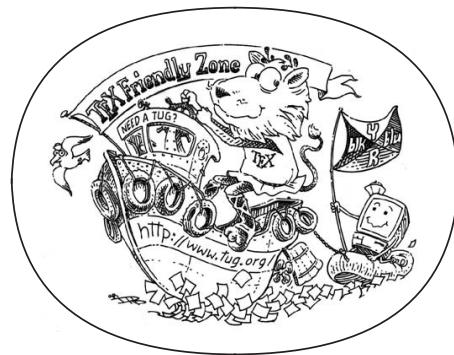


A CLASSIC THESIS STYLE

ANDRÉ MIEDE



An Homage to The Elements of Typographic Style

September 2015 – version 4.2

André Miede: *A Classic Thesis Style*, An Homage to The Elements of
Typographic Style, © September 2015

Ohana means family.
Family means nobody gets left behind, or forgotten.
— Lilo & Stitch

Dedicated to the loving memory of Rudolf Miede.

1939 – 2005

ABSTRACT

Short summary of the contents... a great guide by Kent Beck how to write good abstracts can be found here:

<https://plg.uwaterloo.ca/~migod/research/beck00PSLA.html>

PUBLICATIONS

Some ideas and figures have appeared previously in the following publications:

Put your publications from the thesis here. The packages `multibib` or `bibtopic` etc. can be used to handle multiple different bibliographies in your document.

*Either way, we're not alone
I'll find a new place to be from
A haunted house with a picket fence
To float around and ghost my friends
No, I'm not afraid to disappear
The billboard said, "The end is near"
I turned around, there was nothing there
Yeah, I guess the end is here*

ACKNOWLEDGEMENTS

Put your acknowledgements here.

Many thanks to everybody who already sent me a postcard!

Regarding the typography and other help, many thanks go to Marco Kuhlmann, Philipp Lehman, Lothar Schlesier, Jim Young, Lorenzo Pantieri and Enrico Gregorio¹, Jörg Sommer, Joachim Köstler, Daniel Gottschlag, Denis Aydin, Paride Legovini, Steffen Prochnow, Nicolas Repp, Hinrich Harms, Roland Winkler, and the whole L^AT_EX-community for support, ideas and some great software.

Regarding LyX: The LyX port was initially done by Nicholas Mariette in March 2009 and continued by Ivo Pletikosić in 2011. Thank you very much for your work and the contributions to the original style.

¹ Members of GuIT (Gruppo Italiano Utilizzatori di T_EX e L^AT_EX)

CONTENTS

I TRANSFER LEARNING IN SUPERVISED LEARNING	1
1 TRANSFER LEARNING FROM THE NATURAL TO THE NON-NATURAL DOMAIN	3
1.1 Introduction and Related Work	3
1.2 Methods	5
1.2.1 Transfer Learning	5
1.2.2 Datasets and Classification Challenges	6
1.2.3 Convolutional Networks and Classification Approaches	8
1.3 Results	9
1.3.1 From Natural to Art Images	10
1.3.2 Discussion	14
1.3.3 From One Art Collection to Another	15
1.3.4 Selective Attention	16
1.4 Conclusion	17
2 TRANSFER LEARNING WITH NATURAL LOTTERY WINNERS	19
2.1 Introduction	19
2.2 Datasets	22
2.3 Experimental Setup	23
2.4 Results	25
2.4.1 On the Importance of Finding Winning Initializations	26
2.4.2 On the Generalization Properties of Lottery Winners	27
2.4.3 Additional Studies	29
2.5 Related Work	32
2.6 Conclusion	33
II TRANSFER LEARNING IN REINFORCEMENT LEARNING	35
3 THE DEEP QUALITY-VALUE LEARNING FAMILY OF ALGORITHMS	37
3.1 Introduction	37
3.2 Preliminaries	38
3.3 Related Work	39
3.4 A Novel Family of Deep Reinforcement Learning Algorithms	41
3.4.1 DQV-Learning	41
3.4.2 DQV-Learning with Multilayer Perceptrons	43
3.4.3 DQV-Max Learning	43
3.5 Results	45
3.5.1 Global Evaluation	45
3.5.2 Convergence Time	46

3.5.3	Quality of the Learned Value Functions	47
3.6	Additional Studies	50
3.7	Discussion and Conclusion	53
III	APPENDIX	57
	BIBLIOGRAPHY	59

LIST OF FIGURES

Figure 1 A visualization of the images that are used for our experiments. It is possible to see how the samples range from images representing plates made of porcelain to violins, and from Japanese artworks to a more simple picture of a key.

Figure 2 Comparison between the fine tuning approach (θ^i) versus the off the shelf one (θ^-) when classifying the material of the heritage objects of the Rijksmuseum dataset. We can observe that for three out of four neural architectures the first approach leads to significant improvements when compared to the latter one. Furthermore, we can also observe that training a randomly initialized model from scratch (solid orange line) leads to worse results than fine-tuning a network that comes as pre-trained on the ImageNet dataset.

Figure 3 A similar analysis as the one which has been reported in Figure 2 but for the second and third classification challenges (left and right figures respectively). The results show again the significant benefits that fine tuning (reported by the dashed line plots) has when compared to the off the shelf approach (reported by the dash-dotted lines) and how this latter strategy miserably under-performs when it comes to artist classification. Furthermore we again see the benefits that using a pre-trained DCNN has over training the architecture from scratch (solid orange line).

Figure 4 Add caption

Figure 5

A visual representation of the LTH as introduced by Frankle and Carbin [20]. Let us consider a simplified version of a two hidden layer feedforward neural network as is depicted in the first image on the left. The LTH states that within this neural network there exist multiple smaller networks (represented in green), which can perform just as well as their larger counterpart. Training these sparse models from scratch successfully is only possible as long as their weights are initialized with the same values that were also used when the larger (black) model was initialized. Furthermore, the structure of these sparse models appears to be crucial as well, since it is not possible to randomly extract any subset of weights from an unpruned model and successfully train the resulting sparse network (represented in red in the last figure) from scratch. We visually represent the performance of models that are the winners of the LTH in the two plots reported in Figure 6. . . . [20](#)

- Figure 9 An overview of the results showing that sparse models that are the winners of the LTH (represented by the coloured lines) significantly outperform unpruned networks which get randomly initialized and trained from scratch (dashed black line). This happens to be the case on all tested datasets, no matter whether a winning initialization comes from a natural image source or not. It is however worth mentioning that, especially on the biomedical datasets, natural image tickets get outperformed by sparse networks that are the winners of the LTH on a biomedical dataset. On the other hand this is not the case when it comes to the classification of arts where natural image tickets outperform the ones which are found within artistic collections.

Figure 10 Our results showing the advantages of transferring lottery winners over pruned models that are fully fine-tuned on natural datasets (CIFAR-10 / 100). We can observe that their performance is overall inferior to the one of lottery tickets and that these models are significantly less robust to pruning. We believe that the reason behind their poor performance revolves around the fact that, once completely trained on a specific source task, and after having gone through the pruning stage, these models lose the necessary flexibility that is required for them to adapt to a new task.

Figure 11 Our results showing the benefits of transferring lottery winners that have been identified on a related source task. We can observe that on the Mouse-LBA dataset, winning tickets that were obtained on the Human-LBA dataset are the ones that are the most robust ones to pruning, while on the Artist-Classification-2 dataset we can observe that lottery winners that have been obtained on the Artist-Classification-1 dataset are both more robust to pruning, while they also yield overall better performance. . .

Figure 12	Our study showing that the robustness to large pruning rates of lottery winners does not depend from the size of the training dataset. We can observe that even when lottery tickets after are trained on only 25% of the dataset their performance remains stable with respect to the fraction of pruned weights. These results suggest that the less stable performance of Bone-Marrow lottery tickets observed in Fig. 9 does not depend from the small training set.	32
Figure 13	Our preliminary results that show the benefits in terms of convergence time that can come from jointly approximating the V function alongside the Q function. We can observe that the DQV-Learning algorithm yields faster convergence when compared to popular algorithms which only approximate the Q function: DQN and DDQN.	43
Figure 14	Learning curves obtained during training on three different Atari games by DQV and DQV-Max, and DQN and DDQN. We can observe that on these games both DQV and DQV-Max converge significantly faster than DQN and DDQN and that they obtain higher cumulative rewards on the Enduro environment.	48
Figure 15	Results investigating the extent to which the DQN algorithm suffers from the overestimation bias of the Q function. We can observe that on the Pong environment during the early stages of training, the $Q(s_{t+1}, a)$ estimates quickly grow, while on the Enduro game the values estimated by the Q network keep indefinitely growing, therefore making the algorithm significantly diverge from the real return that is obtained by a trained agent.	50
Figure 16	Results investigating the extent to which the DDQN algorithm suffers from the overestimation bias of the Q function. We can observe that compared to the analysis presented in Fig. 15, the DDQN algorithm prevents its Q-Network from diverging since on both Atari environments the $Q(s_{t+1}, a)$ estimates do not diverge from the observed real return of a trained agent. Results that replicate the findings reported by Van Hasselt et al. [78].	50

- Figure 17 Results investigating the extent to which the DQV algorithm suffers from the overestimation bias of the Q function. We can observe that the performance of the algorithm is similar to the one observed in Fig. 16 for the DDQN algorithm. On both environments the estimated cumulative reward does not diverge from the real return that is obtained by the end of training, therefore suggesting that DQV-Learning does not suffer from the overestimation bias of the Q function. It is also worth noting the difference between the real return obtained by the DQN and the DDQN algorithms on the Enduro environment, and the one obtained by DQV. As can be seen by the black line, the real return obtained by a DQV agent is higher than DQN and DDQN's one, a result which shows that DQV converges to a better policy than DQN and DDQN.

Figure 18 Results investigating the extent to which the DQV-Max algorithm suffers from the overestimation bias of the Q function. We can observe that on the Pong environment the value estimates of the algorithm are comparable to the ones of DDQN and DQV, therefore showing the DQV-Max also diverges significantly less than DQN. On the Enduro environment we can observe that the algorithm does diverge, although, differently from what is reported in Fig. 15, the $Q(s_{t+1}, a)$ estimates seem to converge towards an upper bound (≈ 15). Similarly to what is reported in Fig. 17 we can again observe that the real return obtained by a trained agent is higher compared to the one obtain by DQN, DDQN and DQV, therefore confirming the results presented in Table 7 which see the DQV-Max algorithm as the best performing algorithm on the Enduro game.

Figure 19 Our results which aim to approximate the V and the Q function with a unique, shared parameterized network, an approach that is heavily inspired by multi-task learning studies that can be found in supervised learning [10, 49, 91]. We can see that this extension of DQV, named Hard-DQV, significantly underperforms the original DQV-Learning algorithm.

Figure 20

Our extensions of DQV that aim to reduce the amount of trainable parameters of the algorithm by following an approach similar to the one presented by Wang et al. [80] when “Dueling Networks” for DRL have been introduced. We can observe that among all the three Dueling-DQV extensions, only the Dueling-DQV-3rd one yielded good performance, but as highlighted by the results obtained on the Enduro environment, its performance is still inferior when compared to the one of the original DQV algorithm.

54

Figure 21

Learning curves obtained when reducing the capacity of the convolutional networks that approximate the V and the Q functions. We can observe that albeit each value function is approximated with its own parametrized network, the tiny-dqv extension still yields worse performance. These results highlight that it is not sufficient to simply have two separate neural networks for DQV to perform well, but that a crucial role in DQV's performance is played by the capacity of the networks that are used as well. 55

LIST OF TABLES

Table 1	An overview of the two datasets that are used in our experiments. Each color of the table corresponds to a different classification challenge, starting from challenge 1 which is represented in yellow, challenge 2 in blue and finally challenge 3 in red. Furthermore we represent with N_t the amount of samples constituting the datasets and with Q_t the number of labels. Lastly, we also report if there are common labels between the two heritage collections.	7
Table 2	An overview of the results obtained by the different models on the testing set when classifying the heritage objects of the Rijksmuseum. The overall best performing architecture is reported in a green cell, while the second best performing one is reported in a yellow one. The additional columns “Params” and “X” report the amount of parameters the networks have to learn and the size of the feature vector that is used as input for the softmax classifier.	14
Table 3	The results obtained on the classification experiments performed on the Antwerp dataset with models that have been initially pre-trained on ImageNet (θ^i) and the same architectures which have been fine tuned on the Rijksmuseum dataset (θ^r). Our results show that the latter pre-trained networks yield better results both if used as off the shelf feature extractors and if fine tuned.	15
Table 4	A brief overview of the seven different datasets which have been used in this work. As usual throughout this thesis N_t corresponds to the total amount of samples that are present in the dataset, while Q_t represents the number of classes.	23

Table 5	The results comparing the performance that is obtained on the testing-set by the best pruned model winner of the LTH, and an unpruned architecture trained from scratch. The overall best performing model is reported in a green cell, while the second best one in a yellow cell. We can observe that pruned models winners of the LTH perform significantly better than a larger over-parametrized architecture that gets trained from scratch. As can be seen by the results obtained on the Mouse-LBA and Artist-Classification-1 datasets the difference in terms of performance can be particularly large ($\approx 20\%$).
Table 6	Some additional information about the lottery winners which performance is reported in Table 5. For each winning ticket we report the fraction of weights that is pruned from an original ResNet-50 architecture and that therefore characterizes the level of sparsity of the overall best performing lottery ticket. The results in the Scratch-Training column are not reported since these are unpruned models that are trained from scratch.
Table 7	The results obtained by DQV and DQV-Max on a subset of 15 Atari games. We can see that our newly introduced algorithms have a comparable, and often even better performance than DQN and DDQN. As highlighted by the green cells the overall best performing algorithm in our set of experiments is DQV-Max while the second-best performing algorithm is DQV (as reported by the yellow cells). Specific attention should be given to the games BankHeist and Enduro where DQV and DQV-Max are the only algorithms which can master the game with a final super-human performance.

LISTINGS

ACRONYMS

DRY Don't Repeat Yourself

API Application Programming Interface

UML Unified Modeling Language

Part I

TRANSFER LEARNING IN SUPERVISED LEARNING

TRANSFER LEARNING FROM THE NATURAL TO THE NON-NATURAL DOMAIN

CONTRIBUTIONS AND OUTLINE

This chapter contributes to the field of (Deep) Transfer Learning (TL) by investigating whether popular neural networks that come as pre-trained on datasets containing natural images can perform equally well once they are used on non-natural datasets. Specifically, we explore whether these models can be used for tackling three different art classification problems. Furthermore, assuming this is the case, we also explore whether it is possible to improve on such performance. The chapter is structured as follows: we start by providing the reader with some background information in Section 1.1. In Section 1.2 we present a brief theoretical reminder of the field of TL, a description of the datasets that we have used and the methodological details about the experiments that we have performed. In Section 3.5 we present and discuss our results. A summary of the main contributions of this work ends the chapter in Section 2.6.

This chapter is based on the publication Sabatelli et al. [60].

1.1 INTRODUCTION AND RELATED WORK

Over the past decade Deep Convolutional Neural Networks (DCNNs) have become one of the most used and successful algorithms in Computer Vision (CV) [15, 40, 74]. Due to their ability to automatically learn representative features by incrementally down sampling the input via a set of non linear transformations, these kind of neural networks have rapidly established themselves as the state of the art algorithm on a large set of CV problems. Within different CV testbeds large attention has been paid to the ImageNet challenge [14], a CV benchmark that aims to test the performance of different image classifiers on a dataset that contains one million natural images distributed over thousand different classes. The availability of such a large dataset, combined with the possibility of training deep neural networks in parallel over several GPUs [34], has lead to the development of a large set of different neural architectures that have continued to outperform each other over the years [12, 28, 30, 62, 70]. A promising research field in which the classification performances of such DCNNs can be exploited is that of *Digital Heritage* [51]. Due to

a growing and rapid process of digitization, museums have started to digitize large parts of their cultural heritage collections, leading to the creation of several digital open datasets [4, 44]. The images constituting these datasets are mostly matched with descriptive metadata which, as presented by Mensink and Van Gemert [44], can be used to define a set of challenging machine learning tasks. However, the number of samples in these datasets is far smaller than those in, for instance, the ImageNet challenge and this can become a serious constraint when trying to successfully train deep networks from scratch.

The lack of available training data is a well known issue in the deep learning community and is one of the main reasons that has led to the development of the research field of Transfer Learning (TL). The main idea of TL consists of training a machine learning algorithm on a new task (e.g. a classification problem) while exploiting knowledge that the algorithm has already learned on a previously related task (a different classification problem). This machine learning paradigm has proved to be extremely successful in deep learning, where it has been shown how popular models that were trained on many large datasets [31, 63], were able to achieve very promising results on classification problems from heterogeneous domains, ranging from medical imaging [71] or gender recognition [86] over plant classification [55] to galaxy detection [3].

In this work we explore whether the TL paradigm can be successfully applied to three different art classification problems. We use four neural architectures that have obtained strong results on the ImageNet challenge in recent years and we investigate their performance when it comes to attributing the *authorship* to different artworks, recognizing the *material* which has been used by the artists in their creations, and identifying the *artistic category* these artworks fall into. We do so by comparing two possible approaches that can be used to tackle the different classification tasks. The first one, known as off the shelf classification [54], simply retrieves the features that were learned by the networks on other datasets and uses them as input for a new classifier. In this scenario the weights of the model do not change during the training phase, and the final, top-layer classifier is the only component of the architecture which is actually trained. This changes in our second explored approach, known as fine tuning, where the weights of the original network are “unfrozen” and the neural architectures are trained together with the final classifier.

Kornblith, Shlens, and Le [33] have shown the benefits that this particular pre-training approach has. In particular, DCNNs which have been trained on the ImageNet challenge typically lead to superior results when compared to the same architectures trained from scratch. However, this is not necessarily beneficial and in some cases networks that are randomly initialized are able to achieve the same performance as ImageNet pre-trained models. However, none of the

results presented in [33] report experiments on datasets containing heritage objects, it is thus still an open question how such pre-trained DCNNs would perform in such a classification scenario. In the rest of this chapter we report results that extensively study the performance of such neural networks; at the same time we also assess whether better TL performance can be obtained when using neural networks that, in addition to the ImageNet dataset, have additionally been pre-trained on a large artistic collection.

1.2 METHODS

We now present the methods that underpin our research. We start by giving a brief formal reminder of TL. We then introduce the three classification tasks under scrutiny, together with a brief description of the datasets. Finally, we present the neural architectures that we have used for our experiments.

1.2.1 Transfer Learning

A supervised learning (SL) problem can be identified by three elements: an input space \mathcal{X}_t , an output space \mathcal{Y}_t , and a probability distribution $p_t(x, y)$ defined over $\mathcal{X}_t \times \mathcal{Y}_t$ (where t stands for ‘target’, as this is the main problem we would like to solve). The goal of SL is then to build a function $f : \mathcal{X}_t \rightarrow \mathcal{Y}_t$ that minimizes the expectation over $p_t(x, y)$ of a given loss function ℓ assessing the predictions made by f :

$$E_{(x,y) \sim p_t(x,y)} \{\ell(y, f(x))\}, \quad (1)$$

when the only information available to build this function is a learning sample of input-output pairs $LS_t = \{(x_i, y_i) | i = 1, \dots, N_t\}$ drawn independently from $p_t(x, y)$. In the general transfer learning setting, one assumes that an additional dataset LS_s , called the source data, is available that corresponds to a different, but related, SL problem. More formally, the source SL problem is assumed to be defined through a triplet $(\mathcal{X}_s, \mathcal{Y}_s, p_s(x, y))$, where at least either $\mathcal{X}_s \neq \mathcal{X}_t$, $\mathcal{Y}_s \neq \mathcal{Y}_t$, or $p_s \neq p_t$. The goal of TL is then to exploit the source data LS_s together with the target data LS_t to potentially find a better model f in terms of the expected loss (1) than when only LS_t is used for training this model. Transfer learning is especially useful when there is a lot of source data, whereas target data is more scarce.

