

# Hierarchical Reinforcement Learning for Multi-modal Continuous Control Environments with Sparse Rewards

by

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A Thesis Submitted to  
The Hong Kong University of Science and Technology  
in Partial Fulfillment of the Requirements for  
the Degree of Doctor of Philosophy  
in Master of Philosophy in Computer Engineering and Science

TODO 2018, Hong Kong

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This is to certify that I have examined the above PhD thesis  
and have found that it is complete and satisfactory in all respects,  
and that any and all revisions required by  
the thesis examination committee have been made.

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## Acknowledgments

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# Hierarchical Reinforcement Learning for Multi-modal Continuous Control Environments with Sparse Rewards

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Abstract

# Chapter 1

## Introduction

### 1.1 Overview

Deep reinforcement learning methods have become popular in the machine learning field in the recent years. Through the combination of deep neural network models and reinforcement learning theory, advances in deep reinforcement learning have achieved human level control performance in playing Atari games [3], mastered the board game GO [4], learned to play Texas Hold'em poker [5], and learned to solve simple robot control tasks [6].

However, the capability of reinforcement learning is still very limited. The end-to-end deep reinforcement learning methods are not able to solve general real-world challenging problems, such as playing the StarCraft games, controlling industrial assembly robots and making stock trading decisions. The contemporary end-to-end deep reinforcement learning methods have been able to handle simple tasks with unknown environment dynamics, or relatively complex environments that have known models. The real-world problems, however, usually have uncertain dynamics, noisy observation space and relative complex task logics. The study on improving the capability of deep reinforcement learning is thus still an important issue.

In this study, we investigate a set of challenging robot control environments and propose several methods that can solve the tasks.

## 1.2 Background

### 1.2.1 Reinforcement Learning (RL)

Reinforcement learning [7] is learning a policy (map from situations to actions) in order to maximize a numerical reward signal. The learner must discover the optimal policy by trying them. Reinforcement learning is different from supervised learning that the learner is not provided any labelled examples by any knowledgeable external supervisor. Reinforcement learning is also different from unsupervised learning, whose objective is finding hidden structures in unlabeled data.

Most reinforcement learning study is based on the problem formulation of Markov Decision Processes (MDPs). MDP is a framework defining the problem of learning from interaction. The learner is called the *agent*. Everything outside that interacts with the agent is called the *environment*. The agent and environments interact during a finite sequence of discrete time steps,  $t = 0, 1, 2, 3, \dots$ . At each time step  $t$ , the agent receives an observation of the environment's *state*,  $s \in S$  and selects an *action*  $a \in A$ . The agent receives a numerical reward  $r$ , and also the next state  $s'$ . A finite-horizon discounted Markov decision process (MDP) is defined by the tuple  $(S, A, P, r, \rho_0, \gamma)$  where the  $\rho_0 : S \mapsto \mathbb{R}$  is the initial state distribution,  $P(s'|s, a) : S \times A \mapsto \mathbb{R}$  is the distribution describing the state transition dynamics,  $r : S \times A \mapsto \mathbb{R}$  is the expected reward function, and  $\gamma \in (0, 1]$  is the discount factor.

Let  $\pi : S \times A \mapsto [0, 1]$  denote a policy, following are definitions of the action value function  $Q_\pi$ , the value function  $V_\pi$  and the advantage function  $A_\pi$ :

$$Q_\pi(s_t, a_t) = \mathbb{E}_{s_{t+1}, a_{t+1}, \dots} \left[ \sum_{l=0}^{\infty} r(s_l) \right],$$
$$V_\pi(s_t) = \mathbb{E}_{a_t, s_{t+1}, a_{t+1}, \dots} \left[ \sum_{l=0}^{\infty} r(s_l) \right],$$

$$A_\pi(s, a) = Q_\pi(s, a) - V_\pi(s), \text{ where } a_t \sim \pi(a_t | s_t), \text{ for } t \geq 0$$

### 1.2.2 Hierarchical reinforcement learning based on transferred policies from easy tasks

This study focus on a class of reinforcement learning problems, where the objective is to solve a *target task* given a set of trained *source tasks*. The policies that can solve the source tasks, namely the *actuator policies*, are available for the agent. It is known that target task can be solved by a sequential execution of a subset of the source-task policies. The agent needs to learn a *scheduler policy*, which chooses the source-task policy to be executed and decides when to switch the currently running source-task policy.

This paradigm is related to hierarchical reinforcement learning (HRL) [8], which focuses on learning and utilizing closed-loop partial policy / skills to solve a complex task. However, our case is different from the standard setting of HRL where the agent needs to extract the useful closed-loop partial policy from the original task. However, we focus on extracting and reusing partial policies from other tasks.

This paradigm is also related to transfer learning in reinforcement learning [9], because the source-task policies are reused by the high-level scheduler agent. However, conventional transfer learning paradigms usually don't assume a hierarchical relationship between the target task and the source tasks.

## 1.3 Scope of study

Real-world robot control problems involves many sources of complexity. However, we only focus on some critical properties of real-world robot control problems. This study focus on the reinforcement learning problems with multi-modality state space, continuous action space and sparse reward in a continual learning setting.

### 1.3.1 Multi-modality state space

The reinforcement learning problems with multi-modality state space refers to the environments whose state space is a combination of signals with different modality.

Specifically, the study focus on realistic robot control environments whose state space is a combination of a low-dimensional state sensor and a image sensor observation.

The low-dimensional state input provides accurate information about the agent’s physical system. The image input provides information about the external environment and has a datatype that is in much higher dimension.

Most recent works in reinforcement learning for continuous control focus on the RL tasks with low-dimensional state input only [6]. There are also works [10] trying to handle some tasks with image input only, but these image-based tasks are very simple to solve.

However, the proposed multi-modality environment is the most common case in real-world robotic problems, and is considerably more complex and realistic than solving a low-dimensional state input only task or an image only task.

### 1.3.2 Sparse reward function

The problem of sparse / delayed reward signal has been one of the major problems to be tackled in reinforcement learning. Many methods are proposed to solve the sparse reward problem in environments with discrete action spaces. However, the problem is much more difficult for the environments with continuous action spaces, and few works have focused on the class of system. By the time of writing, we haven’t seen any method that has been proposed to effectively solve continuous control tasks with sparse rewards.

