## ex5

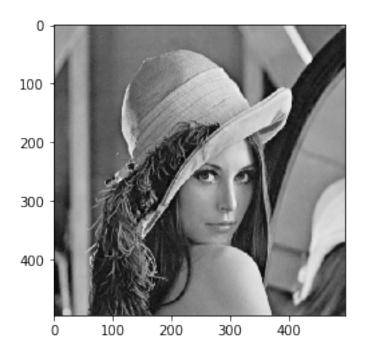
### May 8, 2019

#### 0.0.1 TODO Exercise 5. ex

(a) Read the image lena.png and convert it to grayscale.

```
[67]: import matplotlib.pyplot as plt
import cv2
import numpy as np
imageLena = mpimg.imread("./data/lena.png")
imageLena = imageLena *256
imageLena
output = cv2.cvtColor(
    imageLena,
    cv2.COLOR_RGB2GRAY
)
gray__imageLena= output .copy()

plt.imshow(gray__imageLena, cmap = 'gray')
plt.show()
(h, w) = gray__imageLena.shape[:2]
```



```
[67]: array([[160.80013 , 162.80797 , 162.80797 , ..., 171.45676 , 172.23178 , 152.41035 ],
[161.80405 , 163.58301 , 162.80797 , ..., 171.22787 , 175.71841 , 155.42213 ],
[163.29387 , 163.65428 , 162.28995 , ..., 169.69487 , 171.70271 , 155.18219 ],
...,
[ 50.322575 , 44.299046 , 50.208126 , ..., 101.09691 , 102.66905 , 97.44264 ],
[ 45.302967 , 42.291203 , 51.212048 , ..., 100.48653 , 103.755295 , 99.30392 ],
[ 43.295124 , 43.295124 , 55.227734 , ..., 101.49045 , 105.24512 , 104.39479 ]], dtype=float32)
```

# 0.0.2 2.b.1) Add a watermark to the image with and without applying NVF function the different values of $\frac{z}{2}$ (10, 25, 50, 75) and D. Choose the window size appropriate to used image.

The Noise Visibility Function (NVF) describes noise visibility in an image. The most known form of NVF is given as:

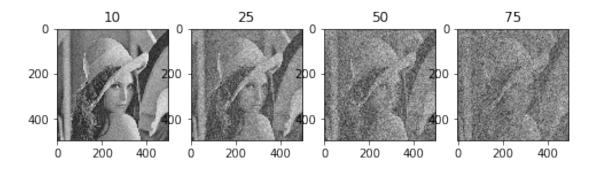
$$NVF = \frac{1}{1 + \theta \sigma_x^2(i,j)} \ \theta = \frac{D}{\sigma_{x_{max}}^2}$$

- $\sigma_{x_{max}}$  (i, j) denotes the local variance of the image in a window centred on the pixel with coordinates (i, j),
- plays the role of contrast adjustment for every particular image,  $\sigma_{x_{max}}^2$  is the maximum local variance for a given image

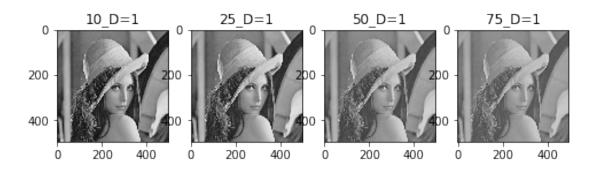
- D is an experimentally determined parameter.
- The final embedding equation is:  $y_{i,j} = x_{i,j} + (1NVF)z_{i,j}$

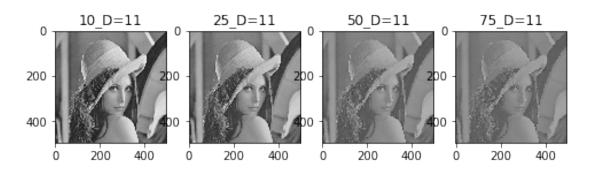
```
[87]: # Here we generate the different watermarks for variances [10, 25, 50, 75]
     def generateWatermark(window_size, sigma, mu=0, ):
         (row, col) = window_size
         return np.random.normal(mu,sigma,(row,col))
     watermark_size = gray__imageLena.shape[:2]
     watermark list = [
         (generateWatermark(watermark_size, sigma), sigma)
         for sigma in [10, 25, 50, 75]
     ]
     # Add watermark to the image without the NVF function
     #with equation y = x + z which is equivalent to adding gaussian noise
     def addWatermark(img, z):
         return np.add(img, z)
     def showImages(images, titles):
         fig=plt.figure(figsize=(8, 8))
         columns = 4
         rows = round(len(images)/columns)
         for i in range(1, columns*rows +1):
             fig.add_subplot(rows, columns, i)
             img = images[k-1]
             plt.imshow(img, cmap = 'gray')
             plt.title(titles[k-1])
             k+=1
         plt.show()
     noNVFwatermarked_Img_list = [
         (addWatermark(gray__imageLena, watermark[0]), str(watermark[1]))
         for watermark in watermark_list
     ]
     showImages(
         [im[0] for im in noNVFwatermarked_Img_list],
         [im[1] for im in noNVFwatermarked_Img_list]
     )
     # Here we implement the description functions
     from scipy import ndimage
     lena_variance_matrix = ndimage.generic_filter(gray__imageLena, np.var, size=4)
```

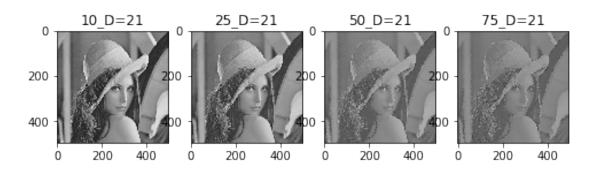
```
maxLocalVar = lena_variance_matrix.max()
Ds = range(1,51, 10)
for D in Ds:
    theta = D / maxLocalVar
    print(theta)
    NVF_matrix = 1/(1+ theta*lena_variance_matrix)
    def embeddingEquation(NVF_matrix, x, z):
        return np.add(x, np.multiply((1-NVF_matrix ), z))
    NVFwatermarked_Img_list = [
        (
            embeddingEquation(NVF_matrix, gray__imageLena, watermark[0]),
            str(watermark[1]) + "_D=" + str(D)
        for watermark in watermark_list
    showImages(
        [im[0] for im in NVFwatermarked_Img_list],
        [im[1] for im in NVFwatermarked_Img_list]
    )
```

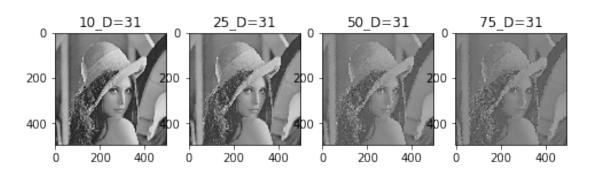


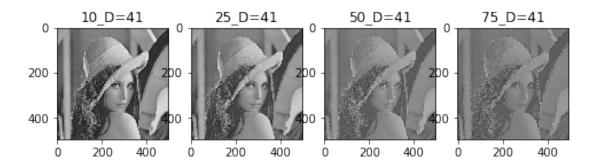
- 0.0001630953068290187
- 0.0017940483751192058
- 0.0034250014434093925
- 0.00505595451169958
- 0.006686907579989767











## 0.0.3 2.c) Report the dependency between the parameters $\frac{z}{2}$ , D and original image.

From the small experiment we ran above we determine that greater values of D make the influece of the window bigger. The  $\frac{z}{2}$  as expected increases the noise in the image.