

Automated Generation of Decision Table and Boundary Values from VDM++ Specification

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and Tomohiro Oda**

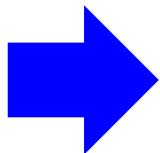
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1. background
2. VDTable
3. BWDM
4. Conclusion

VDM + Decision Table = VDTable

VDM++ Specification



VDTable

CLASS

- summation
- NatSeqSum
- bin2dec
- revBin2dec
- rev
- Add01
- length

```
001 class Sample
002
003 functions
004 summation( n:nat, a:seq of nat ) s:nat
005 pre (n = len a) and (n >= 1)
006 post s = NatSeqSum( a );
007
008 NatSeqSum: (seq of nat) -> nat
009 NatSeqSum( s ) ==
010 cases s :
011 [] -> 0,
012 others -> hd s + NatSeqSum( tl s )
013 end;
014
015 bin2dec : seq of nat -> nat
016 bin2dec(s) ==
017 revBin2dec( rev(s) );
018
019 revBin2dec : seq of nat -> nat
020 revBin2dec( s ) ==
021 cases s :
022 [] -> 0,
023 [0] -> 0,
024 [1] -> 1,
025 others -> hd s + 2 * revBin2dec( tl s )
026 end;
027
```

Decision Table

Rule	#1	#2
Pre Condition	((n = (len a)) and (n >= 1))	Y N
Action	summation	X -

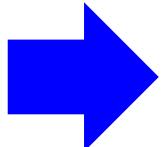
class name : Sample	
function name : SampleFunction	
Condition	a < 5
#1	T
#2	T
#3	F
#4	F
Condition	12 <= a
#1	T
#2	F
#3	T
#4	F
Action	"a < 5"
#1	T
#2	T
#3	F
#4	F
Action	"12 <= a"
#1	F
#2	F
#3	T
#4	F
Action	"5 <= a < 12"
#1	F
#2	F
#3	F
#4	T

1. **Condition part** – Describe the conditional expressions in software and the possible combinations of these Boolean values
2. **Action part** – Describe the operation in the software and the action on the truth value of the condition part
3. **Rule part** – Describe Behavior of software between condition part and action part

Boundary Value + Vienna Development Method = BWDM

VDM++
Specification

Decision
Table



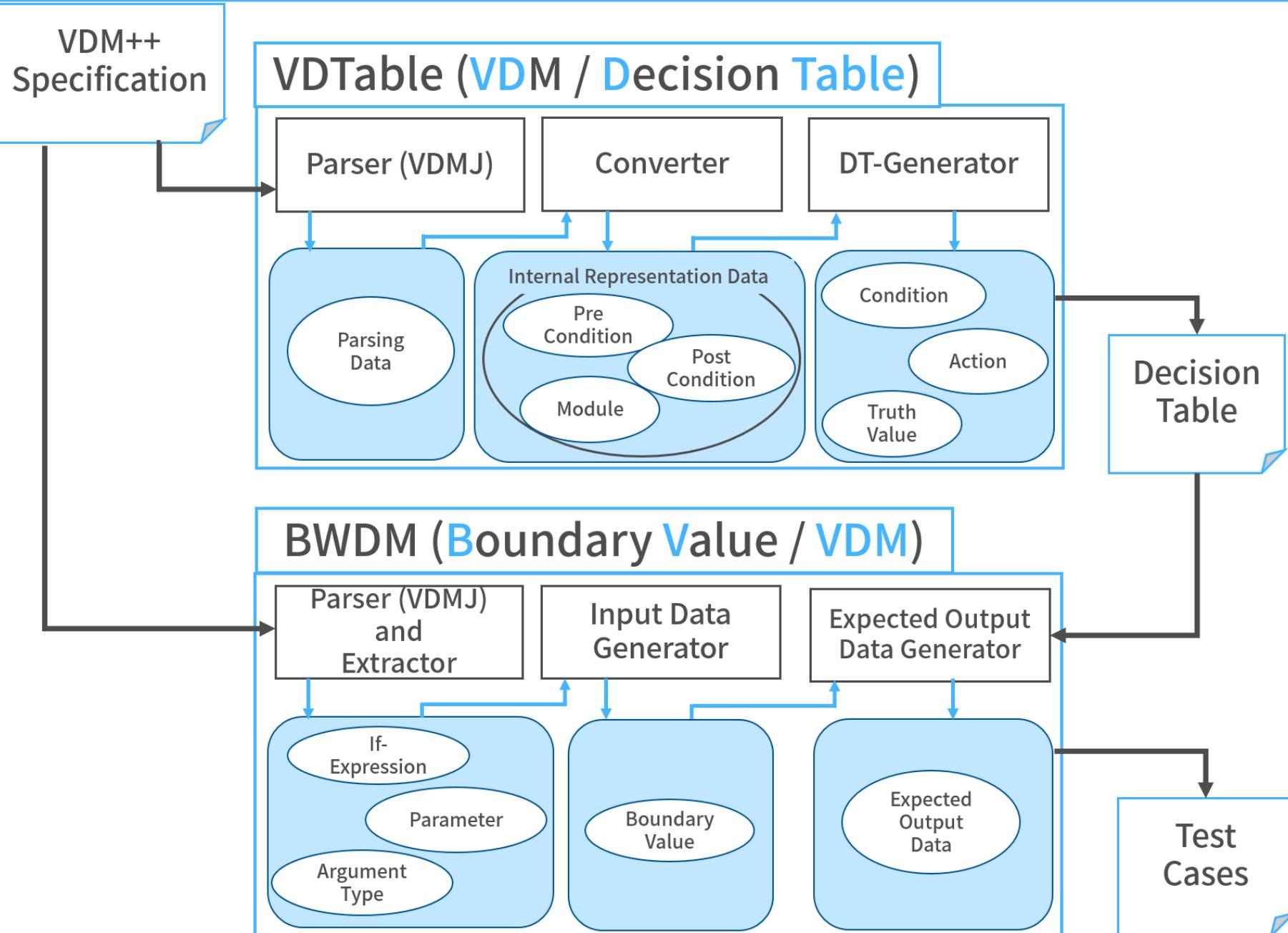
Test Cases

No.	natMin-1	v	-->	underlined Action
No.6	natMin-1	-1	-->	Undefined Action
No.7	natMin	intMin-1	-->	Undefined Action
No.8	natMin	intMin	-->	arg1:even arg2:negative
No.9	natMin	intMax	-->	arg1:even arg2:positive
No.10	natMin	intMax+1	-->	Undefined Action
No.11			-->	arg1:even arg2:positive
No.12			-->	arg1:even arg2:negative
No.13			-->	Undefined Action
No.14			-->	arg1:odd arg2:negative
No.15			-->	arg1:odd arg2:positive
No.16			-->	Undefined Action
No.17			-->	arg1:odd arg2:positive
No.18			-->	arg1:odd arg2:negative
No.19			-->	Undefined Action
No.20	natMax+1	intMin	-->	Undefined Action
No.21	natMax+1	intMax	-->	Undefined Action
No.22	natMax+1	intMax+1	-->	Undefined Action
No.23	natMax+1	0	-->	Undefined Action
No.24	natMax+1	-1	-->	Undefined Action
No.25	2	intMin-1	-->	Undefined Action
No.26	2	intMin	-->	arg1:even arg2:negative
No.27	2	intMax	-->	arg1:even arg2:positive
No.28	2	intMax+1	-->	Undefined Action
No.29	2	0	-->	arg1:even arg2:positive
No.30	2	-1	-->	arg1:even arg2:negative
No.31	1	intMin-1	-->	Undefined Action
No.32	1	intMin	-->	arg1:odd arg2:negative
No.33	1		-->	

overview of two tools

background

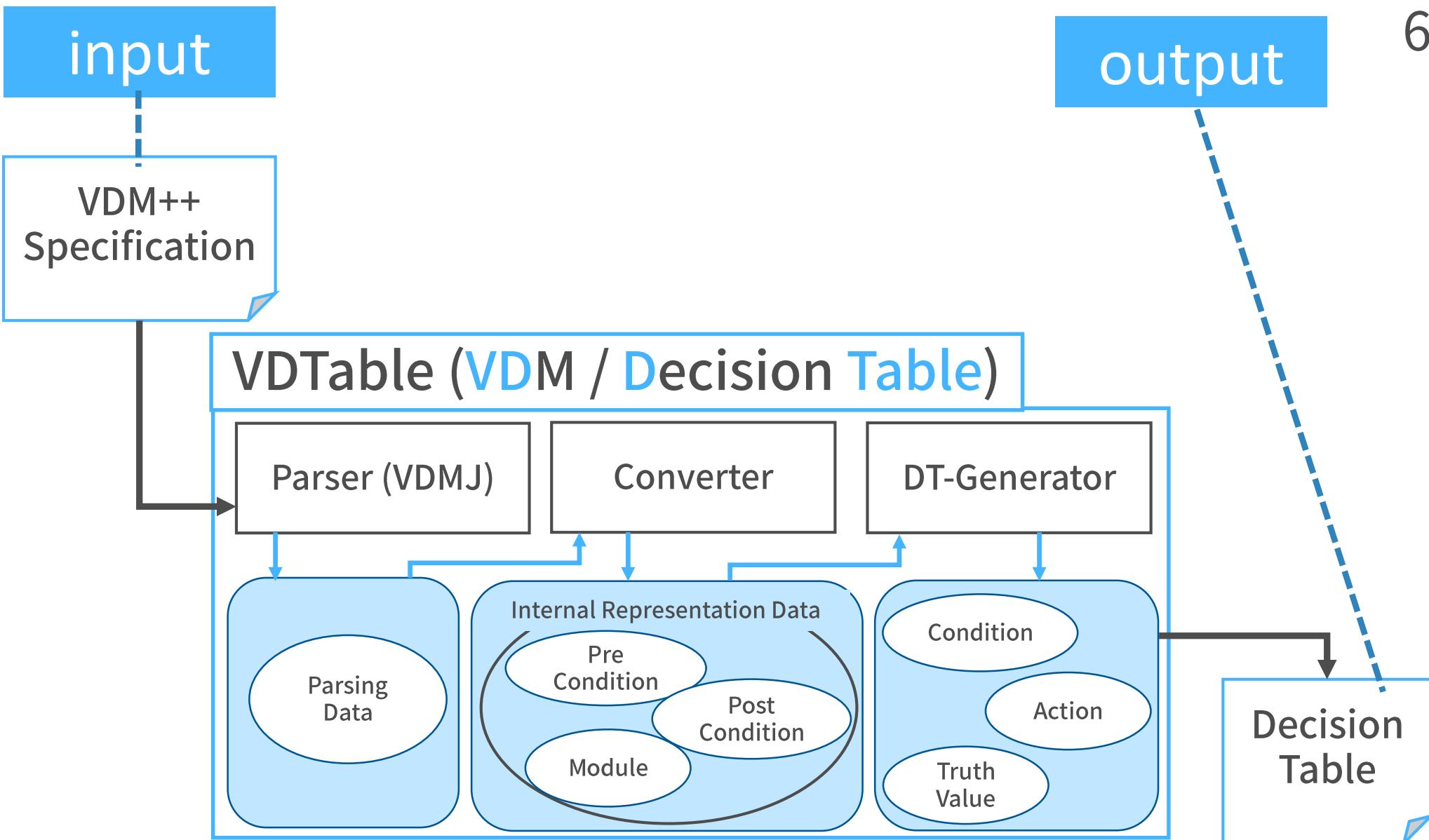
5



overview of VDTable

VDTable : decision table

6



D-Tree

VS-Screen

The screenshot shows the VDTable application interface. At the top, there's a title bar with three colored buttons (red, yellow, green) and the text "VDTable". Below the title bar, there are two main sections:

- D-Tree:** A sidebar on the left with a blue header labeled "CLASS". It contains a list of methods:
 - summation
 - NatSeqSum
 - bin2dec
 - revBin2dec
 - rev
 - Add01
 - lengthA red arrow points from the text "D-Tree" to this sidebar.
- VS-Screen:** The main area containing code. The title "VDTable" is at the top. The code is as follows:

```
001 class Sample
002
003 functions
004   summation( n:nat, a:seq of nat ) s:nat
005   pre (n = len a) and (n>=1)
006   post s = NatSeqSum( a );
007
008   NatSeqSum: (seq of nat) -> nat
009   NatSeqSum( s ) ==
010     cases s :
011       [] -> 0,
012       others -> hd s + NatSeqSum( tl s )
013     end;
014
015   bin2dec : seq of nat -> nat
016   bin2dec(s) ==
017     revBin2dec( rev(s) );
018
019   revBin2dec : seq of nat -> nat
020   revBin2dec( s ) ==
021     cases s :
022       [] -> 0,
023       [0] -> 0,
024       [1] -> 1,
025       others -> hd s + 2*revBin2dec( tl s )
026     end;
```

A green arrow points from the text "VS-Screen" to this area.

