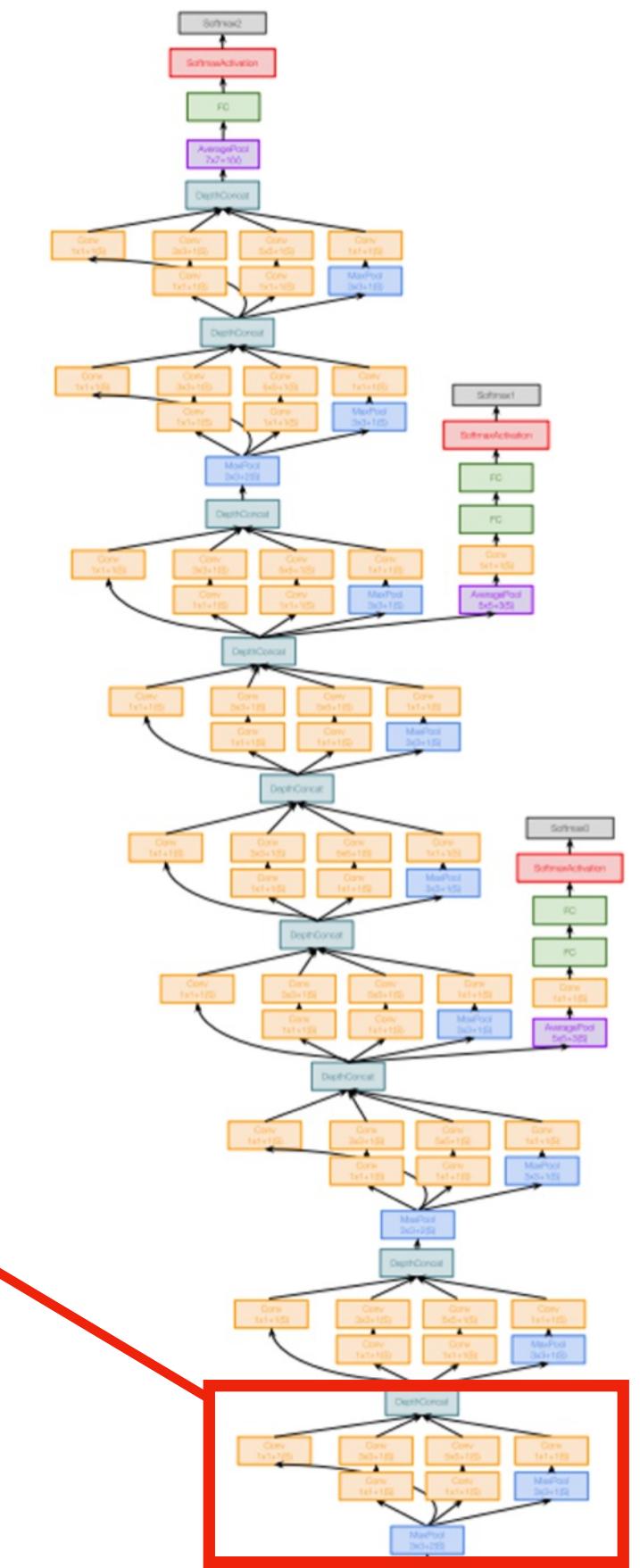
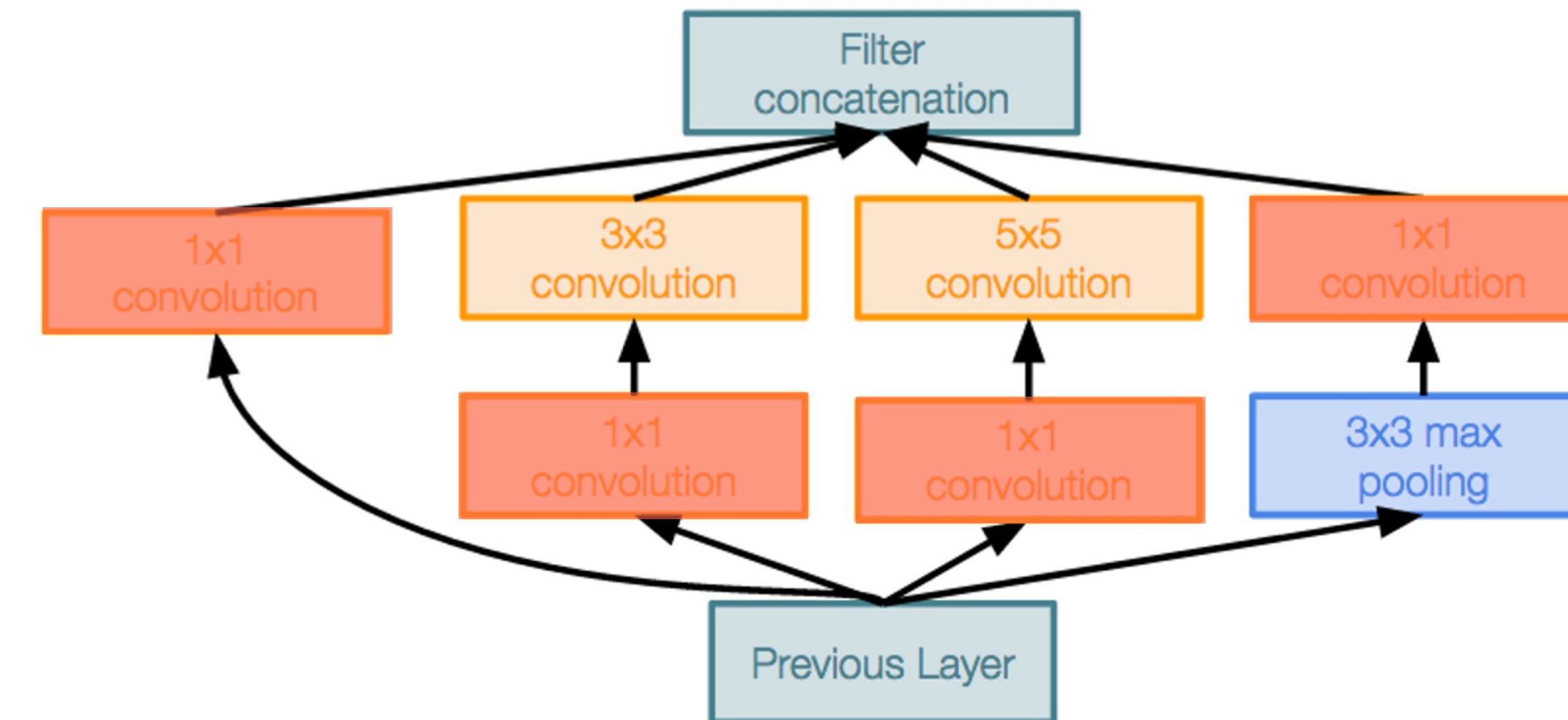


GoogLeNet: Inception Module

Inception module: Local unit with parallel branches

Local structure repeated many times throughout the network

Uses 1x1 “Bottleneck” layers to reduce channel dimension before expensive conv (we will revisit this with ResNet!)





GoogLeNet: Global Average Pooling

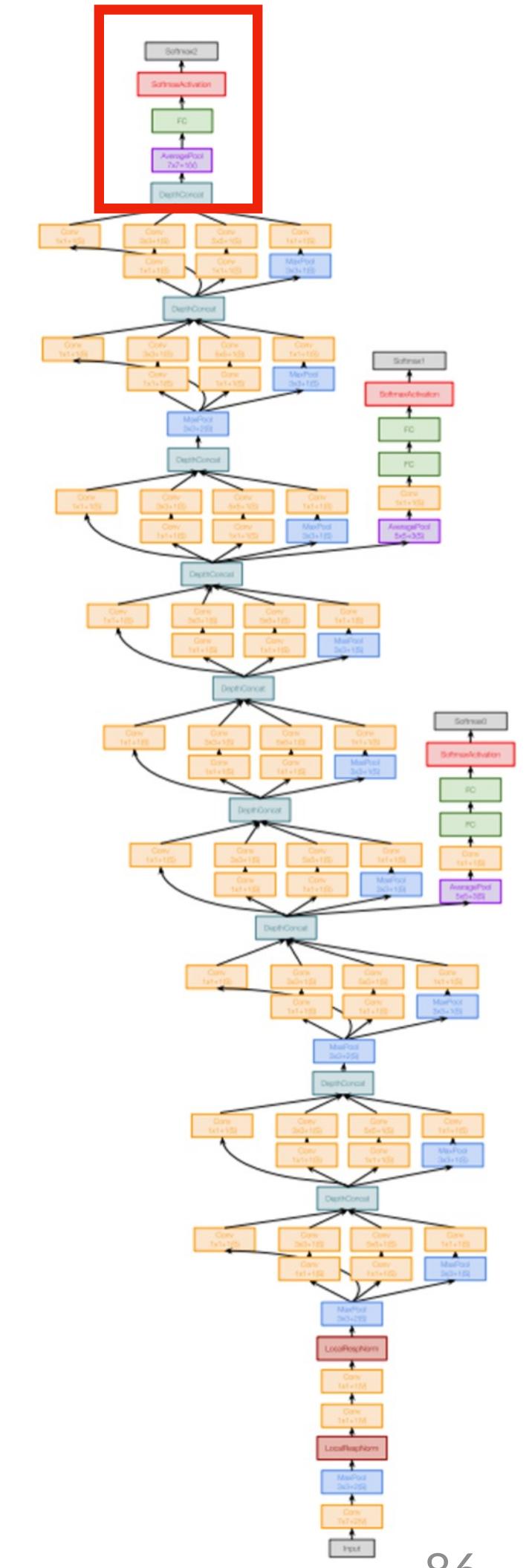
No large FC layers at the end!

Instead use **global average pooling** to collapse spatial dimensions, and one linear layer to produce class scores
(Recall VGG-16: Most parameters were in the FC layers!)

Layer	Input size		Layer				Output size		Memory (KB)	Params	Flop (M)
	C	H/W	Filters	Kernel	Stride	Pad	C	H/W			
avg-pool	1024	7		7	1	0	1024	1	4	0	0
fc	1024		1000				1000	0	0	1025	1

Compare with VGG-16:

Layer	Input size		Layer				Output size		Memory (KB)	Params	Flop (M)
	C	H/W	Filters	Kernel	Stride	Pad	C	H/W			
Flatten	512	7					25088		98		
FC6	25088			4096			4096		16	102760	103
FC7	4096			4096			4096		16	16777	17
FC8	4096		1000				1000		4	4096	4



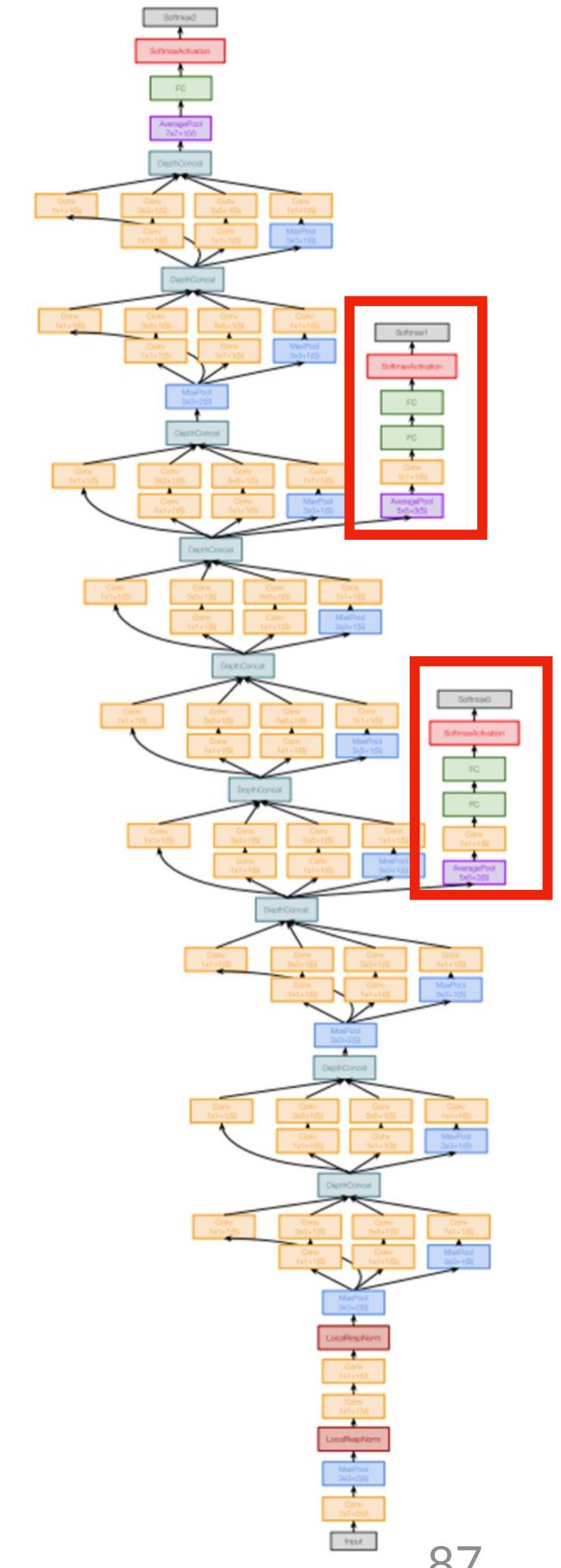


GoogLeNet: Auxiliary Classifiers

Training using loss at the end of the network didn't work well: Network is too deep, gradients don't propagate cleanly

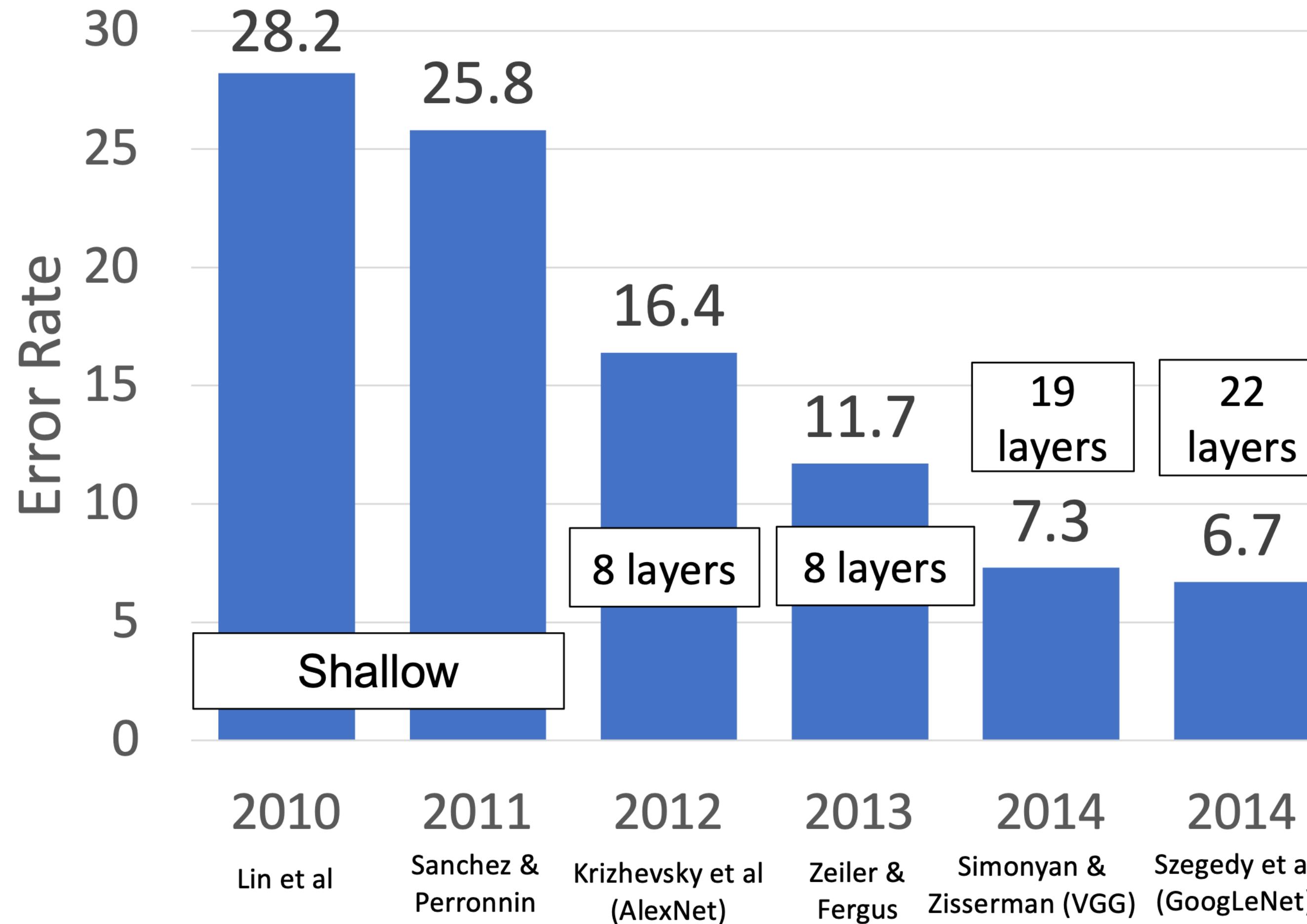
As a hack, attach “auxiliary classifiers” at several intermediate points in the network that also try to classify the image and receive loss

GoogLeNet was before batch normalization! With **BatchNorm**, we no longer need to use this trick



