

Some R2 complex exponential calculations using CliffordBasic.

```
<< CliffordBasic`;
$SetSignature = {2, 0};

ClearAll[ a, b, c, angle, exp, r ]
exp[ t_ ] := Module[ {abs},
  abs = Sqrt[-GeometricProduct[t, t]];
  Cos[ abs ] + (t / abs) Sin[ abs ]];
r[t_] := GeometricProduct[ e[1], exp[t] ];
a = r[e[1, 2] Pi / 3]
b = r[e[1, 2] Pi / 6]
c = GeometricProduct[ a, b] // Simplify
angle = exp[ e[1, 2] Pi (-1 / 3 + 1 / 6)]
iangle = MultivectorInverse[angle] // Simplify
GeometricProduct[ c, iangle ]
```

$$\frac{e[1]}{2} + \frac{1}{2} \sqrt{3} e[2]$$

$$\frac{1}{2} \sqrt{3} e[1] + \frac{e[2]}{2}$$

$$\frac{1}{2} \left(\sqrt{3} - e[1, 2] \right)$$

$$\frac{\sqrt{3}}{2} - \frac{1}{2} e[1, 2]$$

$$\frac{1}{2} \left(\sqrt{3} + e[1, 2] \right)$$

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{Cos[Pi / 3], Sin[Pi / 3]}

{Cos[Pi / 6], Sin[Pi / 6]}

$$\left\{ \frac{1}{2}, \frac{\sqrt{3}}{2} \right\}$$

$$\left\{ \frac{\sqrt{3}}{2}, \frac{1}{2} \right\}$$