Studies have shown that smooth and informative reward function can generally make the training of reinforcement learning agents easier. Theoretically, any reinforcement learning problems when given a reward function that is good enough.

However, the reward function of a realistic robot control environment is usually discontinuous and sparse. Reward shaping techniques may improve the reward function, but it usually relies on domain-specific engineering. In our study, we try to solve some realistic robot problems without reward shaping, which essentially indicates the problems have sparse reward functions.

### 1.3.3 Assumption on hierarchical relationship of tasks

We focus on solving the reinforcement learning setting described in section 1.2.2 . We assume that the agent has already learned the optimal policies for a set of source tasks before solving the target problem, and we also assume that the target task can be solved by executing a subset of the source task policies in according to some ”high level policy”.

However, we don't pose any other assumption on the relationship between the source tasks and the target task. We don't know whether any specific source task is useful. A source task policy might be useful in some cases, or it could be completely useless. We also don't make assumption on how long an actuator policy should be executed in its term. The scheduler agent need to learn it instead. An actuator policy might be executed for only 1 time-step before the agent switch to another one, or it could be executed for a longer time, or until a specific condition.

This assumption is the only assumption that is involved in domain-specific design. However, we observe that many real-world complex robot control problems can usually be decomposed to primary tasks. Classical robot control methods also organize the abstract problems (such as trajectory planning) and low level problems (such as model control) in hierarchical structures.

If this hierarchical task relationship assumption was removed, the problem becomes the fully autonomous hierarchical reinforcement learning problem, where the agents need to learn not only a task structure but also all actuator policies from scratch. This problem is considered in-feasible to solve for general robot control problems [8].

## 1.4 Research Questions

We will propose several reinforcement learning environments for continuous control in section 3.1 according to the stated scope and assumption. The study will mainly focus on solving the proposed problems. The primary research question that we focus on is:

*Can we develop an agent that can achieve good performance (in terms of total reward) in the reinforcement learning environments defined in section 3.1 within reasonable training time, with an RL model that doesn't rely on domain-specific techniques (including reward shaping, manual definition of policy hierarchy, manual / heuristic methods to define sub-goals, or manual criteria on the switching of actuator policies)?*

We will first answer the question on whether the previous work already solve the problem: *Can the contemporary flat reinforcement learning methods achieve good performance in the proposed environments?*

We will then answer the question on whether our proposed model can solve this: A model that solves the primary question needs to address two issues: reusing the policies

learned in source tasks and solving the target task. To solve the first issue, we need to answer the question of "*Can a trained actuator policy achieve a good performance (in terms of the expected total return of the original problem), with or without fine-tuning methods, in a target environment which has different initial state distribution?*".

To address the second issue, we will answer the question of "*Can the target scheduler agent learn the optimal policy given the trained sub-task policies, without any domain-specific design defined previously?*".

# Chapter 2

## Related works

### 2.1 Policy Gradient Methods

Policy gradient method is a class of reinforcement learning methods that solve the problem by optimizing a parametrized policy model  $\pi_\theta(a|s)$ ,  $a \in A, s \in S$ , so that the expected return:

$$J(\theta) = \mathbb{E} \left[ \sum_{t=0}^T \gamma^t r_t \right]$$

is maximized, where  $\gamma$  is a discount factor and  $T$  is the episode length.

Policy gradient methods maximize the expected return iteratively by estimating the gradient  $g := \nabla \mathbb{E} \left[ \sum_{t=0}^T \gamma^t r_t \right]$ , which has the form [11]:

$$g = \mathbb{E}_{t,s_t,a_t} \left[ \Psi_t \frac{\nabla_\theta \pi_\theta(a_t|s_t)}{\pi_\theta(a_t|s_t)} \right] = \mathbb{E}_{t,s_t,a_t} \left[ \Psi_t \nabla_\theta \log \pi_\theta(a_t|s_t) \right] \quad (2.1)$$

$\Psi_t$  may be one of the following:

1.  $\sum_{t=0}^\infty r_t$  expected total return
2.  $\sum_{t'=t}^\infty r_t$  expected return following  $a_t$
3.  $\sum_{t'=t}^\infty [r_t - b(s_t)]$
4.  $Q_\pi(s_t, a_t)$
5.  $A_\pi(s_t, a_t)$
6.  $\hat{A}_t^{(1)} := \delta_t = r_t + V_\pi(s_{t+1}) - V_\pi(s_t)$  : 1-step TD residual
7.  $\hat{A}_t^{(2)} := \delta_t + \gamma \delta_{t+1} = r_t + \gamma r_{t+1} + \gamma^2 V_\pi(s_{t+2}) - V_\pi(s_t)$  : 2-step TD residual

8.  $\hat{A}_t^{(k)} := \sum_{l=0}^{k-1} \gamma^l \delta_{t+l} = r_t + \gamma r_{t+1} + \dots + \gamma^{k-1} r_{t+k-1} + \gamma^k V(s_{t+k}) - V(s_t)$  : k-step TD residual
9.  $GAE(\lambda) = \frac{1}{(1+\lambda+\lambda^2+\dots)} (\hat{A}_t^{(1)} + \lambda \hat{A}_t^{(2)} + \lambda^2 \hat{A}_t^{(3)} + \dots) \approx \sum_{l=0}^{\infty} (\gamma \lambda)^l \delta_{t+l}$ , where  $\lambda \in [0, 1]$  : the generalized advantage estimator proposed by [11]

Several optimization method for updating the policy parameters given the policy gradient have been proposed. The following section will discuss some state-of-art methods.

### 2.1.1 Trust Region Policy Optimization

The method proposed by [12], namely Trust Region Policy Optimization (TRPO) is one of the early works in deep reinforcement learning for continuous control. The method formulates the policy optimization problem as a constraint optimization problem:

$$\begin{aligned} & \underset{\theta}{\text{maximize}} \quad J(\theta) \\ & \text{subject to} \quad \overline{D_{KL}}(\pi_{\theta_{old}} \| \pi_{\theta}) \leq \delta_{KL} \end{aligned} \tag{2.2}$$

where  $\pi_{\theta_{old}}$  is the old policy parameter before performing parameter update, and  $\overline{D_{KL}}$  is the average KL divergence over the samples,  $\delta_{KL}$  is the hyper-parameter that control the step size of updates.

