

This is a check (up to the 7th derivative) that shows that the massive field wipes out the odd derivatives that contribute to the Euler-Maclaurin sum used to calculate the magnitude of the Casimir effect.

\$Assumptions = b > 0;

ClearAll[fp, fpp]

fp = -2 n Sqrt[n^2 + b^2] f[(Pi / a) Sqrt[n^2 + b^2]]

fpp = D[fp, n]

f3p = D[fpp, n]

$$\text{Out}[307]= -2 n \sqrt{b^2 + n^2} f\left[\frac{\sqrt{b^2 + n^2} \pi}{a}\right]$$

$$\text{Out}[308]= -\frac{2 n^2 f\left[\frac{\sqrt{b^2 + n^2} \pi}{a}\right]}{\sqrt{b^2 + n^2}} - 2 \sqrt{b^2 + n^2} f\left[\frac{\sqrt{b^2 + n^2} \pi}{a}\right] - \frac{2 n^2 \pi f'\left[\frac{\sqrt{b^2 + n^2} \pi}{a}\right]}{a}$$

$$\text{Out}[309]= \frac{2 n^3 f\left[\frac{\sqrt{b^2 + n^2} \pi}{a}\right]}{(b^2 + n^2)^{3/2}} - \frac{6 n f\left[\frac{\sqrt{b^2 + n^2} \pi}{a}\right]}{\sqrt{b^2 + n^2}} - \frac{6 n \pi f'\left[\frac{\sqrt{b^2 + n^2} \pi}{a}\right]}{a} - \frac{2 n^3 \pi f'\left[\frac{\sqrt{b^2 + n^2} \pi}{a}\right]}{a (b^2 + n^2)} - \frac{2 n^3 \pi^2 f''\left[\frac{\sqrt{b^2 + n^2} \pi}{a}\right]}{a^2 \sqrt{b^2 + n^2}}$$

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In[321]:= f4p = D[f3p, n];
          f5p = D[f4p, n];
          f6p = D[f5p, n];
          f7p = D[f6p, n];
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f3p /. n -> 0
f4p /. n -> 0 // Simplify
f5p /. n -> 0
f6p /. n -> 0 // Simplify
f7p /. n -> 0
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Out[325]= 0
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Out[326]= -2 b f\left[\frac{b \pi}{a}\right]
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Out[327]= 0
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Out[328]= -\frac{6 f\left[\frac{b \pi}{a}\right]}{b} - \frac{6 \pi f'\left[\frac{b \pi}{a}\right]}{a}
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Out[329]= 0
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Out[330]= \frac{30 \left(a^2 f\left[\frac{b \pi}{a}\right] - b \pi \left(a f'\left[\frac{b \pi}{a}\right] + b \pi f''\left[\frac{b \pi}{a}\right]\right)\right)}{a^2 b^3}
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Out[331]= 0
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