DT-Panel: A bottom panel with a red border. It has tabs: {P}, A, and {Q}. The "A" tab is selected. It contains a table:

Rule	#1	#2
Pre Condition	Y	N
Action	X	-

A red arrow points from the text "DT-Panel" to this panel.

A : module tab

Rule	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10	#11	#12	#13
Condition													
1	Y	N	N	N	N	N	N	N	N	N	N	N	N
2	-	Y	N	N	N	N	N	N	N	N	N	N	N
3	-	-	Y	N	N	N	N	N	N	N	N	N	N
4	-	-	-	Y	N	N	N	N	N	N	N	N	N
5	-	-	-	-	Y	N	N	N	N	N	N	N	N
6	-	-	-	-	-	Y	N	N	N	N	N	N	N
7	-	-	-	-	-	-	Y	N	N	N	N	N	N
8	-	-	-	-	-	-	-	Y	N	N	N	N	N
9	-	-	-	-	-	-	-	-	Y	N	N	N	N
10	-	-	-	-	-	-	-	-	-	Y	N	N	N
11	-	-	-	-	-	-	-	-	-	-	Y	N	N
12	-	-	-	-	-	-	-	-	-	-	-	Y	N
13	-	-	-	-	-	-	-	-	-	-	-	-	Y

{P} : pre condition tab

Rule	#1	#2
Pre Condition (月 <= 12)	Y	N
Action	X	-
日付表示	X	-

{Q} : post condition tab

Rule	#1	#2
Post Condition (31 <= RESULT)	Y	N
Action	X	-
日付表示	X	-



draw

Rule	#1	#2
Condition	Y	N
Action	X	-
((hd s) + NatSeqSum((tl s)))	-	X

click any definition



re-draw

Rule	#1	#2	#3	#4
Condition	Y	N	N	N
Action	X	X	-	-
0,	-	-	X	-
1	-	-	-	X
((hd s) + (2 * revBin2dec((tl s))))	-	-	-	-

```
class Day
functions
public dateDisp: nat1 * nat1 -> nat1
dateDisp(year, month) ==
cases month:
1 -> 31,
2 -> judgeLeapYear (year),
3 -> 31,
4 -> 30,
5 -> 31,
6 -> 30,
7 -> 31,
8 -> 31,
9 -> 30,
10 -> 31,
11 -> 30,
12 -> 31,
others -> undefined
end;
```

...

Day specification

- ✓ Inputs are year and month.
- ✓ Return value is the date at the end of the month of the input.
year / month.
- ✓ If it was entered a month other than January to December, the return value is an undefined expression.
- ✓ condition : 12
 - 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12
- ✓ action : 4
 - 31 judgeLeapYear (year), 30, undefined

Application result

VDTTable : decision table

VDTTable

CLASS

dateDisp
judgeLeapYear

```
001 class Day
002
003 functions
004
005 public dateDisp:nat1>nat1>nat1
006     dateDisp (year, month) ==
007         cases month:
008             1 > 31,
009             2 > judgeLeapYear (year),
010             3 > 31,
011             4 > 30,
012             5 > 31,
013             6 > 30,
014             7 > 31,
015             8 > 31,
016             9 > 30,
017             10 > 31,
018             11 > 30,
019             12 > 31,
020             others > undefined
021     end;
022
023 public judgeLeapYear:nat1>nat1
024     judgeLeapYear (year) ==
025         if (year mod 4 = 0) then
026             if (year mod 100 = 0) then
027                 if (year mod 400 = 0) then 29
028                 else 28
029             else 29
030             else 28;
031
032 end Day
```

{P} A {Q}

Rule	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10	#11	#12	#13
Condition													
1.	Y	N	N	N	N	N	N	N	N	N	N	N	N
2.	-	Y	N	N	N	N	N	N	N	N	N	N	N
3.	-	-	Y	N	N	N	N	N	N	N	N	N	N
4.	-	-	-	Y	N	N	N	N	N	N	N	N	N
5.	-	-	-	-	Y	N	N	N	N	N	N	N	N
6.	-	-	-	-	-	Y	N	N	N	N	N	N	N
7.	-	-	-	-	-	-	Y	N	N	N	N	N	N
8.	-	-	-	-	-	-	-	Y	N	N	N	N	N
9.	-	-	-	-	-	-	-	-	Y	N	N	N	N
10.	-	-	-	-	-	-	-	-	-	Y	N	N	N
11.	-	-	-	-	-	-	-	-	-	-	Y	N	N
12.	-	-	-	-	-	-	-	-	-	-	-	Y	N
Action													
31.	X	-	X	-	X	-	X	X	-	X	-	X	-
judgeLeapYea...	-	X	-	-	-	-	-	-	-	-	-	-	-
30.	-	-	-	X	-	X	-	-	X	-	X	-	-
(undefined)	-	-	-	-	-	-	-	-	-	-	-	-	X



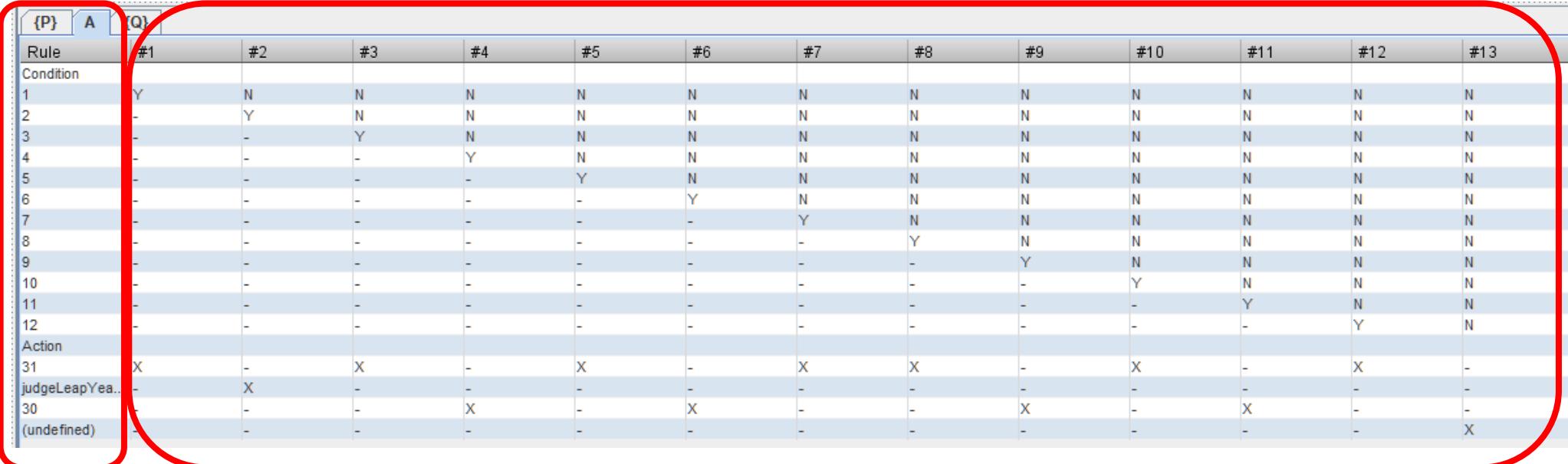
generated decision table (DT-Panel)

Application result

VDTTable : decision table

12 conditions and 4 actions (all conditions and actions)
are extracted.

12

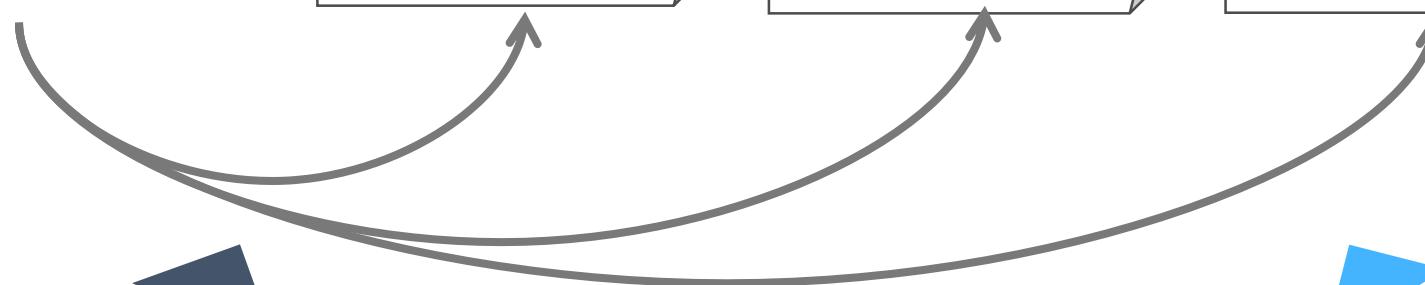
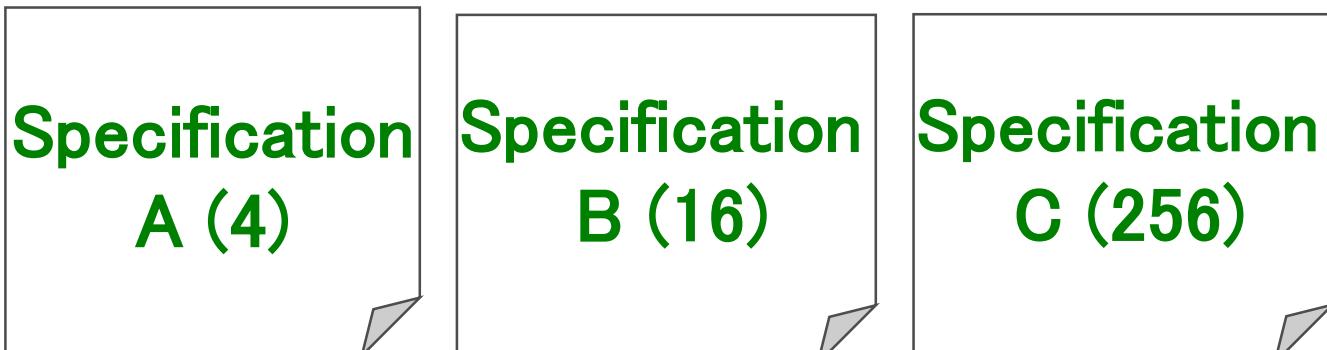


{P}	A	(Q)	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10	#11	#12	#13
Rule															
Condition															
1	Y		N	N	N	N	N	N	N	N	N	N	N	N	N
2	-		Y	N	N	N	N	N	N	N	N	N	N	N	N
3	-		-	Y	N	N	N	N	N	N	N	N	N	N	N
4	-		-	-	Y	N	N	N	N	N	N	N	N	N	N
5	-		-	-	-	Y	N	N	N	N	N	N	N	N	N
6	-		-	-	-	-	Y	N	N	N	N	N	N	N	N
7	-		-	-	-	-	-	Y	N	N	N	N	N	N	N
8	-		-	-	-	-	-	-	Y	N	N	N	N	N	N
9	-		-	-	-	-	-	-	-	Y	N	N	N	N	N
10	-		-	-	-	-	-	-	-	-	Y	N	N	N	N
11	-		-	-	-	-	-	-	-	-	-	Y	N	N	N
12	-		-	-	-	-	-	-	-	-	-	-	Y	N	N
Action															
31	X		-	X	-	X	-	X	X	-	X	-	X	-	-
judgeLeapYear	-		X	-	-	-	-	-	-	-	-	-	-	-	-
30	-		-	-	X	-	X	-	-	X	-	X	-	-	X
(undefined)	-		-	-	-	-	-	-	-	-	-	-	-	-	-