The method solves this problem through 4 steps. The first step computes  $g$  following the Equation 2.1. The second step computes the Riemannian metric tensor of the parameter space of the policy model  $A = H_{\theta}(\overline{D_{KL}}(\pi_{\theta_{old}} \| \pi_{\theta}))$ , where  $H_{\theta}(.)$  denotes the Hessian matrix with respect to  $\theta$ . The third step obtains which is the natural gradient update direction  $s = A^{-1}g$  by solving  $g = As$  through the conjugate gradient algorithm. The fourth step computes the maximum step-size  $\beta = \sqrt{2\delta_{KL}/s^T As}$  and performs a line search to ensure the improvement of the objective function.

The method is able to solve some primary robot control tasks in [13] within a few number of training samples. However, both the computation of the Hessian matrix and the conjugate gradient algorithm are too expensive for deep neural network models.

### 2.1.2 Kronecker-factored Trust Region

The work of [10] proposes to reduce the computation time solving the natural gradient by Kronecker-factored approximation method. The Fisher Information Matrix

$F = \mathbb{E}[\nabla_\theta L \nabla_\theta L^T]$ , where  $L = \log \pi(a|s)$  is used here to approximate the Riemannian metric tensor. The matrix is approximated by:

$$F = \mathbb{E}[\nabla_\theta L \nabla_\theta L^T] = \mathbb{E}[aa^T \otimes \nabla_s L \nabla_s L^T] \approx \mathbb{E}[aa^T] \otimes \mathbb{E}[\nabla_s L \nabla_s L^T]$$

where  $a$  is the input activation vector corresponding to the neural network weight parameters and  $s$  is the corresponding preactivation vector. The natural gradient is then solved by:

$$s = A^{-1}g \approx F^{-1}g \approx (\mathbb{E}[aa^T] \otimes \mathbb{E}[\nabla_s L \nabla_s L^T])^{-1} g = \mathbb{E}[aa^T]^{-1}g\mathbb{E}[\nabla_s L \nabla_s L^T]^{-1} \quad (2.3)$$

The proposed method further speeds up the optimization by reusing recently computed statistic matrices in the previous steps and performing asynchronous computation, and finally achieves a computation time comparable to ordinary gradient decent algorithms. The method manages to computationally efficiently perform trust region natural policy gradient optimization without sacrificing the reinforcement learning performance.

### 2.1.3 Proximal Policy Gradient Method

The author of [14] proposed a first-order policy optimization method, namely proximal policy gradient with clipping (PPO). The method clips the surrogate objective according to the following equation:

$$L_{CLIP}(\theta) = \mathbb{E} \left[ \min \left( r_t(\theta) A_t, \text{clip}(r_t(\theta), 1 - \epsilon, 1 + \epsilon) A_t \right) \right] \quad (2.4)$$

where  $r_t(\theta) = \pi_\theta / \pi_{\theta_{old}}$  is the likelihood ratio of the current policy over the sample policy, and  $\epsilon \in [0, 1]$  is a hyperparameter.

The algorithm performs minibatch stochastic optimization at each batch of collected agent's experience, for a number of epochs. Therefore it is actually an off-policy method since the policy has already deviated from the sampling policy once updated for the first minibatch.

The method can achieve a relatively fast improvement rate in the early phase (within 1 million training steps) of training in several continuous control environments. However, the method is more difficult to tune compared to trust region methods, and might become increasingly unstable in the late phase of training. The method might also converge too early and stuck at a local minimum point, because updating the parameter too many times on a single batch might lead to overfitting.

### 2.1.4 Other Methods in Deep Reinforcement Learning for Continuous Control

Other methods related to deep reinforcement learning for continuous control include the Deep Deterministic Policy Gradient Method (DDPG) [15], Actor-Critic with Experience Replay (ACER) [16], and Trust-PCL [17]. These methods are first order off-policy algorithm, and are not the focus of our study because they're not reported to significantly outperform the above mentioned methods in terms of training time, final performance and stability.

## 2.2 Hierarchical Reinforcement Learning Methods

The paradigm of hierarchical reinforcement learning focuses on solving challenging reinforcement learning problems through temporal abstraction [8]. A hierarchical reinforcement learning agent's decisions invoke temporally extended activities instead of taking primary actions, so that it does not need to make decision at every time step.

The history of hierarchical reinforcement learning study can be dated back to late 1990s. Many methods have been proposed in the past 20 years, including option framework [18], hierarchies of abstract machines [19], and MAXQ value function decomposition [20].

Any hierarchical reinforcement learning method needs to solve 2 problems. First is to define and learn the temporally extended activities, which are low-level closed-loop partial policies. Second is to learn the decision scheduling of the low-level partial policies, including the selection of the partial policies and the scheduling of these decision points.

Many paradigms have been proposed to solve the first problem. The ideal formulation is for the agent to directly discover low-level policies that could be reused. However, this formulation has made the problem infeasible although some methods have been proposed [21], [22] in some special cases.

The most widely applied formulation is to manually define the low-level policies, or their corresponding MDPs. The problem is that this formulation basically relies on intensive domain-specific design, and manually defining them may not be feasible for real-world challenging environments.

Another popular formulation is to propose a set of auxiliary tasks to define and train

the low-level policies. However, the method of proposing auxiliary tasks is only feasible in some special cases and its development needs domain-specific engineering.

Finally, this thesis assumes the low-level policies are trained in a set of given source tasks that are primary problems. This formulation is general in the sense that the target problem can be solved as long as it can be decomposed into executing a series of some source task policies.

The solution to the first part of the second problem, which is learning to select among low-level policies, has been thoroughly studied since the work of [18]. However, the second part, which is to schedule the decision points, have not been solved for general environments. The most popular choice is to schedule decision points at fixed predefined periods, which is inflexible.

The following sections, will discuss the related hierarchical reinforcement learning methods in details.

### 2.2.1 Option framework

The work of [18] is among the earliest studies of hierarchical reinforcement learning, which uses the notion of *option* to define the partial policies / subroutines. An option consists of a policy  $\pi$ , a termination condition  $\beta$  and an input set  $I$  that indicates whether the partial policy is available at the current state. Once an option is executed, then actions are chosen according to  $\pi$  until  $\beta(s)$  outputs a termination signal.