Depending on the availability of labels in the target and source data and on how the source and target problems differ, one can distinguish different TL settings [50]. In what follows, we assume that labels are available in both the source and target data and that the input spaces \mathcal{X}_t and \mathcal{X}_s , that both correspond to color images, match. Output spaces and joint distributions will however differ between

the source and target problems, as they will typically correspond to different classification problems (ImageNet object recognition versus art classification tasks). Our problem is thus an instance of *inductive transfer learning* [50]. While several inductive transfer learning algorithms exist, hereafter we focus on model transfer techniques, where information between the source and target problems is exchanged in the form of a neural network that comes as pre-trained on the source data. Although potentially suboptimal, this approach has the advantage of being more computationally efficient, as it does not require to train a model using both the source and the target data.

1.2.2 Datasets and Classification Challenges

For our experiments we use two datasets which come from two different heritage collections. The first one contains the largest number of samples and comes from the Rijksmuseum in Amsterdam¹. On the other hand, our second ‘Antwerp’ dataset is much smaller. This dataset presents a random sample that is available as open data from a larger heritage repository: DAMS (Digital Asset Management System)². This repository can be searched manually via the web-interface or queried via a Linked Open Data API. It aggregates the digital collections of the foremost GLAM institutions (Galleries, Libraries, Archives, Museums) in the city of Antwerp in Belgium. Thus, this dataset presents a varied and representative sample of the sort of heritage data that is nowadays being collected at the level of individual cities across the globe. While it is much smaller, its coverage of cultural production is similar to that of the Rijksmuseum dataset and presents an ideal testing ground for the transfer learning task under scrutiny here.

Both image datasets come with metadata encoded in the Dublin Core metadata standard [82]. We selected three well-understood classification challenges: (1) “material classification” which consists in identifying the material the different heritage objects are made of (e.g paper, gold, porcelain, ...); (2) “type classification” in which the neural networks have to classify in which artistic category the samples fall into (e.g. print, sculpture, drawing, ...), and finally (3) “artist classification”, where the main goal is to appropriately match each sample of the dataset with its creator (from now on we refer to these classification tasks as challenge 1, 2 and 3 respectively). As reported in Table 1 we can see that the Rijksmuseum collection is the dataset with the largest amount of samples per challenge (N_t) and the highest amount of labels to classify (Q_t). Furthermore it is also worth noting that there was no metadata available when it comes to the first classification challenge for the Antwerp dataset (as marked by the \times symbol),

¹ <https://staff.fnwi.uva.nl/t.e.j.mensink/uval2/rijks/>

² <https://dams.antwerpen.be/>



Figure 1: A visualization of the images that are used for our experiments. It is possible to see how the samples range from images representing plates made of porcelain to violins, and from Japanese artworks to a more simple picture of a key.

and that there are some common labels between the two heritage collections when it comes to challenge 2. A visualization reporting some of the images that are present in both datasets is shown in Figure 1.

Table 1: An overview of the two datasets that are used in our experiments. Each color of the table corresponds to a different classification challenge, starting from challenge 1 which is represented in yellow, challenge 2 in blue and finally challenge 3 in red. Furthermore we represent with N_t the amount of samples constituting the datasets and with Q_t the number of labels. Lastly, we also report if there are common labels between the two heritage collections.

Challenge	Dataset	N_t	Q_t	% of overlap
Material	Rijksmuseum	110,668	206	None
	Antwerp	×	×	
Type	Rijksmuseum	112,012	1,054	
	Antwerp	23,797	920	≈ 15%
Artist	Rijksmuseum	82,018	1,196	None
	Antwerp	18,656	903	

We use 80% of the datasets for training while the remaining $2 \times 10\%$ is used for validation and testing respectively. Furthermore, we ensure that only classes which occur at least once in all the splits are used for our experiments. Naturally, in order to keep all comparisons fair between neural architectures and different TL approaches, all experiments have been performed on the exact same data splits which, together with the code used for all our experiments, are publicly released to the CV community ³.

³ <https://github.com/paintception/Deep-Transfer-Learning-for-Art-Classification-Problems>

1.2.3 Convolutional Networks and Classification Approaches

For our experiments we use four pre-trained DCNNs that have all obtained state of the art results on the ImageNet classification challenge. The neural architectures are VGG19 [62], Inception-V3 [70], Xception [12] and ResNet50 [88]. We use the implementations of the networks that are provided by the Keras Deep Learning library [13] together with their appropriate Tensorflow weights [1] that come from the Keras official repository as well. Since all architectures have been built in order to deal with the ImageNet dataset we replace the final classification layer of each network with a new one. This final layer simply consists of a new *softmax* output, with as many neurons as there are classes to classify, which follows a 2D global average pooling operation. We rely on this dimensionality reduction step because we do not add any fully connected layers between the last convolution layer and the *softmax* output. Hence, in this way we are able to obtain a feature vector, X , out of the rectified activation feature maps of the network that can be properly classified. Since all experiments are treated as a multi-class classification problem all networks minimize the *categorical crossentropy* function loss function.

We investigate two possible classification approaches that are based on the previously mentioned pre-trained architectures. The first one, denoted as off the shelf classification, only trains a final *softmax* classifier on X , which is retrieved from the different models after performing one forward pass of the image through the network⁴. This approach is intended to explore whether the features that are learned by the network on the ImageNet dataset are informative enough in order to properly train a machine learning classifier on the previously introduced art classification challenges. If this would be the case, such pre-trained models could be used as appropriate feature extractors without having to rely on expensive GPU computations for training. Naturally, they would only require the training of the final classifier without having to compute any backpropagation operations over the entire network. From now on we will refer to these networks with θ^- .

Our second approach is generally known as fine tuning and differs from the previous one by the fact that together with the final *softmax* output the entire network is trained as well. This means that unlike the off the shelf approach, the entirety of the neural architecture gets “unfrozen” and is optimized during training. The potential benefit of this approach lies in the fact that the models get independently trained on samples coming from the artistic datasets, and therefore their classification predictions will not be restricted to what the networks previously learned on the ImageNet dataset only. Evidently,

⁴ Please note that instead of a *softmax* layer any kind of machine learning classifier can be used instead. We experimented with both Support Vector Machines (SVMs) and Random Forests but since the results did not significantly differ between classifiers we decided to not include them here.

such an approach is computationally more demanding. We refer to these networks as θ^i , where i stands for the source task these models have been trained on, namely the ImageNet dataset. We visually present a simplified representation of the classification approaches considered in this chapter together with how they differ from not pre-trained model in Fig. ??.

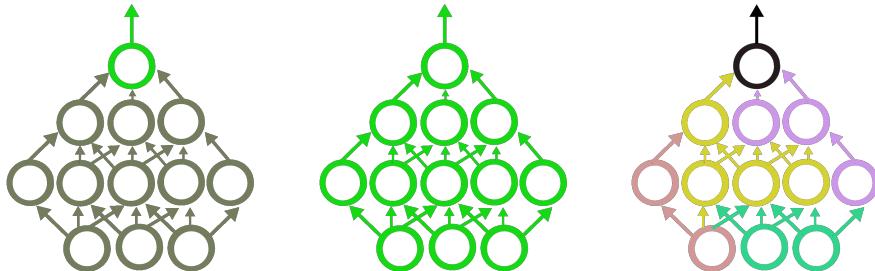


Figure 2: A simplified visual representation of the different training paradigms that are considered in this chapter. The first plot represents a model that comes as pre-trained on a source task but which is not allowed to update most of its weights during training (represented in gray): the only trainable parameters of this network are the ones that parametrize the final layer of the network and that are represented in green. In the second plot we visually represent a model that is parametrized with weights that have been learned on a certain source task, and that when training the model on the target task get “unfrozen”, therefore making the model fully trainable. Lastly we visualize a model that does not come as pre-trained on any source task at all but that is initialized with random weights instead (represented by the various colours).

In order to maximize the performance of all models we follow some of the recommendations presented by Masters and Luschi [42] and train the networks with a relatively small batch size of 32 samples. We do not perform any data augmentation operations besides a standard pixel normalization to the $[0, 1]$ range and a re-scaling operation which resizes the images to the input size that is required by the different models. Regarding the stochastic optimization procedures of the different classifiers, we use two different optimizers, that after preliminary experiments, turned out to be the best performing ones. For the off the shelf approach we use the RMSprop optimizer [73] which has been initialized with its default hyperparameters (learning rate = 0.001, a *momentum* value $\rho = 0.9$ and $\epsilon = 1e - 08$). On the other hand, when we fine tune the DCNNs we use the standard (and less greedy) Stochastic Gradient Descent (SGD) algorithm with the same learning rate, 0.001, and a *Nesterov Momentum* value set to 0.9. Training has been controlled by the *Early Stopping* method [11] which interrupted training as soon as the validation loss did not decrease for

7 epochs in a row. The model which is then used on the testing set is the one which obtained the smallest validation loss while training.

To the best of our knowledge, the results presented in this chapter are the first ones that systematically assess to which extent models pre-trained on the ImageNet dataset can be used as valuable architectures when tackling art classification problems. Furthermore, we also present the first results that investigate if it is also not known whether the fine tuning approach can yield better results than the off the shelf one, and if using such pre-trained models would yield better performance than training the same architectures from scratch as observed by Kornblith, Shlens, and Le [33].

1.3 RESULTS

Our experimental results are divided in two different sections, depending on which kind of dataset has been used. We first report the results that we have obtained when using architectures that were pre-trained on the ImageNet dataset only, and aimed to tackle the three classification problems of the Rijksmuseum dataset that were presented in Section 1.2.2. We report these results in Section 1.3.1 where we explore the benefits of using the ImageNet dataset as the TL source data, and how well such pre-trained models generalize when it comes to the artistic domain. We then present the results from classifying the Antwerp dataset, using models that are both pre-trained on the ImageNet dataset and on the Rijksmuseum collection in Section 1.3.3. We investigate whether these neural architectures, which have already been trained to tackle art classification problems before, perform better than the ones which have been trained on the ImageNet dataset only.

All results show comparisons between the off the shelf classification approach and the fine tuning scenario. In addition to that, in order to establish the potential benefits that TL from ImageNet has over training a model from scratch, we also report the results that have been obtained when training a network with weights that have been initially sampled from a “He-Uniform” distribution [27]. Since we take advantage of the work presented by Bidoia et al. [7] we use the Inception-V3 architecture. We refer to it in all figures as Scratch-V3 and always visualize it with a solid orange line. Figures 2 and 3 report the performance in terms of accuracy that the models have obtained on the validation sets. While the performances that the neural architectures have obtained on the final testing set are reported in Tables 2 and 3.

1.3.1 From Natural to Art Images

The first results that we report have been obtained on the “material” classification challenge. We believe that this can be considered as the easiest classification task within the ones that we have introduced in Section 1.2.2 for two main reasons. First, the number of possible classes the networks have to deal with is more than five times smaller when compared to the other two challenges. Furthermore, we also believe that this classification task is, within the limits, the most similar one when compared to the original ImageNet challenge. Hence, the features that might be useful in order to classify the different natural images on the latter classification testbed might be not too dissimilar from the ones that are needed to properly recognize the material that the different samples of the Rijksmuseum collection are made of. If this would be the case we would expect a very similar performance between the off the shelf classification approach and the fine tuning one. Comparing the learning curves of the two classification strategies in Figure 2, we actually observe that the fine tuning approach leads to significant improvements when compared to the off the shelf one, for three architectures out of the four tested ones. Note however that, in support of our hypothesis, the off the shelf approach can still reach high accuracy values on this problem and is also competitive with the DCNN trained from scratch. This suggests that features extracted from networks pretrained on ImageNet are relevant for material classification.

When comparing the learning curves of the two classification strategies reported in Figure 2, we can observe that the fine tuning approach leads to significant improvements when compared to the off the shelf one, for three architectures out of the four tested ones. Note however that, in support of our hypothesis, the off the shelf approach can still reach high accuracy values on this problem and is also competitive with the network that is trained from scratch. This suggests that features extracted from pretrained ImageNet models are relevant for material classification.

We can also observe that the ResNet50 architecture is the architecture which, when fine tuned, performs overall best when compared to the other three models. This happens despite it being the network that initially performed worse as a simple feature extractor in the off the shelf experiments. As reported in Table 2 we can see that this kind of behavior reflects itself on the separated testing set as well, where it obtained the highest testing set accuracy when fine tuned (92.95%), and the lowest one when the off the shelf approach was used (86.81%). It is worth noting that the performance between the different neural architectures do not strongly differ between each other once they are fine tuned, with all models performing around $\approx 92\%$ on the final testing set. Furthermore, special attention needs to be given to the

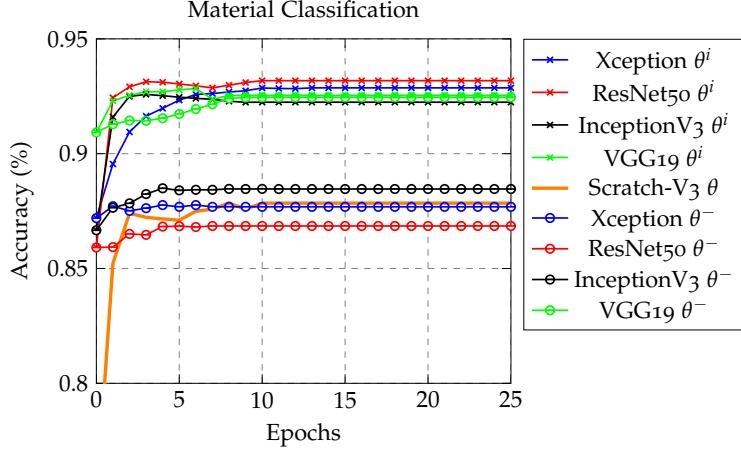


Figure 3: Comparison between the fine tuning approach (θ^i) versus the off the shelf one (θ^-) when classifying the material of the heritage objects of the Rijksmuseum dataset. We can observe that for three out of four neural architectures the first approach leads to significant improvements when compared to the latter one. Furthermore, we can also observe that training a randomly initialized model from scratch (solid orange line) leads to worse results than fine-tuning a network that comes as pre-trained on the ImageNet dataset.

VGG19 architecture, which does not seem to benefit from the fine tuning approach as much as the other architectures do. In fact, its off the shelf performance on the testing set (92.12%) is very similar to its fine tuned one (92.23%). This suggests that this neural architecture is the only one which, in this task, and when pre-trained on ImageNet, can successfully be used as a simple feature extractor without having to rely on complete retraining.

When analyzing the performance of the different neural architectures on the “type” and “artist” classification challenges (respectively the left and right plots reported in Figure 3), we observe that on these problems fine tuning strategy leads to even more significant improvements when compared to what we observed in the previous experiment. The results obtained on the second challenge show again that the ResNet50 architecture is the architecture which leads to the worse results if the off the shelf approach is used (its testing set accuracy is as low as 71.23%) and similarly to what has been observed before, it then becomes the best performing model when fine tuned, with a final accuracy of 91.30%. Differently from what has been observed in the previous experiment, the VGG19 architecture, despite being the network performing best when used as off the shelf feature extractor, this time performs significantly worse than when it is fine tuned, which highlights the benefits of this latter training approach. Similarly to what has been observed before, our results are again not significantly in favor of any fine tuned neural architecture, with all final accuracies being around $\approx 91\%$.

If the classification challenges that we have analyzed so far have highlighted the significant benefits of the fine tuning approach over the off the shelf one, it is also important to note that the latter approach is still able to lead to satisfying results. In fact, a final accuracy of 92.12% has been obtained when using the VGG19 architecture on the first challenge and a classification rate of 77.33% was reached by the same architecture on the second challenge. Despite the latter accuracy being very far in terms of performance from the one obtained when fine tuning the network (90.27%), these results still show that models pre-trained on ImageNet do learn particular features that can also be used for classifying the “material” and the “type” of heritage objects. However, when analyzing the results from the “artist” challenge, we can see that this is partially not the case anymore.

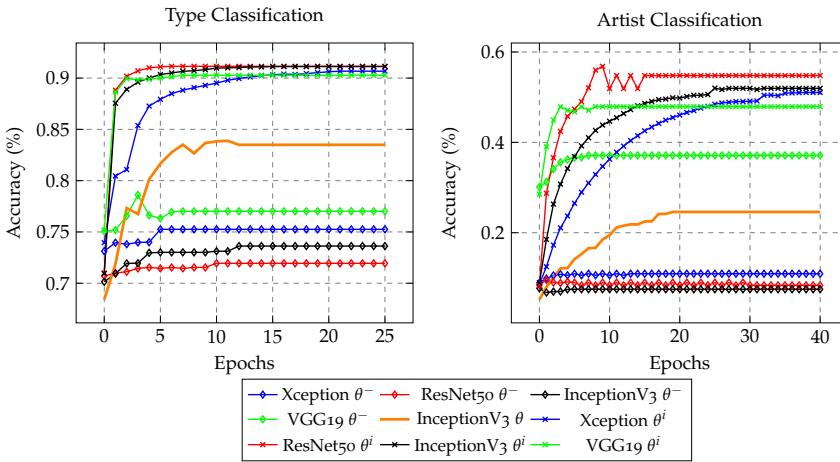


Figure 4: A similar analysis as the one which has been reported in Figure 2 but for the second and third classification challenges (left and right figures respectively). The results show again the significant benefits that fine tuning (reported by the dashed line plots) has when compared to the off the shelf approach (reported by the dash-dotted lines) and how this latter strategy miserably underperforms when it comes to artist classification. Furthermore we again see the benefits that using a pre-trained DCNN has over training the architecture from scratch (solid orange line).

When considering the third classification challenge we can observe that the Xception, ResNet50, and Inception-V3 architectures all perform extremely poorly if not fine tuned, with the latter two models not being able to even reach a 10% classification rate. Better results are obtained when using the VGG19 architecture, which reaches a final accuracy of 38.11%. Most importantly, the performance of each model are again significantly improved when the networks are fine tuned. As already observed in the previous experiments, ResNet50 outperforms the other architectures on the validation set. However, on the test set (see Table 2), the overall best performing network is Inception-V3 (with a final accuracy of 51.73%), which suggests that

ResNet50 suffered from overfitting. It is important to state two major important points about this set of experiments. The first one relates to the final classification accuracy that is obtained by all models, and that at first sight might seem disappointing. While it is true that these classification rates are significantly lower when compared to the ones obtained in the previous two experiments, it is important to highlight how a large set of artists present in the dataset are associated to an extremely limited amount of samples. This reflects a lack of appropriate training data which does not allow the models to learn all the features that are necessary for successfully dealing with this particular classification challenge. In order to do so, we believe that more training data is required. Moreover, it is worth pointing out that despite performing very poorly when used as off the shelf feature extractors, ImageNet pre-trained models do still perform better once they are fine tuned than a model that is trained from scratch. This suggests that these networks do learn potentially representative features when it comes the classification of artists, but in order to properly classify them, the model need to be fine tuned.

Table 2: An overview of the results obtained by the different models on the testing set when classifying the heritage objects of the Rijksmuseum. The overall best performing architecture is reported in a green cell, while the second best performing one is reported in a yellow one. The additional columns “Params” and “X” report the amount of parameters the networks have to learn and the size of the feature vector that is used as input for the softmax classifier.