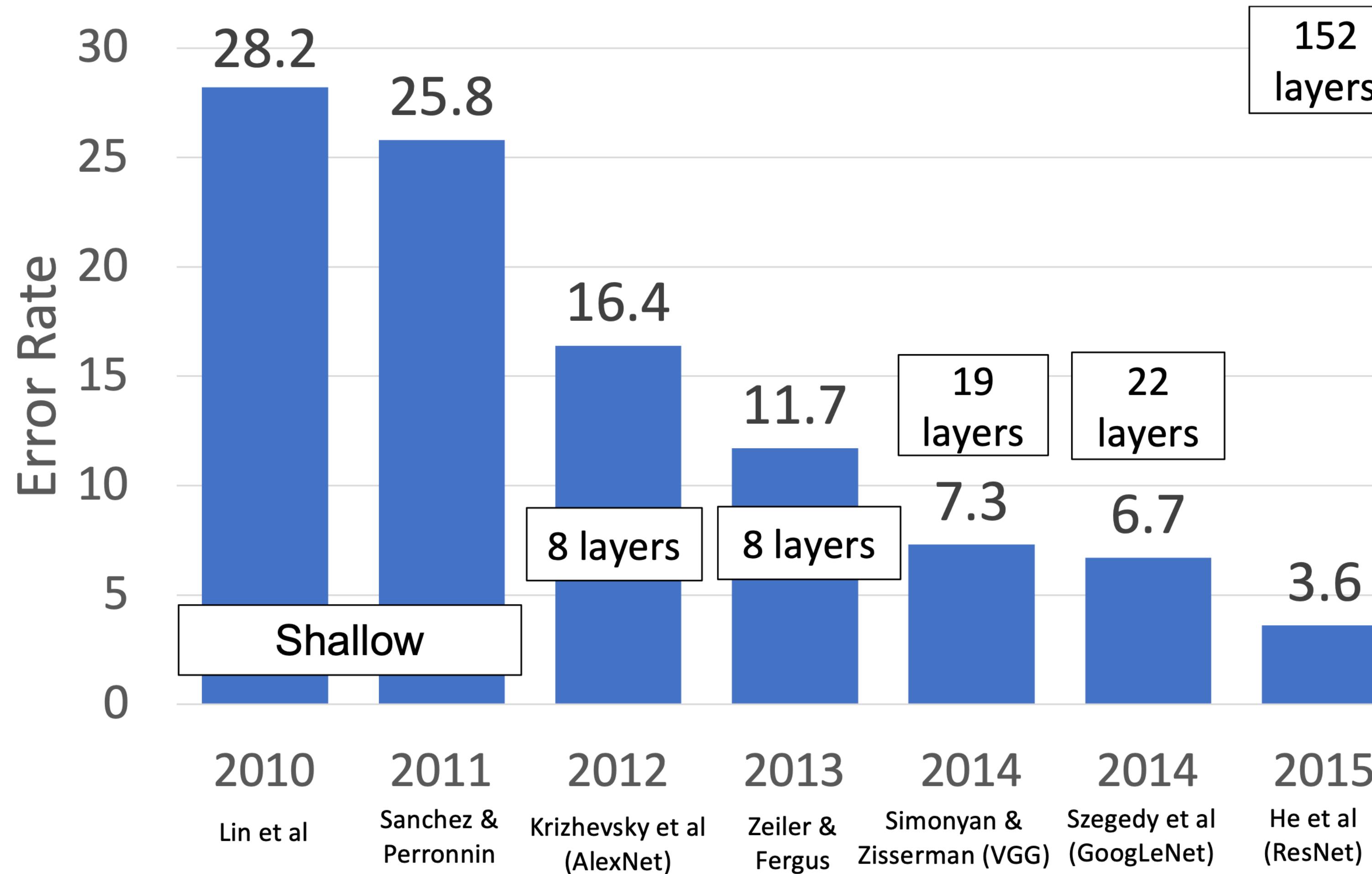


ImageNet Classification Challenge





ImageNet Classification Challenge





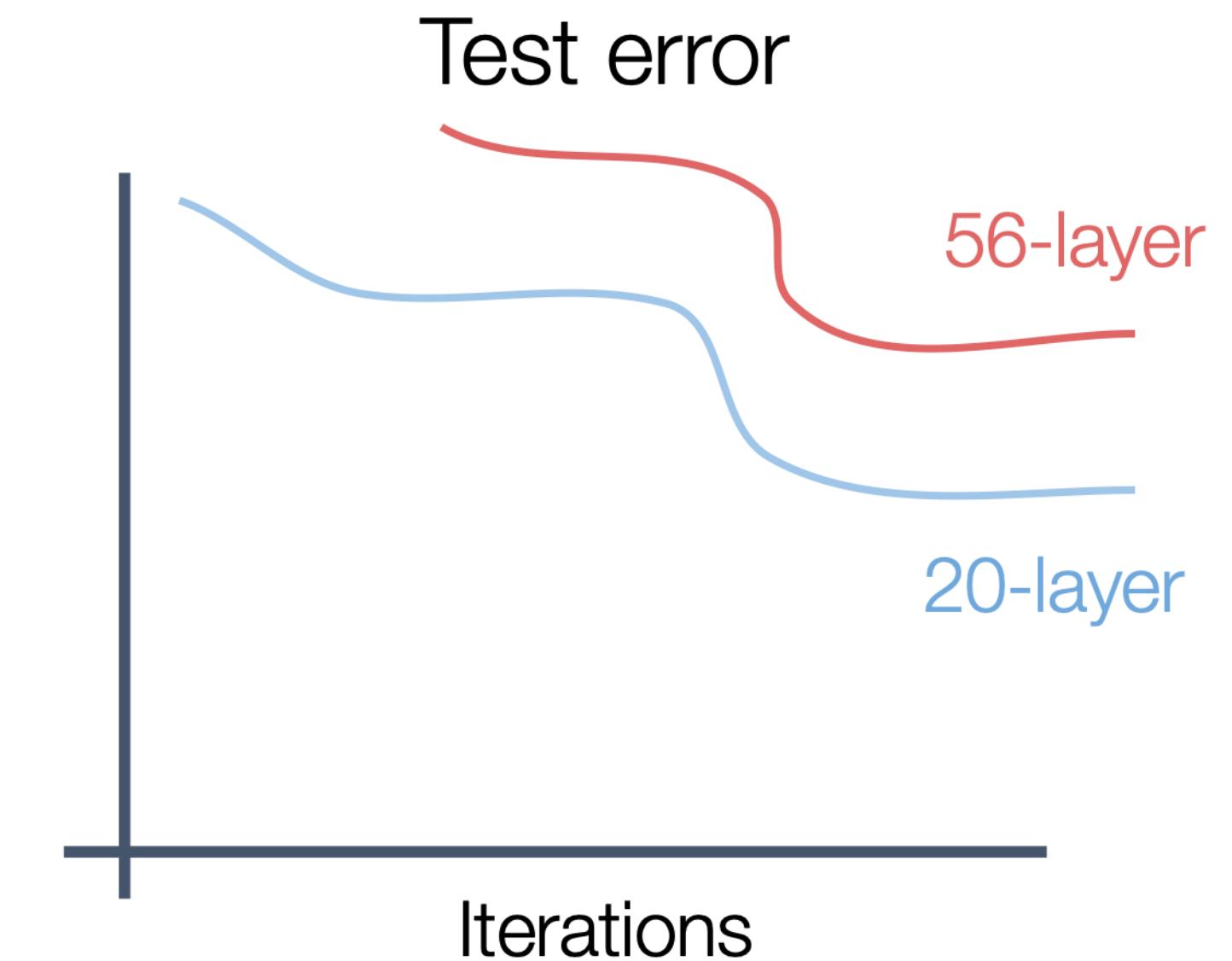
Residual Networks

Once we have Batch Normalization, we can train networks with 10+ layers.

What happens as we go deeper?

Deeper model does worse than shallow model!

Initial guess: Deep model is **overfitting** since it is much bigger than the other model





Residual Networks

Once we have Batch Normalization, we can train networks with 10+ layers.

What happens as we go deeper?



In fact the deep model seems to be **underfitting** since it also performs worse than the shallow model on the training set! It is actually **underfitting**



Residual Networks

A deeper model can emulate a shallower model: copy layers from shallower model, set extra layers to identity

Thus deeper models should do at least as good as shallow models

Hypothesis: This is an optimization problem. Deeper models are harder to optimize, and in particular don't learn identity functions to emulate shallow models



Residual Networks

A deeper model can emulate a shallower model: copy layers from shallower model, set extra layers to identity

Thus deeper models should do at least as good as shallow models

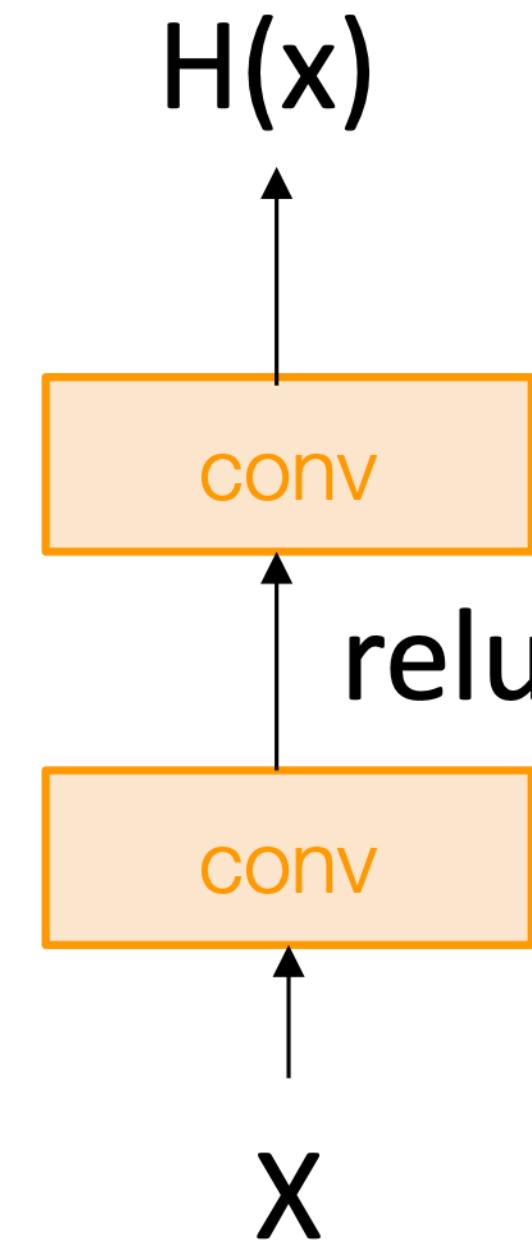
Hypothesis: This is an optimization problem. Deeper models are harder to optimize, and in particular don't learn identity functions to emulate shallow models

Solution: Change the network so learning identity functions with extra layers is easy!

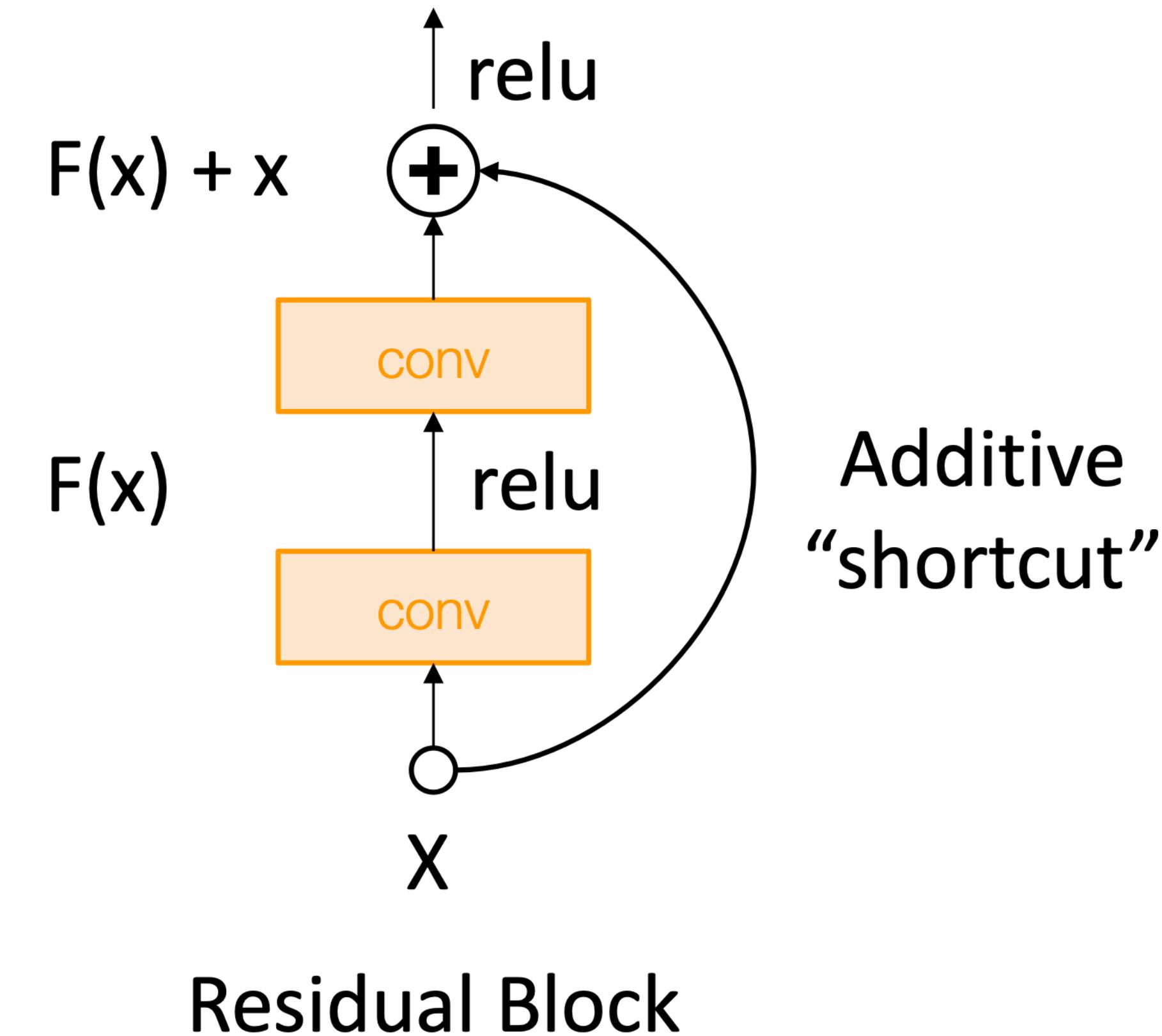


Residual Networks

Solution: Change the network so learning identity functions with extra layers is easy!



“Plain” block

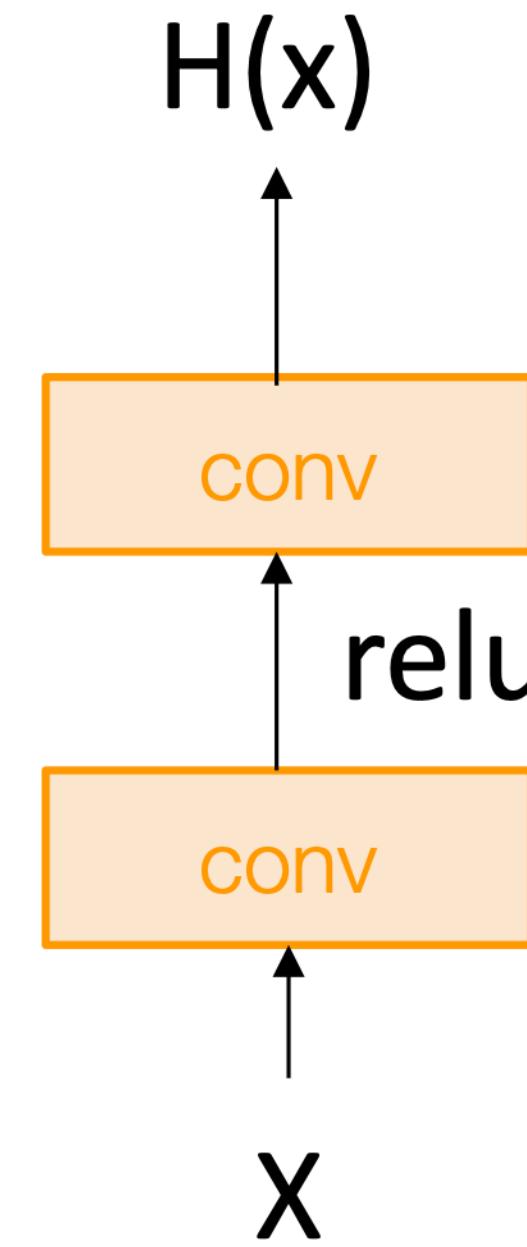


Additive
“shortcut”



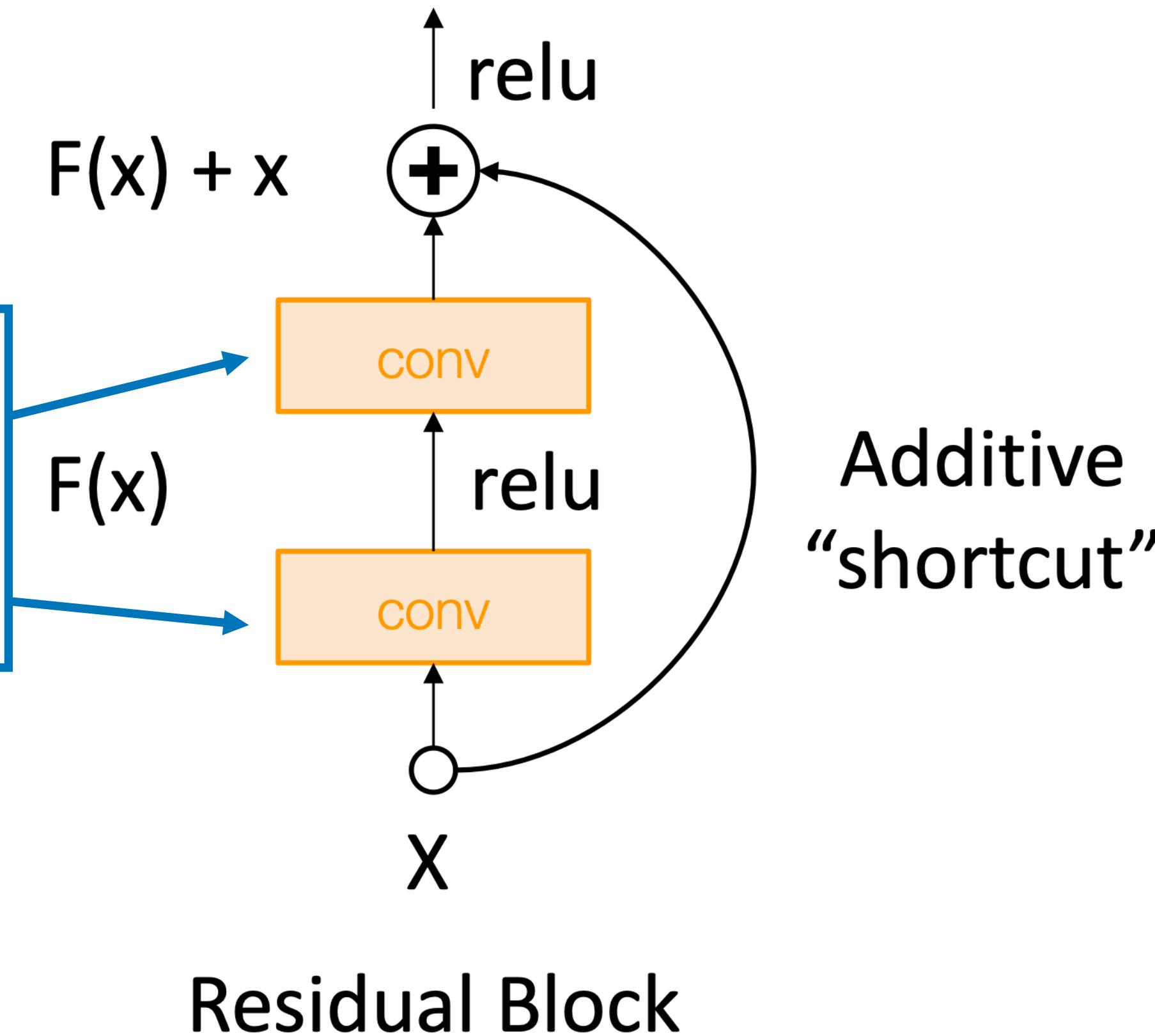
Residual Networks

Solution: Change the network so learning identity functions with extra layers is easy!