An option is Markov if its policy is Markov. Semi-Markov options, on the other hand, are options whose policies are based on the entire history since the option was initiated. Semi-Markov options include options that terminates after a specific number of time steps, which could be particularly useful when considering policies over options.

A policy over options  $\mu$  selects option  $o$  in state  $s$  with probability  $\mu(s, o)$ .

A concept of multi-step model is proposed as a generalization of single-step models. For any option  $o$ , let  $E(o, s, t)$  denote the event of the option  $o$  initialized in state  $s$  at time  $t$ . Then the reward of the multi-step model is defined as:

$$R(s, o) = E\{r_{t+1} + \gamma r_{t+2} + \dots + \gamma^{t+\tau} r_{t+\tau} | E(o, s, t)\}$$

where  $t + \tau$  is the termination time of  $o$ . The state transition model for the option is:

$$P(s'|s, o) = \sum_{\tau=1}^{\infty} p(s', \tau) \gamma^{\tau}$$

for all states  $s' \in S$ , where  $p(s', \tau)$  denotes the probability that the option terminates after  $\tau$  steps and results in the state  $s'$ .

A generalized form of the Bellman optimality equation is then proposed:

$$V_O^*(s) = \max_{o \in O_s} \left[ R(s, o) + \sum_{s'} P(s'|s, o) V_O^*(s') \right] \quad (2.5)$$

In conclusion, this work proposes a formulation of hierarchical reinforcement learning and connects it to SMDP theory. The authors also propose the method for training the policy over options. However, the question on how the hierarchy of options are developed are not answered.

### 2.2.2 Modulated hierarchical controller

The work of [1] is among the first studies that applies hierarchical reinforcement learning on robot continuous control problems. They propose a two-level hierarchical agent architecture containing a high-level (HL) policy and a low-level (LL) policy. The high-level policy outputs a modulation signal which the low level agent then takes as part of its input. The architecture is demonstrated in Figure 2.1. The hierarchical agent is characterized by a policy  $\pi$  with parameter  $\theta$ . The policy is defined by the composition of the high-level controller  $F_H$  and low-level controller  $F_L$ . The low-level controller is a feed-forward neural network that maps the preprocessed current state  $o(s)$  and the control signal from the high-level controller  $c$  to the policy output.

$$\pi(a|s) = F_L(o(s), c) \quad (2.6)$$

where the preprocessed state  $o(s)$  removes task-specific information from the current state. The high-level controller is a recurrent neural network:  $F_H = (f_z, f_c)$  that produces the new control signal at every  $K$  time step:

$$z_t = f_z(s_t, z_{t-1}) \quad (2.7)$$

$$c_t = f_c(z_{t_r}) \quad (2.8)$$

where  $t_r$  is the most recent update output of the control signal. A predefined Gaussian noise component is added to the output  $c_t$  during the training of the high level controller, so that the agent has a better performance in exploration. The training of the hierarchical agent consists of two separate phases: pre-training and transfer. The tasks used for pre-training are relatively simple tasks that facilitate the development of generic locomotion

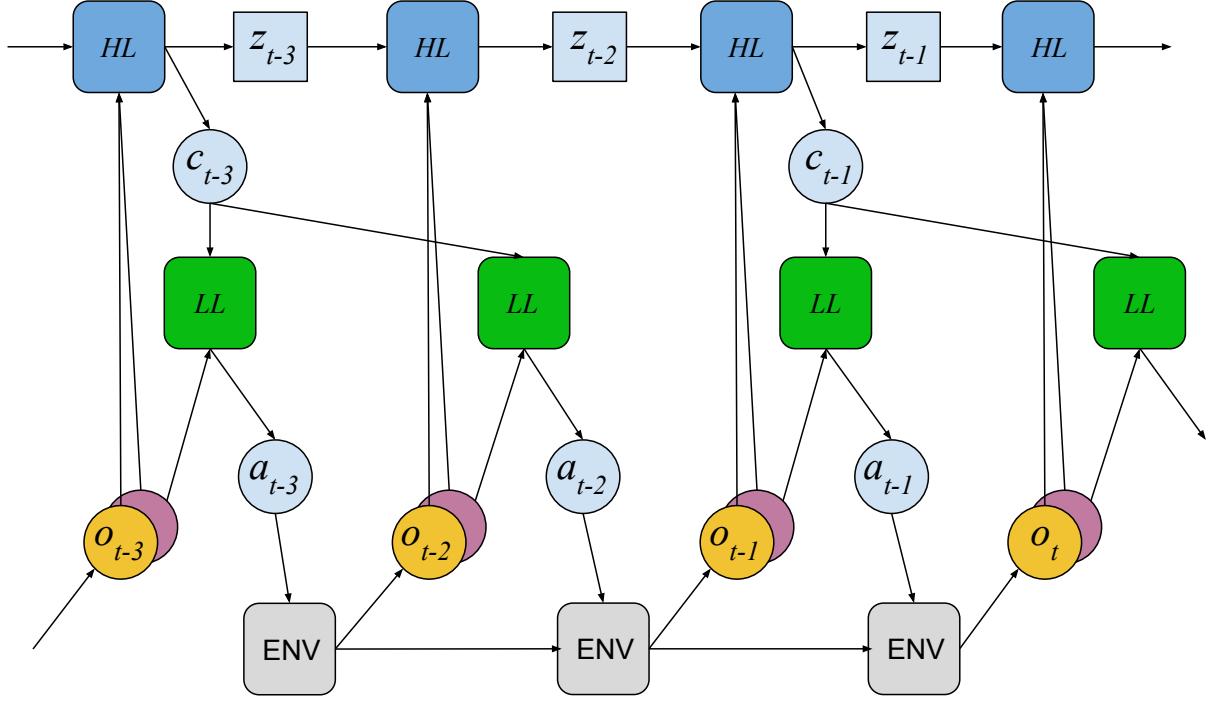


Figure 2.1: The hierarchical structure of the modulated controller [1], which consists of the recurrent high-level controller (HL, dark blue) and feedforward low-level controller (LL, green). The high-level controller has access to all observations (yellow and red). While both controllers observe sensory input at the world-clock frequency, the modulatory control signal from the high-level is updated every K steps (here  $K = 2$ )

skills. After pre-training, the high-level controller is re-initialized and the weights of low-level controller are frozen. The high-level controller is then trained in the transfer task, which has a sparse reward function. This method achieves better performance than flat agents on a few realistic robot control tasks. The limitation is that the architecture is highly engineered and domain-specific. The observation of the low-level agent  $o(s)$  need to be designed specifically for each task, and the However, the hierarchical relationships between the two agent, including the pre-training task definition and modulation model, need to be manually predefined. Apart from that, the design of the output modulated signal the high-level agent is limited to several locomotion tasks. This involves the agent. The parameter  $K$  is also predefined, and thus the time scale of the high level agent lacks the flexibility.