Challenge	DCNN	off the shelf	fine tuning	Params	X
1	Xception	87.69%	92.13%	21K	2048
1	InceptionV3	88.24%	92.10%	22K	2048
1	ResNet50	86.81%	92.95%	24K	2048
1	VGG19	92.12%	92.23%	20K	512
2	Xception	74.80%	90.67%	23K	2048
2	InceptionV3	72.96%	91.03%	24K	2048
2	ResNet50	71.23%	91.30%	25K	2048
2	VGG19	77.33%	90.27%	20K	512
3	Xception	10.92%	51.43%	23K	2048
3	InceptionV3	.07%	51.73%	24K	2048
3	ResNet50	.08%	46.13%	26K	2048
3	VGG19	38.11%	44.98%	20K	512

1.3.2 Discussion

In the previous section, we have investigated whether four different architectures pre-trained on the ImageNet dataset can be successfully

used to address three art classification problems. We have observed that this is particularly the case when it comes to classifying the material and the type, where in fact, the off the shelf approach already yielded satisfactory results. However, most importantly, we have also shown that the performance of all models can be significantly improved when the networks are fine tuned, and that an ImageNet initialization is beneficial when compared to training a randomly initialized network from scratch. Furthermore, we have discovered that the pre-trained DCNNs fail if used as simple feature extractors when having they are used for attributing the authorship to the different heritage objects. In the next section, we explore the performance of fine tuned models that are trained for tackling two of the already seen classification challenges on a different heritage collection. For this problem, we will again compare the off the shelf approach with the fine tuning one.

1.3.3 *From One Art Collection to Another*

Table 3 compares the results that we obtained on the Antwerp dataset when using ImageNet pre-trained models (θ^i) versus the same architectures that were fine tuned on the Rijksmuseum dataset (θ^r). While looking at the performance of the different neural architectures two interesting results can be highlighted. First, models which have been fine tuned on the Rijksmuseum dataset outperform the ones pre-trained on ImageNet in both classification challenges. This happens to be the case both when the networks are used as simple feature extractors and when they are fine tuned. On the “type” classification challenge, this result is not surprising since, as discussed in Section 1.2.2, the types corresponding to the heritage objects of the two collections partially overlap. This is more surprising on the “artist” classification challenge however, since there is no overlap at all between the artists of the Rijksmuseum and the ones from the Antwerp dataset. A second interesting result, which is consistent with the results presented in the previous section, revolves around the observation that it is always beneficial to fine tune the networks over just using them as off the shelf feature extractors. Once the models get fine tuned on the Antwerp dataset, these DCNNs, which have also been fine tuned on the Rijksmuseum dataset, outperform the architectures that were pre-trained on ImageNet only. This happened to be the case for both classification challenges and for all considered architectures, as reported in Table 3. This demonstrates how beneficial it is for the models to have been trained on a similar source task and how this can lead to significant improvements both when the networks are used as feature extractors and when they are fine tuned.

Table 3: The results obtained on the classification experiments performed on the Antwerp dataset with models that have been initially pre-trained on ImageNet (θ^i) and the same architectures which have been fine tuned on the Rijksmuseum dataset (θ^r). Our results show that the latter pre-trained networks yield better results both if used as off the shelf feature extractors and if fine tuned.

Challenge	DCNN	$\theta^i + \text{off the shelf}$	$\theta^r + \text{off the shelf}$	$\theta^i + \text{fine tuning}$	$\theta^r + \text{fine tuning}$
2	Xception	42.01%	62.92%	69.74%	72.03%
2	InceptionV3	43.90%	57.65%	70.58%	71.88%
2	ResNet50	41.59%	64.95%	76.50%	78.15%
2	VGG19	38.36%	60.10%	70.37%	71.21%
3	Xception	48.52%	54.81%	58.15%	58.47%
3	InceptionV3	21.29%	53.41%	56.68%	57.84%
3	ResNet50	22.39%	31.38%	62.57%	69.01%
3	VGG19	49.90%	53.52%	54.90%	60.01%

1.3.4 Selective Attention

The benefits of the fine tuning approach over the off the shelf one are clear from our previous experiments. Nevertheless, we do not have any insights yet as to what exactly allows fine tuned models to outperform the architectures which are pre-trained on ImageNet only. In order to provide an answer to that, we investigate which pixels of each input image contribute the most to the final classification predictions of the networks. We do this by using the “VisualBackProp” algorithm presented by [8], which is able to identify which feature maps of the networks are the most informative ones with respect to their final prediction. Once these feature maps are identified, they get backpropagated to the original input image, and visualized as a saliency map according to their weights. The higher the activation of the filters, the brighter the set of pixels covered by these filters are represented.

The results that we have obtained provide interesting insights about how fine tuned models develop novel selective attention mechanisms over the images, which are very different from the ones that characterize the networks that are pre-trained on ImageNet. We report the existence of these mechanisms in Figure 4 where we visualize the different saliency maps between a model pre-trained on ImageNet and the same neural architecture which has been fine tuned on the Rijksmuseum collection. In Figure 4 we visualize which sets of pixels allow the fine tuned model to successfully classify an artist of the Rijksmuseum collection that the same architecture was not able to initially recognize. It is possible to notice that the saliency maps of the latter architecture either correspond to what is more similar to a natural image, as represented by the central image of the first row of plots, or even to what appear to be non informative pixels at all, as shown by the second image in the second row. However, when considering the fine tuned model we clearly observe that these

saliency maps change. In this case the network attends towards the set of pixels that represent people in the bottom, suggesting that this is what allows the model to appropriately recognize the artist of the considered artwork.

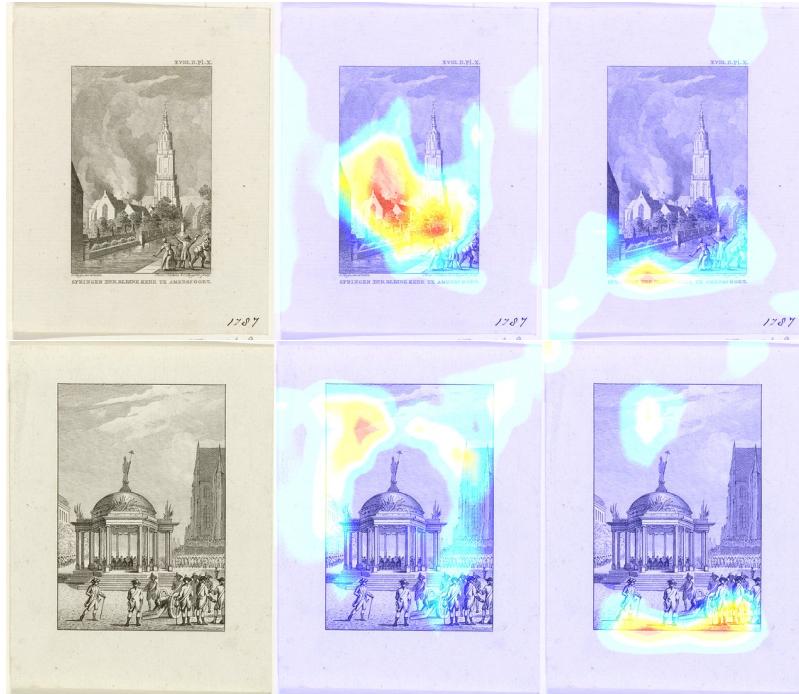


Figure 5: Add caption

These observations can be related to parallel insights in authorship attribution research [17], an established task from Natural Language Processing that is highly similar in nature to artist recognition. In this field, preference is typically given to high-frequency function words (articles, prepositions, particles etc.) over content words (nouns, adjectives, verbs, etc.), because the former are generally considered to be less strongly related to the specific content or topic of a work. As such, function words or stop words lend themselves more easily to attribution across different topics and genres. In art history, strikingly similar views have been expressed by the well-known scholar Giovanni Morelli (1816-1891), who published seminal studies in the field of artist recognition [87]. In Morelli's view too, the attribution of a painting could not happen on the basis of the specific content or composition of a painting, because these items were too strongly influenced by the topic of a painting or the wishes of a patron. Instead, Morelli proposed to base attributions to so-called *Grundformen* or small, seemingly insignificant details that occur frequently in all paintings and typically show clear traces of an artist's individual style, such as ears, hands or feet, a painting's function words, so to speak. The saliency maps above reveal a similar shift in attention when the ImageNet weights are adapted on the Rijksmuseum data: instead of

focusing on higher-level content features, the network shifts its attention to lower layers in the network, seemingly focusing on insignificant details, that nevertheless appear crucial to perform artist attribution.

1.4 CONCLUSION

This paper provides insights about the potential that the field of TL has for art classification. We have investigated the behavior of DCNNs which have been originally pre-trained on a very different classification task and shown how their performances can be improved when these networks are fine tuned. Moreover, we have observed how such neural architectures perform better than if they are trained from scratch and develop new saliency maps that can provide insights about what makes these DCNNs outperform the ones that are pre-trained on the ImageNet dataset. Such saliency maps reflect themselves in the development of new features, which can then be successfully used by the DCNNs when classifying heritage objects that come from different heritage collections. It turns out that the fine tuned models are a better alternative to the same kind of architectures which are pre-trained on ImageNet only, and can serve the CV community which will deal with similar machine learning problems.

As future work, we aim to investigate whether the results that we have obtained on the Antwerp dataset will also apply to a larger set of smaller heritage collections. Furthermore, we want to explore the performances of densely connected layers [30] and understand which layers of the currently analyzed networks contribute the most to their final classification performances. This might allow us to combine the best parts of each neural architecture into one single novel DCNN which will be able to tackle all three classification tasks at the same time.

2

TRANSFER LEARNING WITH NATURAL LOTTERY WINNERS

CONTRIBUTIONS AND OUTLINE

In Chapters 1 and we have always performed Transfer Learning (TL) with extremely large and deep convolutional neural networks. In this chapter however, we take a different approach. We use TL as a tool for, not only exploiting the performance of pruned neural networks, but also for characterizing a relatively new deep learning phenomenon that comes with the name of the “Lottery Ticket Hypothesis” (LTH). Specifically we investigate whether lottery winners that are found on datasets of natural images contain inductive biases that are generic enough to allow them to generalize to non-natural image distributions. To do so, we present to the first results that study the transferability of winning initializations in this particular training setting. Furthermore we also show that the LTH offers a novel way for doing TL when the training data is scarce. The rest of this chapter is structured as follows: Sec. 2.1 introduces the LTH and presents the reasons that have motivated studying this phenomenon from a TL perspective. Sec. 2.2 and Sec. 2.3 present the experimental setup that was used throughout this chapter, while Sec. 3.5 and Sec. 2.4.3 present the main findings of our research. The chapter ends by contextualizing its content with respect to the existing literature in Sec. 2.5 and by identifying some potential avenues for future work in Sec. 2.6.

This chapter is based on the publication Sabatelli, Kestemont, and Geurts [58].

2.1 INTRODUCTION

The “Lottery-Ticket-Hypothesis” (LTH) [20] states that within large randomly initialized neural networks there exist smaller sub-networks which, if trained from their initial weights, can perform just as well as the fully trained unpruned network from which they are extracted. This happens to be possible because the weights of these sub-networks seem to be particularly well initialized before training starts, therefore making these smaller architectures suitable for learning (see Fig 5 for an illustration). These sub-networks, i.e., the pruned structure together with their initial weights, are called winning tickets, as they

appear to have won the initialization lottery. Since winning tickets only contain a very limited amount of parameters, they yield faster training, inference, and sometimes even better final performance than their larger over-parametrized counterparts [20, 22]. So far, winning tickets are typically identified by an iterative procedure that cycles through several steps of network training and weight pruning, starting from a randomly initialized unpruned network. While simple and intuitive, the resulting algorithm, has unfortunately a high computational cost. Despite the fact that the resulting sparse networks can be trained efficiently and in isolation from their initial weights, the LTH idea has not yet led to more efficient solutions for training a sparse network, than existing pruning algorithms that all also require to first fully train an unpruned network [16, 26, 37, 46, 92].

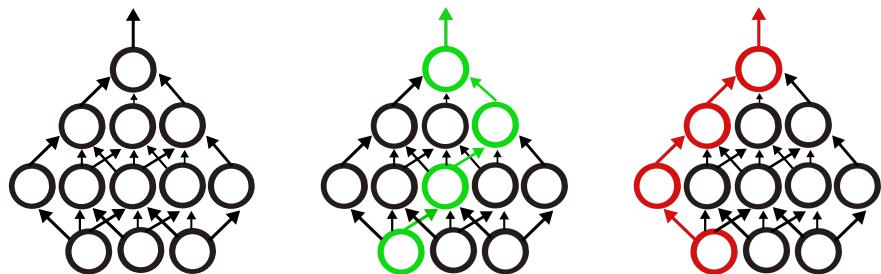


Figure 6: A visual representation of the LTH as introduced by Frankle and Carbin [20]. Let us consider a simplified version of a two hidden layer feedforward neural network as is depicted in the first image on the left. The LTH states that within this neural network there exist multiple smaller networks (represented in green), which can perform just as well as their larger counterpart. Training these sparse models from scratch successfully is only possible as long as their weights are initialized with the same values that were also used when the larger (black) model was initialized. Furthermore, the structure of these sparse models appears to be crucial as well, since it is not possible to randomly extract any subset of weights from an unpruned model and successfully train the resulting sparse network (represented in red in the last figure) from scratch. We visually represent the performance od models that are the winners of the LTH in the two plots reported in Figure 6.

Since the introduction of the idea of the LTH, several research works have focused on understanding what makes some weights so special to be the winners of the initialization lottery. Among the different tested approaches, which will be reviewed in Sec. 2.5, one research direction in particular has looked into how well winning ticket initializations can be transferred among different training settings (datasets and optimizers), an approach which aims at characterizing the winners of the LTH by studying to what extent their inductive biases are generic [47]. The most interesting findings of this study

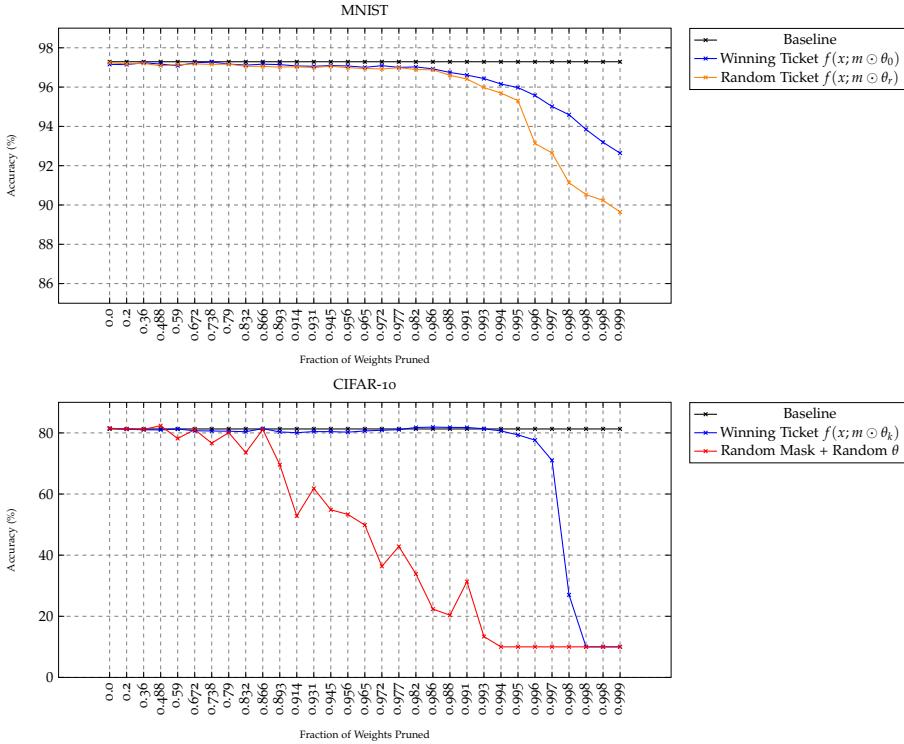


Figure 7: A visual representation of the performance of lottery winners that replicate the findings first presented by Frankle and Carbin [20]. In the first plot we consider a multilayer perceptron that gets trained on the MNIST dataset. After the network gets trained from scratch it obtains a final accuracy of $\approx 97\%$ as reported by the black line. We can observe that winning tickets $f(x; m \odot \theta_0)$ only start performing worse than the network they have been extracted from once a large fraction of their weights gets pruned. We can also observe how crucial it is to re-initialize the weights of the pruned models with the same weights that were used when initializing the unpruned model from scratch (θ_0). If random weights are used instead (θ_r), the pruned masks appear to be less robust to pruning (orange curve). In the second plot we show how important it is for a pruned model to come in the form of $f(x; \odot \theta_k)$ after training a ResNet-50 architecture on the CIFAR-10 dataset, since we show that it is not possible to simply extract any random subset of weights from a deep convolutional network and obtain a performance that is robust to pruning after randomly initializing the parameters of the model (red curve).

are that winning tickets generalize across datasets, within the natural image domain at least, and that tickets obtained from larger datasets typically generalize better. This opens the door to the transfer of winning tickets between datasets, which makes the high computational cost required to identify them much more acceptable practically, as this cost has to be paid only once and can be shared across datasets.

In this paper, we build on top of this latter work. While Morcos et al. [47] focused on the natural image domain, we investigate the

possibility of transferring winning tickets obtained from the natural image domain to datasets in non natural image domains. This question has an important practical interest as datasets in non natural image domains are typically scarcer than datasets in natural image domains. They would therefore potentially benefit more from a successful transfer of sparse networks, since the latter can be expected to require less data for training than large over-parametrized networks. Furthermore, besides studying their generalization capabilities, we also focus on another interesting property that characterizes models that win the LTH, and which so far has received less research attention. As originally presented in [20], pruned models which are the winners of the LTH can yield a final performance which is better than the one obtained by larger over-parametrized networks. In this work we explore whether it is worth seeking for such pruned models when training data is scarce, a scenario that is well known to constraint the training of deep neural networks. To answer these two questions, we carried out experiments on several datasets from two very different non natural image domains: digital pathology and digital heritage.

2.2 DATASETS

We consider seven datasets that come from two different, unrelated sources: histopathology and digital heritage. Each dataset comes with its training, validation and testing splits. Furthermore the datasets change in terms of size, resolution, and amount of labels that need to be classified. We report an overview about the size of these datasets in Table 4 while a visual representation of the samples constituting these datasets in Fig. 7. The Digital-Pathology (DP) data comes from the Cytomine [41] web application, an open-source platform that allows interdisciplinary researchers to work with large-scale images. While Cytomine has collected a large number of datasets over the years, in this work we have limited our analysis to a subset of four datasets that all represent tissues and cells from either human or animal organs: Human-LBA, Lung-Tissues, and Mouse-LBA were originally proposed in [48], while Bone-Marrow comes from [32]. All four datasets have been used in [48], that researched whether neural networks pre-trained on natural images could successfully be re-used in the DP domain. In this paper, we explore whether an alternative to the transfer-learning approaches presented in [48] could be based on training pruned networks that are the winners of the LTH. This will allow us to investigate the two research questions introduced in Sec. 2.1: we will explore whether winning initializations that are found on datasets of natural images do generalize to non-natural domains, and whether sparse models winners of the LTH can perform better than larger unpruned models that get trained from scratch. Regarding the field of Digital-Humanities (DH) we have created three novel datasets that

all revolve around the classification of artworks. We consider two different classification tasks that have already been thoroughly studied by researchers bridging between the fields of Computer Vision (CV) and DH [44, 60, 64]. The first task consists in identifying the artist of the different artworks, while the second one aims at classifying which kind of artwork is depicted in the different images, a challenge which is usually referred to in the literature as type-classification [44, 60]. When it comes to the artist-classification task we have created two different datasets, which purpose will be better explained in Sec. 2.4.3. All images are publicly available as part of the WikiArt gallery [53] and can also be found within the large popular OmniArt dataset [65]. Albeit as we have seen in Chapter 1 in DH it is actually easier to find large datasets than in histopathology, it is worth mentioning that we have kept the size of these datasets intentionally small in order to fit the research questions introduced in Sec. 2.1. Furthermore, it is also worth noting that there are several additional challenges that need to be overcome when training deep neural networks on artistic collections, which therefore motivate the use of this kind of datasets in this work. The size, texture, and resolution of the images coming from the DH are usually representative of different time periods, artistic movements and might have gone through different digitization processes, which are all reasons that make these datasets largely varied and challenging.