“Plain” block

If you set these to 0, the whole block will compute the identity function!



Residual Block

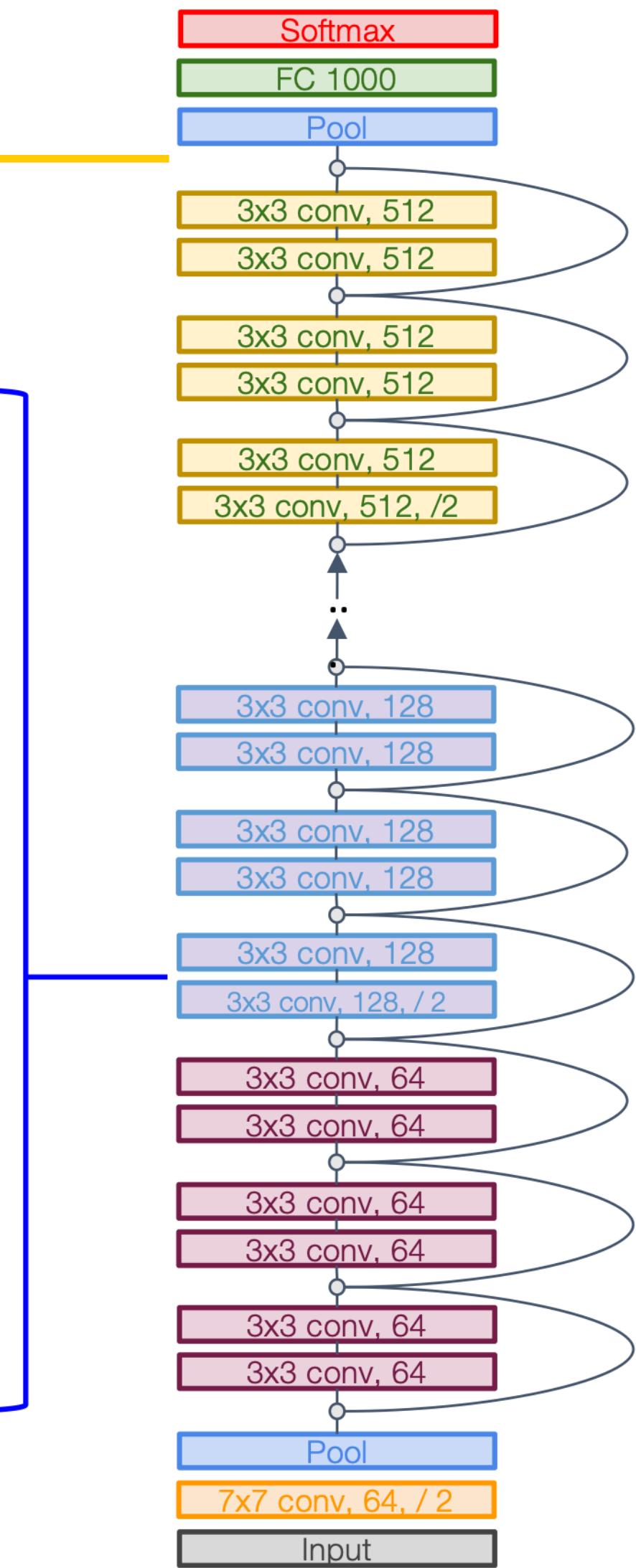
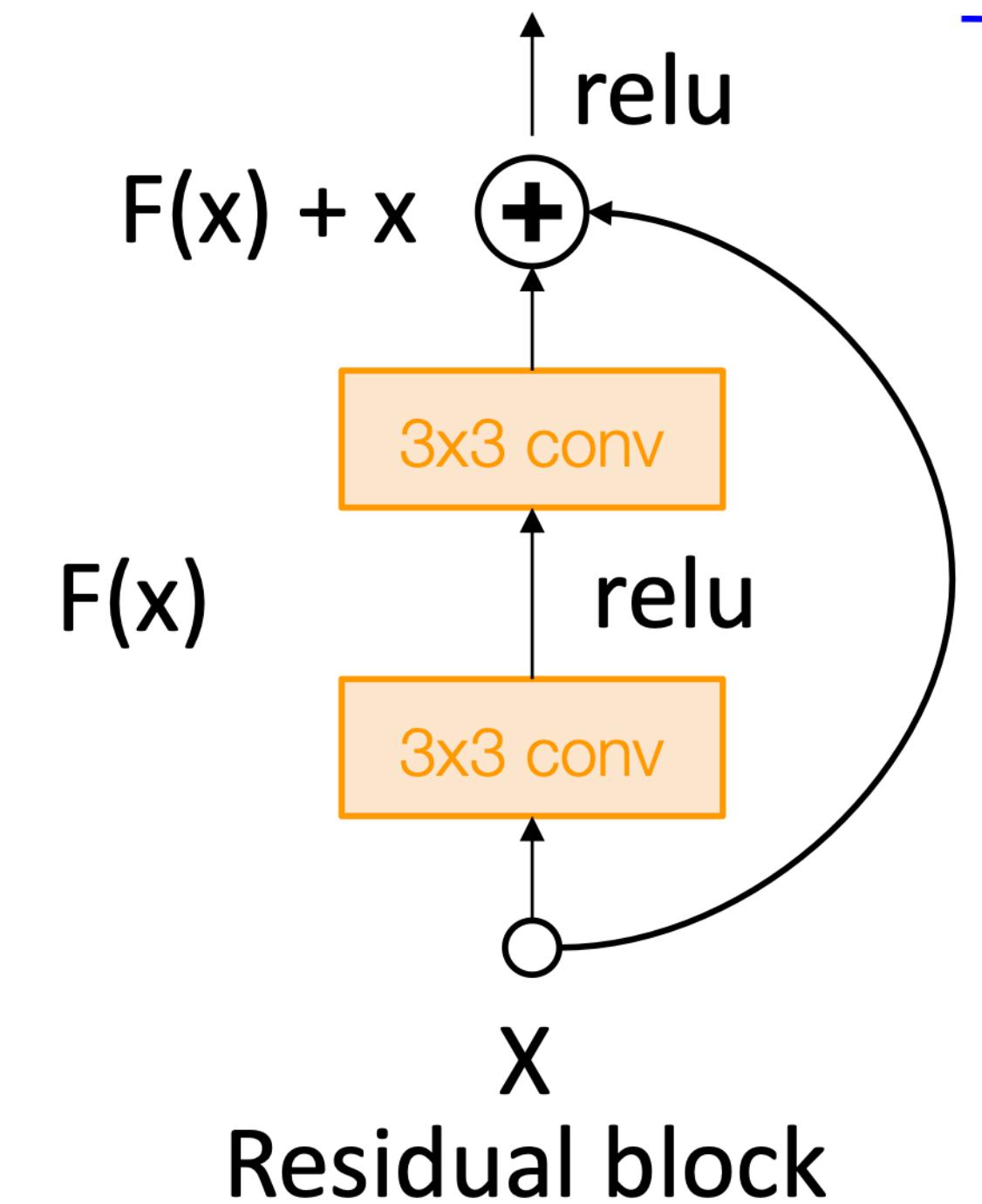


Residual Networks

A residual network is a stack of many residual blocks

Regular design, like VGG: each residual block has two 3x3 conv

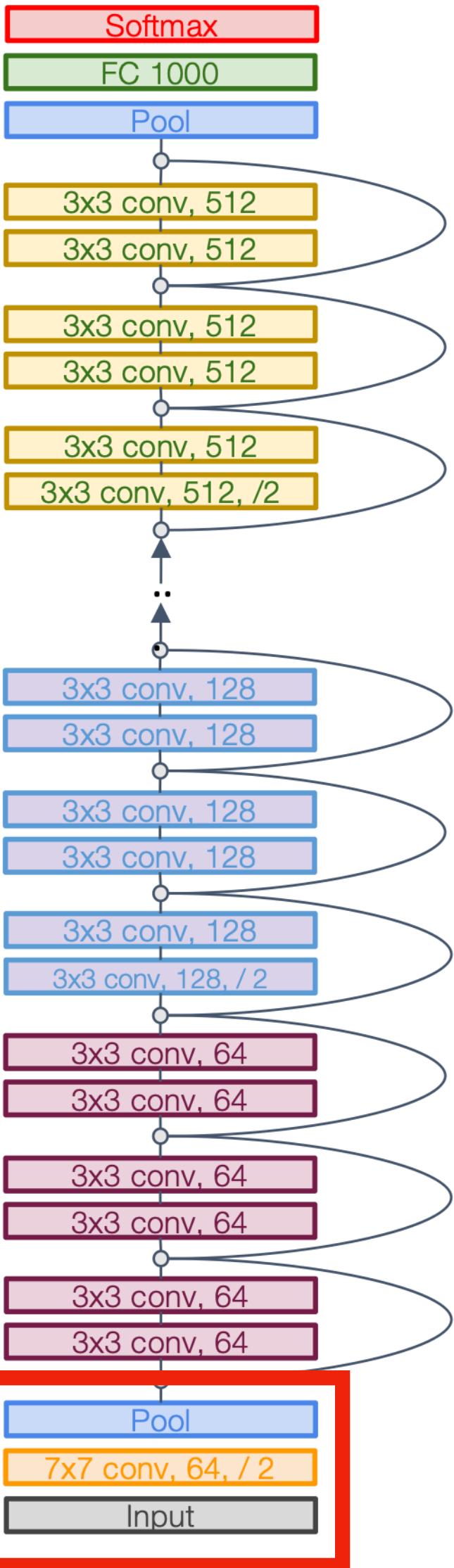
Network is divided into **stages**: the first block of each stage halves the resolution (with stride-2 conv) and doubles the number of channels





Residual Networks

Uses the same aggressive **stem** as GoogleNet to downsample the input 4x before applying residual blocks:

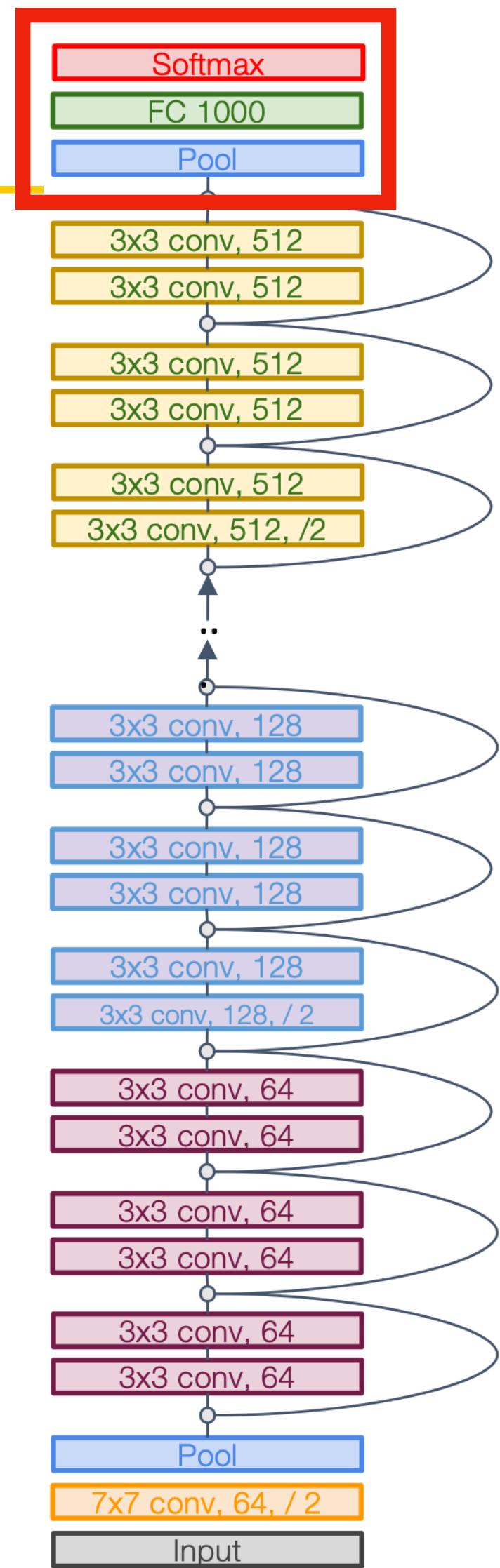


	Input size		Layer				Output size				
Layer	C	H/W	Filters	Kernel	Stride	Pad	C	H/W	Memory (KB)	Params (k)	Flop (M)
Conv Poo	3	224	64	7	2	3	64	112	3136	9	118
Max-pool	64	112		3	2	1	64	56	784	0	2



Residual Networks

Like GoogLeNet, no big fully-connected-layers: Instead use **global average pooling** and a single linear layer at the end





ResNet-18:

Stem: 1 conv layer

Stage 1 (C=64): 2 res. block = 4 conv

Stage 2 (C=128): 2 res. block = 4 conv

Stage 3 (C=256): 2 res. block = 4 conv

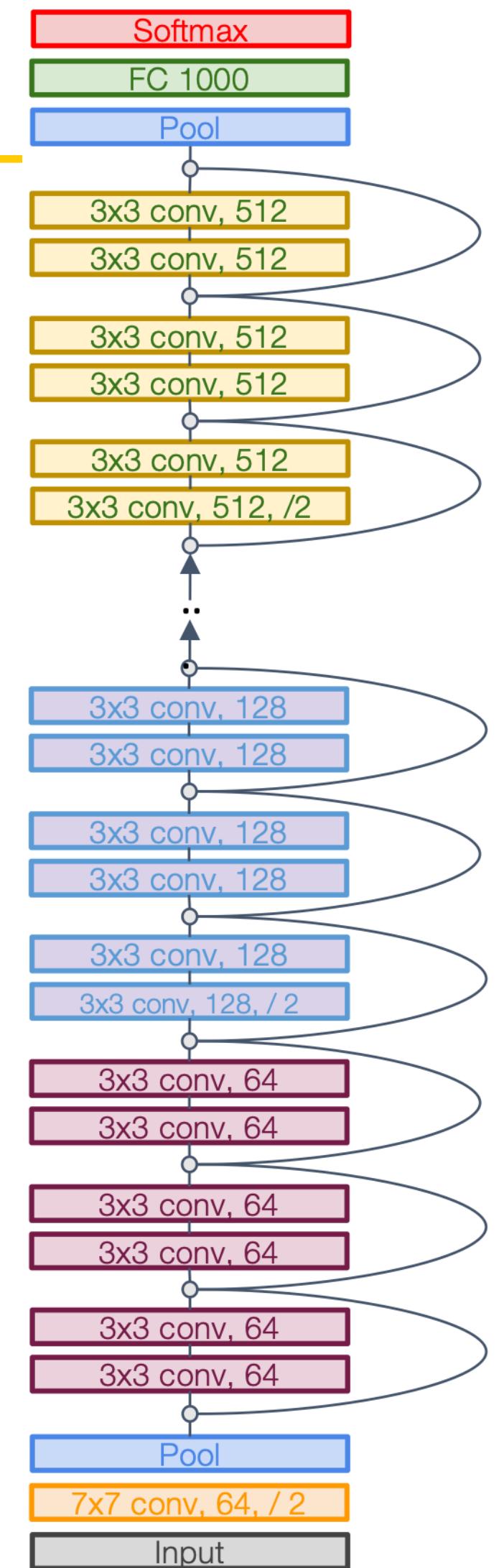
Stage 4 (C=512): 2 res. block = 4 conv

Linear

ImageNet top-5 error: 10.92

GFLOP: 1.8

Residual Networks





Residual Networks

ResNet-18:

Stem: 1 conv layer

Stage 1 (C=64): 2 res. block = 4 conv

Stage 2 (C=128): 2 res. block = 4 conv

Stage 3 (C=256): 2 res. block = 4 conv

Stage 4 (C=512): 2 res. block = 4 conv

Linear

ImageNet top-5 error: 10.92

GFLOP: 1.8

VGG-16:

ImageNet top-5 error: 9.62

GFLOP: 13.6

ResNet-34:

