

Quiz 3

Student ID:

Name:

1. X_1 and X_2 are independent exponential random variables, each with rate λ . The random variable Y is defined as $Y = \min(X_1, X_2)$.

Please find $E[Y]$.

$$Y \sim \text{Exp}(\lambda + \lambda) = \text{Exp}(2\lambda)$$

$$E[Y] = \frac{1}{2\lambda}$$

2. Let $X \sim \text{Exponential}(\lambda)$. Use Chebyshev's inequality to find an upper bound of $P(|X - E[X]| \geq b)$.

Since $X \sim \text{Exponential}(\lambda)$, we have $E[X] = \frac{1}{\lambda}$ and $\text{Var}[X] = \frac{1}{\lambda^2}$.

Using Chebyshev's inequality, we have

$$\begin{aligned} P(|X - E[X]| \geq b) &\leq \frac{\text{Var}(X)}{b^2} \\ &= \frac{1}{\lambda^2 b^2} \end{aligned}$$