Table 4: A brief overview of the seven different datasets which have been used in this work. As usual throughout this thesis N_t corresponds to the total amount of samples that are present in the dataset, while Q_t represents the number of classes.

Dataset	Training-Set	Validation-Set	Testing-Set	N_t	Q_t
Human-LBA	4051	346	1023	5420	9
Lung-Tissues	4881	562	888	6331	10
Mouse-LBA	1722	716	1846	4284	8
Bone-Marrow	522	130	639	1291	8
Artist-Classification-1	3103	389	389	3881	20
Type-Classification	2868	360	360	3588	20
Artist-Classification-2	2827	353	353	3533	19

2.3 EXPERIMENTAL SETUP

We follow an experimental set-up similar to the one that was introduced in [47] (and that has been validated by [25]). Let us define a neural network $f(x; \theta)$ that gets randomly initialized with parameters $\theta_0 \sim \mathcal{D}_\theta$ and then trained for j iterations over an input space \mathcal{X} , and an output space \mathcal{Y} . At the end of training a percentage of the parameters in θ_j gets pruned, a procedure which results in a mask m . The

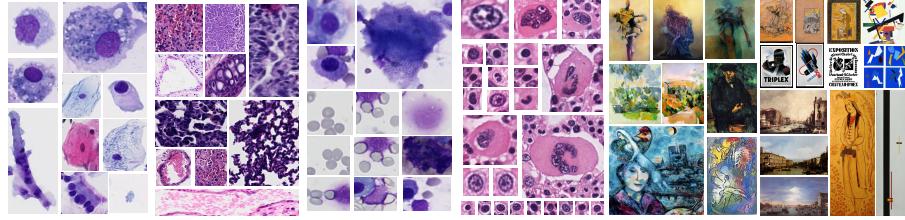


Figure 8: Some image samples that constitute the non-natural image datasets which have been used in this work. From left to right we have the Human-LBA, Lung-Tissues, Mouse-LBA and Bone-Marrow datasets, while finally we report some examples that represent artworks which come from the field of digital heritage and that are therefore similar to the images we have used for the experiments reported in Chapter 1.

parameters in θ_j which did not get pruned are then reset to the values they had at θ_k , where k represents an early training iteration. A winning ticket corresponds to the combination between the previously obtained mask, and the parameters θ_k , and is defined as $f(x; m \odot \theta_k)$ ¹. Constructing a winning ticket with parameters θ_k , instead of θ_0 , is a procedure which is known as late-resetting [22], and is a simple but effective trick that makes it possible to stably find winning initializations in deep convolutional neural networks [22, 47]. In this study $f(x; \theta)$ comes in the form of a ResNet-50 architecture [26] which gets trained on the three popular CV natural image datasets (visually represented in Fig. 8): CIFAR-10/100 and Fashion-MNIST. Following [26, 47], 31 winning tickets $f(x; m \odot \theta_k)$ of increasing sparsity are obtained from each of these three datasets by repeating 31 iterations of network training and magnitude pruning with a pruning rate of 20%. More precisely, at each pruning iteration, the network is trained for several epochs (using early stopping on the validation set as described in the appendix) and then the 20% of weights with the lowest magnitudes are pruned. The parameters θ_k that define each of the 31 tickets are then taken as the weights of the corresponding pruned networks at the k th epoch of the first pruning iteration. Once these pruned networks are found we aim at investigating whether their parameters θ_k contain inductive biases that allow them to generalize to the non-natural image domain. To do so we replace the final fully connected layer of each winning ticket with a randomly initialized layer that has as many output nodes as there are classes to classify. We then fine-tune each of these networks on the non-natural image datasets considered in this study. At the end of training, we study the performance of each winning ticket in two different ways. First,

¹ Note that this formulation generalizes the original version of the LTH [20] that we have represented in Fig. 5, where a winning ticket is obtained after resetting the unpruned parameters of the network to the values they had right after initialization, therefore defining a winning ticket as $f(x; m \odot \theta_0)$.



Figure 9: The three natural datasets used in our experiments to find winning tickets. From left to right samples from the CIFAR-10/100 and Fashion-MNIST datasets.

we compare the performance of each network to the performance of a fully unpruned network that gets randomly initialized and trained from scratch. Second, we also compare the performance of winning tickets that have been found on a natural image dataset to 31 new sparse models that are the winners of the LTH on the considered target dataset. Since it is not known to which extent pruned networks that contain weights that are the winners of the LTH on a natural image dataset can generalize to target distributions that do not contain natural images, we report the first results that investigate the potential of a novel transfer-learning scheme which has so far only been studied on datasets from the natural image domain. Moreover, testing the performance of sparse networks that contain winning tickets that are specific to a non-natural image target distribution also allows us to investigate whether it is worth pruning large networks with the hope of finding smaller models that might perform better than a large over-parametrized one. As mentioned in Sec. 2.1, pruned networks that are initialized with the winning weights can sometimes perform better than a fully unpruned network. Identifying such sparse networks leads to a very significant reduction of model size, which can be a very effective way of regularization when training data is scarce.

2.4 RESULTS

The results of all our experiments are visually reported in the plots of Fig. 9. Each line plot represents the final performance that is obtained by a pruned model that contains a winning ticket initialization on the final testing-set of our target datasets. This performance is reported on the y-axis of the plots, while on the x-axis we represent the fraction of weights that is pruned from the original ResNet-50 architecture. As explained in the previous section the performance of each winning ticket is compared to the performance that is obtained by an unpruned, over-parametrized architecture that is reported by the black dashed lines. The models that are the winners of the LTH

on a natural image dataset are reported by the green, red and purple lines, while the winners of the LTH on a non-natural target dataset are reported by the blue lines. Furthermore, when it comes to the latter lottery tickets, we also report the performance that is obtained by winning tickets that get randomly reinitialized ($f(x; m \odot \theta'_0)$ with $\theta'_0 \sim \mathcal{D}_\theta$). These results are reported by the orange lines. Shaded areas around all line plots correspond to ± 1 std. that has been obtained after repeating and averaging the results of our experiments over four different random seeds.

2.4.1 *On the Importance of Finding Winning Initializations*

We can start by observing that pruned models which happen to be the winners of the LTH either on a natural dataset, or on a non-natural one, can maintain a good final performance until large pruning rates are reached. This is particularly evident on the first three datasets, where models that keep only $\approx 1\%$ of their original weights barely suffer from any drop in performance. This gets a little bit less evident on the last three datasets, where the performance of winning ticket initializations that are directly found on the considered target dataset starts getting harmed once a fraction of $\approx 97\%$ of original weights are pruned. These results show that an extremely large part of the parameters of a ResNet-50 architecture can be considered as superfluous, therefore confirming the LTH when datasets contain non-natural images. More importantly, we also observe that pruned models winners of the LTH, significantly outperform larger over-parametrized models that get trained from scratch. This can be very clearly seen in all plots where the performance of pruned models is always consistently better than what is reported by the black dashed line. To get a better sense of how much these pruned networks perform better than their larger unpruned counterparts, we report in Table 5 the performance that is obtained by the best performing pruned model, found over all 31 possible pruned models, and compare it to the performance of an unpruned architecture. The exact fraction of weights which is pruned from an original ResNet-50 architecture is reported in Table 6 for each configuration. We can observe that no matter which dataset has been used as a source for finding a winning ticket initialization, all pruned networks reach a final accuracy that is significantly higher than the one that is obtained after training an unpruned model from scratch. While in most cases the difference in terms of performance is of $\approx 10\%$ (see e.g. the Human-LBA, Lung-Tissues and the Type-Classification datasets), it is worth highlighting that there are other cases in which this difference is even larger. This is the case for the Mouse-LBA and Artist-Classification-1 datasets where a winning ticket coming from the CIFAR-10 dataset performs more than 20% better than a model trained from scratch. These results show that

in order to maximize the performance of deep networks it is always worth finding and training pruned models which are the winners of the LTH.

Table 5: The results comparing the performance that is obtained on the testing-set by the best pruned model winner of the LTH, and an unpruned architecture trained from scratch. The overall best performing model is reported in a green cell, while the second best one in a yellow cell. We can observe that pruned models winners of the LTH perform significantly better than a larger over-parametrized architecture that gets trained from scratch. As can be seen by the results obtained on the Mouse-LBA and Artist-Classification-1 datasets the difference in terms of performance can be particularly large ($\approx 20\%$).

Target-Dataset	Scratch-Training	CIFAR-10	CIFAR-100	Fashion-MNIST	Target-Ticket
Human-LBA	71.85 ± 1.12	79.17 ± 1.85	76.97 ± 0.73	77.32 ± 1.85	81.72 ± 0.39
Lung-Tissues	84.75 ± 0.81	88.90 ± 1.97	87.61 ± 0.90	87.61 ± 0.11	90.48 ± 0.16
Mouse-LBA	48.17 ± 1.18	74.20 ± 2.04	57.42 ± 0.48	52.27 ± 1.73	68.20 ± 3.79
Bone-Marrow	64.66 ± 1.36	71.75 ± 3.36	69.87 ± 0.39	68.77 ± 0.39	72.55 ± 0.46
Artist-Classification-1	45.88 ± 0.42	66.58 ± 1.54	65.55 ± 1.79	63.88 ± 0.12	58.74 ± 1.92
Type-Classification	41.36 ± 2.31	58.63 ± 2.97	60.56 ± 0.44	58.92 ± 0.59	50.44 ± 2.23

Table 6: Some additional information about the lottery winners which performance is reported in Table 5. For each winning ticket we report the fraction of weights that is pruned from an original ResNet-50 architecture and that therefore characterizes the level of sparsity of the overall best performing lottery ticket. The results in the Scratch-Training column are not reported since these are unpruned models that are trained from scratch.

Target-Dataset	Scratch-Training	CIFAR-10	CIFAR-100	Fashion-MNIST	Target-Ticket
Human-LBA	-	0.945	0.79	0.886	0.832
Lung-Tissues	-	0.977	0.977	0.672	0.965
Mouse-LBA	-	0.972	0.893	0.738	0.931
Bone-Marrow	-	0.866	0.988	0.931	0.914
Artist-Classification-1	-	0.972	0.993	0.991	0.931
Type-Classification	-	0.991	0.931	0.995	0.963

2.4.2 On the Generalization Properties of Lottery Winners

We then investigate whether natural image tickets can generalize to the non-natural setting. Findings differ across datasets. When considering the datasets that come from the field of DP, we can see that, in three out of four cases, winning tickets that are found on a natural image dataset get outperformed by sparse winning networks that come after training a model on the biomedical dataset. This is particularly evident in the results obtained on the Human-LBA and Lung-Tissues datasets where the highest testing-set accuracy is consistently reached by the blue line plots. When it comes to the Bone-Marrow dataset the difference in terms of performance between the best natural image

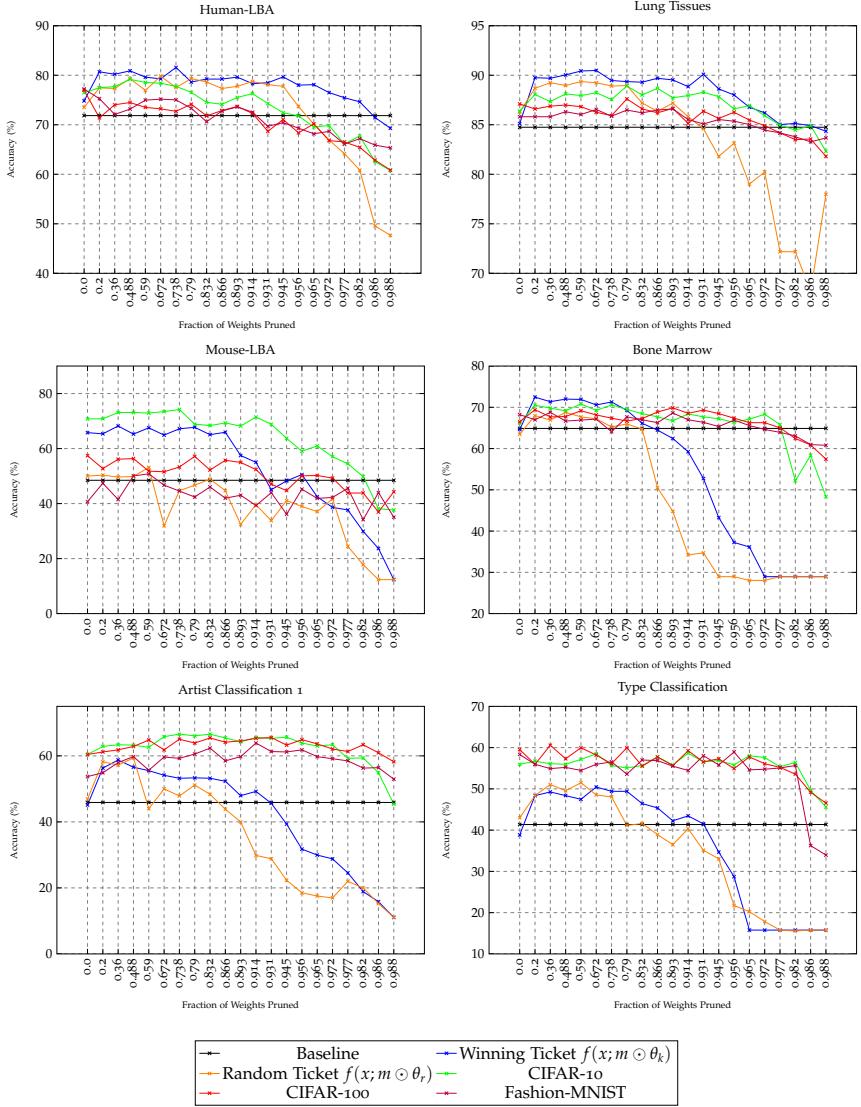


Figure 10: An overview of the results showing that sparse models that are the winners of the LTH (represented by the coloured lines) significantly outperform unpruned networks which get randomly initialized and trained from scratch (dashed black line). This happens to be the case on all tested datasets, no matter whether a winning initialization comes from a natural image source or not. It is however worth mentioning that, especially on the biomedical datasets, natural image tickets get outperformed by sparse networks that are the winners of the LTH on a biomedical dataset. On the other hand this is not the case when it comes to the classification of arts where natural image tickets outperform the ones which are found within artistic collections.

ticket, in this case coming from the CIFAR-10 dataset, and the one coming from the biomedical dataset, is less evident (see Table 5 for the exact accuracies). Furthermore, it is worth highlighting that on the Bone-Marrow dataset, albeit natural image models seem to get outper-

formed by the ones found on the biomedical dataset, the performance of the latter ones appears to be less stable once extremely large pruning rates are reached. When it comes to the Mouse-LBA dataset these results slightly differ. In fact, this dataset corresponds to the only case where a natural image source ticket outperforms a non-natural one. As can be seen, by the green line plot, pruned models coming from the CIFAR-10 dataset outperform the ones found on the Mouse-LBA dataset. When focusing our analysis on the classification of arts, we see that the results change greatly from the ones obtained on the biomedical datasets. In this case, all of the natural image lottery winners, no matter the dataset they were originally found on, outperform the same kind of models that were found after training a full network on the artistic collection. We can see from Table 5 that the final testing performance is similar among all of the best natural image tickets. Similarly to what has been noticed on the Bone-Marrow dataset we can again observe that tickets coming from a non-natural data distribution seem to suffer more from large pruning rates.

These results show both the potential and the limitations that natural image winners of the LTH can offer when they are fine-tuned on datasets of non-natural images. The results obtained on the artistic datasets suggest that winning initializations contain inductive biases that are strong enough to get at least successfully transferred to the artistic domain, therefore confirming some of the claims that were made by Morcos et al. [47]. However, it also appears that there are stronger limitations to the transferability of winning initializations which were not observed by Morcos et al. [47]. In fact, our results show that on DP data the best strategy is to find a winning ticket directly on the biomedical dataset, and that winning initializations found on natural image datasets, albeit outperforming a randomly initialized unpruned network, perform worse than pruned models that are the winners of the LTH on a biomedical dataset.

2.4.3 Additional Studies

To characterize the transferability of winning initializations even more, while at the same time gaining a deeper understanding of the LTH, we have performed a set of three additional experiments which help us characterize this phenomenon even better.

2.4.3.1 Lottery Tickets VS fine-tuned pruned models

So far we have focused our transfer-learning study on lottery tickets that come in the form of $f(x; m \odot \theta_k)$, where, as mentioned in Sec. 2.3, θ_k corresponds to the weights that parametrize a neural network at a very early training iteration. This formalization is however different from more common transfer-learning scenarios like the ones we have explored in Chapter 1 where neural networks get transferred

with the weights that are obtained at the end of the training process [48, 60]. We have therefore studied whether there is a difference in terms of performance between transferring and fine-tuning a lottery ticket with parameters θ_k , and the same kind of pruned network which is initialized with the weights that are obtained once the network is fully trained on a source task. We define these kind of models as $f(x; m \odot \theta_i)$ where i stays for the last training iteration. We report some examples of this behaviour in the plots presented in Fig. 10, where we consider $f(x; m \odot \theta_i)$ models which were trained on the CIFAR-10 and CIFAR-100 datasets, and then transferred and fine-tuned on the Human-LBA dataset. We found that these models overall perform worse than lottery tickets, while also being less robust to pruning. This also shows that on this dataset, the slightly inferior performance of the natural image tickets with respect to the target tickets is not due to the weight re-initialization.

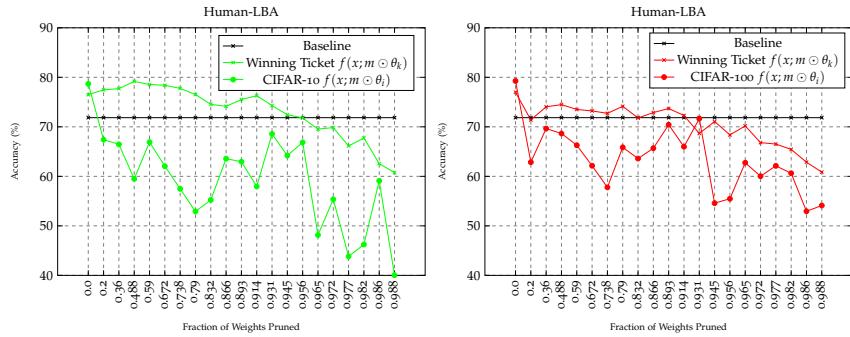


Figure 11: Our results showing the advantages of transferring lottery winners over pruned models that are fully fine-tuned on natural datasets (CIFAR-10/100). We can observe that their performance is overall inferior to the one of lottery tickets and that these models are significantly less robust to pruning. We believe that the reason behind their poor performance revolves around the fact that, once completely trained on a specific source task, and after having gone through the pruning stage, these models lose the necessary flexibility that is required for them to adapt to a new task.