### 2.2.3 Learning a hierarchical model by meta-learning

Another work [2], namely meta learning shared hierarchies (MLSH), proposes a meta-learning approach for learning hierarchically structured policies. The MLSH method formulates the problem as learning a finite set of MDPs  $P_M$  with the same state-action space, with a universal agent architecture. The agent consists of two sets of parameters  $(\phi, \theta)$ , where  $\phi$  is the set of task-independent parameters and  $\theta$  is the set of task-specific parameters. The meta-learning objective is to optimize the expected return during the agent's entire lifetime:

$$\text{maximize}_{\phi} \mathbb{E}_{M \sim P_M}[R] \quad (2.9)$$

The detailed structure of the agent is shown in Figure 2.2. The architecture is basically a two-level hierarchical reinforcement learning agent, the components  $\phi_1, \phi_2, \dots$  are the parameters of the low-level agent policies (called sub-policies) shared across different tasks and  $\theta$  is the parameters of the high-level agent of the current task. The master policy samples the master action at a fixed frequency which selects the active sub-policy. The

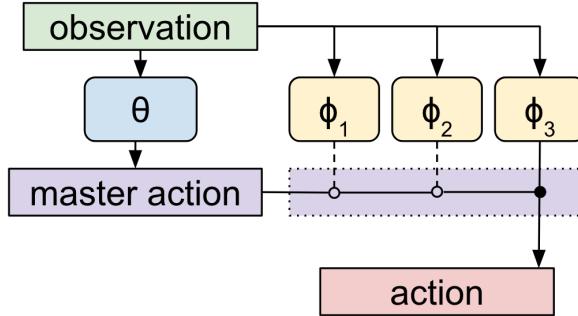


Figure 2.2: The agent setup of the modulated controller [2],  $\theta$  represents the master policy, which selects a sub-policy to be active. In the diagram,  $\phi_3$  is the active sub-policy, and actions are taken according to its output.

agent is trained in the following manner: First a task is sampled  $M$  is sampled and the parameter  $\theta$  is re-initialized randomly. Then there is a warmup phase, where only  $\theta$  is trained to achieve optimal. Then the agent enters the joint update phase, where both  $\theta$  and  $\phi$  are updated simultaneously. The method achieves good performance in several control environments. Including a moving-bandit Ant-robot task, a Ant-robot maze navigation task and an obstacle course task. However the tasks are actually simplified version of the control tasks in [6], where the state of the Ant-robot is periodically reset to prevent episode termination due to the falling over of Ant. That largely reduces the difficulty on

learning the locomotion skills of agents. It is not clear whether the method will perform well on the original version of the Ant-robot environment. The major limitation is that the method relies on a warm up period to learn a high-level agent’s policy. However, the authors didn’t provide a method to learn the high-level agent’s policy  $\theta$  at first task, where the parameters  $\phi$  are also randomly initialized. The method also predefines the temporal relationship between the high level policy and low level policy.

#### 2.2.4 Goal-directed learning method

Several works [23], [24] have tried to solve sparse-reward robot control environments through the learning and scheduling of auxiliary policies. The method of [23], namely Scheduled Auxiliary Control (SAC-X), is based on several main principles. First, the original MDP is modified that every state-action pair has a vector rewards, consisting the reward for the original MDP and a set of internal auxiliary rewards. Second, each internal auxiliary reward function is assigned a low-level agent policy, namely intention in this context. Third, there is a high-level scheduler agent that selects and executes the intentions. Fourth, the learning of intentions is performed off-policy on the same experience. The definitions of internal auxiliary rewards are based on predefined goal states. The internal auxiliary reward with goal state  $g$  is defined as:

$$r_g(s, a) = \begin{cases} \delta_g(s), & \text{if } d(s, g) \\ 0, & \text{else} \end{cases} \quad (2.10)$$

The parameter  $\theta$  of the intentions is trained with the aggregation of loss of all the reward functions:

$$\mathcal{L}(\theta) = \mathcal{L}(\theta; M) + \sum_{k=1}^{|A|} (\theta; \mathcal{A}_k) \quad (2.11)$$

Where  $M$  is the MDP with the original reward function and  $A = \{A_1, \dots, A_k\}$  is the set of MDPs with internal auxiliary rewards. The training of the intention parameter is formulated as a multi-task RL problem. The high-level scheduler policy is the trained using an off-policy policy gradient method with  $\theta$  being fixed. The method manages to solve the object grasping and stacking problems in an robot-arm environment. The major limitations of SAC-X is that the method relies on predefined auxiliary MDPs, which is infeasible to obtain in realistic environments.

### 2.2.5 Other methods targeting at sparse environments

Apart from the above mentioned works, several other methods have also been proposed to solve environments with sparse reward recently, including Unicorn [25], FuN [26], HRL with Stochastic Temporal Grammar [27], policy sketch method [28] and strategic attentive writer [29]. These methods have only been verified in discrete environments that have relatively low complexity, and involve domain-specific engineering components.

# Chapter 3

## Methodology

### 3.1 Target Environments

#### 3.1.1 Summary of environment design

We propose a set of reinforcement learning tasks that are suitable for studies in our target problem of multi-modality and sparse environments. The agents' physical systems are consistent with the 3D robot control environments in OpenAI Gym [13], while the external environments and reward functions of the target tasks are different from the original environments in OpenAI Gym. There are three kinds of 3D robot agents in OpenAI Gym: Ant, Humanoid and Swimmer. The "Ant" agent is a quadruped robot with 8-dimensional action space, the "Humanoid" agent is a humanoid robot with 16-dimensional action space, and the "Swimmer" agent is a worm-like robot with 2-dimensional action space. The three agents are showed in Figure 3.1, Figure 3.2 and Figure 3.3.