Stem: 1 conv layer

Stage 1: 3 res. block = 6 conv

Stage 2: 4 res. block = 8 conv

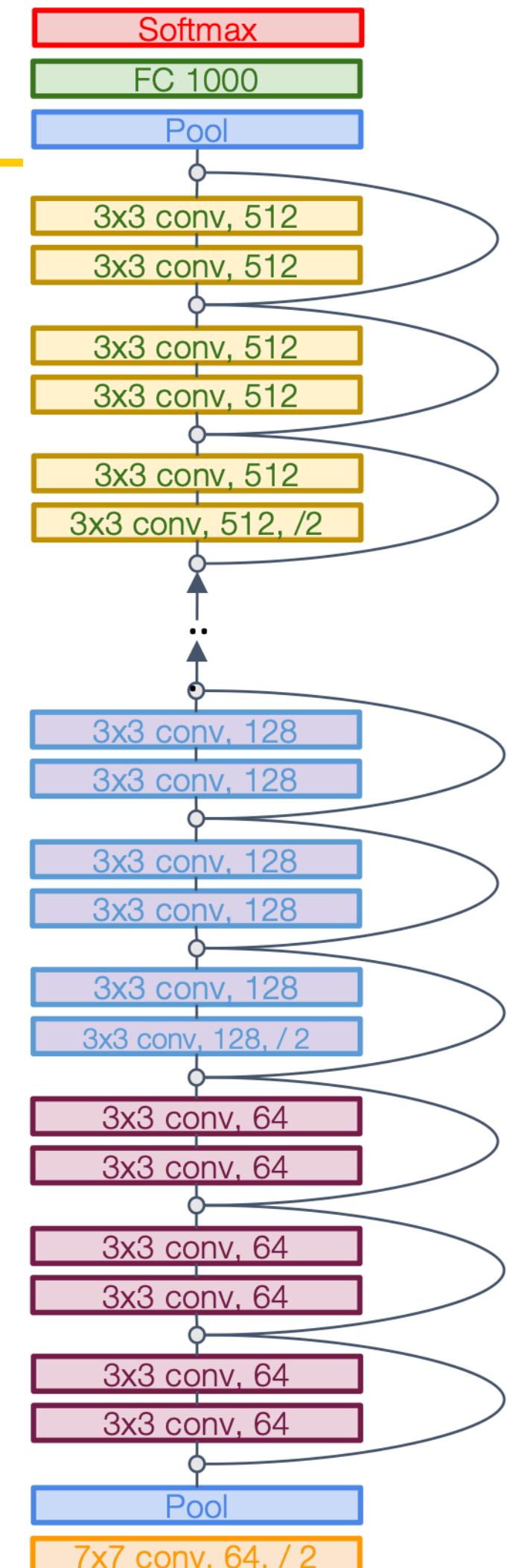
Stage 3: 6 res. block = 12 conv

Stage 4: 3 res. block = 6 conv

Linear

ImageNet top-5 error: 8.58

GFLOP: 3.6

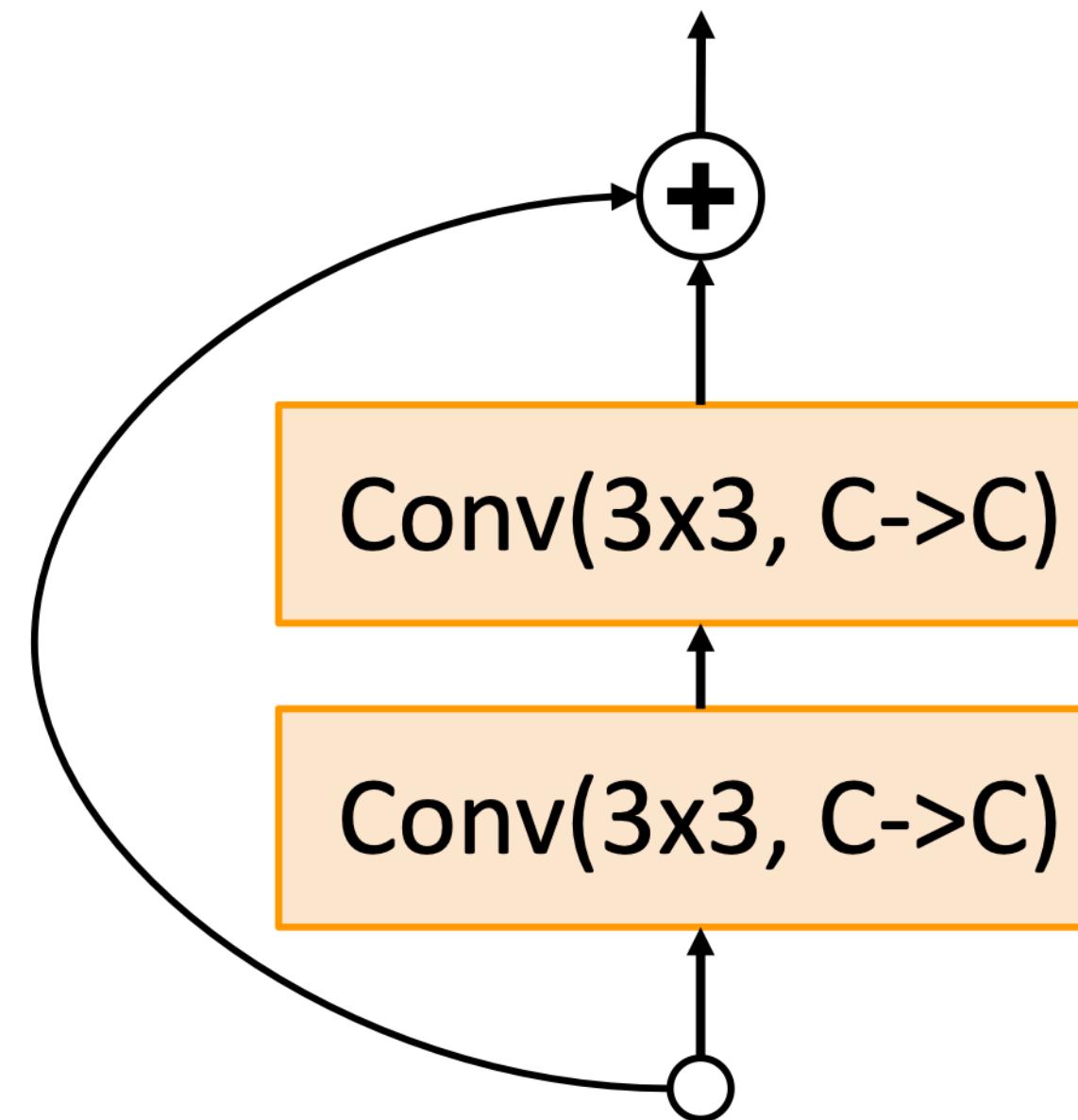


He et al, “Deep Residual Learning for Image Recognition... , CV

Error rates are 224x224 single-crop testing, reported by torch



Residual Networks: Basic Block



“Basic”
Residual block

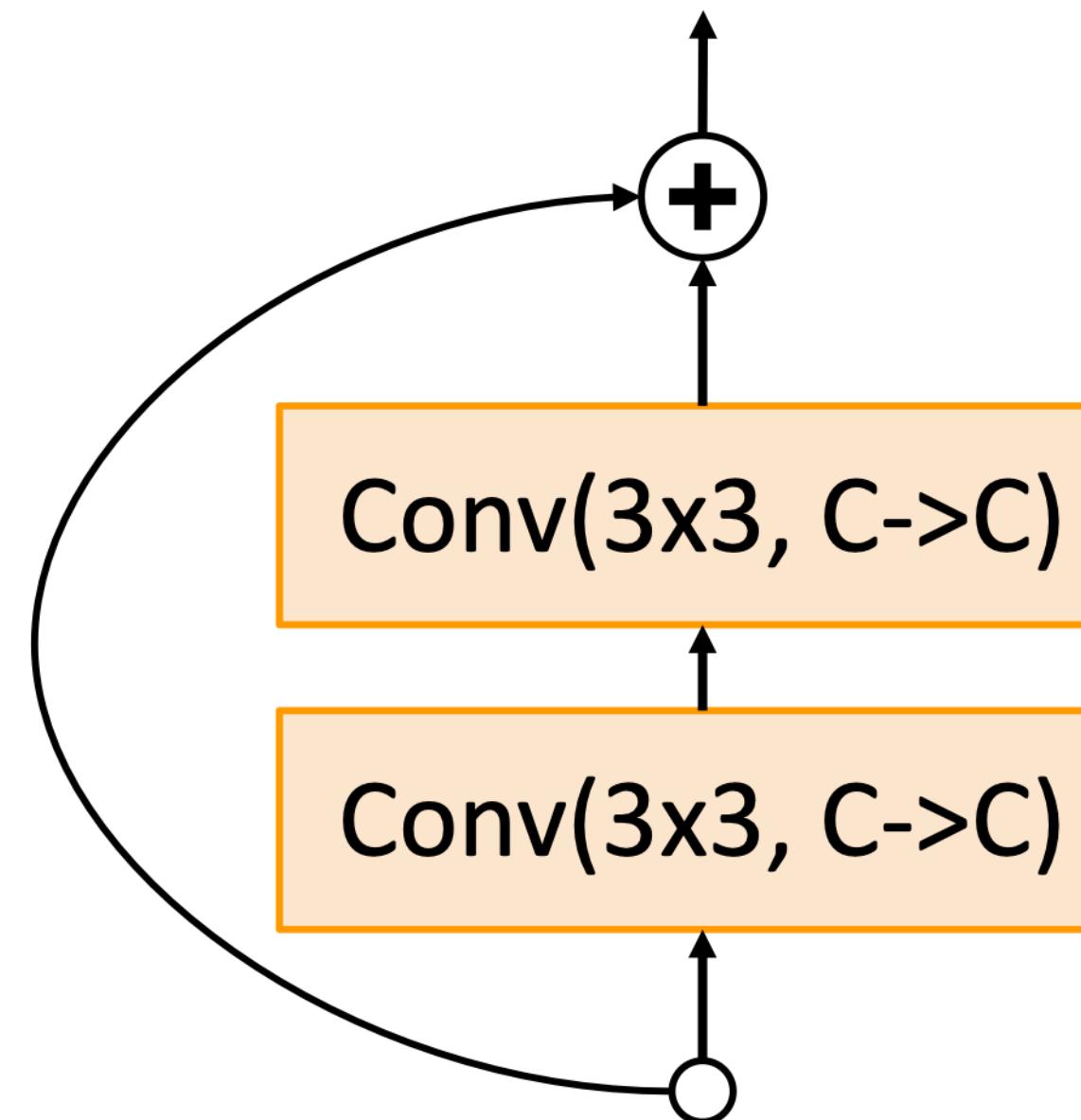
FLOPs: $9HWC^2$

FLOPs: $9HWC^2$

Total FLOPs:
 $18HWC^2$



Residual Networks: Bottleneck Block



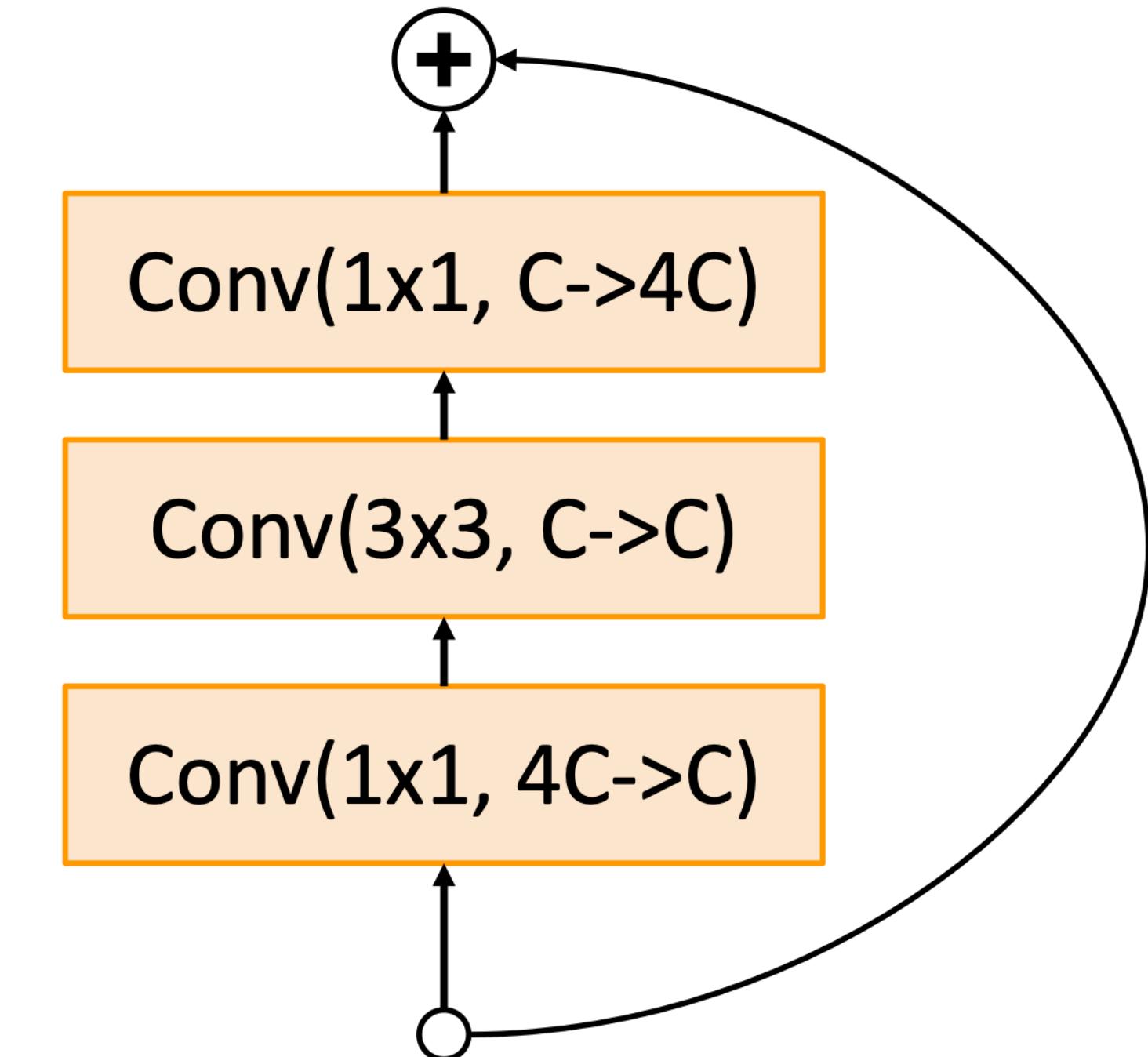
FLOPs: $9HWC^2$

FLOPs: $9HWC^2$

"Basic"
Residual block

Total FLOPs:

$18HWC^2$



FLOPs: $9HWC^2$

FLOPs: $9HWC^2$

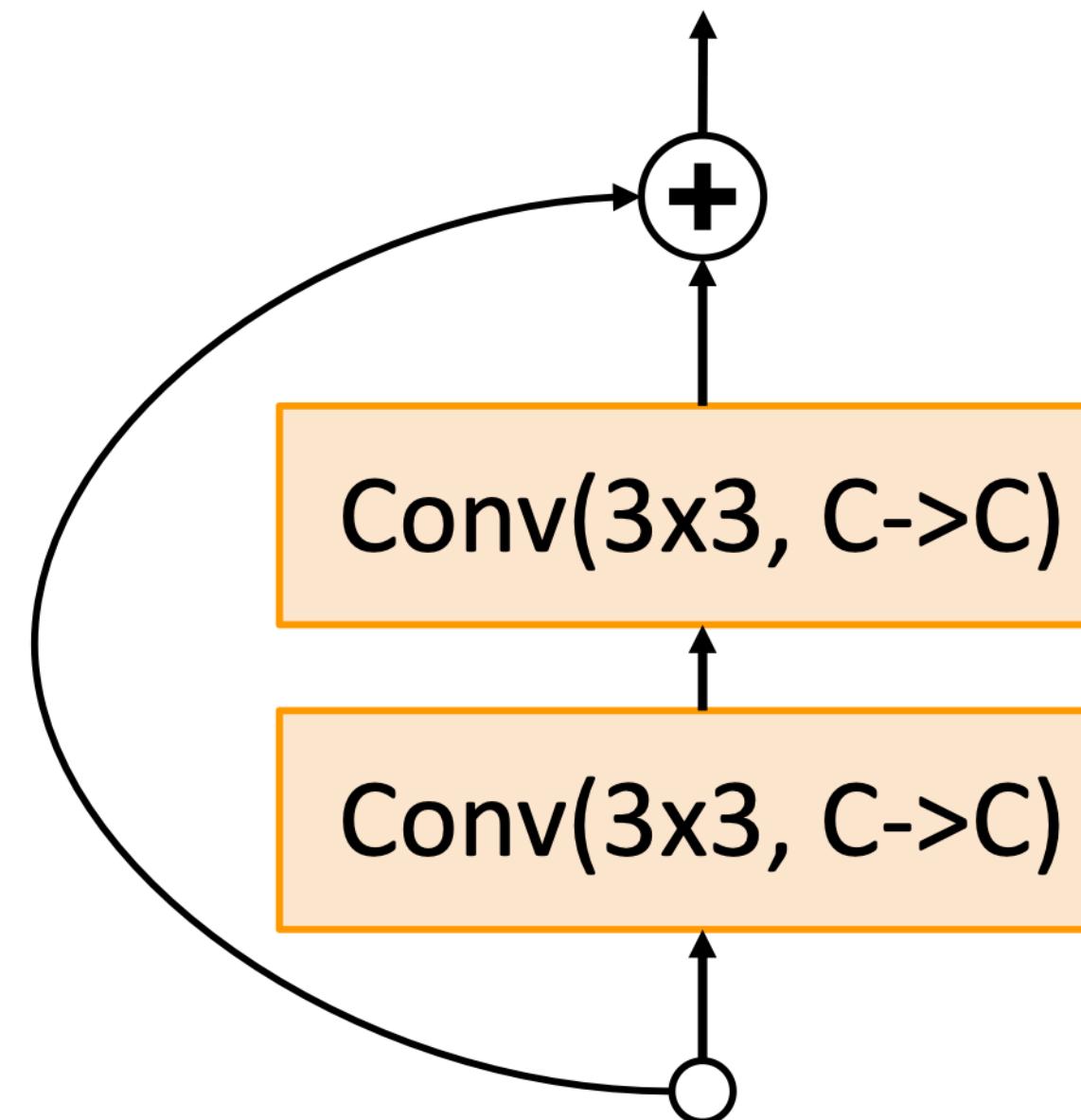
FLOPs: $9HWC^2$

"Bottleneck"
Residual block



Residual Networks: Bottleneck Block

More layers, less computational cost!