2.4.3.2 Transferring tickets from similar non-natural domains

We investigated whether it is beneficial to fine-tune lottery winners that, instead of coming from a natural image distribution, come from a related non-natural dataset. Specifically we tested whether winning tickets generated on the Human-LBA dataset generalize to the Mouse-LBA one (since both datasets are representative of the field of Live-Blood-Analysis), and whether lottery winners coming from the Artist-Classification-1 dataset generalized to the Artist-Classification-2 one. We visually represent these results in Fig. 11. As one might expect, we found that it is beneficial to transfer winning tickets that

come from a related source. Specifically, Human-LBA tickets can perform just as well as winning tickets that are generated on the Mouse-LBA dataset, while at the same time also being more robust to large pruning rates. When it comes to lottery winners found on the Artist-Classification-1 dataset we have observed that these tickets can even outperform the ones generated on the Artist-Classification-2 one. Overall these results confirm the claims that we made in Chapter 1 where we already highlighted the benefits that could come from transferring models that were trained on a similar source as the target task. This conclusion now also holds for models that are the winners of the LTH.

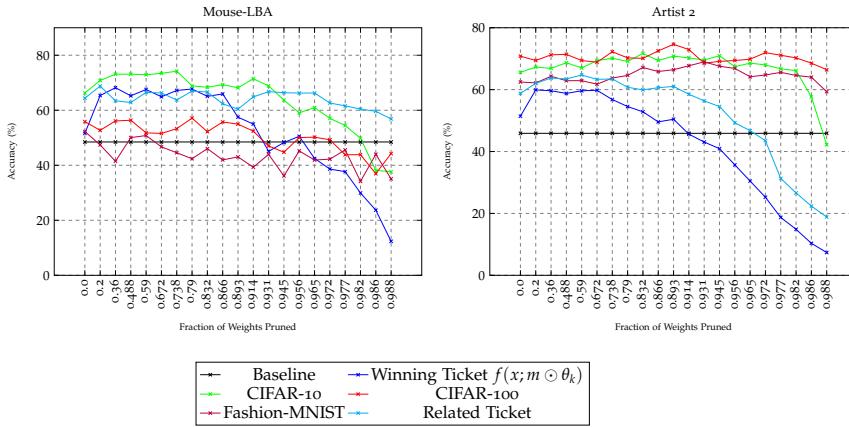


Figure 12: Our results showing the benefits of transferring lottery winners that have been identified on a related source task. We can observe that on the Mouse-LBA dataset, winning tickets that were obtained on the Human-LBA dataset are the ones that are the most robust ones to pruning, while on the Artist-Classification-2 dataset we can observe that lottery winners that have been obtained on the Artist-Classification-1 dataset are both more robust to pruning, while they also yield overall better performance.

2.4.3.3 On the size of the training set

We have observed from the blue line plots of Fig. 9 that there are cases in which lottery winners are very robust to extremely large pruning rates (see as an example the first and second plots), while there are other cases in which their performance deteriorates faster with respect to the fraction of weights that get pruned. The most robust performance is obtained by winning tickets that are generated on the Human-LBA and Lung-Tissues datasets, which are the two target datasets that contain the largest amount of training samples. We have therefore studied whether there is a relationship between the size of the training data that is used for finding lottery winners, and the robustness in terms of performance of the resulting pruned models. We generated lottery winners after incrementally reducing the size of the training data by 75%, 50% and 25%, and then investigated whether

we could observe a similar drop in performance as the one we have observed in the last three blue line-plots of Fig. 9 once a large fraction of weights got pruned. Perhaps surprisingly, we have observed that this was not the case, and as can be seen by the plots represented in Fig. 12, the performance of lottery winners that are found when using only 25% of the training set is just as stable as the one of winning tickets which are generated on the entire dataset. It is however worth mentioning that, albeit the performance of such sparse models is robust, their final performance on the testing set is lower than the one that is obtained by winning tickets that have been trained on the full training data distribution.

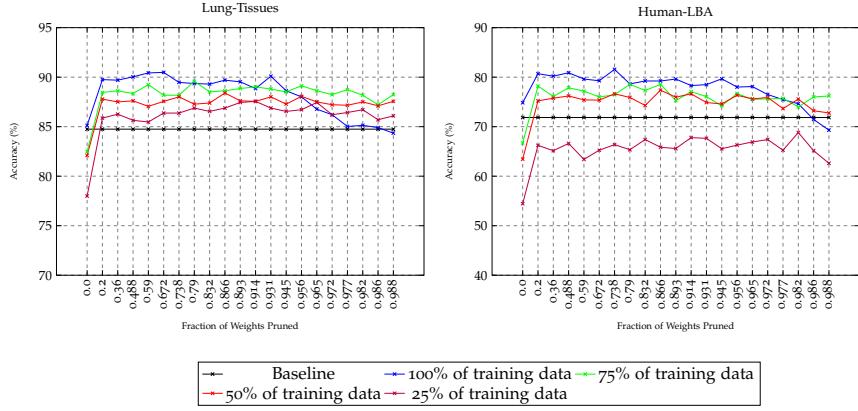


Figure 13: Our study showing that the robustness to large pruning rates of lottery winners does not depend from the size of the training dataset. We can observe that even when lottery tickets after are trained on only 25% of the dataset their performance remains stable with respect to the fraction of pruned weights. These results suggest that the less stable performance of Bone-Marrow lottery tickets observed in Fig. 9 does not depend from the small training set.

2.5 RELATED WORK

The research presented in this paper contributes to a better understanding of the LTH by exploring the generalization and transfer-learning properties of lottery tickets. The closest approach to what has been presented in this work is certainly [47], which shows that winning models can generalize across datasets of natural images and across different optimizers. As mentioned in Sec. 2.3, a large part of our experimental setup is based on this work. Besides the work presented in [47], there have been other attempts that aimed to better understand the LTH after studying it from a transfer-learning perspective. However, just as the study presented by Morcos et al. [47], all this research limited its analysis to natural images. Van Soelen and Sheppard [79] transfer winning tickets among different partitions of

the CIFAR-10 dataset, while Mehta [43] shows that sparse models can successfully get transferred from the CIFAR-10 dataset to other object recognition tasks. While these results seem to suggest that lottery tickets contain inductive biases which are strong enough to generalize to different domains, it is worth highlighting that their transfer-learning properties were only studied after considering the CIFAR-10 dataset as a possible source for winning ticket initializations, a limitation which we overcome in this work. It is also worth mentioning that the research presented in this paper is strongly connected to the work presented by Frankle et al. [22]. While the first paper that introduced the LTH limited its analysis to relatively simple neural architectures, such as multilayer perceptrons and convolutional networks which were tested on small CV datasets, the presence of winning initializations in larger, more popular convolutional models such as the ones that we used in Chapter 1 trained on large datasets [57] was only first presented by [22]. Since in this work we have used a ResNet-50 architecture [28], we have followed all the recommendations that were introduced in [22], for successfully identifying the winners of the LTH in larger models. More specifically we mention the late-resetting procedure which resets the weights of a pruned model to the weights that are obtained after k training iterations instead of to the values which were used at the beginning of training (as explained in Sec. 2.3), a procedure which has shown to be related to *linear mode connectivity* [21]. While the work presented in this paper has limited its analysis to networks that minimize an objective function that is relevant for classification problems, it is worth noting that more recent approaches have identified lottery winners in different training settings. Yu et al. [89] have shown that winning initializations can be found when neural networks are trained on tasks ranging from natural language processing to reinforcement learning, while Sun et al. [66] successfully identify sparse winning models in a multi-task learning scenario. As future work, we want to study whether lottery tickets can be found on different neural architectures, and also when neural networks are trained on CV tasks other than classification. More specifically we aim at studying whether winners of the LTH, which are found on popular natural image datasets such as [39] and [18] when tackling image localization and segmentation tasks, can generalize to non-natural settings which might include the segmentation of biomedical data, or the localization of objects within artworks.

2.6 CONCLUSION

We have investigated the transfer learning potential of pruned neural networks that are the winners of the LTH from datasets of natural images to datasets containing non-natural images. We have explored this in training conditions where the size of the training data is rel-

atively small. All of the results presented in this work confirm that it is always beneficial to train a sparse model, winner of the LTH, instead of a larger over-parametrized one. Regarding our study on the transferability of winning tickets we have reported the first results which study this phenomenon under non-natural data distributions by using datasets coming from the fields of digital pathology and heritage. While for the case of artistic data it seems that winning tickets from the natural image domain contain inductive biases which are strong enough to generalize to this specific domain, we have also shown that this approach can present stronger limitations when it comes to biomedical data. This probably stems from the fact that DP images are further away from natural images than artistic ones. We have also shown that lottery tickets perform significantly better than fully trained pruned models, that it is beneficial to transfer lottery winners from different, but related, non-natural sources, and that the performance of lottery tickets is not dependant on the size of the training data. To conclude, we provide a better characterization of the LTH while simultaneously showing that when training data is limited, the performance of deep neural networks can get significantly improved by using lottery winners over larger over-parametrized ones.

Part II

TRANSFER LEARNING IN REINFORCEMENT LEARNING

THE DEEP QUALITY-VALUE LEARNING FAMILY OF ALGORITHMS

CONTRIBUTIONS AND OUTLINE

In the first part of this thesis we have thoroughly studied the level of transferability of deep neural networks that get trained in a supervised learning fashion. From the results of our studies we concluded that significant benefits can come from using pre-trained models over networks that get trained from scratch, and that transfer learning can be a valuable machine learning paradigm for studying the generalization properties of neural networks. So far we have always considered the setting in which, before getting trained on a new task, a model could rely on some **fixed** knowledge it had learned on a separate but related task. In this chapter however, we take a different approach: we develop a novel family of Deep Reinforcement Learning (DRL) algorithms, that instead of learning on top of what a model has learned in the past, rely on what is **simultaneously** being learned by a different, yet related model. The information that is being learned by one model can be transferred and used by a second one in a very dynamical fashion, which within the DRL context yields faster, more robust and better performance.

This chapter is based on the following two publications: Sabatelli et al. [59] and Sabatelli et al. [61]

3.1 INTRODUCTION

In value-based Reinforcement Learning (RL) the aim is to construct algorithms which learn *value functions* that are either able to estimate how good or bad it is for an agent to be in a particular state, or how good it is for an agent to perform a particular action in a given state. Such functions are respectively denoted as the state-value function $V(s)$, and the state-action value function $Q(s, a)$ [69]. In Deep Reinforcement Learning (DRL) the aim is to approximate these value functions with e.g. deep convolutional neural networks [35], which can serve as universal function approximators and powerful feature extractors. Classic model-free RL algorithms like Q-Learning [81], Double Q-Learning [76] and SARSA [56] have all led to the development of a “deep” version of themselves in which the original RL update rules are expressed as objective functions that can be minimized by

gradient descent [45, 77, 90]. Despite their successful applications [36], the aforementioned algorithms only aim at approximating the Q function, while completely ignoring the V function. This approach, however, is prone to issues that go back to standard RL literature. As shown by Van Hasselt, Guez, and Silver [77] the DQN algorithm [45] is known to overestimate the values of the Q function and requires an additional target network to not diverge (which role, as shown by Achiam, Knight, and Abbeel [2], is not yet fully understood). These overestimations can partially be corrected by the DDQN [77] algorithm, which, despite yielding stability improvements, does not always prevent its Q networks from diverging [78] and sometimes even underestimating the Q function. Furthermore, DRL algorithms are also extremely slow to train. In what follows, we introduce a new family of DRL algorithms based on the key idea of simultaneously learning the V function alongside the Q function with two separate neural networks. Our main insight is that by jointly approximating the V function and the Q function, the task of learning one of these value functions can be sped up if the model that is responsible for learning it, can rely on what is being learned by the model responsible for learning the remaining value function. We show that this simple, yet effective idea yields faster, more robust and better model-free Deep Reinforcement Learning.

3.2 PRELIMINARIES

We formally define the RL setting as a Markov Decision Process (MDP) where the main components are a finite set of states $\mathcal{S} = \{s^1, s^2, \dots, s^n\}$, a finite set of actions \mathcal{A} and a time-counter variable t . In each state $s_t \in \mathcal{S}$, the RL agent can perform an action $a_t \in \mathcal{A}(s_t)$ and transit to the next state as defined by a transition probability distribution $p(s_{t+1}|s_t, a_t)$. When moving from s_t to a successor state s_{t+1} the agent receives a reward signal r_t coming from the reward function $\mathfrak{R}(s_t, a_t, s_{t+1})$. The actions of the agent are selected based on its policy $\pi : \mathcal{S} \rightarrow \mathcal{A}$ that maps each state to a particular action. For every state $s \in \mathcal{S}$, under policy π its *value function* V^π is defined as:

$$V^\pi(s) = \mathbb{E} \left[\sum_{k=0}^{\infty} \gamma^k r_{t+k} \middle| s_t = s, \pi \right], \quad (2)$$

which denotes the expected cumulative discounted reward that the agent will get when starting in state s and by following policy π thereafter. Similarly, we can also define the *state-action* value function Q for denoting the value of taking action a in state s based on policy π as:

$$Q^\pi(s, a) = \mathbb{E} \left[\sum_{k=0}^{\infty} \gamma^k r_{t+k} \middle| s_t = s, a_t = a, \pi \right]. \quad (3)$$

Both functions are computed with respect to the discount factor $\gamma \in [0, 1]$ which controls the trade-off between immediate and long term rewards. The goal of an RL agent is to find a policy π^* that realizes the optimal expected return:

$$V^*(s) = \max_{\pi} V^\pi(s), \text{ for all } s \in \mathcal{S} \quad (4)$$

and the optimal Q value function:

$$Q^*(s, a) = \max_{\pi} Q^\pi(s, a) \text{ for all } s \in \mathcal{S} \text{ and } a \in \mathcal{A}. \quad (5)$$

It is well-known that optimal value functions satisfy the Bellman optimality equation as given by

$$V^*(s_t) = \max_a \sum_{s_{t+1}} p(s_{t+1}|s_t, a) \left[\mathfrak{R}(s_t, a, s_{t+1}) + \gamma V^*(s_{t+1}) \right] \quad (6)$$

for the state-value function, and by

$$Q^*(s_t, a_t) = \sum_{s_{t+1}} p(s_{t+1}|s_t, a_t) \left[\mathfrak{R}(s_t, a_t, s_{t+1}) + \gamma \max_a Q^*(s_{t+1}, a) \right], \quad (7)$$

for the state-action value function. Both functions can either be learned via Monte Carlo methods or by Temporal-Difference (TD) learning [67], with the latter approach being so far the most popular choice among model-free RL algorithms [56, 76, 81].

3.3 RELATED WORK

While RL algorithms have been successfully combined with shallow neural networks for over two decades [72], the use of these algorithms with deeper architectures is more recent. The contribution which has established the potential of DRL can certainly be identified with the Deep-Q-Network (DQN), the first algorithm which uses a convolutional neural network for successfully learning an approximation of the Q function from high dimensional inputs [45]. This approximation is learned by reshaping the popular Q-Learning algorithm introduced by Watkins and Dayan [81] to an objective function which can be minimized by gradient descent. The original Q-Learning algorithm learns the state-action value function as follows

$$Q(s_t, a_t) := Q(s_t, a_t) + \alpha [r_t + \gamma \max_{a \in \mathcal{A}} Q(s_{t+1}, a) - Q(s_t, a_t)] \quad (8)$$

where α corresponds to the learning rate. The DQN algorithm adapts this update rule to a differentiable loss function which can be used

for training a neural network that is parametrized by θ . This objective function comes in the following form:

$$L(\theta) = \mathbb{E}_{(s_t, a_t, r_t, s_{t+1}) \sim U(D)} \left[(r_t + \gamma \max_{a \in \mathcal{A}} Q(s_{t+1}, a; \theta^-) - Q(s_t, a_t; \theta))^2 \right]. \quad (9)$$

Within this loss there are two components which ensure stable training. The first one is the Experience-Replay memory buffer (D), first introduced by Lin [38], a buffer coming in the form of a queue which stores RL experiences (s_t, a_t, r_t, s_{t+1}) . When it comes to the popular Atari Arcade Learning (ALE) [6] benchmark, the DQN algorithm uniformly samples mini-batches of 32 experiences for minimizing Eq. 9, a procedure which starts as soon as at least 50.000 experiences are stored within the queue. Furthermore, there is a second component which ensures stable training denoted as the target-network. DQN learns an approximation of the Q function via TD-Learning, meaning that the approximated Q -function is regressed towards TD-targets which are computed by the approximated Q function itself. The TD-target, defined as y_t^{DQN} , is expressed as follows:

$$y_t^{DQN} = r_t + \gamma \max_{a \in \mathcal{A}} Q(s_{t+1}, a; \theta^-), \quad (10)$$

and is computed by the target network θ^- instead from the online Q -network θ . The online network, and its target counterpart, have the exact same structure, with the main difference being that the parameters of the latter do not get optimized each time a mini-batch of experiences is sampled from the memory buffer. On the contrary its weights are temporally frozen and are only periodically updated with the θ weights (as defined by an appropriate hyperparameter). Given a training iteration i , differentiating the objective function of Eq. 9 with respect to θ gives the following gradient:

$$\nabla_{\theta_i} y_t^{DQN}(\theta_i) = \mathbb{E}_{(s_t, a_t, r_t, s_{t+1}) \sim U(D)} \left[(r_t + \gamma \max_{a \in \mathcal{A}} Q(s_{t+1}, a; \theta_{i-1}^-) - Q(s_t, a_t; \theta_i)) \nabla_{\theta_i} Q(s_t, a_t; \theta_i) \right]. \quad (11)$$

Despite yielding super-human performance on most games coming from the ALE, DQN has shown to be suffering from the same issues which characterize the Q-Learning algorithm [76]. Among these issues we mention the overestimation bias of the Q -function which has been well characterized in the tabular setting by Van Hasselt [76] and later in the deep learning context by Van Hasselt, Guez, and Silver [77]. In short, DQN is prone to learn overestimated Q -values because the same values are used both for selecting an action ($\max_{a \in \mathcal{A}}$) and for

evaluating it ($Q(s_{t+1}, a; \theta^-)$). As originally presented by Van Hasselt, Guez, and Silver [77] this becomes clearer when re-writing Eq. 10 as:

$$y_t^{DQN} = r_t + \gamma \max_{a \in \mathcal{A}} Q(s_{t+1}, a; \theta^-). \quad (12)$$

As a result, DQN tends to approximate the expected maximum value of a state, instead of its maximum expected value. To solve this problem the DDQN algorithm untangles the selection of an action from its evaluation by taking advantage of the target network θ^- . DDQN's target is the same as DQN's with the main difference being that the selection of an action, given by the online Q-network θ , and the evaluation of the resulting policy, given by θ^- , can get unbiased by symmetrically updating the two sets of weights (θ and θ^-). This can be achieved by regularly switching their roles during training.

Several extensions of DQN and DDQN have been proposed over the years, to make these algorithms learn faster and more data-efficient. We refer the reader to [36] for a more in-depth review of these contributions. Within this chapter, we are only interested in synchronous DRL algorithms which learn an approximation of a value function. This is achieved by following the same experimental setups that have been used for DQN and DDQN, and that will be reviewed in Sec. 3.5.1 of this chapter. Therefore, in what follows we will aim at comparing our novel DRL algorithms to DQN and DDQN only, while leaving their potential integration within more sophisticated DRL techniques as future work.

3.4 A NOVEL FAMILY OF DEEP REINFORCEMENT LEARNING ALGORITHMS

Just as much as DQN and DDQN are based on two tabular RL algorithms, so are the main contributions presented in this chapter. More specifically we extend two RL algorithms which were first introduced by Wiering [83] and then extended by Wiering and Van Hasselt [84] to the use of deep neural networks that serve as function approximators. Training these algorithms robustly is done by taking advantage of some of the techniques which have been reviewed in the previous section.