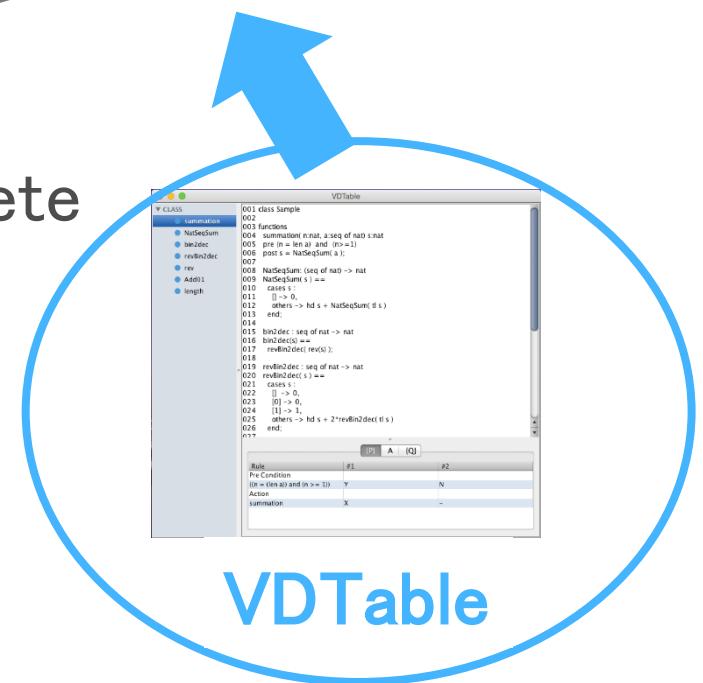
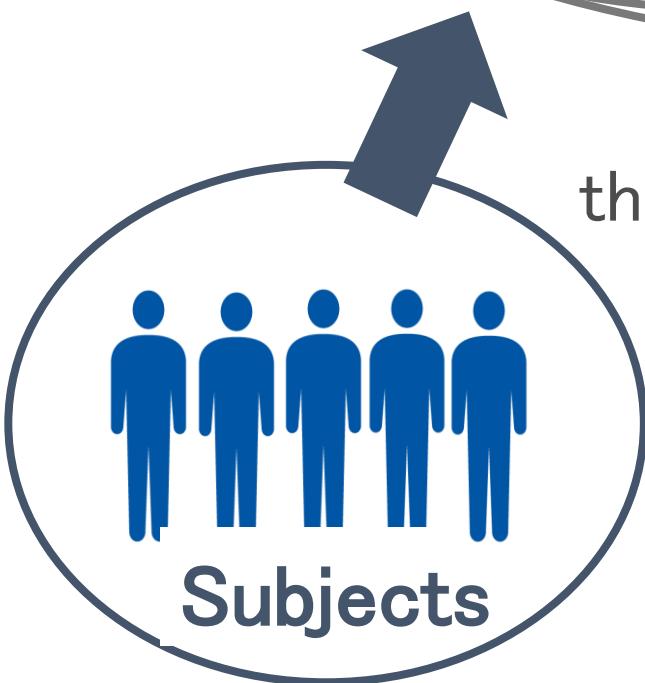
Truth values are properly generated.

We confirmed that the VDTTable operates correctly.

The number of combination of truth values is different



Measure and compare
the time taken to complete
the decision table
for each specification



subject	VDM++ specification (The number of combination of truth values)		
	specification A (4)	specification B (16)	specification C (256)
A	252	405	1131
B	213	559	1292
C	169	499	1194
D	240	435	1859
E	134	557	1397
average	216	498	1629
VDTTable	0.012	0.016	0.02

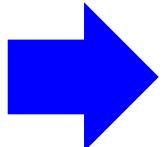
- VDTTable reduced labor and time for manual work.
- VDTTable is useful for improving the work of designing a decision table using the VDM++ specification.

Boundary Value + Vienna Development Method = BWDM

15

VDM++ Specification

Decision Table



Test Cases

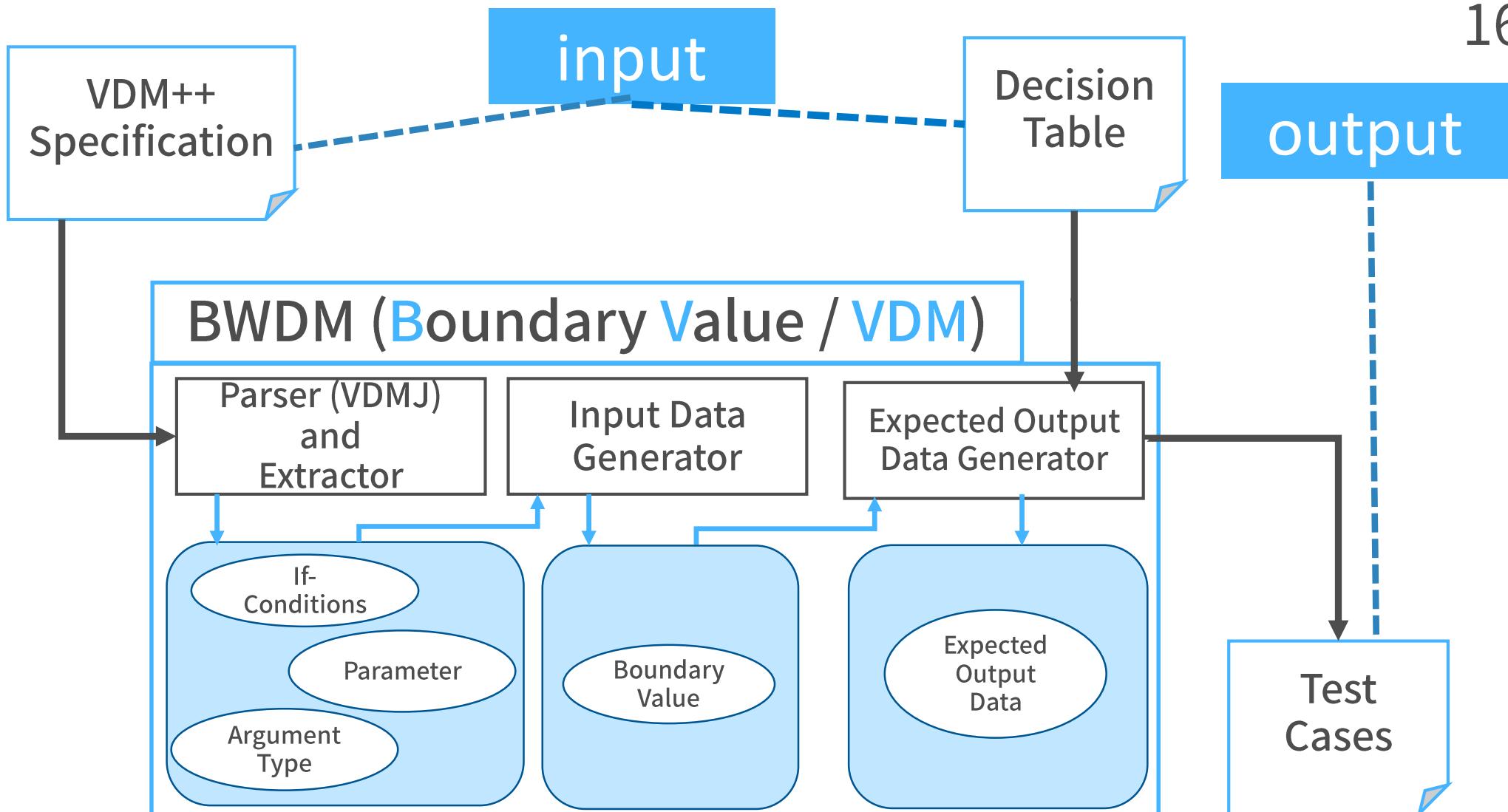
No.	natMIN-1	v	-->	UNDEFINED ACTION
No.6	natMin-1	-1	-->	Undefined Action
No.7	natMin	intMin-1	-->	Undefined Action
No.8	natMin	intMin	-->	arg1:even arg2:negative
No.9	natMin	intMax	-->	arg1:even arg2:positive
No.10	natMin	intMax+1	-->	Undefined Action
No.11	natMin	0	-->	arg1:even arg2:positive
No.12			-->	arg1:even arg2:negative
No.13			-->	Undefined Action
No.14			-->	arg1:odd arg2:negative
No.15			-->	arg1:odd arg2:positive
No.16			-->	Undefined Action
No.17			-->	arg1:odd arg2:positive
No.18			-->	arg1:odd arg2:negative
No.19			-->	Undefined Action
No.20			-->	Undefined Action
No.21			-->	Undefined Action
No.22	natMax+1	intMax+1	-->	Undefined Action
No.23	natMax+1	0	-->	Undefined Action
No.24	natMax+1	-1	-->	Undefined Action
No.25	2	intMin-1	-->	Undefined Action
No.26	2	intMin	-->	arg1:even arg2:negative
No.27	2	intMax	-->	arg1:even arg2:positive
No.28	2	intMax+1	-->	Undefined Action
No.29	2	0	-->	arg1:even arg2:positive
No.30	2	-1	-->	arg1:even arg2:negative
No.31	1	intMin-1	-->	Undefined Action
No.32	1	intMin	-->	arg1:odd arg2:negative

BWDM outputs test cases that based on boundary value analysis.

overview of BWDM

BWDM : boundary values

16



The screenshot shows a window titled "SampleSpecICAROB..." with a menu bar in Japanese. The code editor contains the following VDM++ specification:

```
class Sample
functions
  SampleFunction : int -> seq of char
    SampleFunction(a)==
      if(a < 5) then
        "a < 5"
      else if(12 <= a) then
        "12 <= a"
      else
        "5 <= a < 12";
end Sample
```

- a function definition in VDM++ specification
- an argument of int
- return value is Sequence of char
- two if-conditions

VDM++ specification

SampleSpecCAROB...

```

class Sample
functions
    SampleFunction : int -> seq of char
        SampleFunction(a) ==
            if(a < 5) then
                "a < 5"
            else if(12 <= a) then
                "12 <= a"
            else
                "5 <= a < 12"
end Sample

```

Type Boundary Value

if-condition

boundary value

Boundary Value Analysis

Expected Output Data
of outside input
values of type range

Test Case No.	Input Data	Expected Output Data
No.1	intMin-1	"Undefined Action"
No.2	intMin	"a < 5"
No.3	intMax	"12 <= a"
No.4	intMax+1	"Undefined Action"
No.5	4	"a < 5"
No.6	5	"5 < a <= 12"
No.7	11	"5 < a <= 12"
No.8	12	"12 <= a"

VDM++ Specification

test cases

Input Data

- Generated from function definition in VDM++ specification.
- Consists of 2 kind of boundary value; **type boundary value** that is generated from arguments type, and **if-conditions boundary value** that is generated from if conditions.

type boundary value

Ex.) When the argument of the function is an int



intMin, intMax, intMin-1, intMax+1

Minimum, maximum, and outside values of
Integer range

In testing phase, tester corrects it to actual
numbers, such as intMin:-2147483648,
according to the development environment
(language, bit number, etc.), and performs test.

if-conditions boundary value

Ex.) When the if-condition is “ $a < 4$ ”



3, 4 (3:true, 4:false)

two integer values at the boundary of the inequality (three values when if-condition is modulo)

Expected Output Data

- Output when input data is input to program
- When receiving outside values of type range (*Min-1, *Max+1), the program overflows and the operation can not be predicted so the expected output data is assumed to be “Undefined Action”.

SampleSpecCAROB...

```

class Sample
functions
    SampleFunction : int -> seq of char
        SampleFunction(a) ==
            if(a < 5) then
                "a < 5"
            else if(12 <= a) then
                "12 <= a"
            else
                "5 <= a < 12"
end Sample

```

Type Boundary Value

if-condition

boundary value

Boundary Value Analysis

Expected Output Data
of outside input
values of type range

Test Case No.	Input Data	Expected Output Data
No.1	intMin-1	"Undefined Action"
No.2	intMin	"a < 5"
No.3	intMax	"12 <= a"
No.4	intMax+1	"Undefined Action"
No.5	4	"a < 5"
No.6	5	"5 < a <= 12"
No.7	11	"5 < a <= 12"
No.8	12	"12 <= a"

VDM++ Specification

test cases

Mixed inequality and modulo

24

```
class MixSpecification

functions

mix: nat * int -> seq of char
mix( arg1 , arg2 ) ==
  if( arg1 mod 2 = 0) then
    if (0 <= arg2 ) then
      " arg1:even arg2:positive"
    else
      " arg1:even arg2:negative"
  else
    if( arg2 < 0) then
      " arg1:odd arg2:negative"
    else
      " arg1:odd arg2:positive";

end MixSpecification
```

- two arguments
- determine whether arg1 is an even number in the first remainder expression
- In two inequalities, it judges the sign of arg2

Application result

BWDM : boundary values

25

The number of arguments:2

argument type: argument1:nat argument2:int

No.	input data	-->	expected output data
No.1	natMin-1	intMin-1	--> Undefined Action
No.2	natMin-1	intMin	--> Undefined Action
No.3	natMin-1	intMax	--> Undefined Action
No.4	natMin-1	intMax+1	--> Undefined Action
No.5	natMin-1	0	--> Undefined Action
No.6	natMin-1	-1	--> Undefined Action
No.7	natMin	intMin-1	--> Undefined Action
No.8	natMin	intMin	--> arg1:even arg2:negative
No.9	natMin	intMax	--> arg1:even arg2:positive
No.10	natMin	intMax+1	--> Undefined Action
No.11	natMin	0	--> arg1:even arg2:positive
No.12	natMin	-1	--> arg1:even arg2:negative
No.13	natMax	intMin-1	--> Undefined Action
No.14	natMax	intMin	--> arg1:odd arg2:negative
No.15	natMax	intMax	--> arg1:odd arg2:positive
No.16	natMax	intMax+1	--> Undefined Action
No.17	natMax	0	--> arg1:odd arg2:positive
No.18	natMax	-1	--> arg1:odd arg2:negative
No.19	natMax+1	intMin-1	--> Undefined Action
No.20	natMax+1	intMin	--> Undefined Action
No.21	natMax+1	intMax	--> Undefined Action
No.22	natMax+1	intMax+1	--> Undefined Action
No.23	natMax+1	0	--> Undefined Action

No.24	natMax+1	-1	-->	Undefined Action
No.25	2	intMin-1	-->	Undefined Action
No.26	2	intMin	-->	arg1:even arg2:negative
No.27	2	intMax	-->	arg1:even arg2:positive
No.28	2	intMax+1	-->	Undefined Action
No.29	2	0	-->	arg1:even arg2:positive
No.30	2	-1	-->	arg1:even arg2:negative
No.31	1	intMin-1	-->	Undefined Action
No.32	1	intMin	-->	arg1:odd arg2:negative
No.33	1	intMax	-->	arg1:odd arg2:positive
No.34	1	intMax+1	-->	Undefined Action
No.35	1	0	-->	arg1:odd arg2:positive
No.36	1	-1	-->	arg1:odd arg2:negative
No.37	3	intMin-1	-->	Undefined Action
No.38	3	intMin	-->	arg1:odd arg2:negative
No.39	3	intMax	-->	arg1:odd arg2:positive
No.40	3	intMax+1	-->	Undefined Action
No.41	3	0	-->	arg1:odd arg2:positive
No.42	3	-1	-->	arg1:odd arg2:negative

According to the specification,

- arg1:7, arg2:6 boundary values are output correctly
- Output the input data and the expected output data correctly as the boundary value test case

We input three specifications with different number of if-conditional expressions to BWDM, and measured the time until test cases are generated.