"Basic"
Residual block

FLOPs: $9HWC^2$

FLOPs: $9HWC^2$

Total FLOPs:

$18HWC^2$

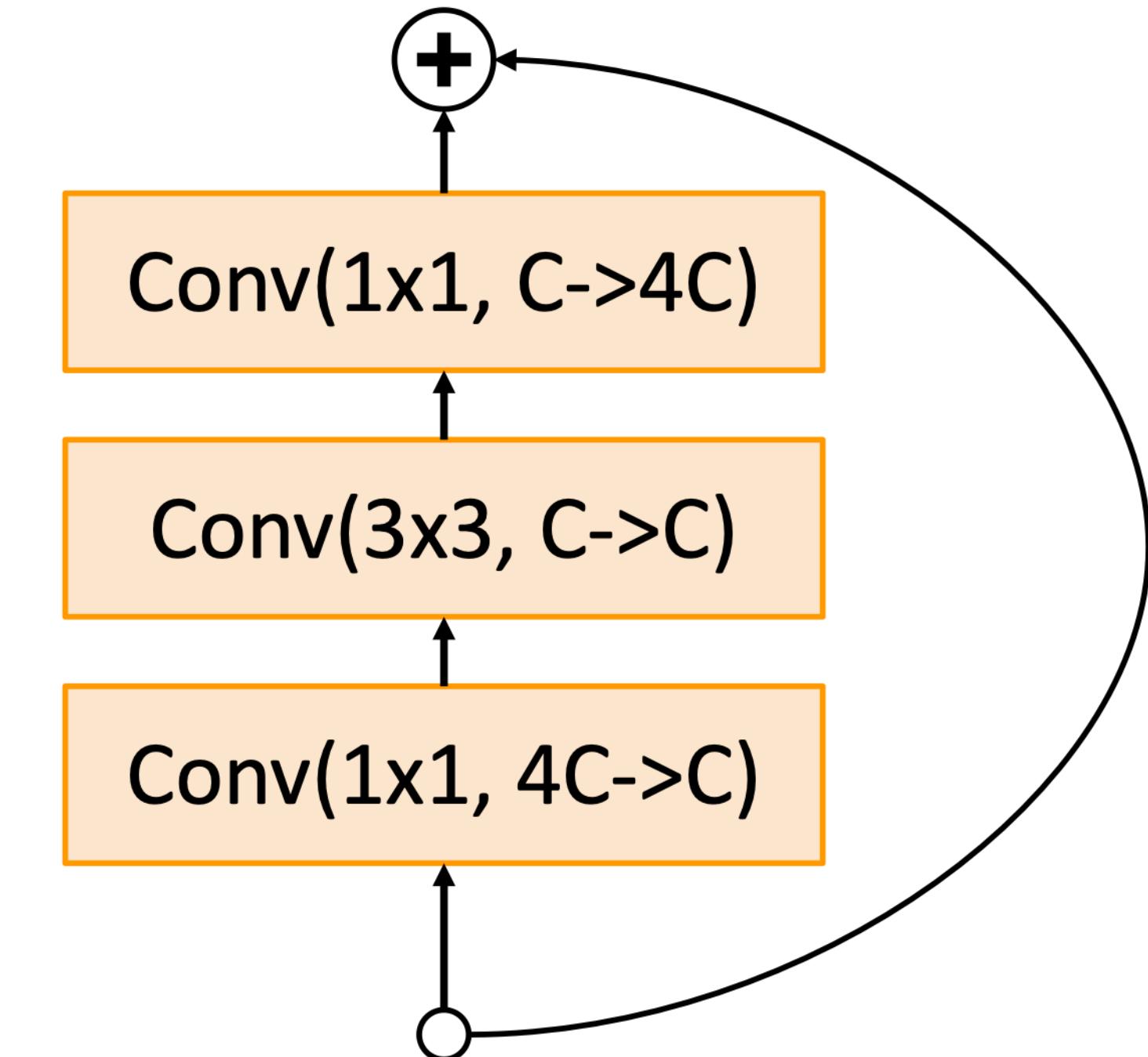
FLOPs: $4HWC^2$

FLOPs: $9HWC^2$

FLOPs: $4HWC^2$

Total FLOPs:

$17HWC^2$



"Bottleneck"
Residual block

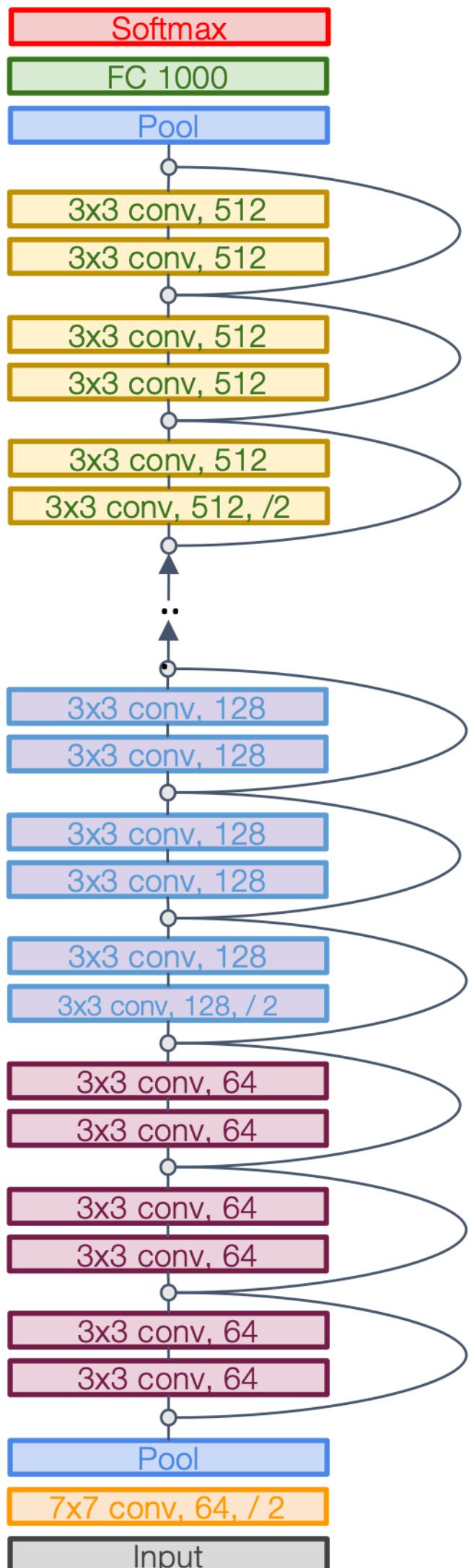


Residual Networks

ResNet-50 is the same as ResNet-34, but replaces Basic blocks with Bottleneck Blocks. This is a great baseline architecture for many tasks even today!

Deeper ResNet-101 and ResNet-152 models are more accurate, but also more computationally heavy

			Stage 1		Stage 2		Stage 3		Stage 4				
	Block type	Stem layers	Block s	Layers	Block s	Layer s	Block s	Layer s	Block s	Layer s	FC Layers	GFLOP	Image Net
ResNet-18	Basic	1	2	4	2	4	2	4	2	4	1	1.8	10.92
ResNet-34	Basic	1	3	6	4	8	6	12	3	6	1	3.6	8.58
ResNet-50	Bottle	1	3	9	4	12	6	18	3	9	1	3.8	7.13
ResNet-101	Bottle	1	3	9	4	12	23	69	3	9	1	7.6	6.44
ResNet-152	Bottle	1	3	9	8	24	36	108	3	9	1	11.3	5.94





Residual Networks

- Able to train very deep networks
- Deeper networks do better than shallow networks (as expected)
- Swept 1st place in all ILSVRC and COCO 2015 competitions
- Still widely used today

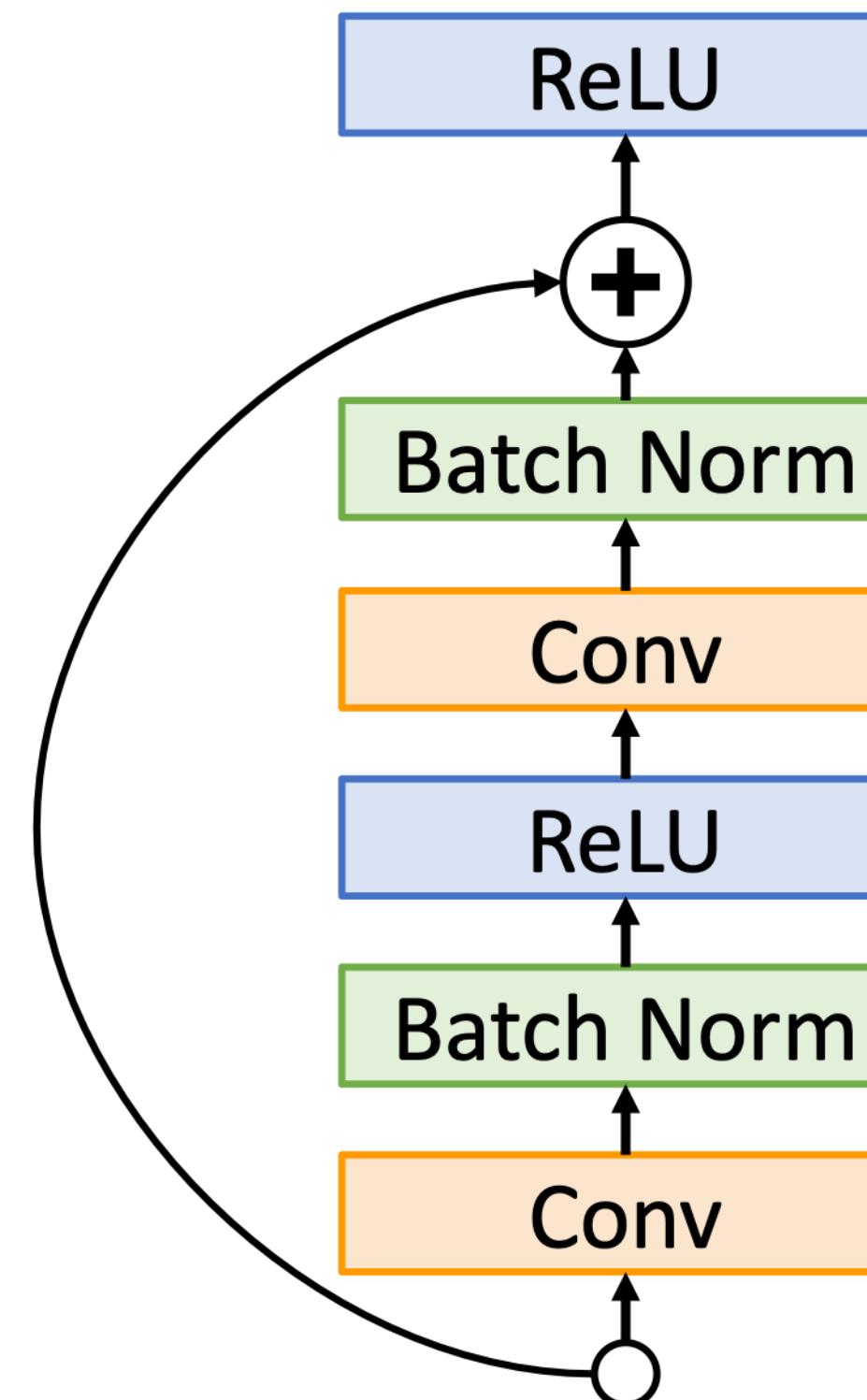
MSRA @ ILSVRC & COCO 2015 Competitions

- **1st places in all five main tracks**
 - ImageNet Classification: “Ultra-deep” (quote Yann) **152-layer** nets
 - ImageNet Detection: **16%** better than 2nd
 - ImageNet Localization: **27%** better than 2nd
 - COCO Detection: **11%** better than 2nd
 - COCO Segmentation: **12%** better than 2nd



Improving Residual Networks: Block Design

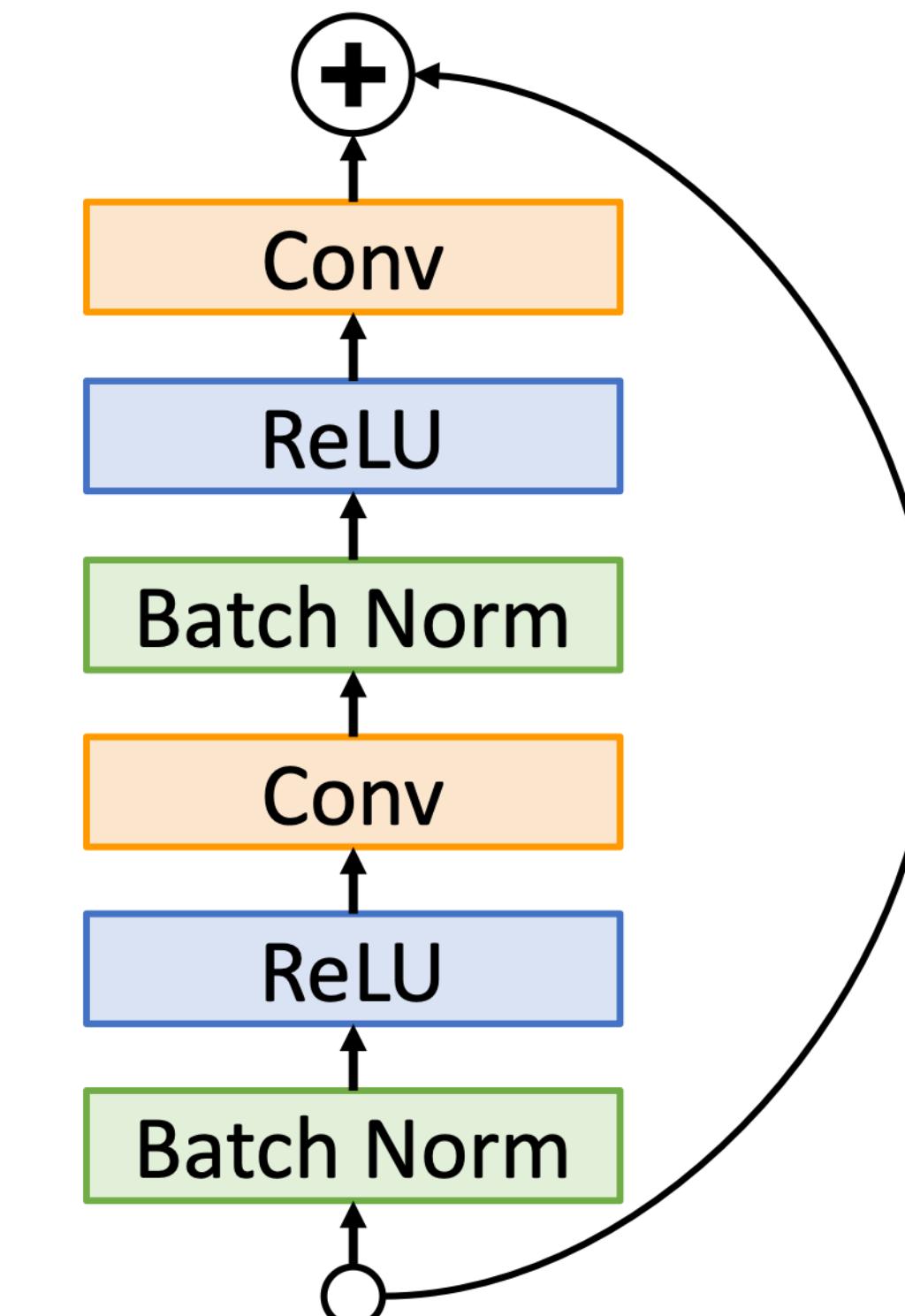
Original ResNet block



Note ReLU **after** residual:

Cannot actually learn identity function since outputs are nonnegative!

“Pre-Activation” ResNet Block



Note ReLU **inside** residual:

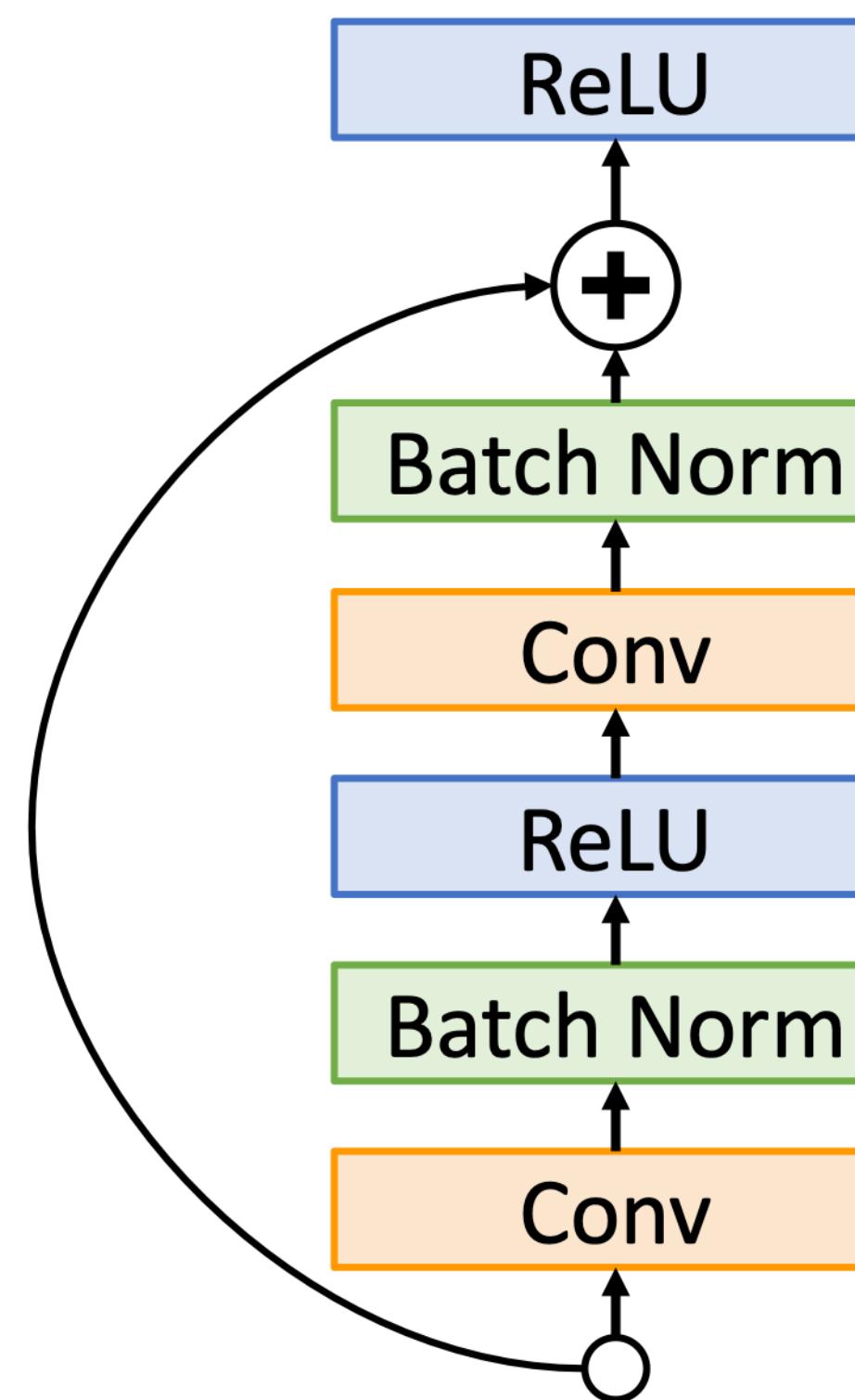
Can learn identity function by setting Conv weights to zero