We will mainly focus on target environments based on the "Ant" agent, because the agent has the capability of solving a rich variety of high-level tasks, while the agent's primary control tasks are reasonably challenging. Compared to the "Ant" agent, the "Swimmer" agent is too simple and its capability of solving more challenging tasks is limited. The "Humanoid" agent's on the other hand, has a much more unstable physical system compared to "Ant".

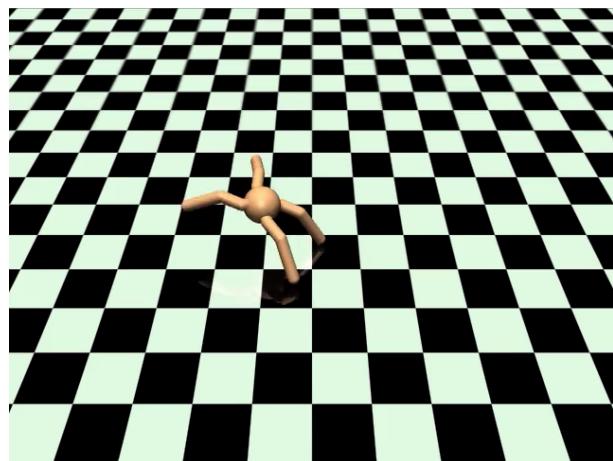


Figure 3.1: The "Ant" agent



Figure 3.2: The "Humanoid" agent

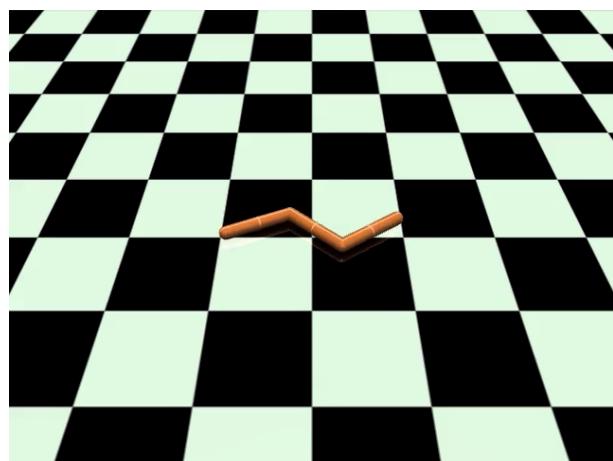


Figure 3.3: The "Swimmer" agent

### 3.1.2 Detailed environment specification

We provide a detailed description of the experiment environments in this section. All of the environments are based on the "Ant" task [13]. In the original "Ant" task, the agent receives a 111-dimensional state input and outputs a 8-dimensional action output. The agent's state consists of a 13-dimensional vector that represents its pose, a 14-dimensional vector that represents its velocity, and a 84-dimensional vector that represents related contact force.

In the settings of the proposed environments, the agent receives not only the 111-dimensional state, but also a  $64 \times 64 \times 1$  dimensional grayscale image observation. A sample image observation is shown in Figure 3.1.2.

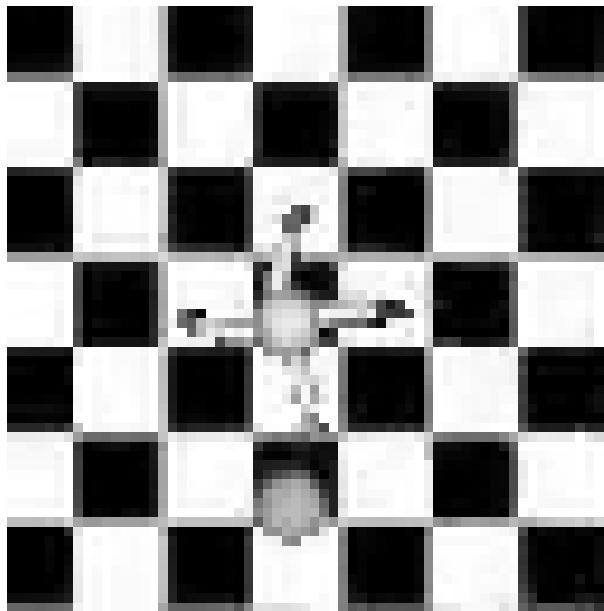


Figure 3.4: A sample image observation of the target environments

A basic task, namely "move0", is the same as the definition of "Ant" in OpenAI Gym [13] except an extra image observation as state. The agent is required to move toward a specific direction  $g_0 = (1, 0)$ , and the reward at each time-step is given by:

$$r = v_g + 1 - c_p - c_c \quad (3.1)$$

Where  $v_g = v \cdot g_0$  is the "forward reward", which rewards the agent for moving toward the goal direction.  $c_p$  is the control cost, which is the power that the agent is consuming, and  $c_c$  is the contact cost, which penalizes the agent for strong collision. The episode

terminates when the agent enters a unrecoverable state, such as being turned over, or if the episode length reaches 1000 time-steps.

Other basic environments that might be used as source tasks are "move1", "move2", "move3", ..., "move7". These tasks are the same as "move0" except that the goal direction is different. The image observation is redundant for all these low-level tasks, because the agent only needs to move toward one specific direction.

The target tasks are designed to be suitable for the definition of multi-modality and sparse-reward. We propose several multi-modality environments, including "moveg2", "moveg4", "moveg8", "movecont", "dynamicg4", "dynamiccont". These tasks require the agent to learn not only from the state representation but also the image representation. We also propose sparse multi-modality environments: "reachg4" and "reachcont". The agent receives very sparse rewards in these environments compared with the previous environments, which have smooth reward function. The goal direction or location is represented by a sphere object in the image observation, thus the image observation plays a critical role in these tasks. The set of all the proposed environments are described in table 3.1.2.