Times	specification1	specification2	specification3
1 st time	325	316	6277
2 nd time	283	389	5321
3 rd time	500	371	6236
4 th time	291	334	5070
5 th time	269	371	5700
Average	334	356	5720

We confirmed that boundary value test cases are automatically generated within a few seconds is the number of conditions is 15

Combinatorial Testing



Overture* supports for Combinatorial Testing.

→ By conducting combinatorial test with test cases generated by BWDM, its possible to conduct more effective testing to find bugs.

*<http://overturetool.org/>

- In this research, we developed two tools to improve testing phase of software development with VDM++.
(1) VDTable : generates a decision table
(2) BWDM : generates boundary values
- We think that our tools have the potential of improving software testing process with VDM++.

Common issues of both tools

29

- Evaluation by using huge specification that used in real development
- Correspondence to exponential explosion
- Expanding coverage of the tool
- Correspondence to other test design techniques

The issue of VDTable

- Correspondence to compound conditional expression

The issue of BWDM

- Implementation of Symbolic Execution


```
#access  
private  
#location  
in '/Users/katlab/Documents/workspace/VDMDT/data/Sample.vdmpp' at line 4:3  
#name  
revBin2dec  
#type  
(seq of (nat) -> nat)  
#kind  
explicit function  
#body  
private revBin2dec: (seq of (nat) -> nat)  
    revBin2dec(s) ==  
        (if (s = [])  
            then 0  
        elseif (s = [0])  
            then 0  
        elseif (s = [1])  
            then 1  
        else ((hd s) + (2 * revBin2dec((tl s)))))
```

#access

- types of access modifiers

#location

- location of VDM++ file
- start position of definition

#name

- name of definition

#type

- argument type

#kind

- types of definition

#body

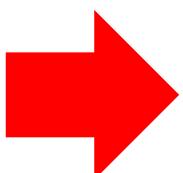
- inside definition

internal representation data

VDTTable : decision table

35

```
...  
  
#kind  
  
explicit function  
  
#body  
  
private revBin2dec: (seq of (nat) → nat)  
    revBin2dec(s) ==  
  
(if (s = [])  
    then 0  
    elseif (s = [0])  
    then 0  
    elseif (s = [1])  
    then 1  
    else ((hd s) + (2 * revBin2dec((tl s)))))
```



```
if1  
(s = [])  
then  
0  
elseif  
(s = [0])  
then  
0  
elseif  
(s = [1])  
then  
1  
else1  
((hd s) + (2 * revBin2dec((tl s))))
```

condition extraction pattern	action extraction pattern
if "condition" then elseif "condition" then	then "action" if then "action" elseif then "action" else else "action" if else "action" elseif else "action" else else "action" EOF
cases "condition" ->	-> "action" cases others "Action" EOF
pre "condition" post pre "condition" EOF post "condition" EOF	

condition array

VDTTable : decision table

internal representation data

if1

(s = [])

then

0

elseif

(s = [0])

then

0

elseif

(s = [1])

then

1

else1

((hd s) + (2 * revBin2dec((tl s))))

condition array

37

index	condition
0	(s = [])
1	(s = [0])
2	(s = [1])

extraction rule ※EOF(End Of File)

condition extraction pattern	action extraction pattern
if "condition" then elseif "condition" then	then "action" if then "action" elseif then "action" else else "action" else else "action" elseif else "action" else else "action" EOF
cases "condition" ->	-> "action" cases others "action" EOF
pre "condition" post pre "condition" EOF post "condition" EOF	

action array

VDTTable : decision table

internal representation data

action array

38

```
if1  
(s = [])  
then  
0  
elseif  
(s = [0])  
then  
0  
elseif  
(s = [1])  
then  
1  
else1  
((hd s) + (2 * revBin2dec((tl s))))
```

index	action
0	0
1	1
2	((hd s) + (2 * revBin2dec((tl s))))

extraction rule ※EOF(End Of File)

condition extraction pattern	action extraction pattern
if “condition” then elseif “condition” then	then “action” if then “action” elseif then “action” else else “action” else else “action” elseif else “action” else else “action” EOF
cases “condition” ->	-> “action” cases others “action” EOF
pre “condition” post pre “condition” EOF post “condition” EOF	

condition-action table

internal representation data

if1

$(s = \boxed{\text{ }})$

then

0

elseif

$(s = [0])$

then

0

elseif

$(s = [1])$

then

1

else1

$((\text{hd } s) + (2 * \text{revBin2dec}(\text{tl } s)))$

VDTTable : decision table

condition
array

39

CA-Table

index	condition
0	$(s = \boxed{\text{ }})$
1	$(s = [0])$
2	$(s = [1])$

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

action array

index	action
0	0
1	1
2	$((\text{hd } s) + (2 * \text{revBin2dec}(\text{tl } s)))$

1. Create an array that is two dimensional and stores truth value.
2. Select the first column of the array.
3. Select a row of CA-Table from the first row.
4. Compare tokens and store truth value in the array
 - A) When "if", "elseif", "cases" are matched,
 - I. Store "Y" to the column selected for the conditional index row and "N" from the next column to the end of the column.
 - II. Store "X" in action index of selected column.
 - B) When "else", "others" are matched,
 - I. Store "N" to the column selected for the conditional index row and "-" from the next column to the end of the column.
 - II. Store "X" in action index of selected column.
5. If there are unselected rows, select the next column of the array and return to 3. When there is no, truth value is completed.

1. Create an array that is two dimensional and stores truth value.
2. Select the first column of the array.
3. Select one row of the CA-Table.

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

number of condition and else and others

index of condition	0	1	2	3
index of action	0	-	-	-
index of action	1	-	-	-
index of action	2	-	-	-

index of condition	0	1	2	3
index of action	0	-	-	-
index of action	1	-	-	-
index of action	2	-	-	-

4. Compare tokens and store truth value in the array

- A) When "if", "elseif", "cases" are matched,
- I. Store "Y" to the column selected for the conditional index row and "N" from the next column to the end of the column.
 - II. Store "X" in action index of selected column.

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

		number of condition and else and others				
index of condition	index of action	0	1	2	3	4
		Y	-	-	-	-
		-	-	-	-	-
index of condition	index of action	X	-	-	-	-
		-	-	-	-	-
		-	-	-	-	-

5. If there are unselected rows, select the next column of the array and return to 3.

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

number of condition and else and others

index of condition	Y	N	N	N
0	-	-	-	-
1	-	-	-	-
2	-	-	-	-

index of action	X	-	-	-
0	-	-	-	-
1	-	-	-	-
2	-	-	-	-

4. Compare tokens and store truth value in the array

- A) When “if”, “elseif”, “cases” are matched,
- I. Store "Y" to the column selected for the conditional index row and "N" from the next column to the end of the column.
 - II. Store “X” in action index of selected column.

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

number of condition and else and others

0	Y	N	N	N
1	-	Y	N	N
2	-	-	-	-
0	X	X	-	-
1	-	-	-	-
2	-	-	-	-

index of condition

index of action

4. Compare tokens and store truth value in the array

- A) When “if”, “elseif”, “cases” are matched,
- I. Store "Y" to the column selected for the conditional index row and "N" from the next column to the end of the column.
 - II. Store “X” in action index of selected column.

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

number of condition and else and others

0	Y	N	N	N
1	-	Y	N	N
2	-	-	Y	N

0	X	X	-	-
1	-	-	X	-
2	-	-	-	-

4. Compare tokens and store truth value in the array

B) When "else", "others" are matched,

- I. Store "N" to the column selected for the conditional index row and "-" from the next column to the end of the column.
- II. Store "X" in action index of selected column.

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

number of condition and else and others

0	Y	N	N	N
1	-	Y	N	N
2	-	-	Y	N
0	X	X	-	-
1	-	-	X	-
2	-	-	-	X

5. If there are unselected rows, select the next column of the array and return to 3.

When there is no, truth value is completed.

index of condition	token	index of action
0	if1	0
1	elseif	0
2	elseif	1
0	else1	2

number of condition and else and others

index of condition	0	1	2	3
0	Y	N	N	N
1	-	Y	N	N
2	-	-	Y	N

index of action	0	1	2	3
0	X	X	-	-
1	-	-	X	-
2	-	-	-	X

completion of the decision table

VDTTable : decision table

48

index	condition
0	(s = [])
1	(s = [0])
2	(s = [1])

index	action
0	0
1	1
2	((hd s) + (2 * revBin2dec((tl s))))

0	Y	N	N	N
1	-	Y	N	N
2	-	-	Y	N

0	X	X	-	-
1	-	-	X	-
2	-	-	-	X

Rule	#1	#2	#3	#4
Condition				
(s = [])	Y	N	N	N
(s = [0])	-	Y	N	N
(s = [1])	-	-	Y	N
Action				
0	X	X	-	-
1	-	-	X	-
((hd s) + (2 * revBin2dec((tl s))))	-	-	-	X



CEGTest*

The tool for automatically generating a decision table.

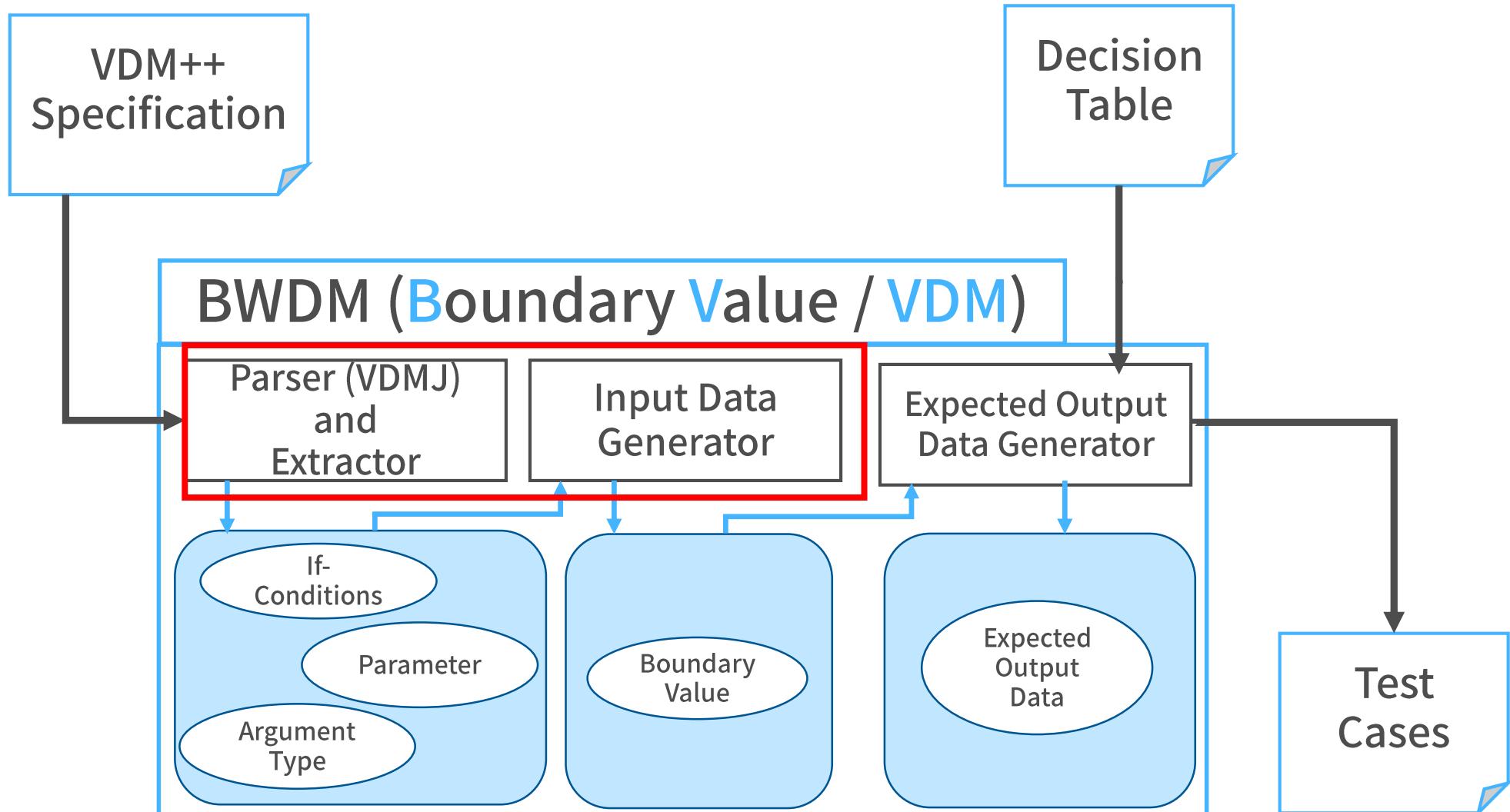
The cause result graph as the input of CEGTest has to be created manually by the user from the VDM++ specification.

