

## skfda.preprocessing.registration.warping\_mean

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**skfda.preprocessing.registration.warping\_mean**(*warping*, \*, *iter*=20, *tol*=1e-05, *step\_size*=1.0, *eval\_points*=None, *return\_shooting*=False) [\[source\]](#)

Compute the karcher mean of a set of warpings.

Let  $\gamma_i, i = 1 \dots n$  be a set of warping functions  $\gamma_i : [a, b] \rightarrow [a, b]$  in  $\Gamma$ , i.e., monotone increasing and with the restriction  $\gamma_i(a) = a$   $\gamma_i(b) = b$ .

The karcher mean  $\bar{\gamma}$  is defined as the warping that minimises locally the sum of Fisher-Rao squared distances. [\[SK16-8-3-2\]](#).

$$\bar{\gamma} = \operatorname{argmin}_{\gamma \in \Gamma} \sum_{i=1}^n d_{FR}^2(\gamma, \gamma_i)$$

The computation is performed using the structure of Hilbert Sphere obtained after a transformation of the warpings, see [\[S11-3-3\]](#).

- Parameters:**
- **warping** (`FDataGrid`) – Set of warpings.
  - **iter** (`int`) – Maximun number of iterations. Defaults to 20.
  - **tol** (`float`) – Convergence criterion, if the norm of the mean of the shooting vectors,  $|\bar{v}| < tol$ , the algorithm will stop. Defaults to 1e-5.
  - **step\_size** (`float`) – Step size  $\epsilon$  used to update the mean. Default to 1.
  - **eval\_points** (`array_like`) – Discretisation points of the warpings.
  - **shooting** (`boolean`) – If true it is returned a tuple with the mean and the shooting vectors, otherwise only the mean is returned.

**Returns:** (`FDataGrid`) Fdatagrid with the mean of the warpings. If shooting is True the shooting vectors will be returned in a tuple with the mean.

### References

[\[SK16-8-3-2\]](#) Srivastava, Anuj & Klassen, Eric P. (2016). Functional and shape data analysis. In *Template: Center of the Mean Orbit* (pp. 274-277). Springer.

[\[S11-3-3\]](#) Srivastava, Anuj et. al. Registration of Functional Data Using Fisher-Rao Metric (2011). In *Center of an Orbit* (pp. 9-10). arXiv:1103.3817v2.