3.4.1 DQV-Learning

Our first contribution is the Deep Quality-Value (DQV) Learning algorithm, a novel DRL algorithm which aims at jointly approximating the V function alongside the Q function in an *on-policy* learning setting. This algorithm is based on the QV(λ) algorithm [83], a tabular RL algorithm which learns the V function via the simplest form of TD-Learning [67], and uses the estimates that are learned by this value

function to update the Q function in a Q-Learning resembling way. Specifically, after a transition $\langle s_t, a_t, r_t, s_{t+1} \rangle$, QV(λ) uses the TD(λ) learning rule [67] to update the V function for all states:

$$V(s) := V(s) + \alpha [r_t + \gamma V(s_{t+1}) - V(s_t)] e_t(s), \quad (13)$$

where α stands again for the learning rate and γ is the discount factor, while $e_t(s)$ are the elibility traces [24, 52, 85] that are necessary for keeping track if a particular state has occurred before a certain time-step or not. These are updated for all states as follows:

$$e_t(s) = \gamma \lambda e_{t-1}(s) + \eta_t(s), \quad (14)$$

where $\eta_t(s)$ is an indicator function that returns a value of 1 whether a particular state occurred at time t and 0 otherwise. Before updating the V function, QV(λ) updates the Q function first, and does this via the following update rule:

$$Q(s_t, a_t) := Q(s_t, a_t) + \alpha [r_t + \gamma V(s_{t+1}) - Q(s_t, a_t)]. \quad (15)$$

We take inspiration from this specific learning dynamic and aim at learning an approximation of both the V function, and the Q function, with two neural networks that are respectively parametrized by Φ and θ . To do so, we follow the same principles which have led to the development of the DQN algorithm and that reshape Eq. 8 to Eq. 9. Therefore, starting from Eq. 13, and after removing $e_t(s)$ for simplicity, we get the following objective function which is used by DQV for learning the state-value function:

$$L(\Phi) = \mathbb{E}_{\langle s_t, a_t, r_t, s_{t+1} \rangle \sim U(D)} \left[(r_t + \gamma V(s_{t+1}; \Phi^-) - V(s_t; \Phi))^2 \right], \quad (16)$$

while the following loss is minimized for learning the Q function when starting from Eq. 15:

$$L(\theta) = \mathbb{E}_{\langle s_t, a_t, r_t, s_{t+1} \rangle \sim U(D)} \left[(r_t + \gamma V(s_{t+1}; \Phi^-) - Q(s_t, a_t; \theta))^2 \right], \quad (17)$$

where D is again the Experience-Replay memory buffer, used for uniformly sampling batches of RL trajectories $\langle s_t, a_t, r_t, s_{t+1} \rangle$, and Φ^- is the target-network used for the construction of the TD-errors. Please note that the role of this target network is different from its role within the DQN algorithm. In DQV this network corresponds to a copy of the network which approximates the state-value function and not the state-action value function. It is also worth noting that both networks learn from the same TD-target which comes in the following form:

$$y_t^{DQV} = r_t + \gamma V(s_{t+1}; \Phi^-). \quad (18)$$

The gradient with respect to both loss functions can be easily expressed similarly as done in Eq. 11 for the DQN algorithm.

3.4.2 DQV-Learning with Multilayer Perceptrons

We start by exploring whether this learning dynamic of jointly approximating two value functions simultaneously, and let the Q function bootstrap from the TD-targets that are learned from the V network can yield successful results on a set of preliminary experiments. To do so, we use two classic control problems that are well known in the RL literature: Acrobot [68] and Cartpole [5] with both environments being provided by the Open-AI Gym package [9]. We approximate the V function and the Q function with a two hidden layer Multilayer Perceptron (MLP) that is activated by a ReLU non linearity ($f(x) = \max(0, x)$) and compare the performance of DQV to the one of the DQN and the DDQN algorithms, which use the same MLP but for approximating the Q function only. Given the simplicity of these two control problems we did not integrate DQV with the target network Φ^- yet. Our preliminary results reported in Fig. 13, show the benefits that can come from training two separate networks with the update rules reported in Eq.16 and Eq.17. We can in fact observe that on both control problems DQV-Learning outperforms DQN and DDQN, by converging significantly faster.

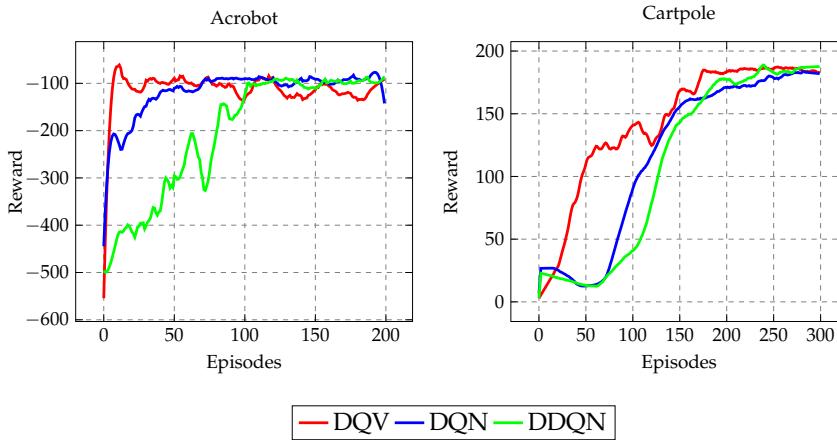


Figure 14: Our preliminary results that show the benefits in terms of convergence time that can come from jointly approximating the V function alongside the Q function. We can observe that the DQV-Learning algorithm yields faster convergence when compared to popular algorithms which only approximate the Q function: DQN and DDQN.

3.4.3 DQV-Max Learning

Based on the successful results presented in Fig. 13 that highlight the potential benefits that could come from jointly approximating two value functions over one, we now introduce the Deep Quality-Value-Max (DQV-Max) algorithm, a novel DRL algorithm which builds on

top of some of the ideas that characterize DQV. Similarly as done for DQV, we still aim at jointly learning an approximation of the V function and the Q function, but in this case, the goal is to do this with an *off-policy* learning scheme. To construct this algorithm we take inspiration from the QV-Max RL algorithm introduced by Wiering and Van Hasselt [84]. The key component of QV-Max is the use of the $\max_{a \in \mathcal{A}} Q(s_{t+1}, a)$ operator, which makes RL algorithms learn *off-policy*. We use this operator when approximating the V function and for computing TD-errors which correspond to the ones that are also used by the DQN algorithm. However, within DQV-Max, these TD-errors are used by the state-value network and not by the state-action value network. This results in the following loss which is used for learning the V function:

$$L(\Phi) = \mathbb{E}_{(s_t, a_t, r_t, s_{t+1}) \sim U(D)} \left[(r_t + \gamma \max_{a \in \mathcal{A}} Q(s_{t+1}, a; \theta^-) - V(s_t; \Phi))^2 \right]. \quad (19)$$

In this case the target network θ^- corresponds to the same target network that is used by DQN. The TD-error $r_t + \gamma \max_{a \in \mathcal{A}} Q(s_{t+1}, a; \theta^-)$ is however only used for learning the V function. When it comes to the Q function we use the same update rule that is presented in Eq. 17 with the only difference being that in this case no Φ^- target network is used. Despite requiring the computation of two different targets for learning, we noticed that DQV-Max did not benefit from using two distinct target networks, therefore its loss function for approximating the Q function is simply:

$$L(\theta) = \mathbb{E}_{(s_t, a_t, r_t, s_{t+1}) \sim U(D)} \left[(r_t + \gamma V(s_{t+1}; \Phi) - Q(s_t, a_t; \theta))^2 \right]. \quad (20)$$

The pseudocode of both DQV and DQV-Max is presented at the end of this thesis in Algorithm ?? which can be found in Appendix. The pseudocode is an adaptation of a standard DRL training loop which corresponds to what is usually presented within the literature [45]. We just make explicit use of the hyperparameters `total_a` and `c` which ensure that enough actions have been performed by the agent before updating the weights of the target network. We also ensure via the hyperparameter `total_e`, that enough episodes are stored within the memory buffer (which has capacity \mathcal{N}) before starting to optimize the neural networks.

3.5 RESULTS

3.5.1 Global Evaluation

We evaluate the performance of DQV and DQV-Max on a subset of 15 games coming from the popular Atari-2600 benchmark [6]. Our newly introduced algorithms are compared against DQN and DDQN. To keep all the comparisons as fair as possible we follow the same experimental setup and evaluation protocol which was used in [45] and [77]. The only difference between DQV and DQV-Max, and DQN and DDQN is the exploration schedule which is used. Differently from the latter two algorithms, which use an epsilon-greedy strategy which has an ϵ starting value of 1.0, DQV and DQV-Max’s exploration policy starts with an initial ϵ value of 0.5. All other hyperparameters, ranging from the size of the Experience-Replay memory buffer to the architectures of the neural networks, are kept the same among all algorithms. We refer the reader to the original DQN paper [45] for an in-depth overview of all these hyperparameters. The performance of the algorithms is tested based on the popular no-op action evaluation regime. At the end of the training, the learned policies are tested over a series of episodes for a total amount of 5 minutes of emulator time. All testing episodes start by executing a set of partially random actions to test the level of generalization of the learned policies. We present our results in Table 7 where the best performing algorithm is reported in a green cell while the second-best performing algorithm is reported in a yellow cell. As is common within the DRL literature, the table also reports the scores which would be obtained by an expert human player and by a random policy. When the scores over games are equivalent, we report in the green and yellow cells the fastest and second fastest algorithm with respect to its convergence time.

We can start by observing that DQV and DQV-Max successfully master all the environments on which they have been tested, with the only exception being the Montezuma’s Revenge game. It is well-known that this game requires more sophisticated exploration strategies than the epsilon-greedy one [19], and was also not mastered by DQN and DDQN when these algorithms were introduced. We can also observe that there is no algorithm which performs best on all the tested environments even though, as highlighted by the green and yellow cells, the algorithms of the DQV-family seem to generally perform better than DQN and DDQN, with DQV-Max being the overall best performing algorithm in our set of experiments. When either DQV or DQV-Max are not the best performing algorithm (see for example the Boxing and CrazyClimber environments), we can still observe that our algorithms managed to converge to a policy which is not significantly worst than the one learned by DQN and DDQN. There is however one exception being the RoadRunner envi-

ronment. In fact, in this game, DDQN significantly outperforms DQV and DQV-Max. It is also worth noting the results on the BankHeist and Enduro environments. Both DQN and DDQN failed to achieve super-human performance on these games, while DQV and DQV-Max successfully managed to obtain a significantly higher score than the one obtained by a professional human player. On the BankHeist environment DQV and DQV-Max obtain ≈ 400 points more than an expert human player, while on the Enduro environment their performance is almost three times better than the one obtained by DQN and DDQN.

Table 7: The results obtained by DQV and DQV-Max on a subset of 15 Atari games. We can see that our newly introduced algorithms have a comparable, and often even better performance than DQN and DDQN. As highlighted by the green cells the overall best performing algorithm in our set of experiments is DQV-Max while the second-best performing algorithm is DQV (as reported by the yellow cells). Specific attention should be given to the games BankHeist and Enduro where DQV and DQV-Max are the only algorithms which can master the game with a final super-human performance.

Environment	Random	Human	DQN [45]	DDQN [77]	DQV	DQV-Max
Asteroids	719.10	13156.70	1629.33	930.60	1445.40	1846.08
Bank Heist	14.20	734.40	429.67	728.30	1236.50	1118.28
Boxing	0.10	4.30	71.83	81.70	78.66	80.15
Crazy Climber	10780.50	35410.50	114103.33	101874.00	108600.00	1000131.00
Enduro	0.00	309.60	301.77	319.50	829.33	875.64
Fishing Derby	-91.70	5.50	-0.80	20.30	1.12	20.42
Frostbite	65.20	4334.70	328.33	241.50	271.86	281.36
Gopher	257.60	2321.00	8520.00	8215.40	8230.30	7940.00
Ice Hockey	-11.20	0.90	-1.60	-2.40	-1.88	-1.12
James Bond	29.00	406.70	576.67	438.00	372.41	440.80
Montezuma's Revenge	0.00	4366.70	0.00	0.00	0.00	0.00
Ms. Pacman	307.30	15693.40	2311.00	3210.00	3590.00	3390.00
Pong	-20.70	9.30	18.90	21.00	21.00	21.00
Road Runner	11.50	7845.00	18256.67	48377.00	39290.00	20700.00
Zaxxon	32.50	9173.30	4976.67	10182.00	10950.00	8487.00

3.5.2 Convergence Time

While DRL algorithms have certainly obtained impressive results on the Atari-2600 benchmark, it is also true that the amount of training time which is required by these algorithms can be very long. Over the years, several techniques, ranging from Prioritized Experience Replay (PER) [80] to the Rainbow extensions introduced by Hessel et al. [29], have been proposed to reduce the training time of DRL algorithms. It is therefore natural to investigate whether jointly approximating the V function alongside the Q function can lead to significant ben-

efits in this behalf. Unlike the Q function, the state-value function is not dependent on the set of possible actions that the agent may take, and therefore requires fewer parameters to converge. Since DQV and DQV-Max use the estimates of the V network to train the Q function, it is possible that the Q function could directly benefit from these estimates and as a result converge faster than when regressed towards itself (as happens in DQN).

We use two self-implemented versions of DQN and DDQN for comparing the convergence time that is required during training by all the tested algorithms on three increasingly complex Atari games: Boxing, Pong and Enduro. Our results, reported in Fig. 14, show that DQV and DQV-Max converge significantly faster than DQN and DDQN, therefore confirming the preliminary results which we reported in Fig. ??, and highlighting once again the benefits of jointly approximating two value functions instead of one when it comes to the overall convergence time that is required by the algorithms. Even though, as presented in Table 7, DQV and DQV-Max do not always significantly outperform DQN and DDQN in terms of the final cumulative reward which is obtained, it is worth noting that these algorithms require significantly less training episodes to converge on all tested games. This benefit makes our two novel algorithms faster alternatives within model-free DRL.

3.5.3 Quality of the Learned Value Functions

It is well-known that the combination of RL algorithms with function approximators can yield DRL algorithms that diverge. The popular Q-Learning algorithm is known to result in unstable learning both if linear [75] and non-linear functions are used when approximating the Q function [78]. This divergence according to Sutton and Barto [69] is caused by the interplay of three elements that are known as the ‘*Deadly Triad*’ of DRL. The elements of this triad are:

- *a function approximator*: which is used for learning an approximation of a value function that could not be learned in the tabular RL setting due to a too large state-action space.
- *bootstrapping*: when the algorithms use a future estimated value for learning the same kind of estimate.
- *off-policy learning*: when a future estimated value is different from the one which would be computed by the policy the agent is following.

Van Hasselt et al. [78] have shown that the ‘*Deadly Triad*’ is responsible for enhancing one of the most popular biases that characterize the Q-Learning algorithm: the overestimation bias of the Q function [76]. It is therefore natural to study how DQV and DQV-Max relate to

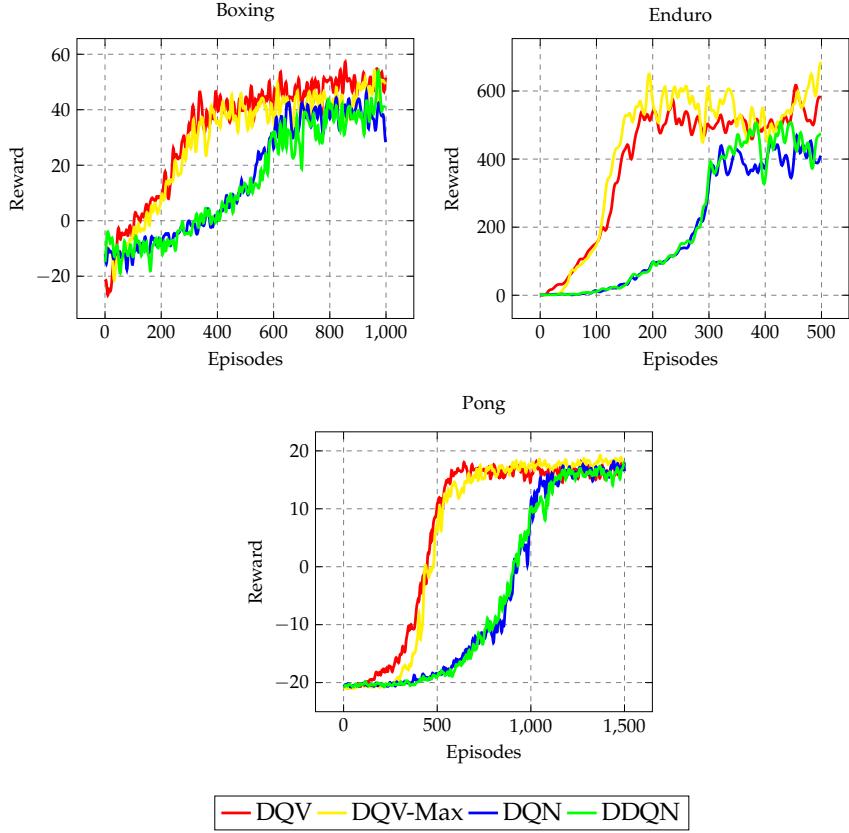


Figure 15: Learning curves obtained during training on three different Atari games by DQV and DQV-Max, and DQN and DDQN. We can observe that on these games both DQV and DQV-Max converge significantly faster than DQN and DDQN and that they obtain higher cumulative rewards on the Enduro environment.

the ‘*Deadly Triad*’ of DRL, and to investigate up to what extent these algorithms suffer from the overestimation bias of the Q function. To do this we monitor the estimates that are given by the network that is responsible for approximating the Q function. More specifically, at training time, we compute the averaged $\max_{a \in \mathcal{A}} Q(s_{t+1}, a)$ over a set (n) of full evaluation episodes as defined by

$$\frac{1}{n} \sum_{t=1}^n \max_{a \in \mathcal{A}} Q(s_{t+1}, a; \theta). \quad (21)$$

As suggested by Van Hasselt, Guez, and Silver [77] these estimates can then be compared to the averaged discounted return of all visited states that comes from an agent that has already concluded training. By analyzing whether the Q values which are estimated while training differ from the ones which should be predicted by the end of it, it is possible to quantitatively characterize the level of divergence of DRL algorithms. We report our results in Figs. 15, 16, 17 and 18 where the black full lines correspond to the value estimates that come from each algorithm at training time, while the coloured lines correspond

to the actual averaged discounted return that is given by an already trained agent.

We can start by observing that the values denoting the averaged discounted return obtained by each algorithm differ among agents. This is especially the case when it comes to the Enduro environment, and is a result which is in line with what has been presented in Table 5: DQV and DQV-Max lead to better final policies than DQN and DDQN. Furthermore, when we compare these baseline values to the value estimates that are obtained during training, we can observe that the ones obtained by the DQN algorithm significantly diverge from the ones which should be predicted by the end of training. This behavior is known to be caused by the overestimation bias of the Q function which can be corrected by the DDQN algorithm. By analyzing the value estimates of DQV and DQV-Max we can observe that both algorithms produce value estimates which are more similar to the ones computed by DDQN than to the ones given by DQN. This is especially the case for DQV, in fact its value estimates nicely correspond to the averaged discounted return baseline, both on the Pong environment and on the Enduro environment. The estimates coming from DQV-Max, however, seem to diverge more when compared to DQV and DDQN's ones. This is clearer on the Enduro environment, where the algorithm does show some divergence. However, we can also observe that this divergence is less strong when compared to DQN's one. The value estimates of the latter algorithm keep growing over time, while DQV-Max's ones get bounded while training progresses. This results in smaller estimated Q values. We believe that there are mainly two reasons why our algorithms suffer less from the overestimation bias of the Q function. When it comes to DQV, we believe that this algorithm suffers less from this bias since it is an *on-policy* learning algorithm. Such algorithms are trained on exploration actions with lower Q values. Because of its *on-policy* learning scheme, DQV also does not present one element of the '*Deadly Triad*', which might help reducing divergence. When it comes to DQV-Max, we believe that the reason why this algorithm does not diverge as much as DQN can be found in the way it approximates the Q function. One key component of the '*Deadly Triad*', is that divergence occurs if the Q function is learned by regressing towards itself. As given by Eq. 20 we can see that this does not hold for DQV-Max, since the Q function bootstraps with respect to estimates that come from the V network. We believe that this specific learning dynamic, which also holds for the DQV algorithm, makes our algorithms less prone to estimate large Q values.