→ VDTTable only needs a VDM++ specification for input.

*<http://softest.jp/tools/CEGTest/>

- Function definition is only supported definition of VDM++ .
- The number of arguments is limited to one or two.
- The type of arguments is limited to Integer. (int, nat, nat1)
- If-conditions are limited to inequalities and modulo.
- If-conditions are limited to those not connected by “and”, “or”.
- If-conditions are limited to ones whose sides are not variables.

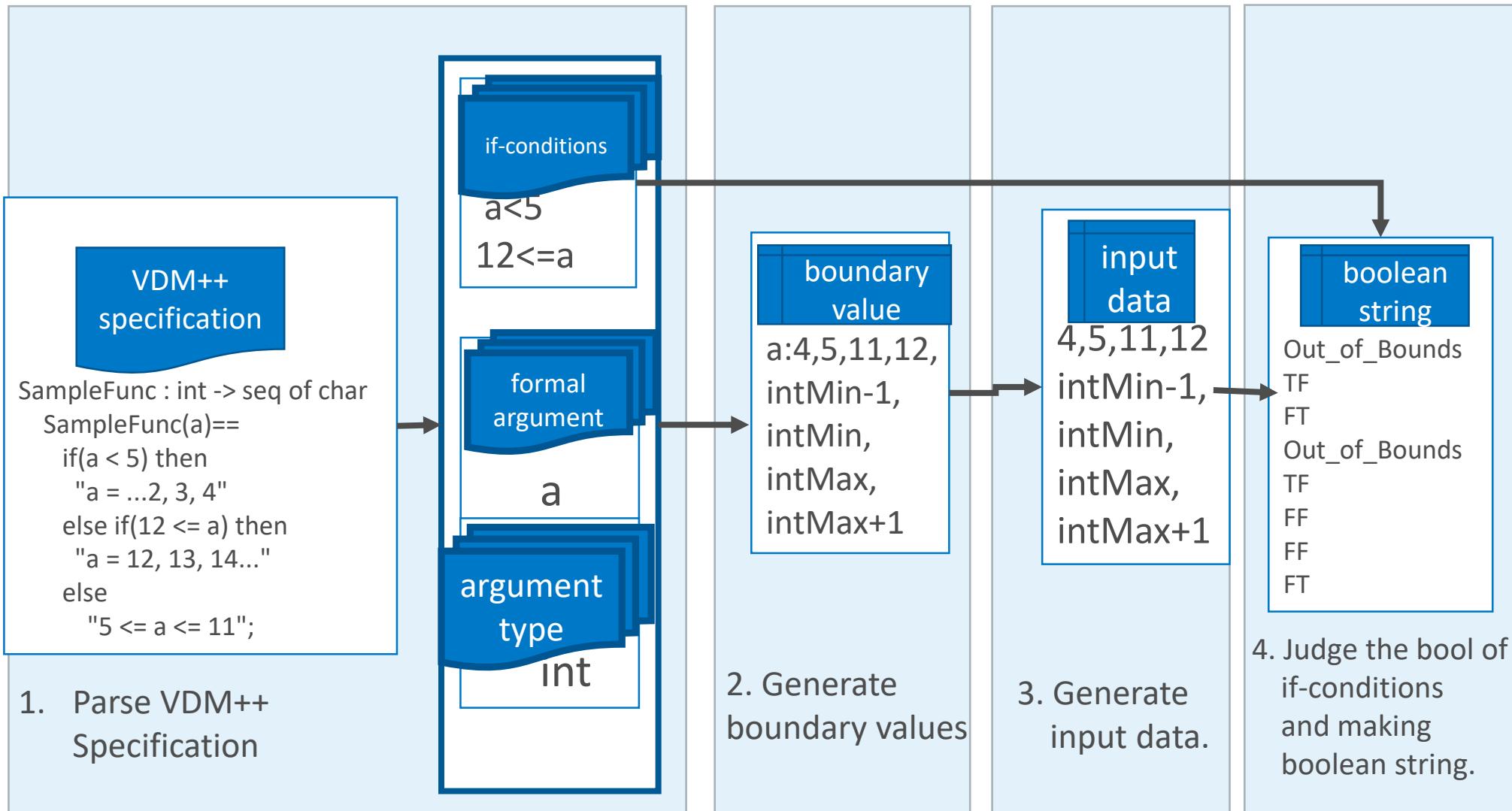
Explain process of making input data.



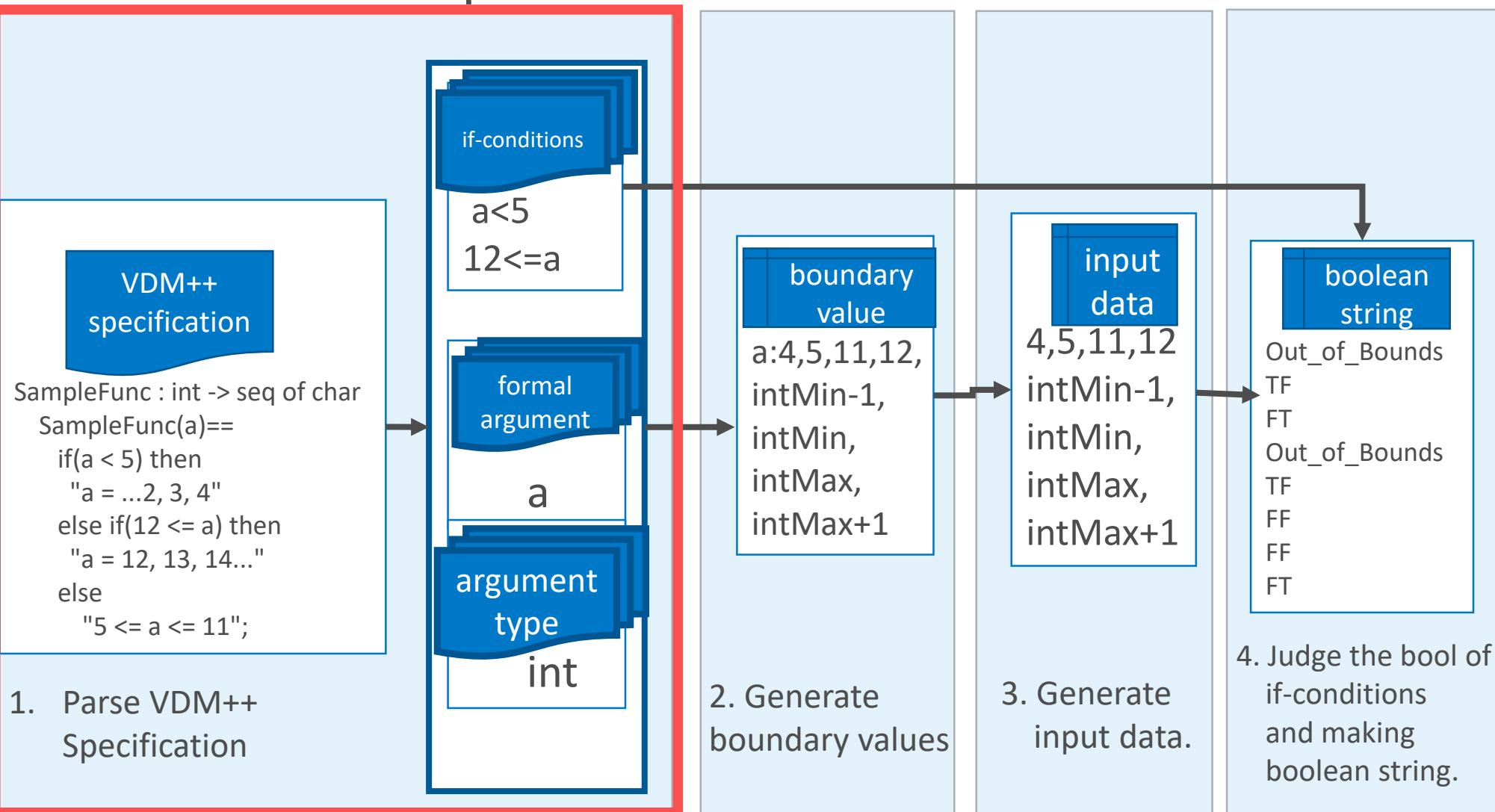
Following four processes are performed for making input data