He et al, "Identity mappings in deep residual networks", ECCV



Improving Residual Networks: Block Design

Original ResNet block



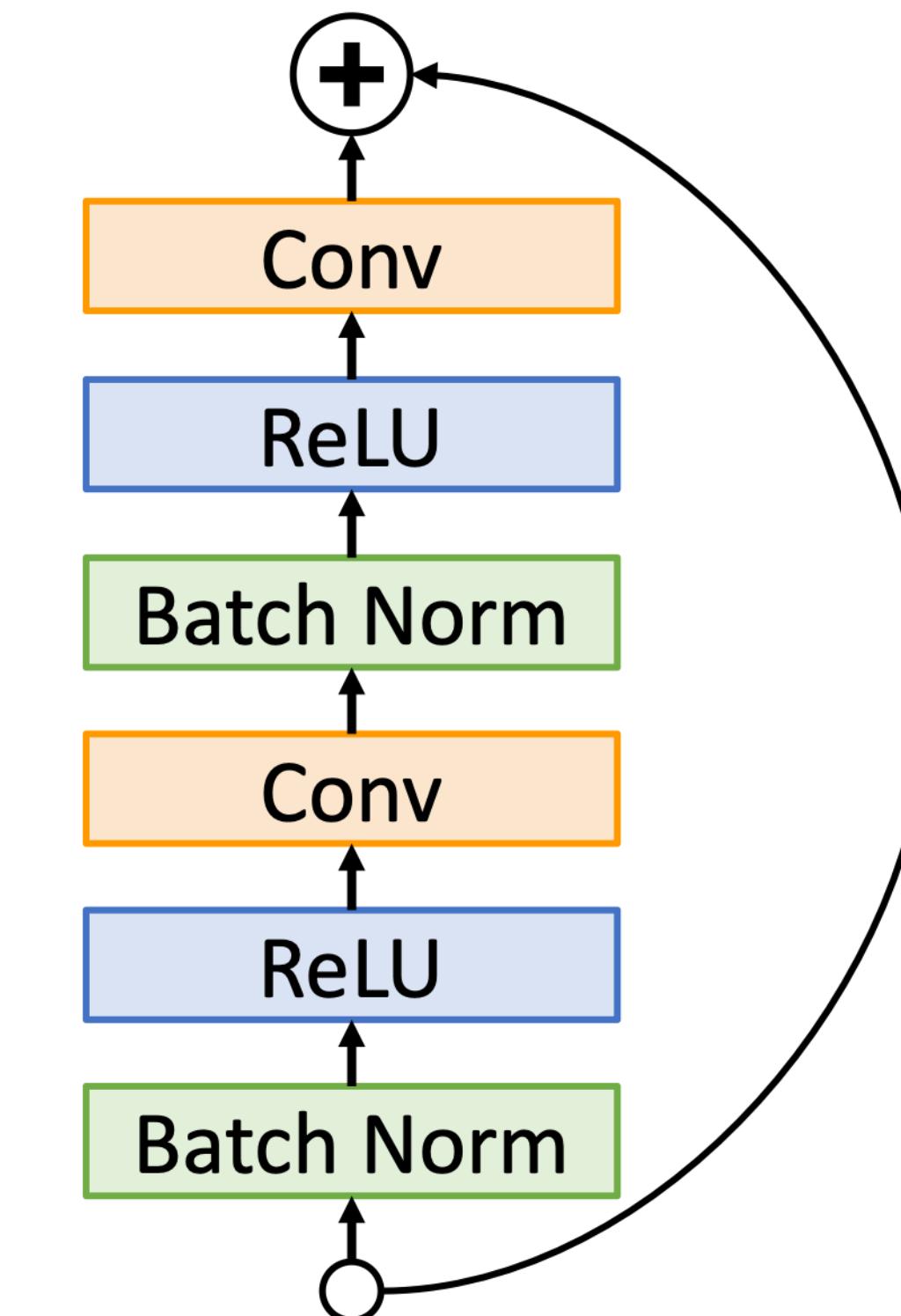
Slight improvement in accuracy
(ImageNet top-1 error)

ResNet-152: 21.3 vs **21.1**

ResNet-200: 21.8 vs **20.7**

Not actually used that much in practice

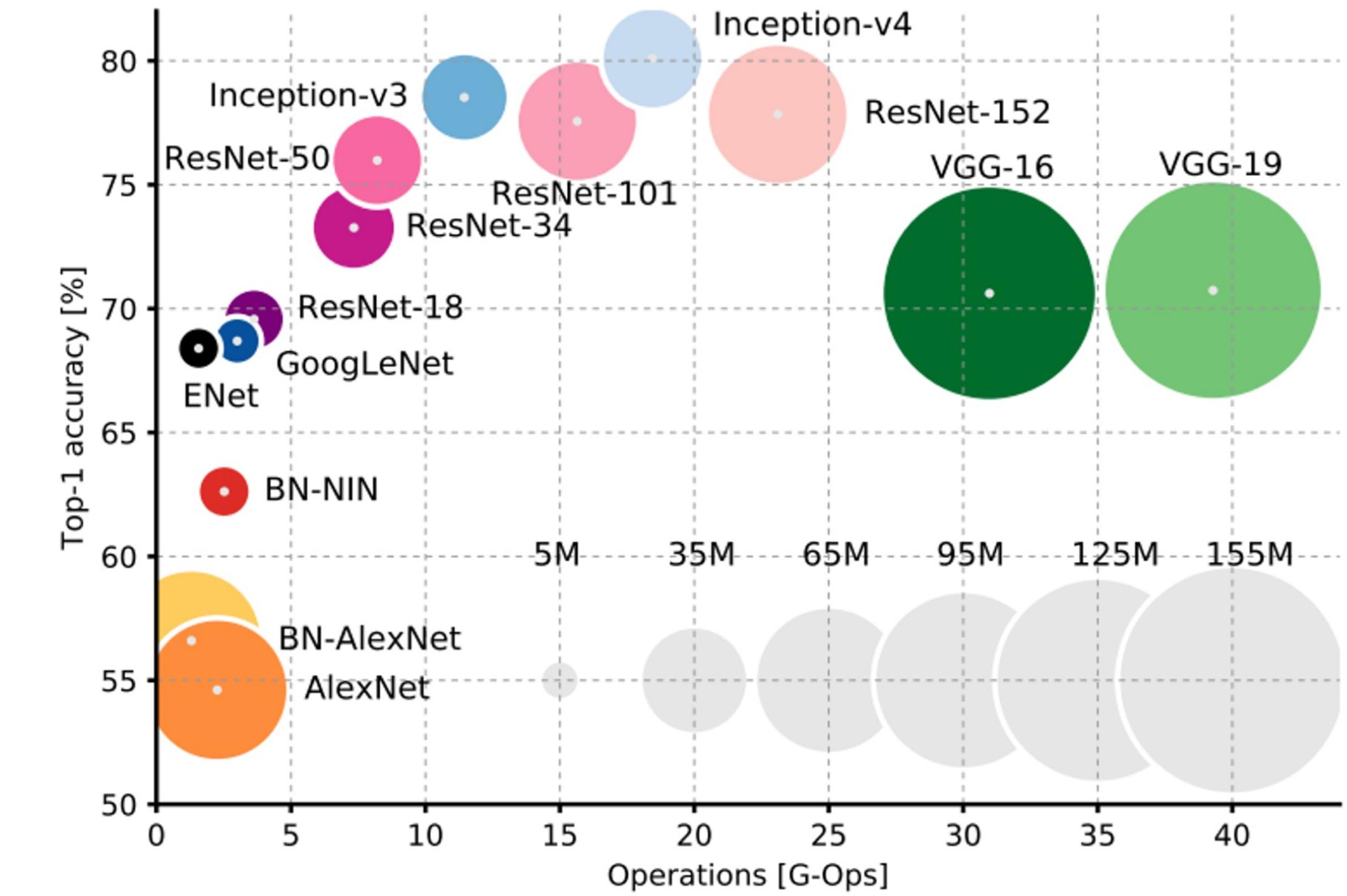
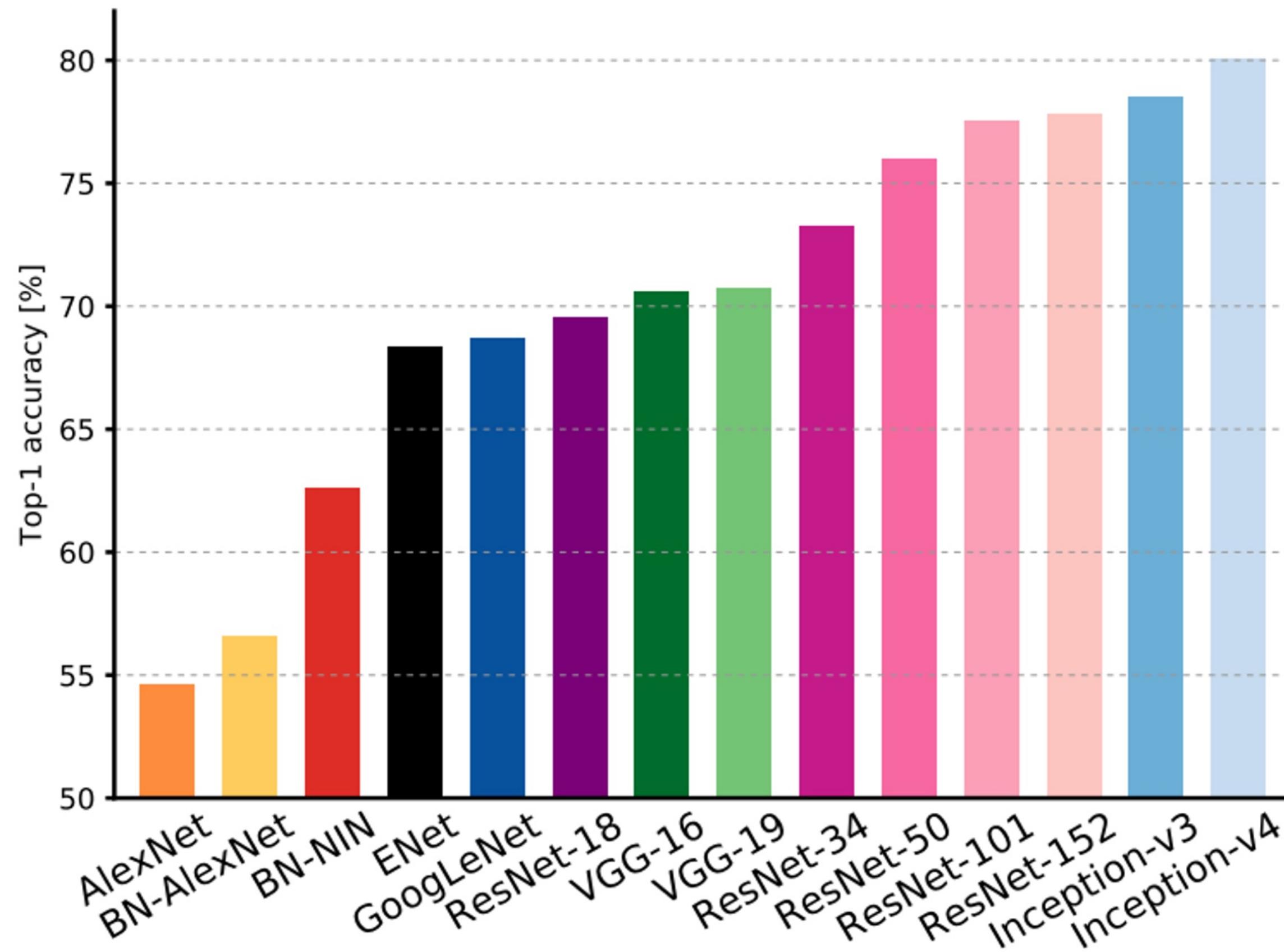
“Pre-Activation” ResNet Block



He et al, "Identity mappings in deep residual networks", ECCV



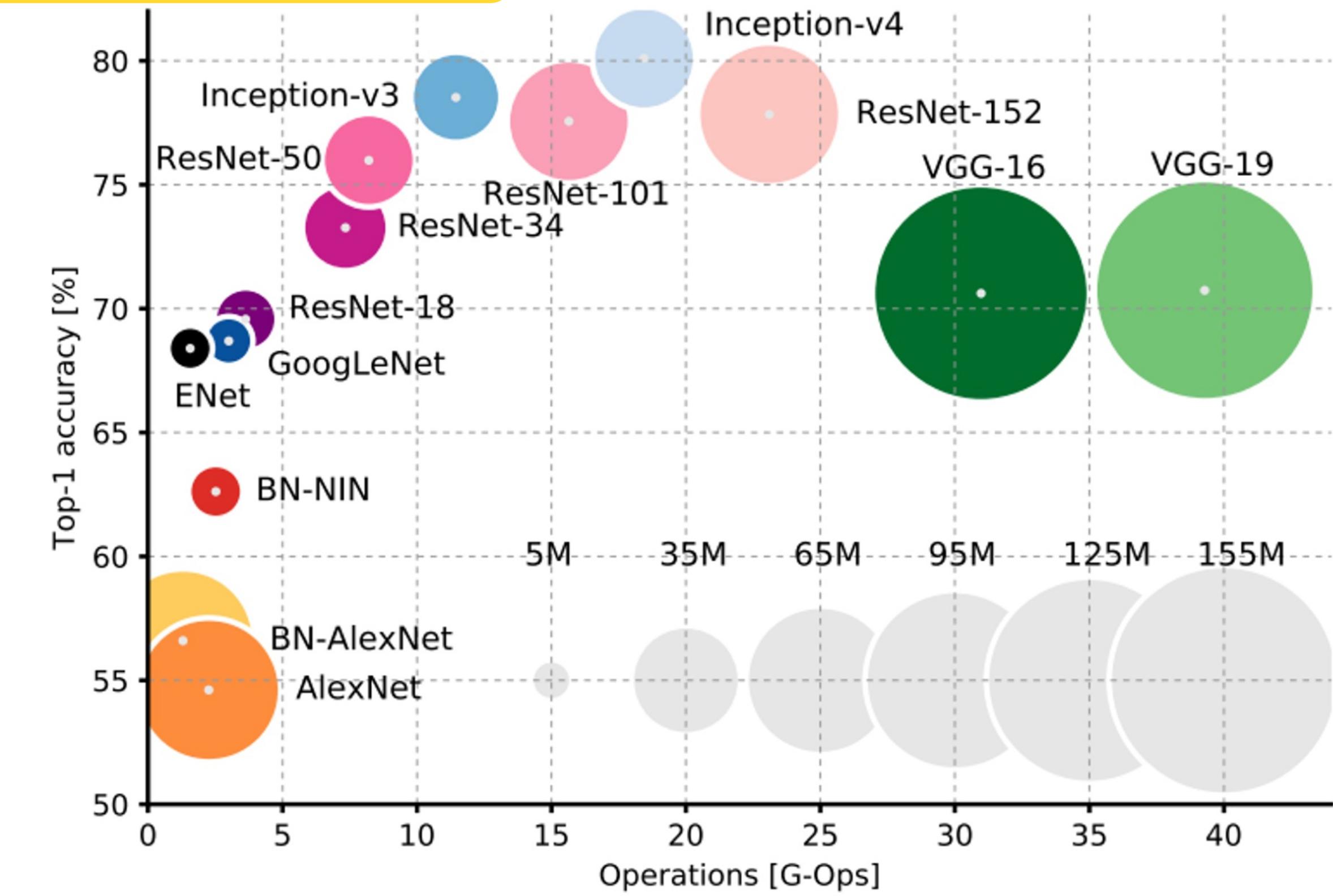
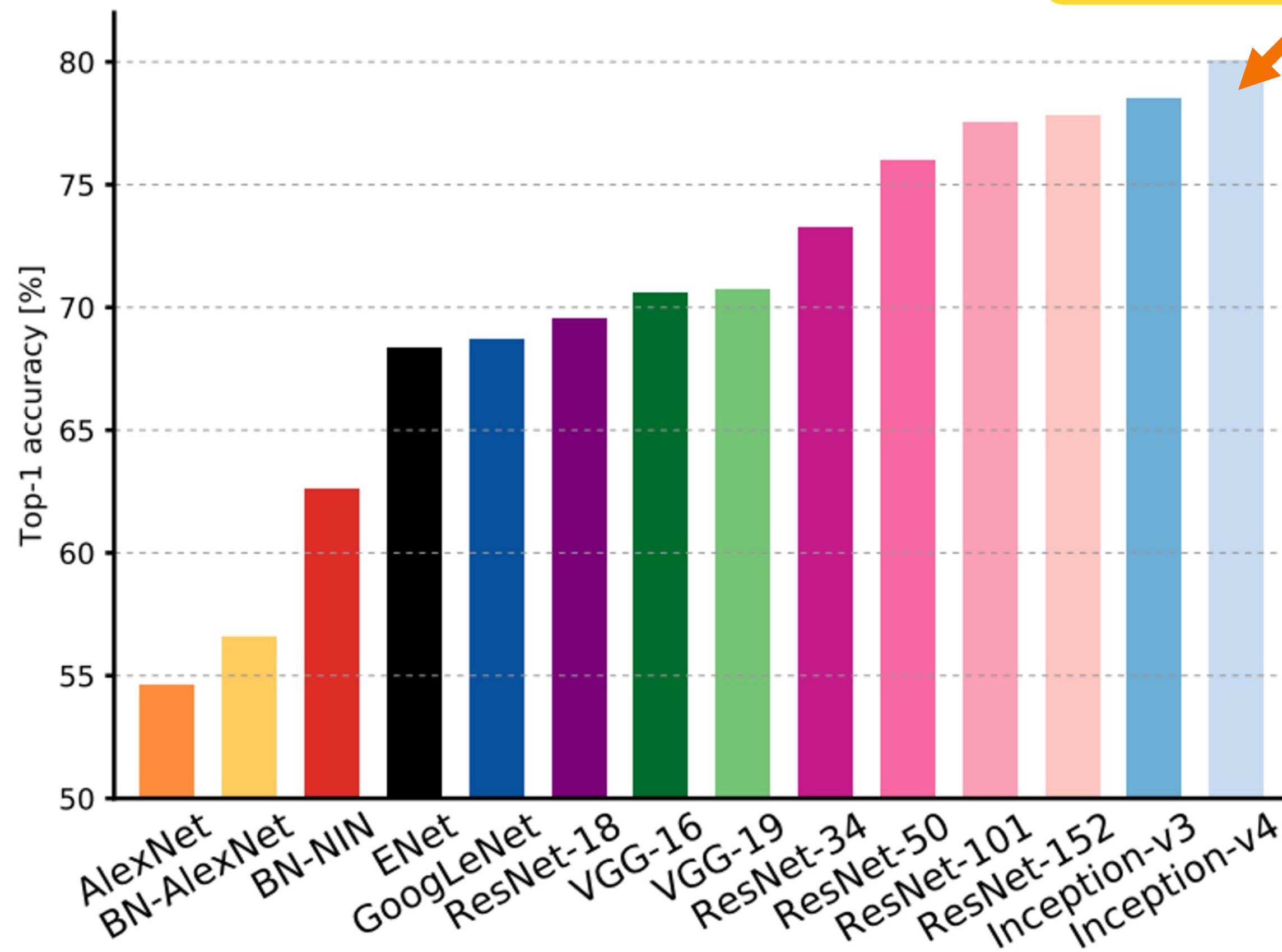
Comparing Complexity