## 3.2 Wasserstein Actor Critic Kronecker-factored Trust Region Policy Optimization method

As is reported in [30], the result of the current state-of-art deep reinforcement learning methods for continuous control, including TRPO, ACKTR, PPO and DDPG are hard to be reproduced, due to they're heavily influenced by a variety of factors including random seed, neural network architecture, activation functions in neural network and software implementation. This means that the state-of-art methods are lack of stability in the agent's final performance and robustness to minor change in parameters. That has greatly diminishes the reliability of contemporary deep reinforcement learning methods.

We propose a new policy optimization method, namely Wasserstein Actor Critic Kronecker-factored Trust Region Policy Optimization (W-KTR). We claim that the proposed method outperform other state-of-art methods in terms of agent's final performance, total training time and reproducibility.

The proposed W-KTR method focus on the problem scope of deep reinforcement

Task name	Goal	Reward	Description
move0	velocity: $g_0 = (1, 0)$	$v_g + 1 - c_p - c_c$	move toward a target direction
move1	velocity: $g_1 = (-1, 0)$	$v_g + 1 - c_p - c_c$	move toward a target direction
move2	velocity: $g_2 = (0, 1)$	$v_g + 1 - c_p - c_c$	move toward a target direction
move3	velocity: $g_3 = (0, -1)$	$v_g + 1 - c_p - c_c$	move toward a target direction
move4	velocity: $g_4 = (\sqrt{2}/2, \sqrt{2}/2)$	$v_g + 1 - c_p - c_c$	move toward a target direction
move5	velocity: $g_5 = (-\sqrt{2}/2, -\sqrt{2}/2)$	$v_g + 1 - c_p - c_c$	move toward a target direction
move6	velocity: $g_6 = (\sqrt{2}/2, -\sqrt{2}/2)$	$v_g + 1 - c_p - c_c$	move toward a target direction
move7	velocity: $g_7 = (-\sqrt{2}/2, \sqrt{2}/2)$	$v_g + 1 - c_p - c_c$	move toward a target direction
moveg2	velocity samples from: $\{g_0, g_1\}$	$v_g + 1 - c_p - c_c$	each episode has a random sampled goal direction
moveg4	velocity samples from: $\{g_0, g_1, g_2, g_3\}$	$v_g + 1 - c_p - c_c$	each episode has a random sampled goal direction
moveg8	velocity samples from: $\{g_0, g_1, \dots, g_7\}$	$v_g + 1 - c_p - c_c$	each episode has a random sampled goal direction
movecont	velocity samples from a continuous range of all unit directions	$v_g + 1 - c_p - c_c$	each episode has a random sampled goal direction
dynamicg4	velocity samples from: $\{g_0, g_1, g_2, g_3\}$	$v_g + 1 - c_p - c_c$	the goal direction is re-sampled with probability 0.005 at each time-step
dynamiccont	velocity samples from a continuous range of all unit directions	$v_g + 1 - c_p - c_c$	the goal direction is re-sampled with probability 0.005 at each time-step
reachg4	position samples from $\{g_0, g_1, g_2, g_3\}$	$I(\ x - g\ _2^2 < 0.5)$	The agent is only rewarded when reaching a goal position
reachcont	position samples from the unit circle	$I(\ x - g\ _2^2 < 0.5)$	The agent is only rewarded when reaching a goal position

Table 3.1: Summary of Ant-based environments

learning for continuous control, specifically robot control problems. The action of these environments usually stands for mechanics-related physical quantity, such as motor torque and target motor phase. However, the traditional KL-divergence based algorithms are not suitable for these problems. Because the KL-divergence cannot represent the "deviation of policy" of the problem well, because a small perturbation in the mean value of a policy will lead to a large KL-divergence when the variance is small.

Therefore, we propose to use another criteria, which is the Wasserstein metric, to measure the deviation of the policy updates. We reformulate the trust region policy optimization problem as follows:

$$\begin{aligned} & \underset{\theta}{\text{maximize}} \quad J(\theta) \\ & \text{subject to} \quad \overline{W}_2(\pi_{\theta_{old}}, \pi_{\theta}) \leq \delta_W \end{aligned} \tag{3.2}$$

where  $\overline{W}_2(\pi_{\theta_{old}}, \pi_{\theta})$  is the average Wasserstein-2 metric between the old policy and the current policy.

The Wasserstein-2 metric is defined by the following equation [31]:

$$W_2(P, Q) = \inf_{\Gamma \in \mathbb{P}(X \sim P, Y \sim Q)} \mathbb{E}_{X, Y \sim \Gamma} [\|X - Y\|_2^2]^{1/2} \tag{3.3}$$

where  $\mathbb{P}(X \sim P, Y \sim Q)$  is the set of all joint distribution of  $X, Y$  with marginals  $P, Q$  respectively.

Specifically, when  $P$  and  $Q$  are Gaussian distributions with mean  $m_1, m_2$  and covariance matrix  $\Sigma_1$  and  $\Sigma_2$ , the squared value of Wasserstein-2 distance  $W_2^2(\cdot)$  is defined as the following equation [32] :

$$W_2^2(P, Q) = \|m_1 - m_2\|_2^2 + \text{Tr} \left( \Sigma_1 + \Sigma_2 - 2(\Sigma_1^{1/2} \Sigma_2 \Sigma_1^{1/2})^{1/2} \right) \tag{3.4}$$

The problem is solved by performing gradient updates iteratively following the natural gradient with the Rianmanian metric as  $W_2$  metric:

$$s = H_{\theta} \left( \overline{W}_2^2(\pi_{old}, \pi) \right)^{-1} g := A^{-1} g \tag{3.5}$$

We use the approximation of the Rianmanian metric tensor A:

$$A \approx \mathbb{E}_{s_t} \left[ \nabla_{\theta} W_2^2(\pi_{old}, \pi) \left( \nabla_{\theta} W_2^2(\pi_{old}, \pi) \right)^T \right] \tag{3.6}$$

The solution of  $s$  is then computed using Kronecker-factor approximation technique [10].

The policy is then updated following the gradient direction  $s$  with ADAM stochastic optimization algorithm [33]. The step size is adjusted in an adaptive manner according to the resulting  $W_2$  distance at each training step.

### 3.3 Efficient Exploration Through Exceptional Advantage Regularization

One of the major reasons that multi-modality robot environments are challenging is because the features in different modalities have different complexities.