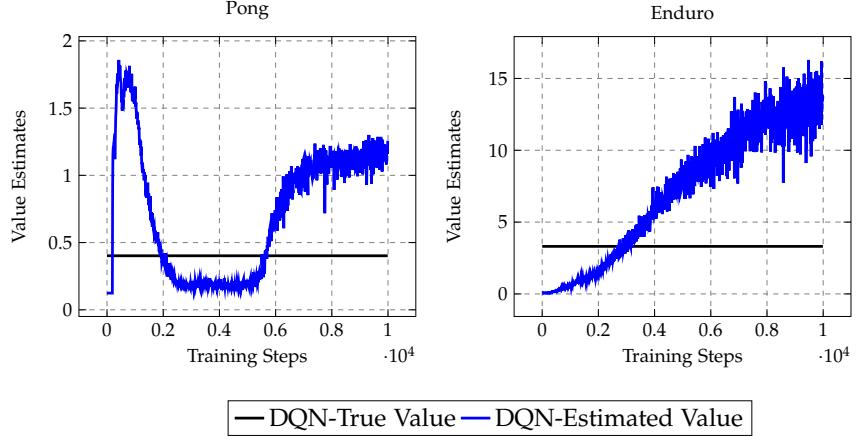


Figure 16: Results investigating the extent to which the DQN algorithm suffers from the overestimation bias of the Q function. We can observe that on the Pong environment during the early stages of training, the $\max_{a \in \mathcal{A}} Q(s_{t+1}, a)$ estimates quickly grow, while on the Enduro game the values estimated by the Q network keep indefinitely growing, therefore making the algorithm significantly diverge from the real return that is obtained by a trained agent.

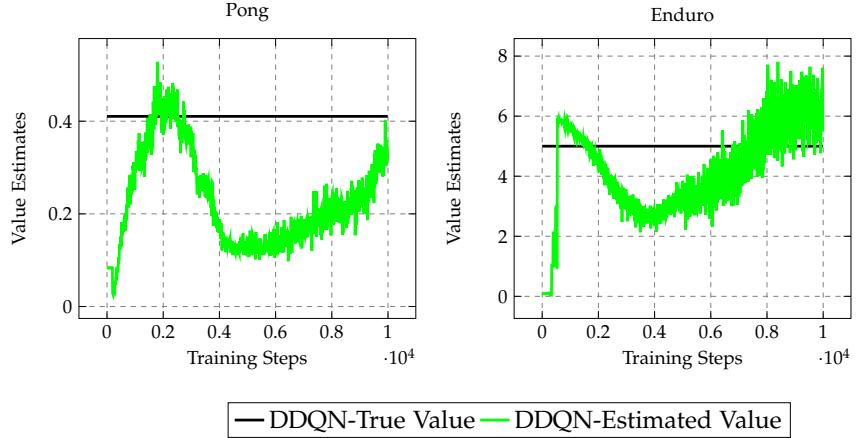


Figure 17: Results investigating the extent to which the DDQN algorithm suffers from the overestimation bias of the Q function. We can observe that compared to the analysis presented in Fig. 15, the DDQN algorithm prevents its Q -Network from diverging since on both Atari environments the $\max_{a \in \mathcal{A}} Q(s_{t+1}, a)$ estimates do not diverge from the observed real return of a trained agent. Results that replicate the findings reported by Van Hasselt et al. [78].

3.6 ADDITIONAL STUDIES

As introduced in Sec. 3.4 DQV and DQV-Max use two separate neural networks for approximating the Q function and the V function. To verify whether two different architectures are needed for making both algorithms perform well, we have experimented with a series of variants of the DQV-Learning algorithm. The aim of these exper-

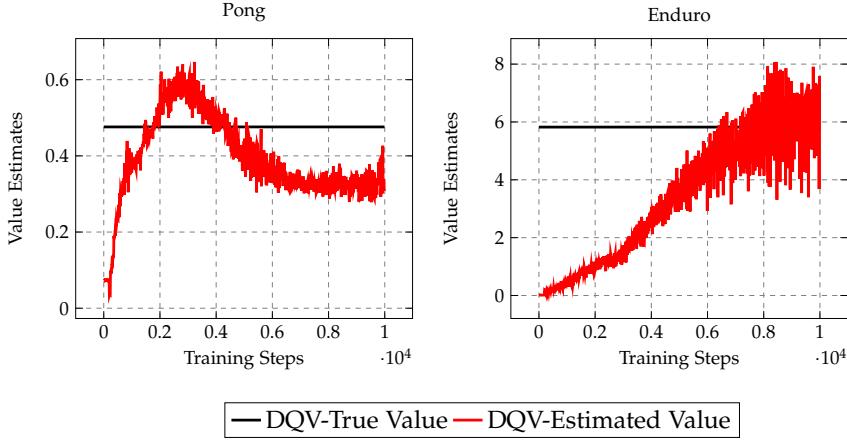


Figure 18: Results investigating the extent to which the DQV algorithm suffers from the overestimation bias of the Q function. We can observe that the performance of the algorithm is similar to the one observed in Fig. 16 for the DDQN algorithm. On both environments the estimated cumulative reward does not diverge from the real return that is obtained by the end of training, therefore suggesting that DQV-Learning does not suffer from the overestimation bias of the Q function. It is also worth noting the difference between the real return obtained by the DQN and the DDQN algorithms on the Enduro environment, and the one obtained by DQV. As can be seen by the black line, the real return obtained by a DQV agent is higher than DQN and DDQN’s one, a result which shows that DQV converges to a better policy than DQN and DDQN.

iments is that of reducing the number of trainable parameters that are required by the original version of DQV, and investigate whether its performance could get harmed when reducing the capacity of the algorithm. The studied DQV’s extensions are the following:

1. *Hard-DQV*: a version of DQV which uses one single common neural network for approximating both the Q and the V functions. An additional output node, needed for estimating the value of a state, is added next to the output nodes which estimate the different Q values. The parameters of this algorithm are therefore ‘hardly-shared’ among the agent, and provide the benefit of halving the total amount of trainable parameters of DQV. The different outputs of the network get then alternatively optimized according to Eq. 16 and 17.
2. *Dueling-DQV*: a slightly more complicated version of Hard-DQV which adds one specific hidden layer before the output nodes that estimate the Q and V functions. In this case, the outputs of the neural network which learn one of the two value functions, partly benefit from some specific weights that are not shared within the neural network. This approach is similar to

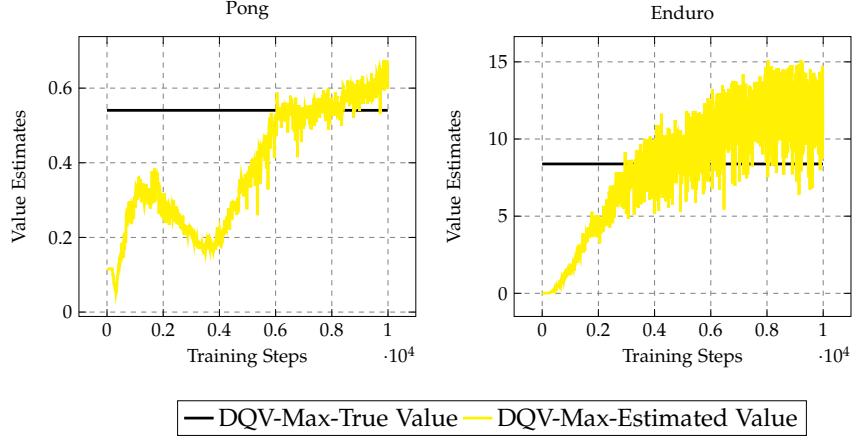


Figure 19: Results investigating the extent to which the DQV-Max algorithm suffers from the overestimation bias of the Q function. We can observe that on the Pong environment the value estimates of the algorithm are comparable to the ones of DDQN and DQV, therefore showing the DQV-Max also diverges significantly less than DQN. On the Enduro environment we can observe that the algorithm does diverge, although, differently from what is reported in Fig. 15, the $\max_{a \in \mathcal{A}} Q(s_{t+1}, a)$ estimates seem to converge towards an upper bound (≈ 15). Similarly to what is reported in Fig. 17 we can again observe that the real return obtained by a trained agent is higher compared to the one obtain by DQN, DDQN and DQV, therefore confirming the results presented in Table 7 which see the DQV-Max algorithm as the best performing algorithm on the Enduro game.

the one used by the ‘Dueling-Architecture’ presented by Wang et al. [80], therefore the name Dueling-DQV. While it is well established that three convolutional layers are needed [45, 77] for learning the Q function, the same might not be true when it comes to learning the V function. We thus report experiments with three different versions of Dueling-DQV: Dueling-1st, Dueling-2nd, and Dueling-3rd. The difference between these methods is simply the location of the hidden layer which precedes the output that learns the V function. It can be positioned after the first convolutional layer, the second or the third one. Training this architecture is done as for Hard-DQV.

3. *Tiny-DQV*: the neural architectures used by DQV and DQV-Max that approximate the V function and the Q function follow the one which was initially introduced by the DQN algorithm [45]. This corresponds to a three-hidden layer convolutional neural network which is followed by a fully connected layer of 512 hidden units. The first convolutional layer has 32 channels while the last two layers have 64 channels. In Tiny-DQV we reduce the number of trainable parameters of DQV by reducing the number of channels at each convolution operation. Tiny-DQV

only uses 8 channels after the first convolutional layer and 16 at the second and third convolutional layers. Furthermore, the size of the final fully connected layer is reduced to only 128 hidden units. The choice of this architecture is motivated by the work presented in [78] which studies the role of the capacity of the DDQN algorithm. Unlike the Hard-DQV and Dueling-DQV extensions, the parameters of Tiny-DQV are not shared at all among the networks that are responsible for approximating the V function and the Q function.

The results obtained by these alternative versions of DQV are presented in Figs. 19, 20 and 21 where we report the learning curves obtained by the tested algorithms on six different Atari games. Each DQV extension is directly compared to the original DQV algorithm. We can observe that all the extensions of DQV, which aim at reducing the number of trainable parameters of the algorithm, fail in performing as well as the original DQV algorithm. Starting from Fig. 19 we can observe that *Hard-DQV* does not only yield significantly lower rewards (see the results obtained on *Boxing*) but also presents more unstable training (as highlighted by the results obtained on the *Pong* environment). Lower rewards and unstable training also characterize the *Tiny-DQV* algorithm (see results on *BankHeist* and *CrazyClimber* reported in Fig. 21). Overall the most promising extensions of DQV are its *Dueling* counterparts, we have observed in particular that the best performing architecture over most of our experiments was the *Dueling-DQV-3rd* one. As can be seen by the results reported in Fig. 20 on the *Pong* environment we can observe that *Dueling-DQV-3rd* has a comparable performance to DQV, even though it converges slower. Unfortunately, *Dueling-DQV-3rd* still shows some limitations, in particular when tested on more complicated environments such as *Enduro*, we can observe that it under-performs DQV with ≈ 200 points. It is also worth mentioning that the idea of approximating the V function before the Q function explored by *Dueling-DQV-1st* and *Dueling-DQV-2nd* yielded negative results.

3.7 DISCUSSION AND CONCLUSION

We have presented two novel model-free DRL algorithms which in addition to learning an approximation of the Q function also aim at learning an approximation of the V function. We have compared DQV and DQV-Max Learning to DRL algorithms which only learn an approximation of the Q function, and showed the benefits which come from jointly approximating two value functions over one. Our newly introduced algorithms learn significantly faster than DQN and DDQN and show that approximating both the V function and the Q function can yield significant benefits both in an *on-policy* learning setting as in an *off-policy* learning one. This specific training dynamic

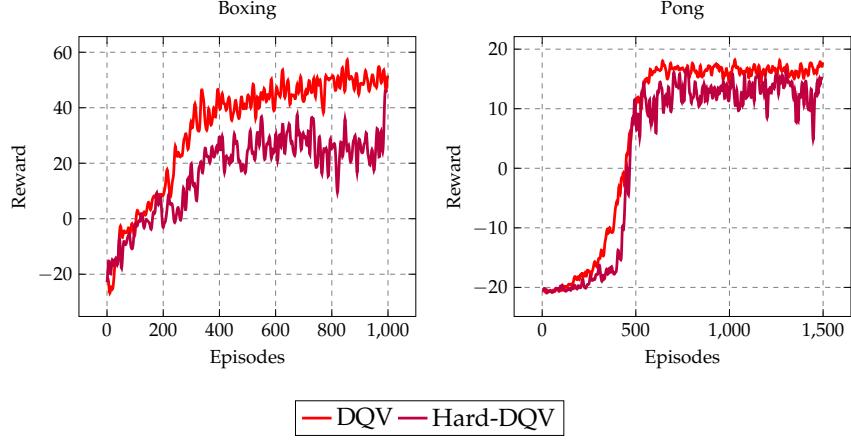


Figure 20: Our results which aim to approximate the V and the Q function with a unique, shared parameterized network, an approach that is heavily inspired by multi-task learning studies that can be found in supervised learning [10, 49, 91]. We can see that this extension of DQV, named Hard-DQV, significantly underperforms the original DQV-Learning algorithm.

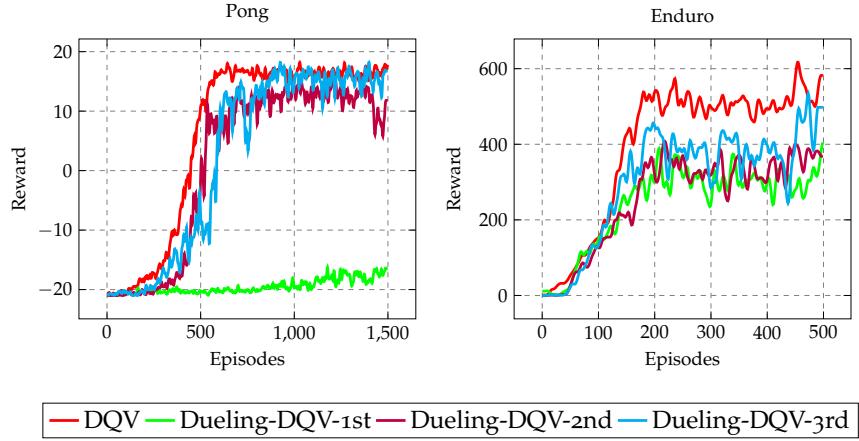


Figure 21: Our extensions of DQV that aim to reduce the amount of trainable parameters of the algorithm by following an approach similar to the one presented by Wang et al. [80] when “Dueling Networks” for DRL have been introduced. We can observe that among all the three Dueling-DQV extensions, only the Dueling-DQV-3rd one yielded good performance, but as highlighted by the results obtained on the Enduro environment, its performance is still inferior when compared to the one of the original DQV algorithm.

allows for a better learned Q function which makes DQV and DQV-Max less prone to estimate unrealistically large Q values. All these benefits come however at a price: to successfully learn two value functions, two separate neural networks with enough capacity are required.

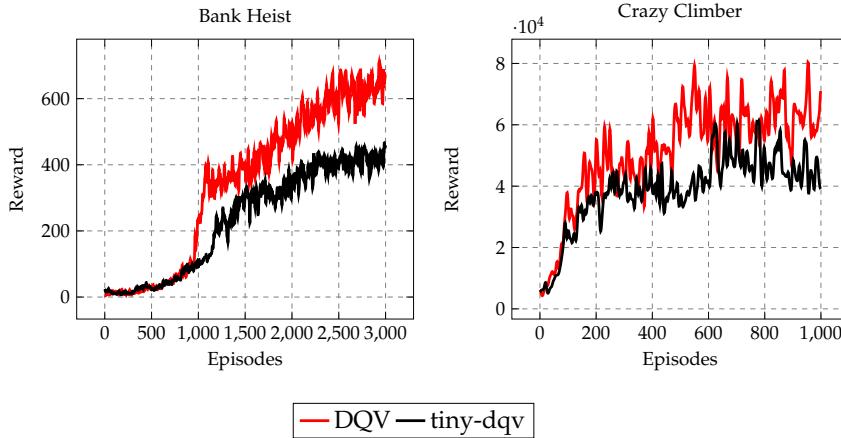


Figure 22: Learning curves obtained when reducing the capacity of the convolutional networks that approximate the V and the Q functions. We can observe that albeit each value function is approximated with its own parametrized network, the tiny-dqv extension still yields worse performance. These results highlight that it is not sufficient to simply have two separate neural networks for DQV to perform well, but that a crucial role in DQV’s performance is played by the capacity of the networks that are used as well.

We identify several directions for further research that focus on the following points: an integration of the algorithms of the DQV-family with all the extensions which have improved the DQN algorithm over the years; an integration of DQV and DQV-Max within an Actor-Critic framework which will allow us to tackle continuous-control problems, and lastly, a study of how the algorithms of the DQV-family will perform in a Batch-DRL setting. It has been shown that DRL algorithms fail when learning from a fixed data set of trajectories instead of dynamically interacting with the environment [23]. This is due to a phenomenon known as extrapolation error. We will investigate to what extent jointly learning two value functions instead of one will cope with this additional DRL bias.

Part III
APPENDIX

BIBLIOGRAPHY

- [1] Martín Abadi, Paul Barham, Jianmin Chen, Zhifeng Chen, Andy Davis, Jeffrey Dean, Matthieu Devin, Sanjay Ghemawat, Geoffrey Irving, Michael Isard, et al. “TensorFlow: A System for Large-Scale Machine Learning.” In: *OSDI*. Vol. 16. 2016, pp. 265–283.
- [2] Joshua Achiam, Ethan Knight, and Pieter Abbeel. “Towards Characterizing Divergence in Deep Q-Learning.” In: *arXiv preprint arXiv:1903.08894* (2019).
- [3] Sandro Ackermann, Kevin Schawinski, Ce Zhang, Anna K Weigel, and M Dennis Turp. “Using transfer learning to detect galaxy mergers.” In: *Monthly Notices of the Royal Astronomical Society* (2018).
- [4] Nancy Allen. “Collaboration through the Colorado digitization project.” In: *First Monday* 5.6 (2000).
- [5] Andrew G Barto, Richard S Sutton, and Charles W Anderson. “Neuronlike adaptive elements that can solve difficult learning control problems.” In: *IEEE transactions on systems, man, and cybernetics* 5 (1983), pp. 834–846.
- [6] Marc G Bellemare, Yavar Naddaf, Joel Veness, and Michael Bowling. “The arcade learning environment: An evaluation platform for general agents.” In: *Journal of Artificial Intelligence Research* 47 (2013), pp. 253–279.
- [7] Francesco Bidoia, Matthias Sabatelli, Amirhossein Shantia, Marco A. Wiering, and Lambert Schomaker. “A Deep Convolutional Neural Network for Location Recognition and Geometry based Information.” In: *Proceedings of the 7th International Conference on Pattern Recognition Applications and Methods, ICPRAM 2018, Funchal, Madeira - Portugal, January 16-18, 2018*. 2018, pp. 27–36.
- [8] Mariusz Bojarski, Anna Choromanska, Krzysztof Choromanski, Bernhard Firner, Larry Jackel, Urs Muller, and Karol Zieba. “VisualBackProp: efficient visualization of CNNs.” In: *arXiv preprint arXiv:1611.05418* (2016).
- [9] Greg Brockman, Vicki Cheung, Ludwig Pettersson, Jonas Schneider, John Schulman, Jie Tang, and Wojciech Zaremba. “Openai gym.” In: *arXiv preprint arXiv:1606.01540* (2016).
- [10] Rich Caruana. “Multitask learning.” In: *Machine learning* 28.1 (1997), pp. 41–75.