1. Parse VDM++ specification
2. Generate boundary values
3. Generate input data
4. Generate boolean strings

Overview of the process flow



1. Parse VDM++ specification



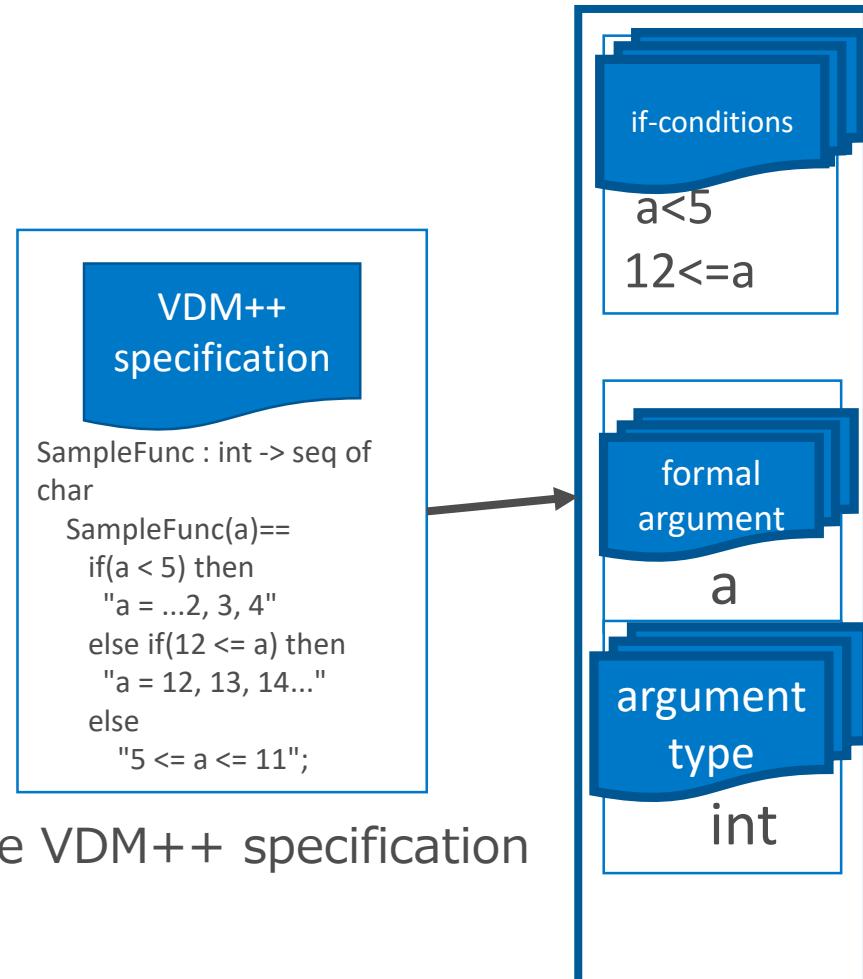
1.Parse VDM++ specification

Parse VDM++ specification
by using VDMJ

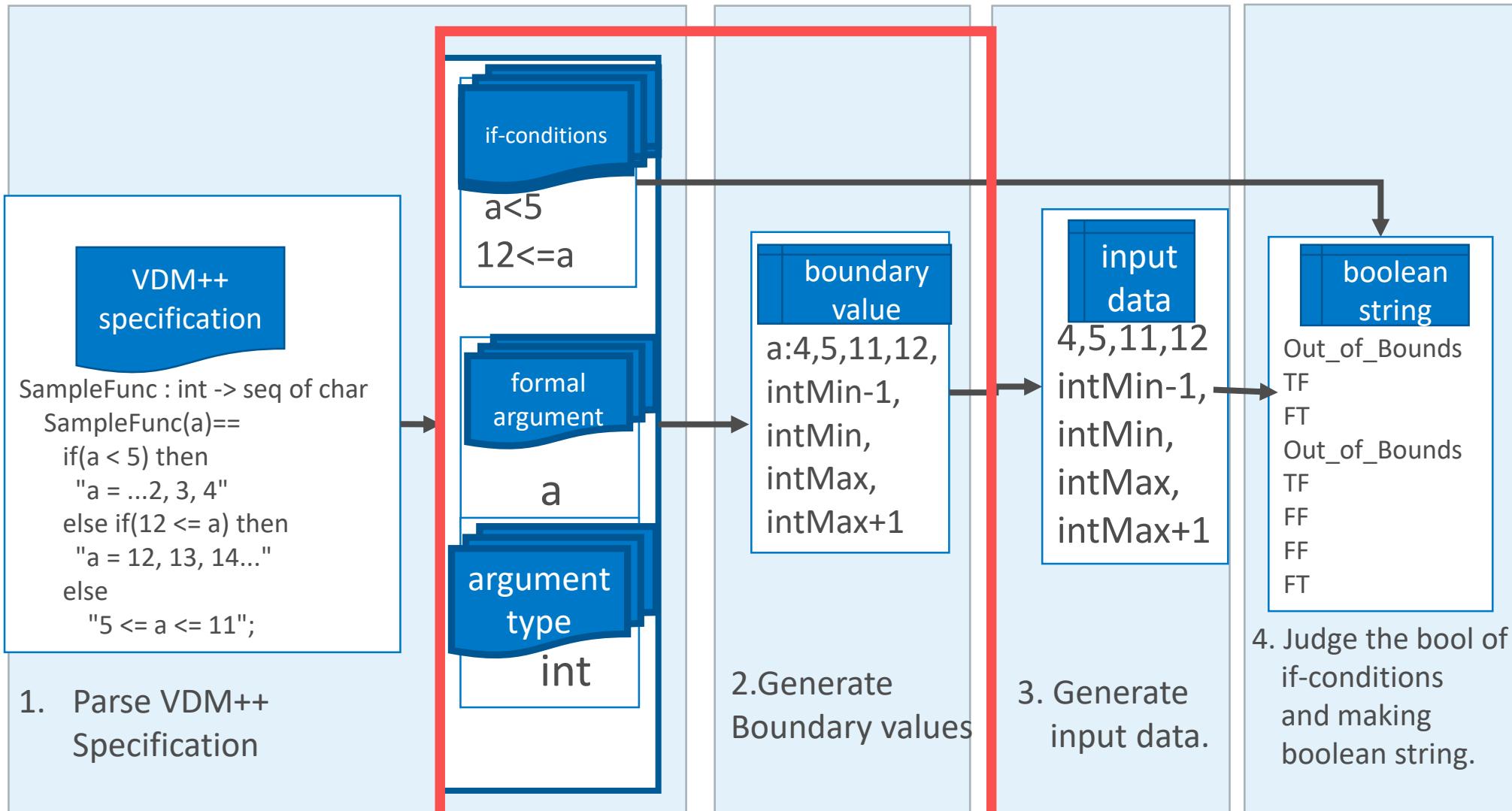


Extract argument types,
formal arguments, and
if-conditions

1.Parse VDM++ specification



2. Generate boundary Values



2. Generate boundary Values

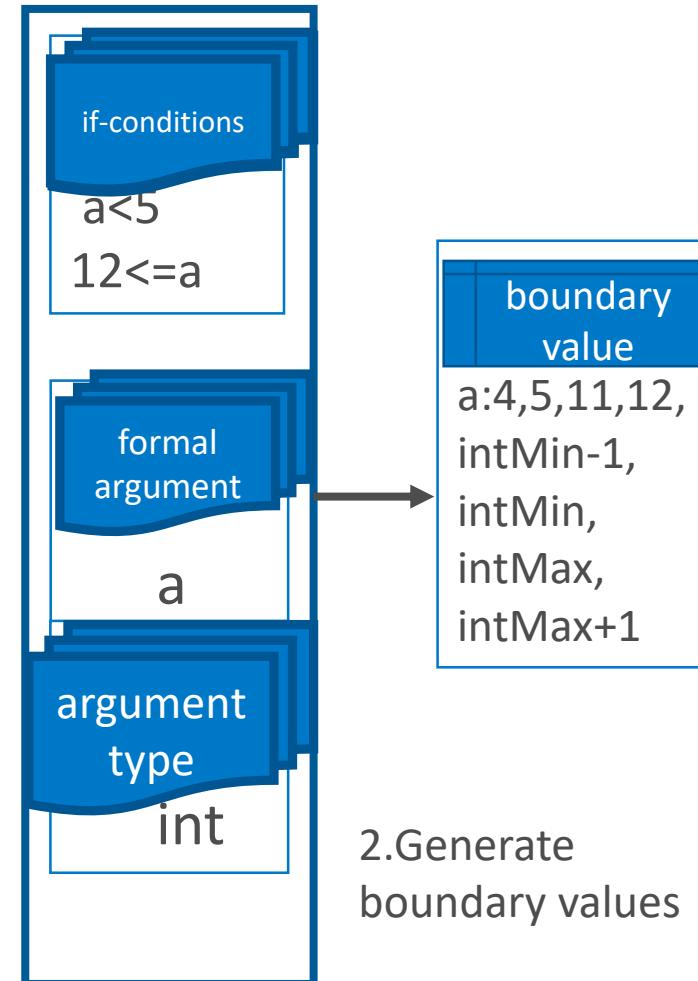
Based on the extracted information,
generate boundary values.

type boundary value

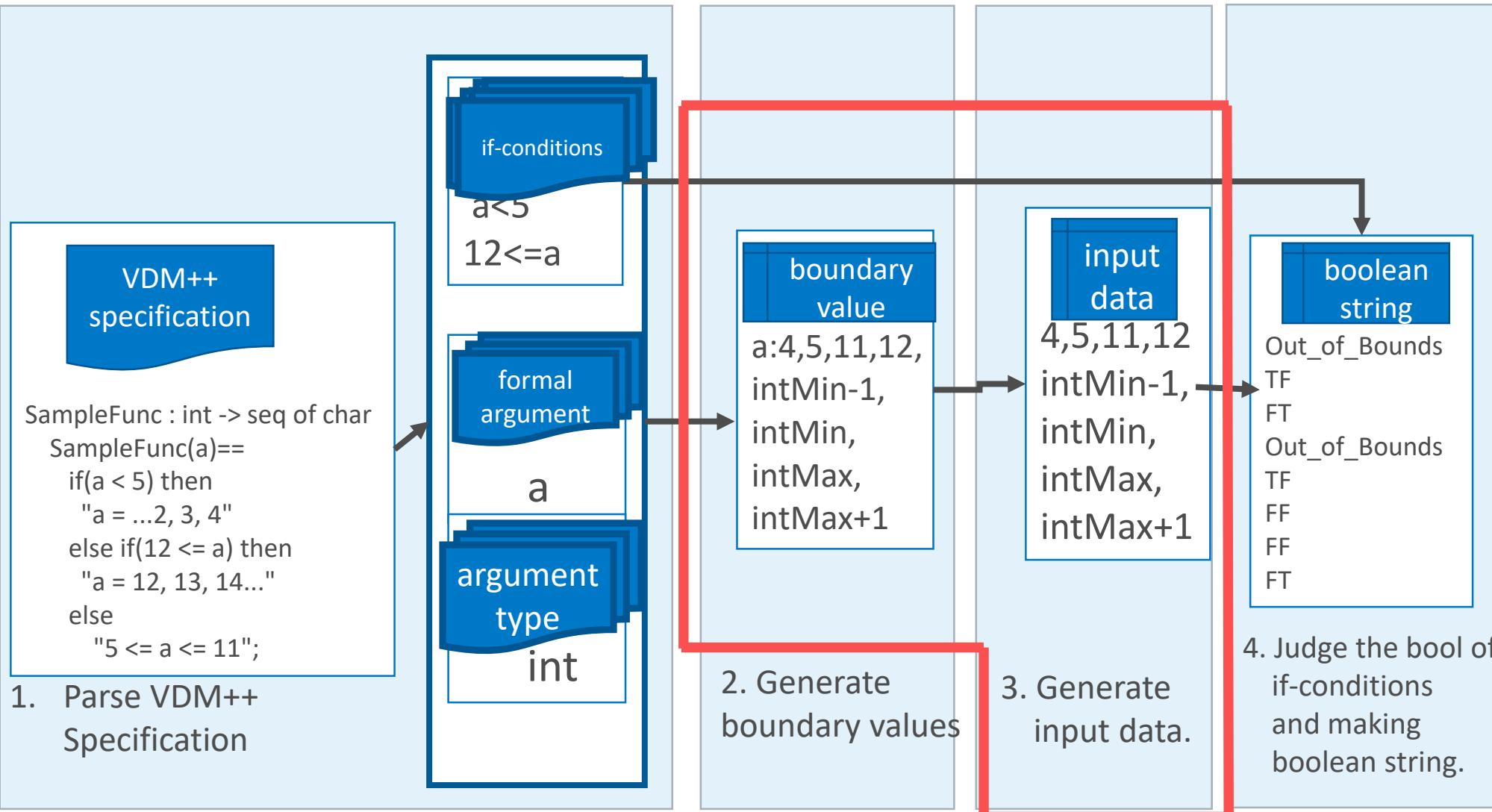
- Generate minimum value, maximum value, minimum value-1, maximum value+1 of argument type

if-condition boundary value

- Generate two boundary values in case of inequality
- three values in case of modulo;
a value that satisfies “=” and two values of ± 1 of it