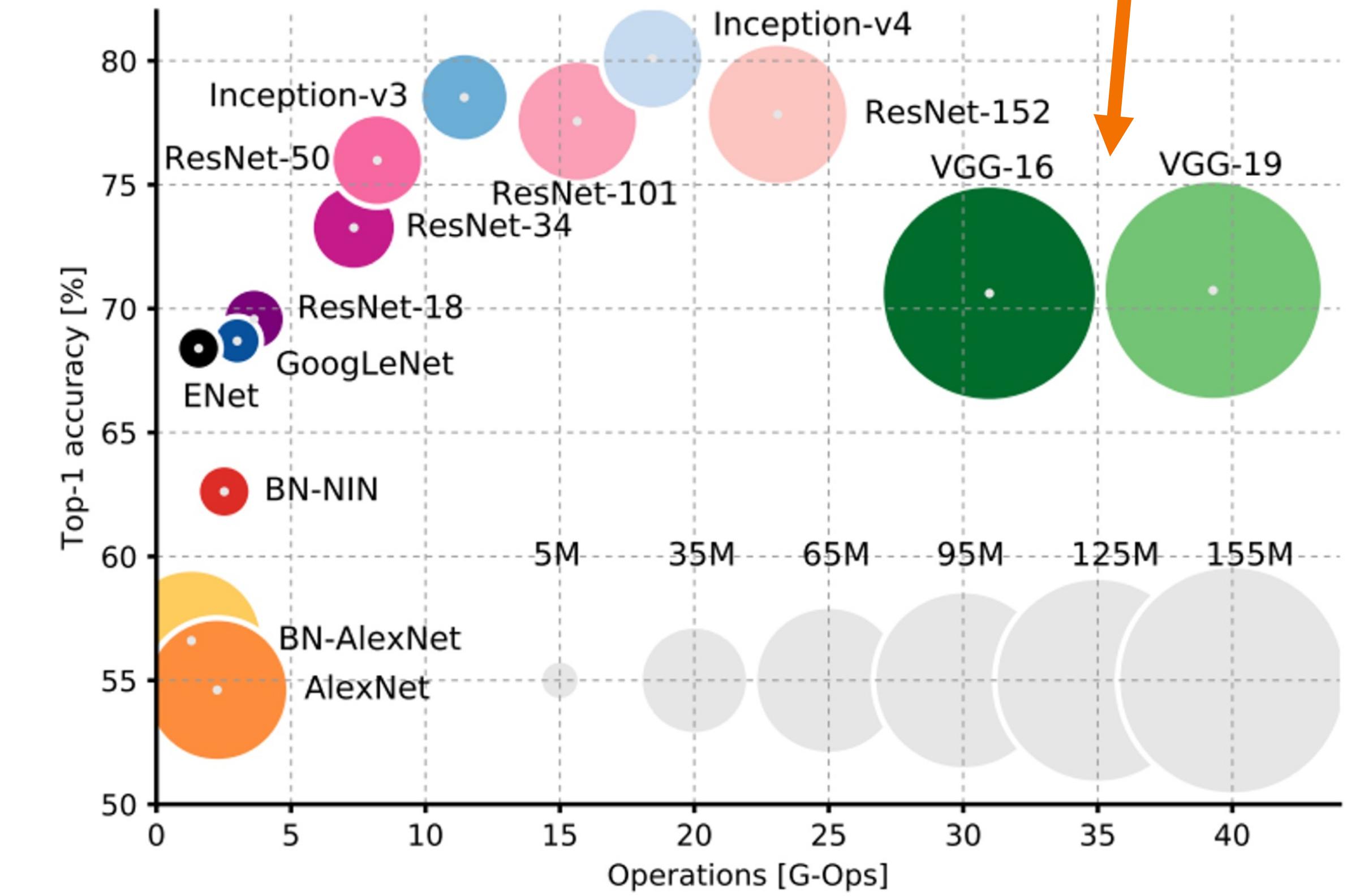
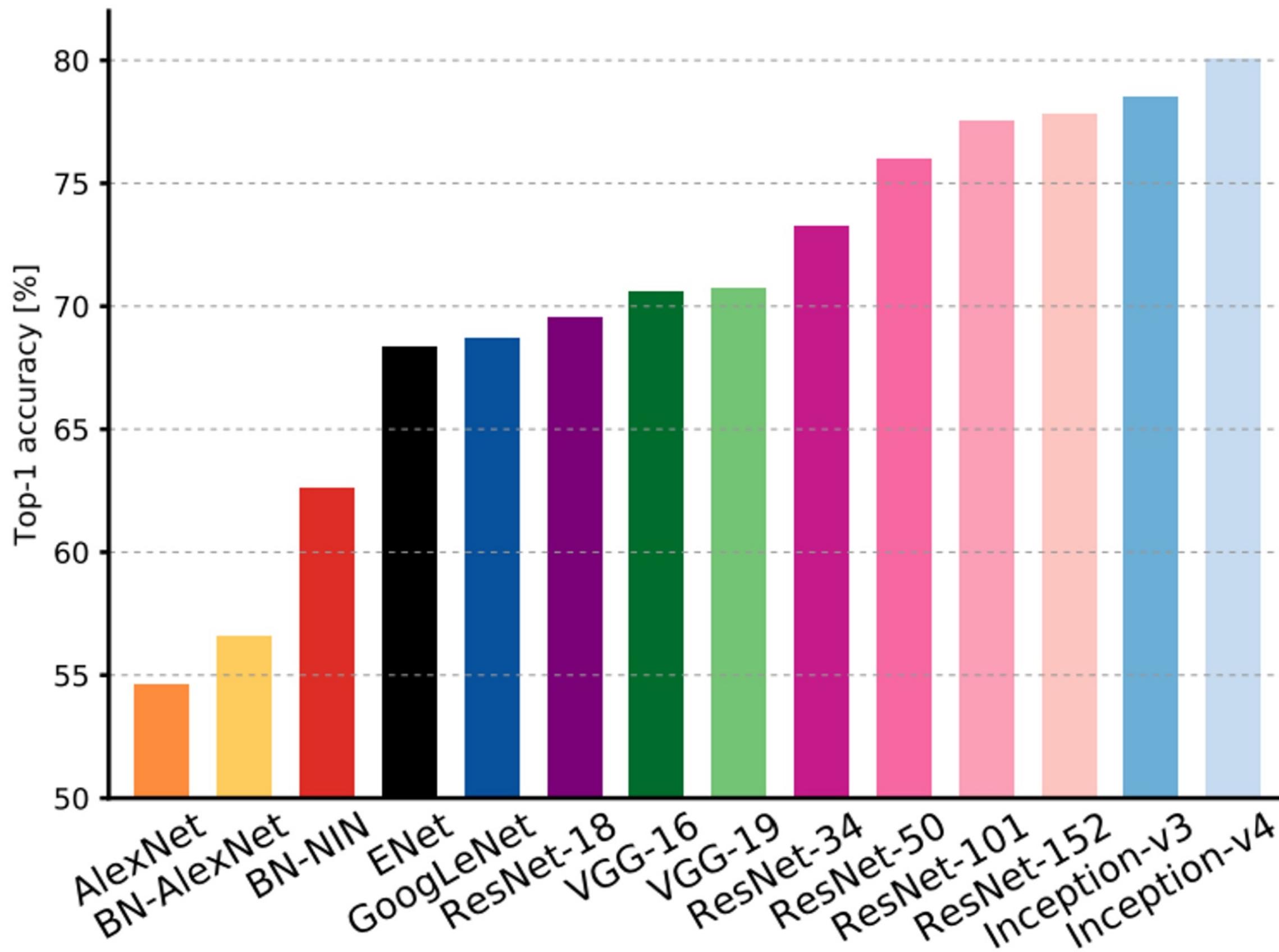
Comparing Complexity

Inception-v4: ResNet + Inception!