- [11] Rich Caruana, Steve Lawrence, and C Lee Giles. "Overfitting in neural nets: Backpropagation, conjugate gradient, and early stopping." In: *Advances in neural information processing systems*. 2001, pp. 402–408.
- [12] François Chollet. "Xception: Deep learning with depthwise separable convolutions." In: *arXiv preprint* (2016).
- [13] François Chollet et al. *Keras*. 2015.
- [14] Jia Deng, Wei Dong, Richard Socher, Li-Jia Li, Kai Li, and Li Fei-Fei. "Imagenet: A large-scale hierarchical image database." In: *Computer Vision and Pattern Recognition, 2009. CVPR 2009. IEEE Conference on*. IEEE. 2009, pp. 248–255.
- [15] Jeff Donahue, Yangqing Jia, Oriol Vinyals, Judy Hoffman, Ning Zhang, Eric Tzeng, and Trevor Darrell. "Decaf: A deep convolutional activation feature for generic visual recognition." In: *International conference on machine learning*. 2014, pp. 647–655.
- [16] Xin Dong, Shangyu Chen, and Sinno Pan. "Learning to prune deep neural networks via layer-wise optimal brain surgeon." In: *Advances in Neural Information Processing Systems*. 2017, pp. 4857–4867.
- [17] Stamatatos Efstathios. "A survey of modern authorship attribution methods." In: *Journal of the American Society for Information Science and Technology* 3 (2009), pp. 538–556. doi: [10.1002/asi.21001](https://doi.org/10.1002/asi.21001).
- [18] Mark Everingham, Luc Van Gool, Christopher KI Williams, John Winn, and Andrew Zisserman. "The pascal visual object classes (voc) challenge." In: *International journal of computer vision* 88.2 (2010), pp. 303–338.
- [19] Meire Fortunato, Mohammad Gheshlaghi Azar, Bilal Piot, Jacob Menick, Ian Osband, Alex Graves, Vlad Mnih, Remi Munos, Demis Hassabis, Olivier Pietquin, et al. "Noisy networks for exploration." In: *arXiv preprint arXiv:1706.10295* (2017).
- [20] Jonathan Frankle and Michael Carbin. "The lottery ticket hypothesis: Finding sparse, trainable neural networks." In: *arXiv preprint arXiv:1803.03635* (2018).
- [21] Jonathan Frankle, Gintare Karolina Dziugaite, Daniel M Roy, and Michael Carbin. "Linear mode connectivity and the lottery ticket hypothesis." In: *arXiv preprint arXiv:1912.05671* (2019).
- [22] Jonathan Frankle, G Karolina Dziugaite, DM Roy, and M Carbin. "Stabilizing the Lottery Ticket Hypothesis." In: *arXiv preprint arXiv:1903.01611* (2019).
- [23] Scott Fujimoto, Edoardo Conti, Mohammad Ghavamzadeh, and Joelle Pineau. "Benchmarking Batch Deep Reinforcement Learning Algorithms." In: *arXiv preprint arXiv:1910.01708* (2019).

- [24] Matthieu Geist, Bruno Scherrer, et al. "Off-policy learning with eligibility traces: a survey." In: *J. Mach. Learn. Res.* 15.1 (2014), pp. 289–333.
- [25] Varun Gohil, S Deepak Narayanan, and Atishay Jain. "One ticket to win them all: generalizing lottery ticket initializations across datasets and optimizers." In: *ReScience-C* (2020).
- [26] Song Han, Huizi Mao, and William J Dally. "Deep compression: Compressing deep neural networks with pruning, trained quantization and huffman coding." In: *arXiv preprint arXiv:1510.00149* (2015).
- [27] Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. "Delving deep into rectifiers: Surpassing human-level performance on imagenet classification." In: *Proceedings of the IEEE international conference on computer vision*. 2015, pp. 1026–1034.
- [28] Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. "Deep residual learning for image recognition." In: *Proceedings of the IEEE conference on computer vision and pattern recognition*. 2016, pp. 770–778.
- [29] Matteo Hessel, Joseph Modayil, Hado Van Hasselt, Tom Schaul, Georg Ostrovski, Will Dabney, Dan Horgan, Bilal Piot, Mohammad Azar, and David Silver. "Rainbow: Combining improvements in deep reinforcement learning." In: *Thirty-Second AAAI Conference on Artificial Intelligence*. 2018.
- [30] Gao Huang, Zhuang Liu, Kilian Q Weinberger, and Laurens van der Maaten. "Densely connected convolutional networks." In: *Proceedings of the IEEE conference on computer vision and pattern recognition*. Vol. 1. 2. 2017.
- [31] Gary B Huang, Manu Ramesh, Tamara Berg, and Erik Learned-Miller. *Labeled faces in the wild: A database for studying face recognition in unconstrained environments*. Tech. rep. Technical Report 07-49, University of Massachusetts, Amherst, 2007.
- [32] Philipp Kainz, Harald Burgsteiner, Martin Asslaber, and Helmut Ahammer. "Training echo state networks for rotation-invariant bone marrow cell classification." In: *Neural Computing and Applications* 28.6 (2017), pp. 1277–1292.
- [33] Simon Kornblith, Jonathon Shlens, and Quoc V Le. "Do Better ImageNet Models Transfer Better?" In: *arXiv preprint arXiv:1805.08974* (2018).
- [34] Alex Krizhevsky, Ilya Sutskever, and Geoffrey E Hinton. "Imagenet classification with deep convolutional neural networks." In: *Advances in neural information processing systems*. 2012, pp. 1097–1105.
- [35] Yann LeCun, Yoshua Bengio, and Geoffrey Hinton. "Deep learning." In: *nature* 521.7553 (2015), p. 436.

- [36] Yuxi Li. "Deep reinforcement learning: An overview." In: *arXiv preprint arXiv:1701.07274* (2017).
- [37] Ji Lin, Yongming Rao, Jiwen Lu, and Jie Zhou. "Runtime neural pruning." In: *Advances in Neural Information Processing Systems*. 2017, pp. 2181–2191.
- [38] Long-Ji Lin. "Self-improving reactive agents based on reinforcement learning, planning and teaching." In: *Machine learning* 8.3-4 (1992), pp. 293–321.
- [39] Tsung-Yi Lin, Michael Maire, Serge Belongie, James Hays, Pietro Perona, Deva Ramanan, Piotr Dollár, and C Lawrence Zitnick. "Microsoft coco: Common objects in context." In: *European conference on computer vision*. Springer. 2014, pp. 740–755.
- [40] Lin Ma, Zhengdong Lu, Lifeng Shang, and Hang Li. "Multi-modal convolutional neural networks for matching image and sentence." In: *Proceedings of the IEEE international conference on computer vision*. 2015, pp. 2623–2631.
- [41] Raphaël Marée, Loïc Rollus, Benjamin Stévens, Renaud Hoyoux, Gilles Louppe, Rémy Vandaele, Jean-Michel Begon, Philipp Kainz, Pierre Geurts, and Louis Wehenkel. "Collaborative analysis of multi-gigapixel imaging data using Cytomine." In: *Bioinformatics* 32.9 (2016), pp. 1395–1401.
- [42] Dominic Masters and Carlo Luschi. "Revisiting Small Batch Training for Deep Neural Networks." In: *arXiv preprint arXiv:1804.07612* (2018).
- [43] Rahul Mehta. "Sparse Transfer Learning via Winning Lottery Tickets." In: *arXiv preprint arXiv:1905.07785* (2019).
- [44] Thomas Mensink and Jan Van Gemert. "The rijksmuseum challenge: Museum-centered visual recognition." In: *Proceedings of International Conference on Multimedia Retrieval*. 2014, pp. 451–454.
- [45] Volodymyr Mnih, Koray Kavukcuoglu, David Silver, Andrei A Rusu, Joel Veness, Marc G Bellemare, Alex Graves, Martin Riedmiller, Andreas K Fidjeland, Georg Ostrovski, et al. "Human-level control through deep reinforcement learning." In: *Nature* 518.7540 (2015), p. 529.
- [46] Pavlo Molchanov, Stephen Tyree, Tero Karras, Timo Aila, and Jan Kautz. "Pruning convolutional neural networks for resource efficient inference." In: *arXiv preprint arXiv:1611.06440* (2016).
- [47] Ari Morcos, Haonan Yu, Michela Paganini, and Yuandong Tian. "One ticket to win them all: generalizing lottery ticket initializations across datasets and optimizers." In: *Advances in Neural Information Processing Systems*. 2019, pp. 4933–4943.

- [48] Romain Mormont, Pierre Geurts, and Raphaël Marée. "Comparison of deep transfer learning strategies for digital pathology." In: *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition Workshops*. 2018, pp. 2262–2271.
- [49] Romain Mormont, Pierre Geurts, and Raphaël Marée. "Multi-task pre-training of deep neural networks for digital pathology." In: *IEEE journal of biomedical and health informatics* (2020).
- [50] Sinno Jialin Pan and Qiang Yang. "A survey on transfer learning." In: *IEEE Transactions on knowledge and data engineering* (2010), pp. 1345–1359.
- [51] Ross Parry. "Digital heritage and the rise of theory in museum computing." In: *Museum management and Curatorship* (2005), pp. 333–348.
- [52] Jing Peng and Ronald J Williams. "Incremental multi-step Q-learning." In: *Machine Learning Proceedings 1994*. Elsevier, 1994, pp. 226–232.
- [53] Fred Phillips and Brandy Mackintosh. "Wiki Art Gallery, Inc.: A case for critical thinking." In: *Issues in Accounting Education* 26.3 (2011), pp. 593–608.
- [54] Ali Sharif Razavian, Hossein Azizpour, Josephine Sullivan, and Stefan Carlsson. "CNN features off-the-shelf: an astounding baseline for recognition." In: *Computer Vision and Pattern Recognition Workshops (CVPRW), 2014 IEEE Conference on*. IEEE. 2014, pp. 512–519.
- [55] Angie K Reyes, Juan C Caicedo, and Jorge E Camargo. "Fine-tuning Deep Convolutional Networks for Plant Recognition." In: *CLEF (Working Notes)*. 2015.
- [56] Gavin A Rummery and Mahesan Niranjan. *On-line Q-learning using connectionist systems*. Vol. 37. University of Cambridge, Department of Engineering Cambridge, England, 1994.
- [57] Olga Russakovsky, Jia Deng, Hao Su, Jonathan Krause, Sanjeev Satheesh, Sean Ma, Zhiheng Huang, Andrej Karpathy, Aditya Khosla, Michael Bernstein, et al. "Imagenet large scale visual recognition challenge." In: *International journal of computer vision* 115.3 (2015), pp. 211–252.
- [58] Matthia Sabatelli, Mike Kestemont, and Pierre Geurts. "On the transferability of winning tickets in non-natural image datasets." In: *arXiv preprint arXiv:2005.05232* (2020).
- [59] Matthia Sabatelli, Gilles Louppe, Pierre Geurts, and Marco Wiering. "Deep Quality-Value (DQV) Learning." In: *Advances in Neural Information Processing Systems, Deep Reinforcement Learning Workshop*. Montreal. 2018.

- [60] Matthia Sabatelli, Mike Kestemont, Walter Daelemans, and Pierre Geurts. "Deep transfer learning for art classification problems." In: *Proceedings of the European Conference on Computer Vision (ECCV) Workshops*. 2018, pp. 631–646.
- [61] Matthia Sabatelli, Gilles Louppe, Pierre Geurts, and Marco A Wiering. "The deep quality-value family of deep reinforcement learning algorithms." In: *2020 International Joint Conference on Neural Networks (IJCNN)*. IEEE. 2020, pp. 1–8.
- [62] Karen Simonyan and Andrew Zisserman. "Very deep convolutional networks for large-scale image recognition." In: *arXiv preprint arXiv:1409.1556* (2014).
- [63] Johannes Stallkamp, Marc Schlipsing, Jan Salmen, and Christian Igel. "The German traffic sign recognition benchmark: a multi-class classification competition." In: *Neural Networks (IJCNN), The 2011 International Joint Conference on*. IEEE. 2011, pp. 1453–1460.
- [64] Gjorgji Strezoski and Marcel Worring. "Omniart: multi-task deep learning for artistic data analysis." In: *arXiv preprint arXiv:1708.00684* (2017).
- [65] Gjorgji Strezoski and Marcel Worring. "Omniart: a large-scale artistic benchmark." In: *ACM Transactions on Multimedia Computing, Communications, and Applications (TOMM)* 14.4 (2018), pp. 1–21.
- [66] Tianxiang Sun, Yunfan Shao, Xiaonan Li, Pengfei Liu, Hang Yan, Xipeng Qiu, and Xuanjing Huang. "Learning Sparse Sharing Architectures for Multiple Tasks." In: *arXiv preprint arXiv:1911.05034* (2019).
- [67] Richard S Sutton. "Learning to predict by the methods of temporal differences." In: *Machine learning* 3.1 (1988), pp. 9–44.
- [68] Richard S Sutton. "Generalization in reinforcement learning: Successful examples using sparse coarse coding." In: *Advances in neural information processing systems*. 1996, pp. 1038–1044.
- [69] Richard S Sutton and Andrew G Barto. *Reinforcement learning: An introduction*. MIT press, 2018.
- [70] Christian Szegedy, Vincent Vanhoucke, Sergey Ioffe, Jon Shlens, and Zbigniew Wojna. "Rethinking the inception architecture for computer vision." In: *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*. 2016, pp. 2818–2826.
- [71] Nima Tajbakhsh, Jae Y Shin, Suryakanth R Gurudu, R Todd Hurst, Christopher B Kendall, Michael B Gotway, and Jianming Liang. "Convolutional neural networks for medical image analysis: Full training or fine tuning?" In: *IEEE transactions on medical imaging* (2016), pp. 1299–1312.

- [72] Gerald Tesauro. "TD-Gammon, a self-teaching backgammon program, achieves master-level play." In: *Neural computation* 6.2 (1994), pp. 215–219.
- [73] Tijmen Tieleman and Geoffrey Hinton. "Lecture 6.5-rmsprop: Divide the gradient by a running average of its recent magnitude." In: COURSERA: *Neural networks for machine learning* (2012), pp. 26–31.
- [74] Denis Tomè, Federico Monti, Luca Baroffio, Luca Bondi, Marco Tagliasacchi, and Stefano Tubaro. "Deep convolutional neural networks for pedestrian detection." In: *Signal Processing: Image Communication* (2016), pp. 482–489.
- [75] John N Tsitsiklis and Benjamin Van Roy. "Analysis of temporal-difference learning with function approximation." In: *Advances in neural information processing systems*. 1997, pp. 1075–1081.
- [76] Hado Van Hasselt. "Double Q-learning." In: *Advances in Neural Information Processing Systems*. 2010, pp. 2613–2621.
- [77] Hado Van Hasselt, Arthur Guez, and David Silver. "Deep reinforcement learning with double Q-learning." In: *Thirtieth AAAI Conference on Artificial Intelligence*. 2016.
- [78] Hado Van Hasselt, Yotam Doron, Florian Strub, Matteo Hessel, Nicolas Sonnerat, and Joseph Modayil. "Deep Reinforcement Learning and the Deadly Triad." In: *arXiv preprint arXiv:1812.02648* (2018).
- [79] Ryan Van Soelen and John W Sheppard. "Using winning lottery tickets in transfer learning for convolutional neural networks." In: *2019 International Joint Conference on Neural Networks (IJCNN)*. IEEE. 2019, pp. 1–8.
- [80] Ziyu Wang, Tom Schaul, Matteo Hessel, Hado Van Hasselt, Marc Lanctot, and Nando Freitas. "Dueling Network Architectures for Deep Reinforcement Learning." In: *International Conference on Machine Learning*. 2016, pp. 1995–2003.
- [81] Christopher JCH Watkins and Peter Dayan. "Q-learning." In: *Machine learning* 8.3-4 (1992), pp. 279–292.
- [82] Stuart Weibel, John Kunze, Carl Lagoze, and Misha Wolf. *Dublin core metadata for resource discovery*. Tech. rep. 1998.
- [83] Marco A Wiering. "QV (lambda)-learning: A new on-policy reinforcement learning algorithm." In: *Proceedings of the 7th European Workshop on Reinforcement Learning*. 2005, pp. 17–18.
- [84] Marco A Wiering and Hado Van Hasselt. "The QV family compared to other reinforcement learning algorithms." In: *Adaptive Dynamic Programming and Reinforcement Learning, 2009. ADPRL'09. IEEE Symposium on*. IEEE. 2009, pp. 101–108.

- [85] Marco Wiering and Jürgen Schmidhuber. "Speeding up Q (λ)-learning." In: *European Conference on Machine Learning*. Springer. 1998, pp. 352–363.
- [86] Jos van de Wolfshaar, Mahir F Karaaba, and Marco A Wiering. "Deep convolutional neural networks and support vector machines for gender recognition." In: *Computational Intelligence, 2015 IEEE Symposium Series on*. IEEE. 2015, pp. 188–195.
- [87] R. Wollheim. *On Art and the Mind. Essays and Lectures*. Allen Lane, 1972.
- [88] Saining Xie, Ross Girshick, Piotr Dollár, Zhuowen Tu, and Kaiming He. "Aggregated residual transformations for deep neural networks." In: *Computer Vision and Pattern Recognition (CVPR), 2017 IEEE Conference on*. IEEE. 2017, pp. 5987–5995.
- [89] Haonan Yu, Sergey Edunov, Yuandong Tian, and Ari S Morcos. "Playing the lottery with rewards and multiple languages: lottery tickets in RL and NLP." In: *arXiv preprint arXiv:1906.02768* (2019).
- [90] Dongbin Zhao, Haitao Wang, Kun Shao, and Yuanheng Zhu. "Deep reinforcement learning with experience replay based on SARSA." In: *2016 IEEE Symposium Series on Computational Intelligence (SSCI)*. IEEE. 2016, pp. 1–6.
- [91] Sheng-hua Zhong, Xingsheng Huang, and Zhiqiao Xiao. "Fine-art painting classification via two-channel dual path networks." In: *International Journal of Machine Learning and Cybernetics* 11.1 (2020), pp. 137–152.
- [92] Zhuangwei Zhuang, Mingkui Tan, Bohan Zhuang, Jing Liu, Yong Guo, Qingyao Wu, Junzhou Huang, and Jinhui Zhu. "Discrimination-aware channel pruning for deep neural networks." In: *Advances in Neural Information Processing Systems*. 2018, pp. 875–886.

DECLARATION

Put your declaration here.

Saarbrücken, September 2015

André Miede

COLOPHON

This document was typeset using the typographical look-and-feel `classicthesis` developed by André Miede. The style was inspired by Robert Bringhurst's seminal book on typography "*The Elements of Typographic Style*". `classicthesis` is available for both L^AT_EX and LyX:

<https://bitbucket.org/amiede/classicthesis/>

Happy users of `classicthesis` usually send a real postcard to the author, a collection of postcards received so far is featured here:

<http://postcards.miede.de/>

Final Version as of March 1, 2021 (classicthesis version 4.2).