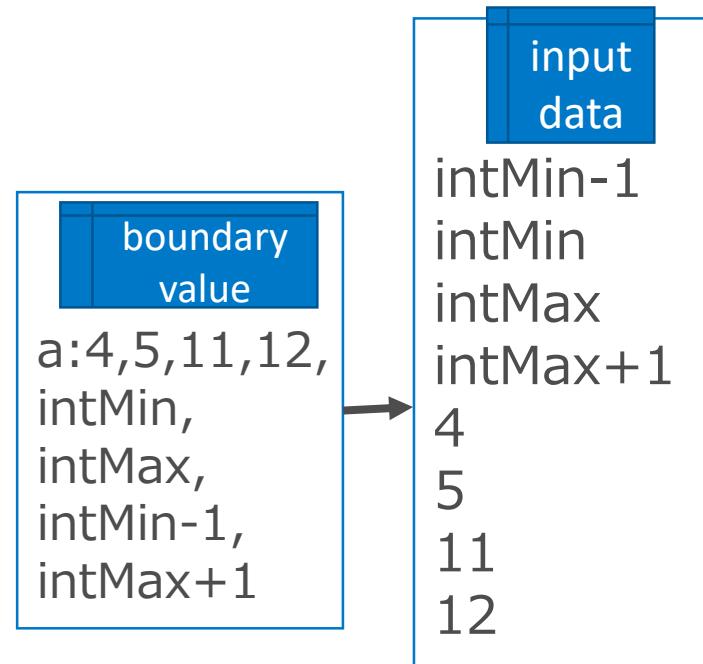
- 3. Generate Input Data



3. Generate Input Data

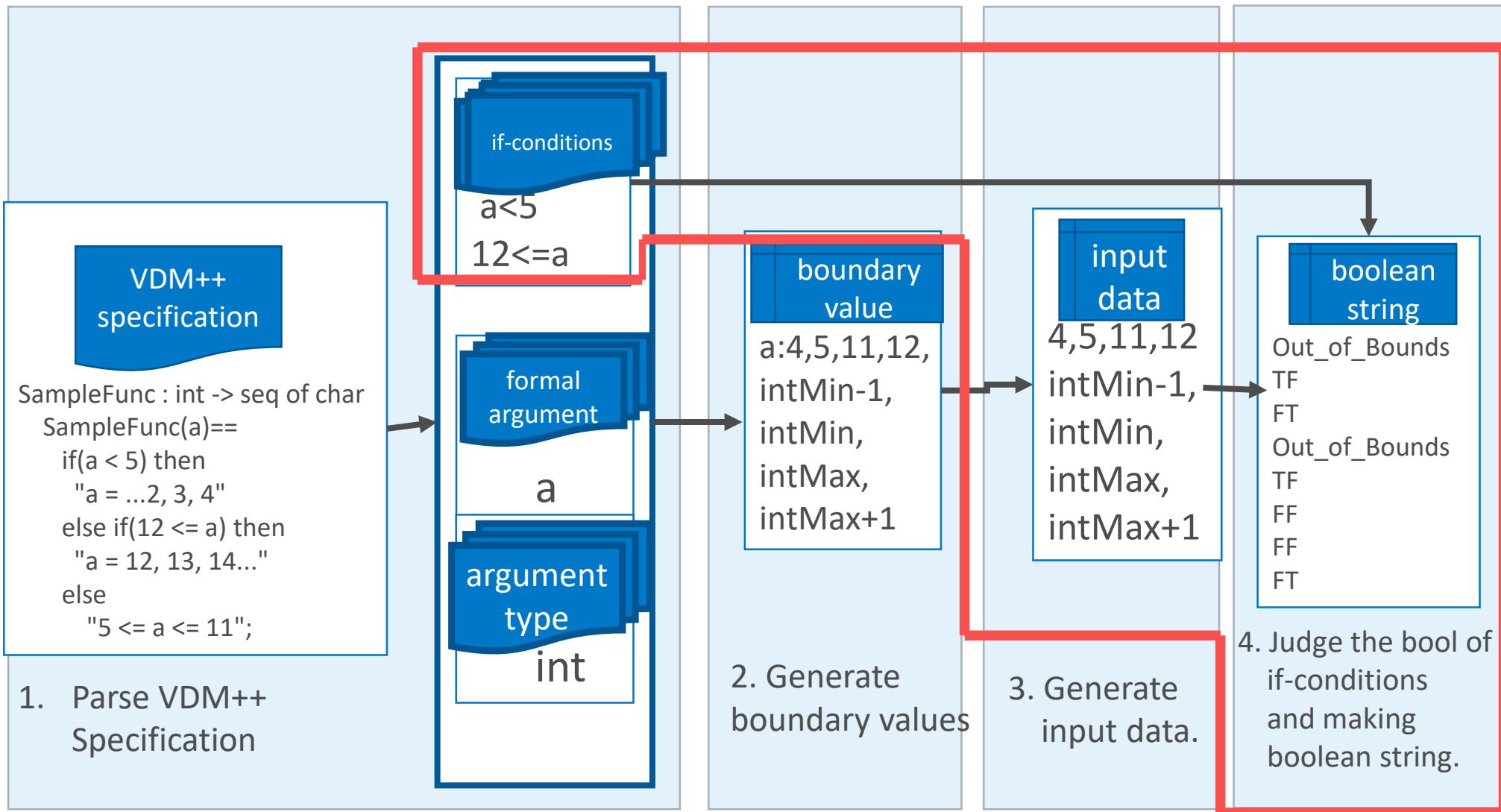
Generate input data from generated boundary value

In the case of two arguments, all combinations of boundary values of each arguments are generated for input data.



3. Generate input data

- 4. Generate Boolean Strings



making input data

BWDM : boundary values

4. Genarate Boolean Strings

Generate Boolean strings from
the generated input data
and if-conditional expressions



used in the expected output data generator

Boolean String

- Assigning input data to the if-conditional expressions to determine a Boolean value and characterizing the result of judgement as T or F

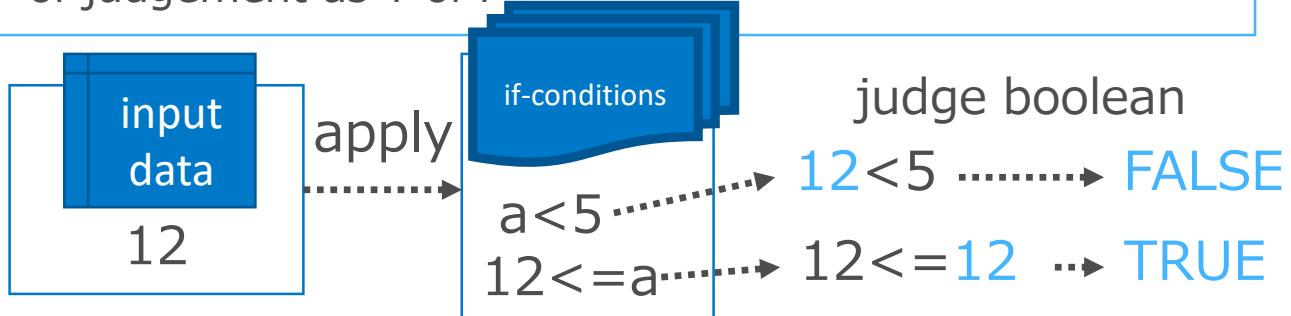
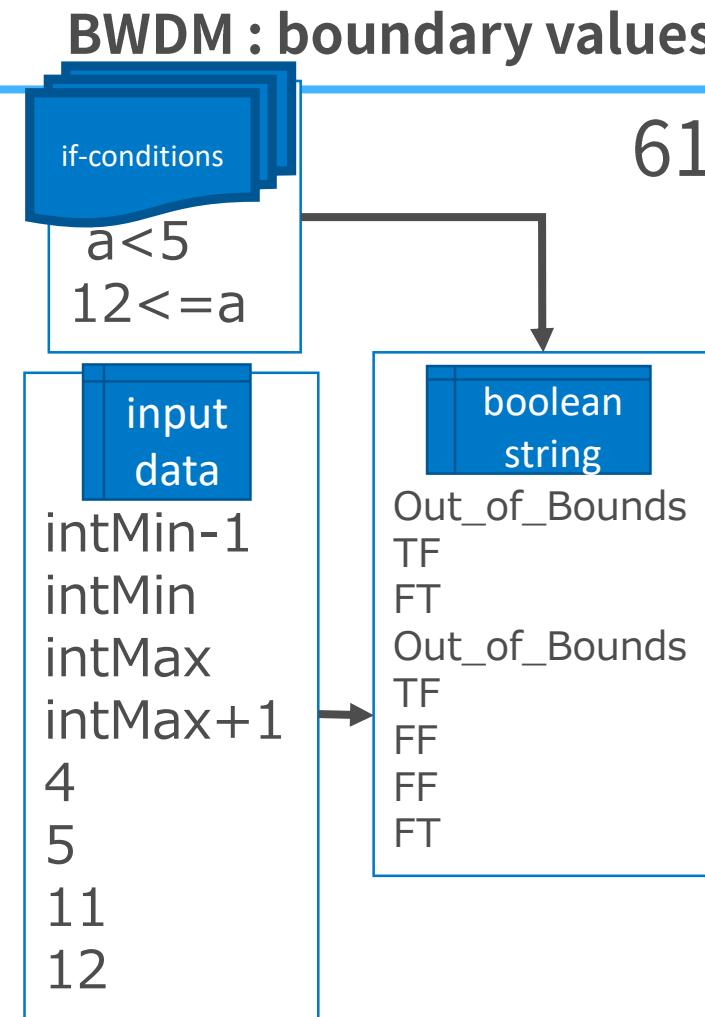
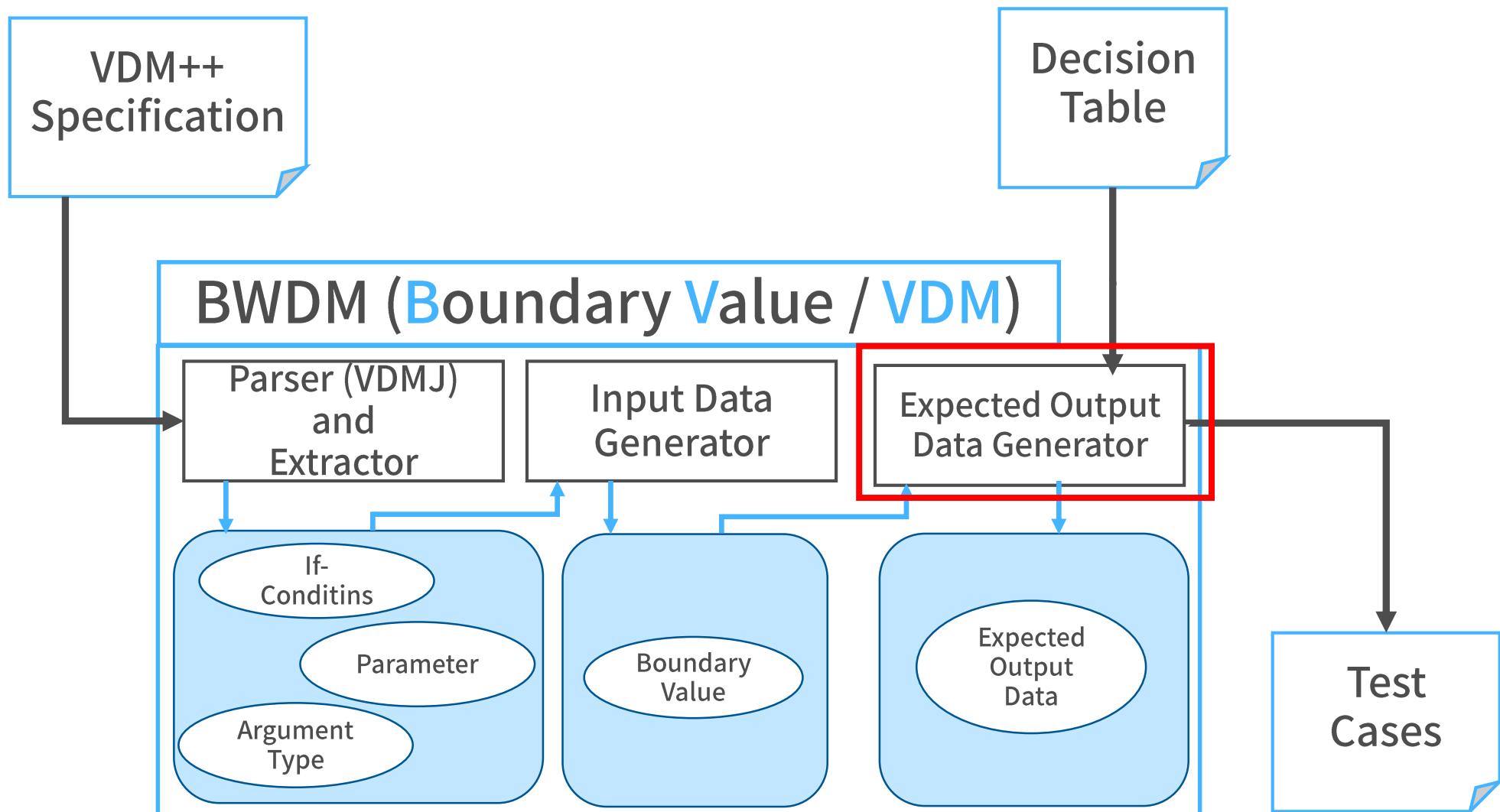


figure: Example of creating a Boolean string “FT” from input data “1, 2” and if-conditional expressions “ $a < 5$, $12 \leq a$ ”



4. Judge the bool of
if-conditions
and making
boolean string.

Explain process of making expected output data.



Following two steps are performed
to make expected output data.

