

- 1 Three Types of Nonresponse
- 2 Subsampling: a technique to reduce nonresponse (or produce unbiased estimates)
- 3 Randomized Response: a technique to reduce nonresponse
- 4 Nonresponse- & Poststratification-adjusted Sampling Weights

First, partition the population $\mathcal{U} = \{1, 2, \dots, N\}$ into H disjoint *poststrata*, i.e. $\mathcal{U} = \bigsqcup_{\beta=1}^H \mathcal{P}_\beta$. For each $i \in \mathcal{U}$, let $\mathcal{P}_{\beta(i)}$ be the unique poststratum that contains i . Let $N_\beta := \#(\mathcal{P}_\beta)$ be the number of units in the poststratum \mathcal{P}_β .

Next, let \mathcal{S} be any realized sample.

Response distribution conditional on the realized sample \mathcal{S} :

$$p_{\mathcal{S}} : \text{PowerSet}(\mathcal{S}) \longrightarrow [0, \infty)$$

For each $i \in \mathcal{S}$, the *response probability* of i is given by:

$$p_{\mathcal{S}}(i) := \Pr(i \in \mathcal{R} | \mathcal{S}) = \sum_{\mathcal{R} \ni i} p_{\mathcal{S}}(\mathcal{R})$$

We now make the assumption (i.e. model) on the response distribution $p_{\mathcal{S}}$:

Suppose $\mathcal{S} = \bigsqcup_{\alpha=1}^{A(\mathcal{S})} \mathcal{H}_\alpha$ can be partitioned such that the elements in each \mathcal{H}_α all have the same response probability.

The disjoint subsets $\mathcal{H}_\alpha, \alpha = 1, 2, \dots, A(\mathcal{S})$, are called the *response homogeneity groups* of the realized sample \mathcal{S} . We emphasize that the number $A(\mathcal{S})$ of response homogeneity groups may vary from sample to sample.

Let $\mathcal{R} \subset \mathcal{S}$ be a response set, selected from $\text{PowerSet}(\mathcal{S})$ according to the \mathcal{S} -conditional response distribution $p_{\mathcal{S}}$.

Then, $\mathcal{R} = \bigsqcup_{\alpha=1}^{A(\mathcal{S})} \mathcal{R}_\alpha$, where $\mathcal{R}_\alpha := \mathcal{H}_\alpha \cap \mathcal{R}$.

For each $i \in \mathcal{R}$, let $\alpha(i) \in \{1, 2, \dots, A\}$ be the unique element such that $i \in \mathcal{R}_{\alpha(i)} \subset \mathcal{H}_{\alpha(i)}$. In other words, for each $i \in \mathcal{R}$, we let $\mathcal{H}_{\alpha(i)}$ denote the unique response homogeneity group that contains i , and $\mathcal{R}_{\alpha(i)} \subset \mathcal{H}_{\alpha(i)}$ is the respondent subset of $\mathcal{H}_{\alpha(i)}$.

$$\begin{aligned}
 W_{1,i} &:= \frac{1}{\pi_i}, \quad \text{for } i \in \mathcal{U} = \{1, 2, \dots, N\} \\
 W_{2,i} &:= \begin{cases} W_{1,i} \cdot \frac{\sum_{j \in \mathcal{H}_{\alpha(i)}} W_{1,j}}{\sum_{j \in \mathcal{R} \cap \mathcal{H}_{\alpha(i)}} W_{1,j}}, & \text{if } i \in \mathcal{R} = \bigsqcup_{\alpha=1}^{A(\mathcal{S})} \mathcal{R}_{\alpha} \\ 0, & \text{if } i \notin \mathcal{R} \end{cases} \\
 W_{3,i} &:= W_{2,i} \cdot \frac{N_{\beta(i)}}{\sum_{j \in \mathcal{S} \cap \mathcal{P}_{\beta(i)}} W_{2,j}}
 \end{aligned}$$

We let the final nonresponse- and poststratification-adjusted sampling weights be defined as:

$$W_i := W_{3,i}$$

IMPORTANT OBSERVATION: The quantity $\sum_{j \in \mathcal{H}_{\alpha(i)}} W_{1,j}$ is simply the weight-derived “size” of the response homogeneity group $\mathcal{H}_{\alpha(i)}$. Similarly, $\sum_{j \in \mathcal{R}_{\alpha(i)}} W_{1,j}$ is the weight-derived “size” of the respondent subset $\mathcal{R}_{\alpha(i)} \subset \mathcal{H}_{\alpha(i)}$. Similarly, $\sum_{j \in \mathcal{S} \cap \mathcal{P}_{\beta(i)}} W_{2,j}$ is the weight-derived “size” of the set $\mathcal{S} \cap \mathcal{P}_{\beta(i)}$ of sampled units in the poststratum $\mathcal{P}_{\beta(i)}$. In other words, the “adjustments” described above are essentially based on “weight-derived sizes.”

5 Imputation: techniques for substituting for missing data

1. Deductive Imputation.
2. Overall mean imputation.
3. Class mean imputation.
4. Hot-deck Imputation.
 - Sequential Hot-deck Imputation.
 - Distance Function Matching.
5. Cold-deck Imputation.
6. Regression Imputation.
7. Multiple Imputation.