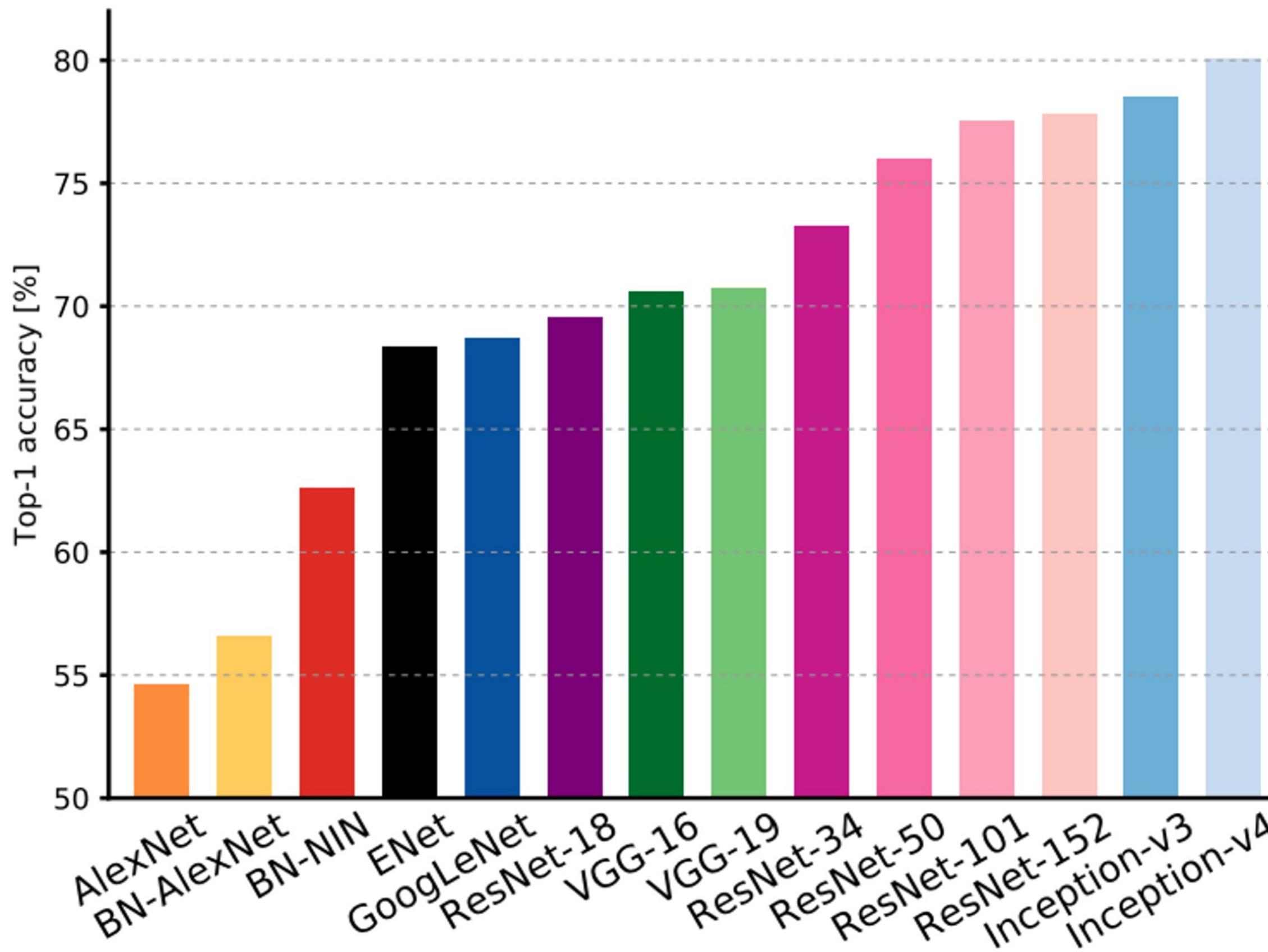
Comparing Complexity



VGG:
Highest memory,
most operations

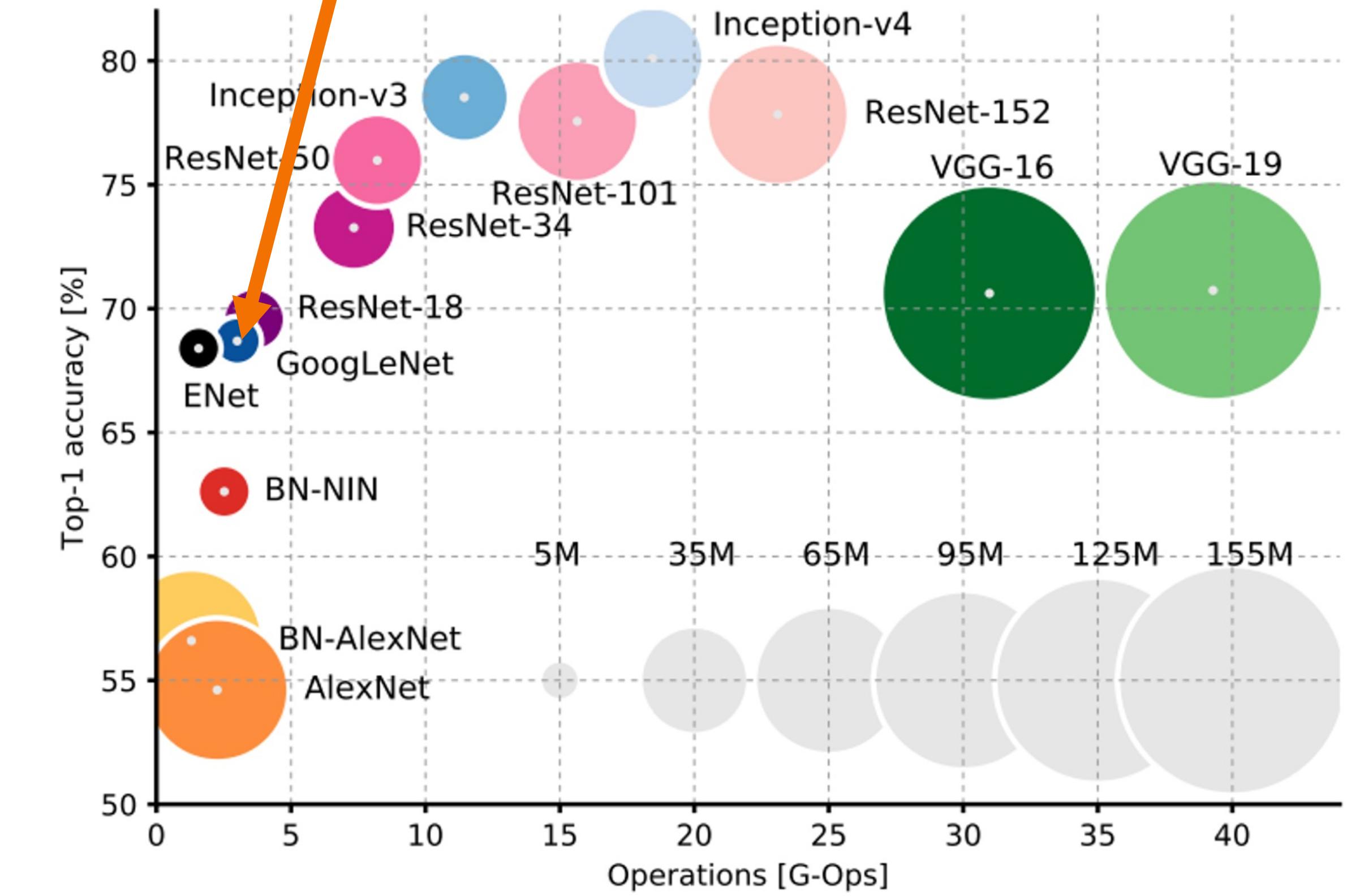


Comparing Complexity



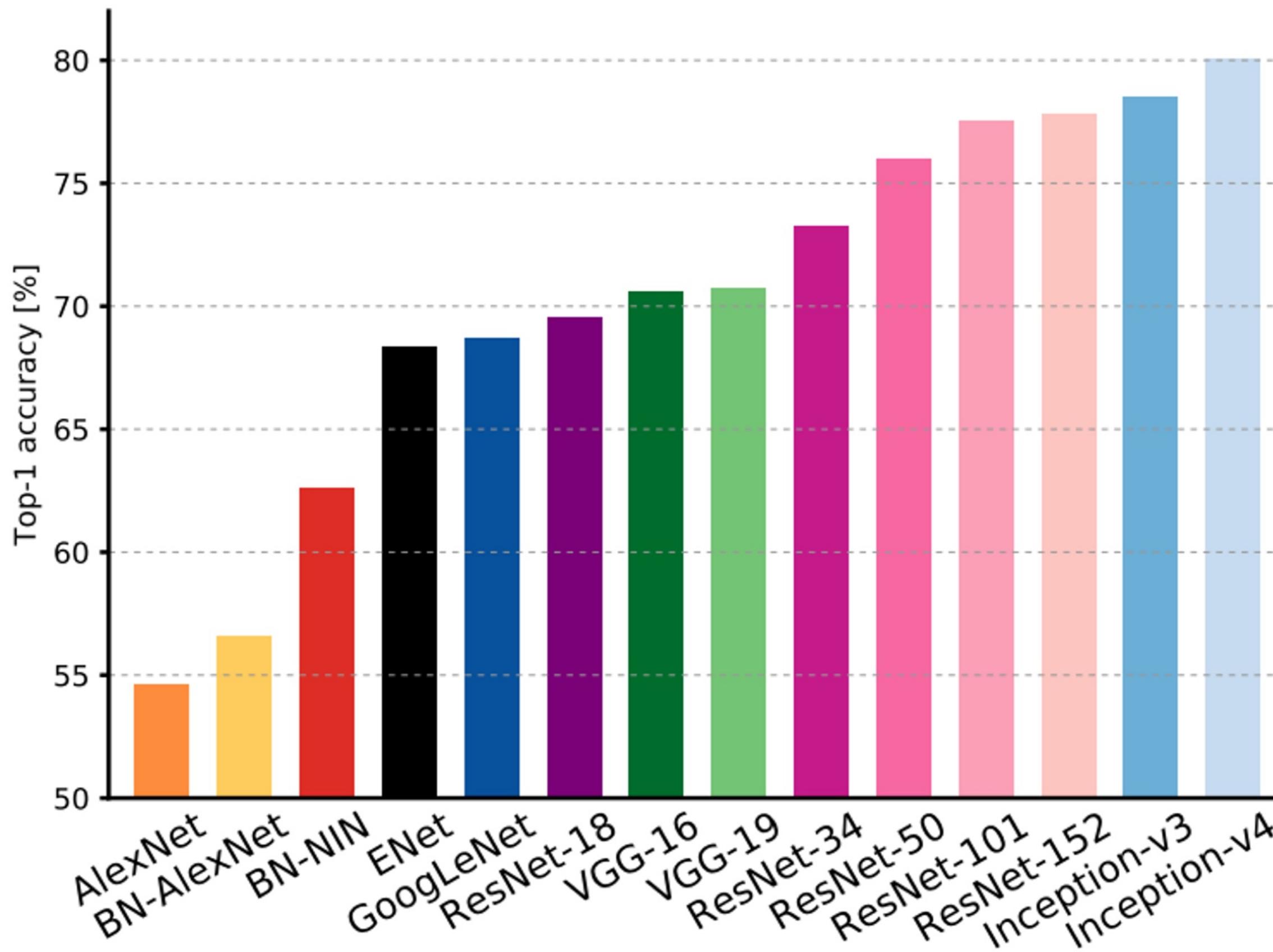
GoogLeNet:

Very efficient!

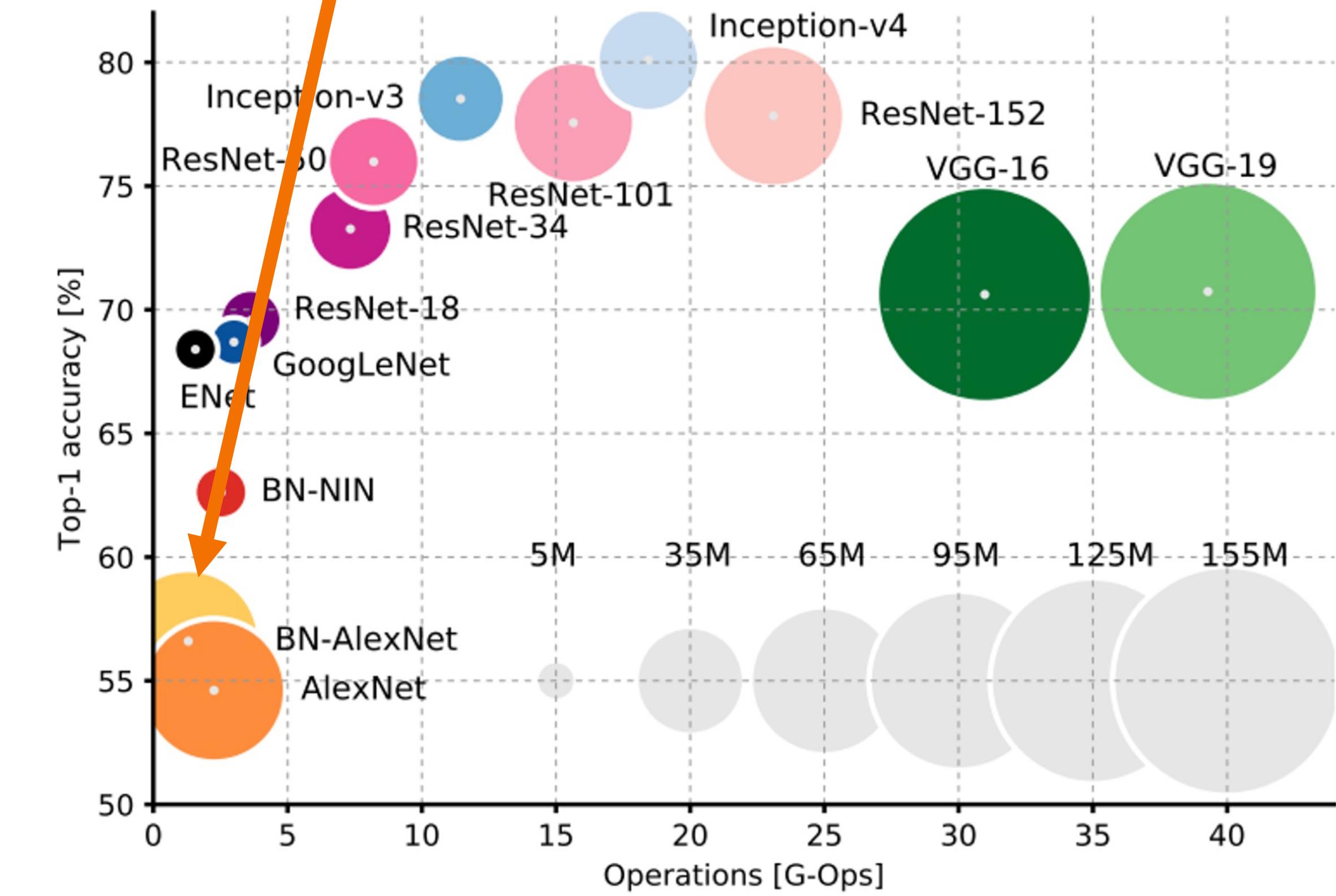




Comparing Complexity



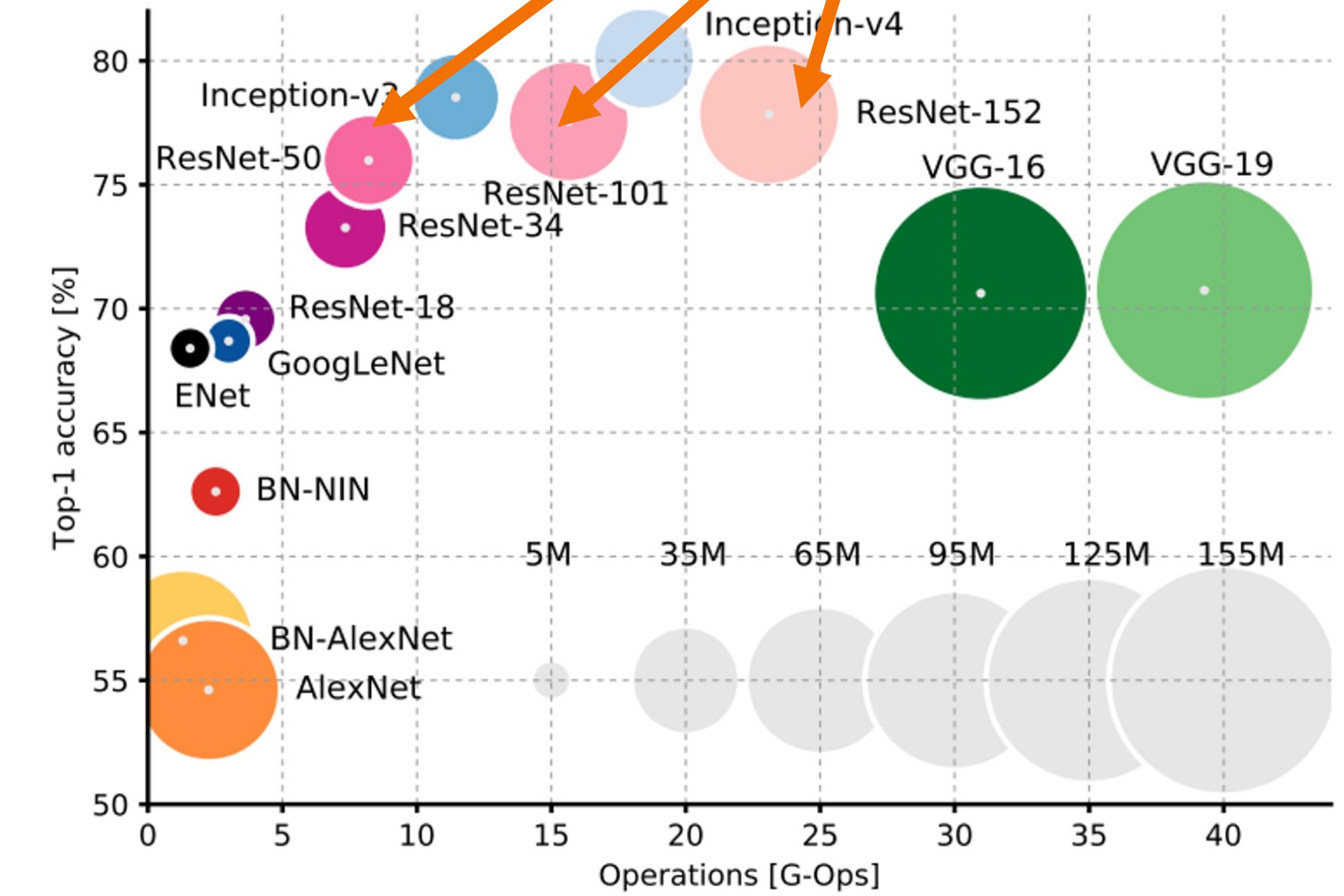
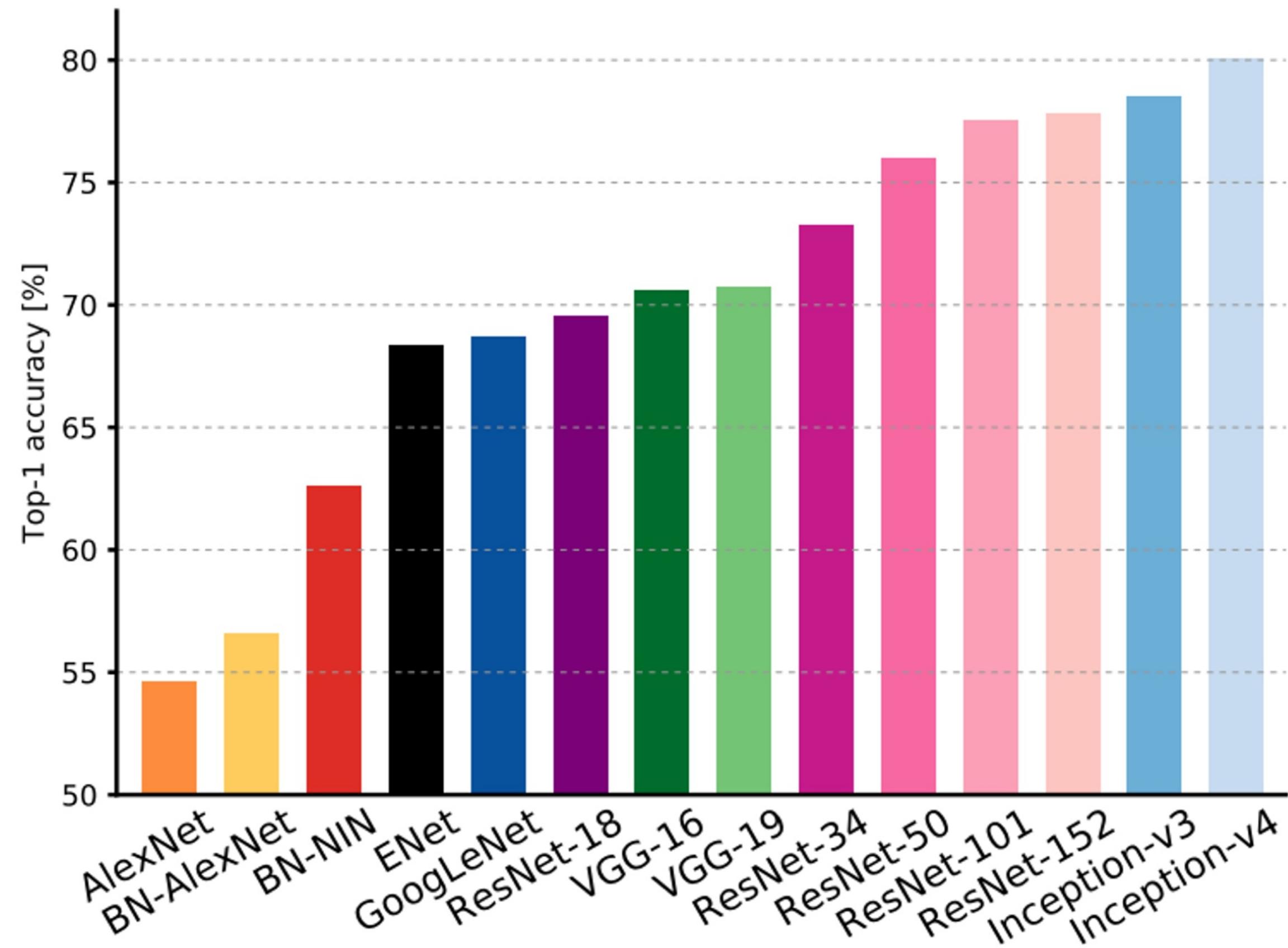
AlexNet: Low
compute, lots of
parameters





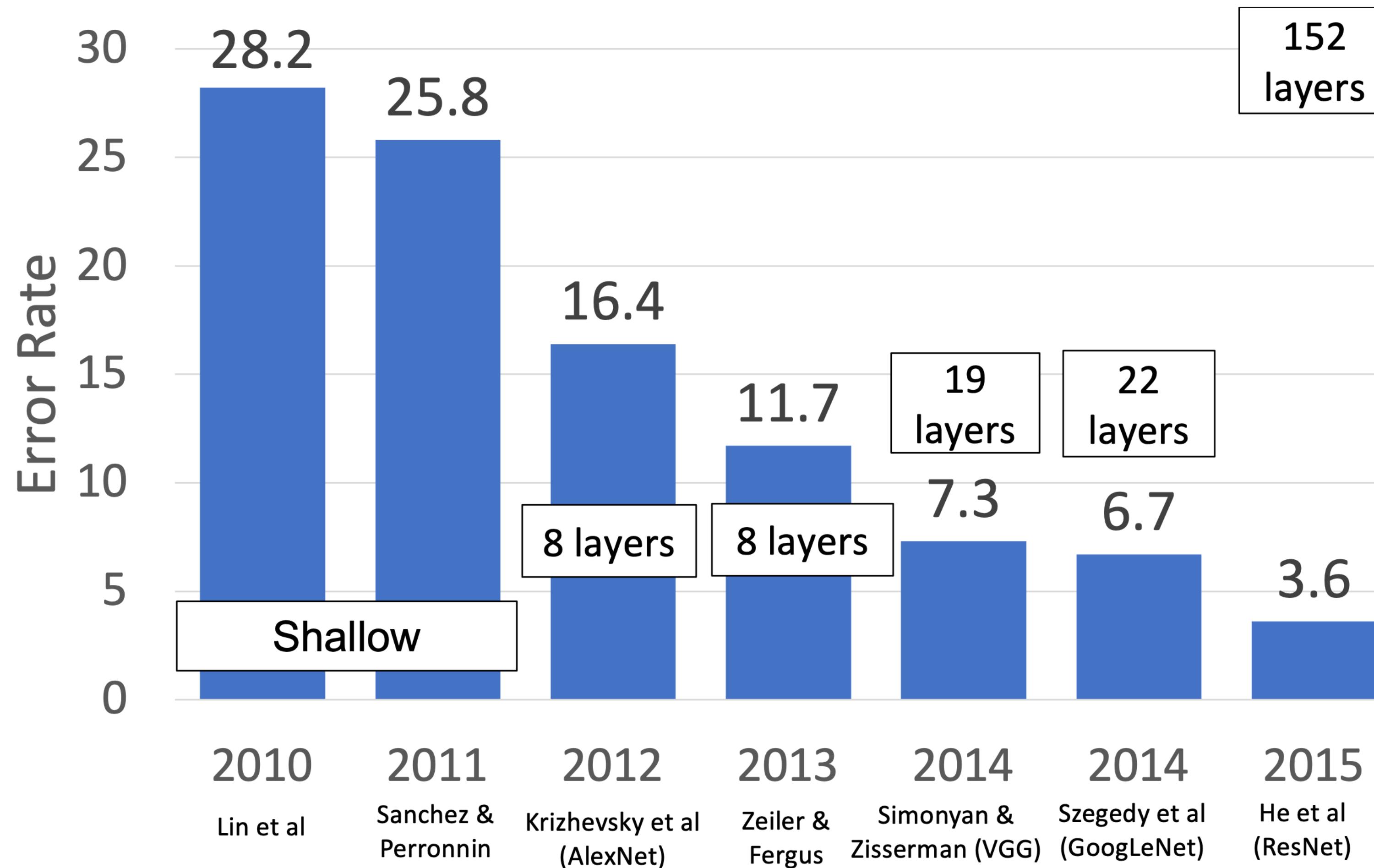
Comparing Complexity

ResNet: Simple design,
moderate efficiency, high
accuracy





ImageNet Classification Challenge



CNN architectures have continued to evolve!



DEEPRob

Lecture 7
CNN Architectures
University of Michigan | Department of Robotics