1. Load decision table and generate corresponding table of Boolean string and action
2. Generate expected output data and test cases

making expected output data

BWDM : boundary values

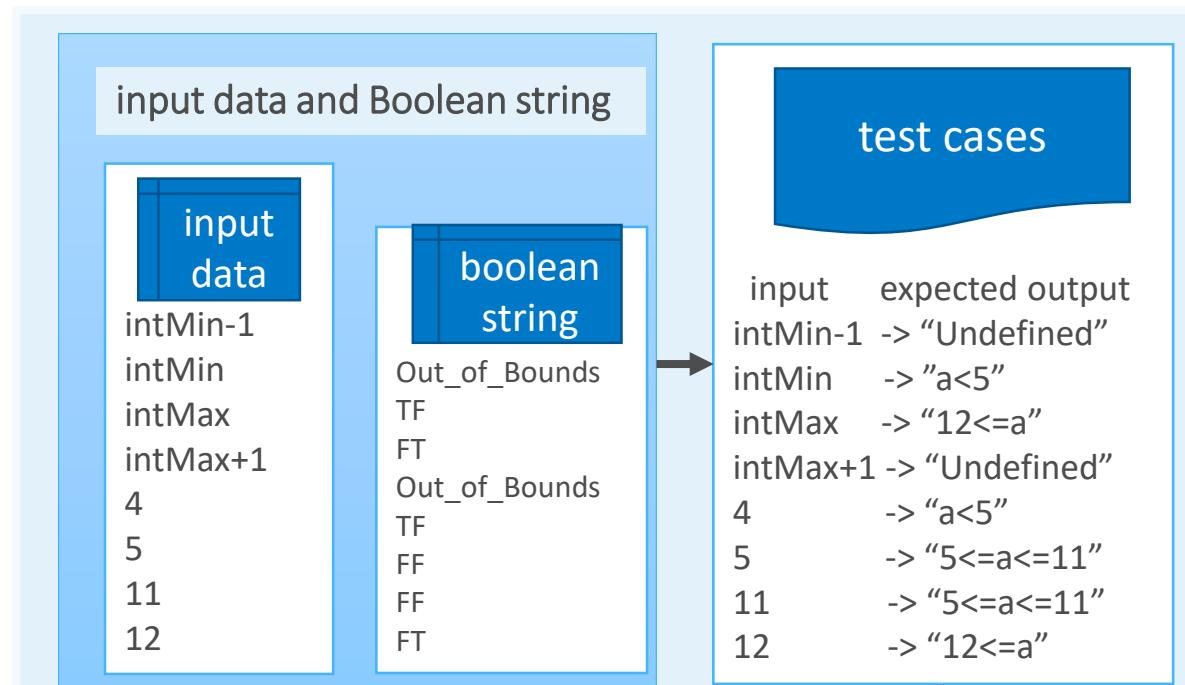
• Overview of the Process Flow

59

Decision Table		#1	#2	#3	#4
Condition	a < 5	T	T	F	F
Condition	12 <= a	T	F	T	F
Action	"a<5"	T	T	F	F
Action	"12 <= a"	F	F	T	F
Action	"5<=a<=11"	F	F	F	T

corresponding table of boolean strings and actions		
boolean string	action	
TT	"a<5"	
TF	"a<5"	
FT	"12<=a"	
FF	"5<=a<=11"	

1. Load decision table and generating table of Boolean string and action.



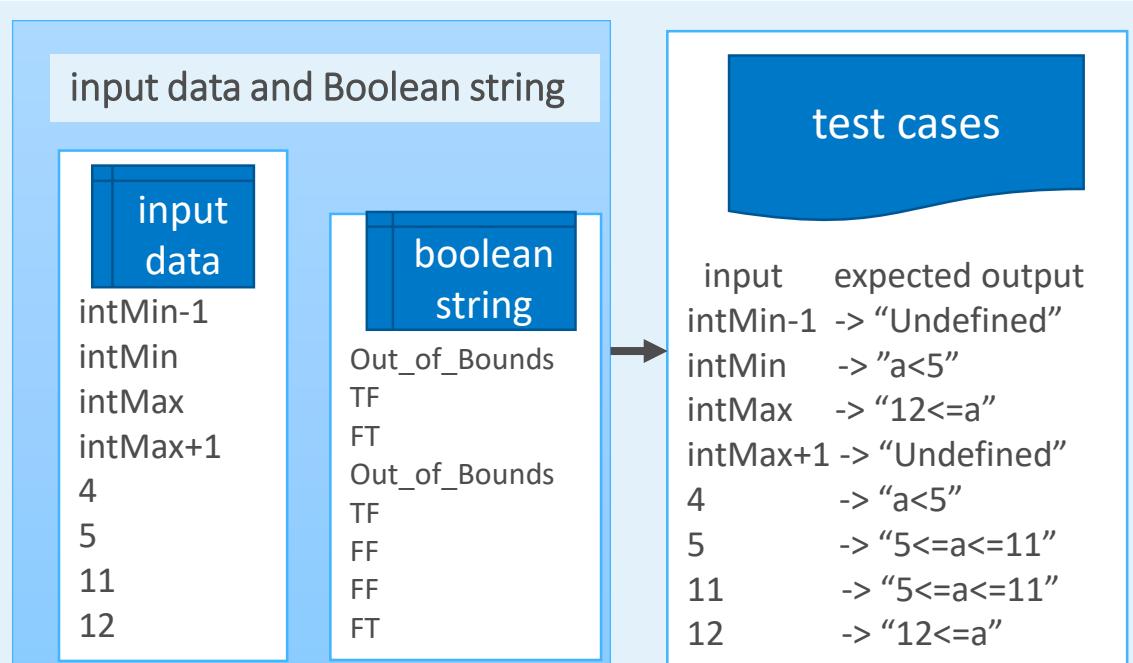
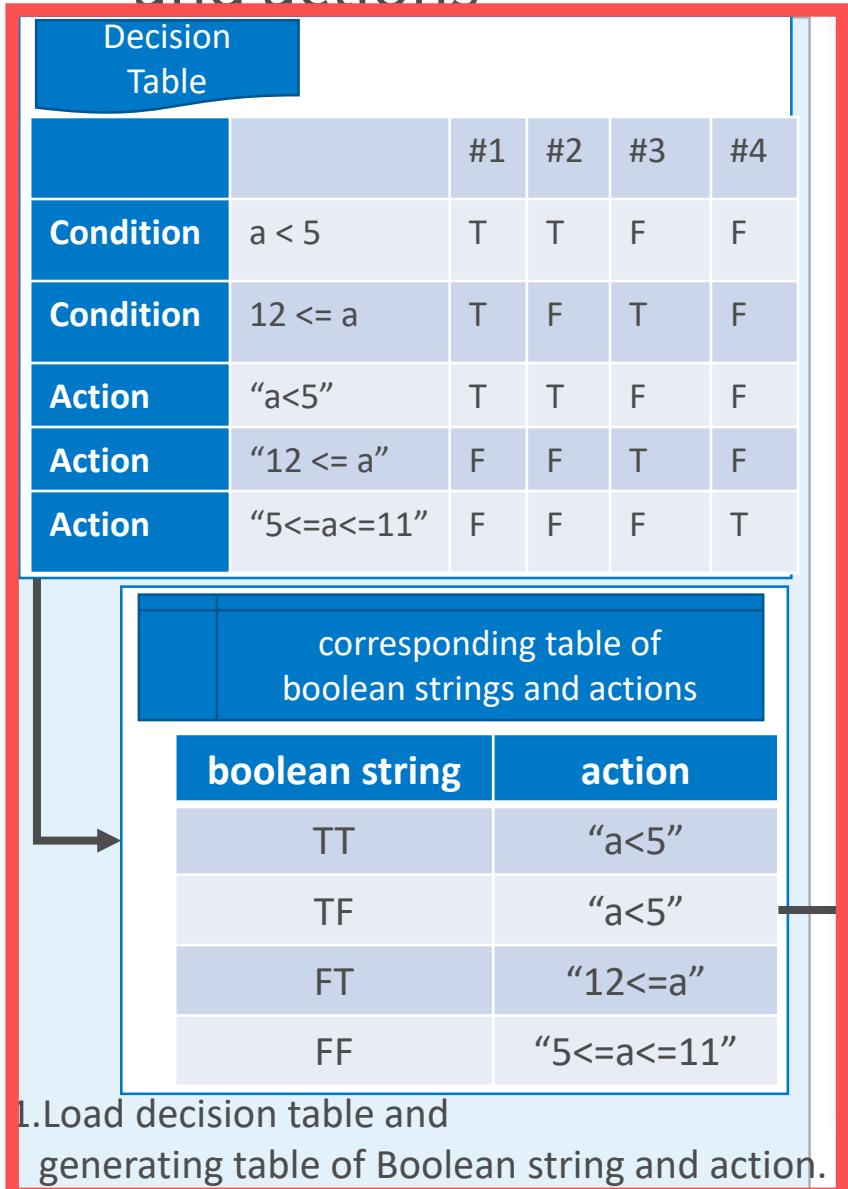
2. Generate expected output data from input data, boolean string, and corresponding table of boolean string and action. And generate test cases.

making expected output data

BWDM : boundary values

- 1. Load decision table and generate table of Boolean strings and actions

65



2. Generate expected output data from input data, boolean string, and corresponding table of boolean string and action. And generate test cases.

- 1.Load decision table and generate table of Boolean strings and actions

66

Load the decision table that generated by VDTable.



Generate correspondence table of Boolean strings and actions.

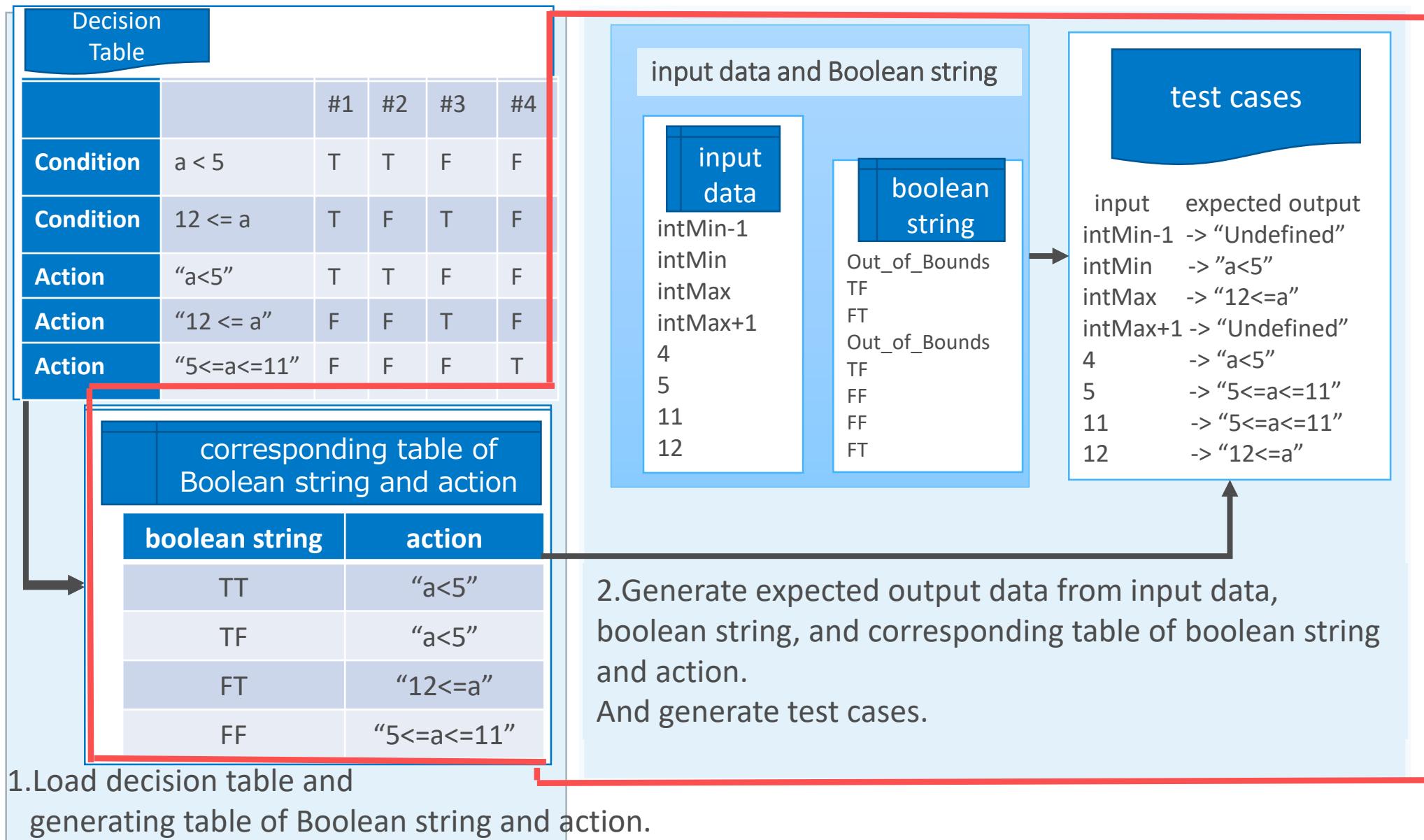
Decision Table		#1	#2	#3	#4
Condition	a < 5	T	T	F	F
Condition	12 <= a	T	F	T	F
Action	"a<5"	T	T	F	F
Action	"12 <= a"	F	F	T	F
Action	"5<=a<=11"	F	F	F	T

corresponding table of boolean strings and actions

boolean string	action
TT	"a<5"
TF	"a<5"
FT	"12<=a"
FF	"5<=a<=11"

1.Load decision table and generating table of Boolean string and action.

2. Generate expected output data and test cases



2. Generate Expected Output Data and Test Cases

Generate expected output data from input data, boolean strings, and corresponding table of boolean string and action.



Finally, BWDM outputs test cases that consist input data and expected output data.