In the target case, where there are two modality: the locomotion state vector and the image input, the agent is very likely to get stuck at a local minimum after having learned the features of the locomotion state vectors while haven't learned the image features. However, the policy is at a much lower entropy at the phase when the agent starts to learn image features.

As far as we know, the distribution type of the continuous stochastic policy in reinforcement learning is always chosen to be normal distribution with diagonal covariance matrices in the works on policy gradient methods . We have observed a phenomenon in the training process of policy gradient methods that, the variance of the policy is extremely unlikely to be increased, even when the agent has just escaped from a local minimum. Therefore, a regulation method becomes necessary to encourage the exploration of the agent when it finds that its policy has converged too fast at a sub-optimal point.

A conventional regularization method for encouraging exploration is entropy regularization:

$$g' = g + \beta_{ent} \nabla_\theta \mathbb{E}[H(\pi_\theta(a|s))] \quad (3.7)$$

Where  $\beta_{ent}$  is the weight controlling the penalty on low entropies. The entropy of a normal distribution  $\mathcal{N}(\mu, \Sigma)$  is defined as:

$$H(\pi) = \frac{1}{2} \ln \det(2\pi e \Sigma) \quad (3.8)$$

When the policy distribution is a normal distribution with diagonal covariance matrix, the entropy regularization basically introduces a constant bias in the gradient of the

logarithm of variance parameters. As a result, the entropy regularization method is usually hard to tune, and leads to degradation on learning performance.

Here we propose a novel method that can efficiently encourage exploration without large penalty on the agent’s learning performance. We add a loss, namely Exceptional Advantage Regularization loss (EAR), to the original gradient of the variance parameters:

$$g'_\Sigma = g_\Sigma + \beta_{exc} \mathbb{E} \left[ \max \left( 0, I(\hat{A}^{GAE} > 0) \hat{A}^{GAE} \nabla_\Sigma \log \pi(a|s) \right) \right] \quad (3.9)$$

where  $\beta_{exc}$  is the weight controlling the bias on exploration, and  $I(\cdot)$  is the indicator function, which returns 1 if the expression is true, otherwise 0.

The EAR loss add weights for the positive gradients of the variance parameters of the samples with positive advantage values. The reason behind the loss is that we want to add more importance to the samples which produce exceptionally positive advantage value, but with low sampling likelihood. Therefore we first only focus on points with positive advantage values. The problem remaining is to identify the points with low likelihood, namely “exceptional” points. We simply choose these points that produce positive gradients any of the variance parameters.

### 3.4 Efficient Exploration Through Robust Concentric Mixture Gaussian Policy

Apart from the EAR method for exploration, we propose to use an alternative probability distribution type, namely Concentric Mixture Gaussian, instead of a diagonal Gaussian policy.

The proposed policy distribution, namely Robust Concentric Mixture Gaussian (RCMG) Policy, is a mixture of two Gaussian distributions:

$$\pi(a|s) = (1 - \alpha_{ex}) \mathcal{N}(\mu, \Sigma) + \alpha_{ex} \mathcal{N}(\mu, q_{ex} \Sigma) \quad (3.10)$$

where the constant  $\alpha_{ex}$  is the weight of second distribution, which for example can be set at 0.05, and the constant  $q_{ex} > 1$ , for example  $q_{ex} = 5$ , controls the standard deviation of the second deviation.

Although the KL divergence between the two RCMG policy doesn’t have a analytical

form, the Wasserstein-2 distance between two RCMG policy can be given by:

$$W_2(\pi_0(a|\mu_0, \Sigma_0), \pi_1(a|\mu_1, \Sigma_1) = (1 - \alpha_{ex})W_2(\mathcal{N}(\mu_0, \Sigma_0), \mathcal{N}(\mu_1, \Sigma_1)) + \alpha_{ex}W_2(\mathcal{N}(\mu_0, q_{ex}\Sigma_0), \mathcal{N}(\mu_1, q_{ex}\Sigma_1)) \quad (3.11)$$

The RCMG policy is much more robust than an ordinary Gaussian policy because it has much longer tails.

### 3.5 Hierarchical reinforcement learning architecture

We propose to solve the reinforcement learning problem by a two-level hierarchical model.

The hierarchical model consists of a top-level decider agent and a set of bottom-level actuator agents. The actuator agents' policies are trained in the source task environments.

The decider agent takes an action at every time-step. It may either decide which actuator-policy should be executed, or simply skip and continue current actuator-policy. Therefore, assume there are  $n_a$  sub-policies, the action space of the root agent is an  $(n_a + 1)$ -discrete action space.

The observation space of the root agent consists of 2 parts, original state (motion-sensor observation, image observation) and the meta state. The meta observation state the current sub-policy being executed and the number of time-steps since the last decision has been made.

Empirically, the decider agent is parameterized by two policy networks,  $\theta_s$  and  $\theta_d$ . The network  $\theta_s$ , namely switcher network, outputs a binary action that decides whether the agent should simply continue using the current acting actuator policy, or make the full decision based on the current state. The network  $\theta_d$ , namely decider network, outputs an  $n_a$ -discrete action space, that select the acting actuator agent.

The overall decision-making process of the decider agent is shown in Algorithm 1.

---

**Algorithm 1** The decider agent mechanism

---

```

function DECIDERACT(self,st)
    adecider  $\sim \pi_{decider}(s_t)$ 
    if adecider  $\neq 0$  then
        self.currentActuator  $\leftarrow self.allActuators[a_{decider} - 1]$ 
        aactuator  $\leftarrow self.currentActuator.act(s_t)$ 
    return aactuator

```

---

## 3.6 Generalized advantage estimation for the decider agent

We propose a generalized advantage estimation method for decider agents hierarchical reinforcement learning agents.

Assume that a decider agent makes decisions at time  $t_1, t_2, \dots$ , then the execution length of the decisions are  $l_i = t_{i+1} - t_i, i = 1, 2, \dots$ .

Then the definition of reward of the decider action at  $t_i$  is given by:

$$\bar{r}_{t_i} := \sum_{l=0}^{t_{i+1}-t_i-1} \gamma^l r_{t_i+l} \quad (3.12)$$

Define the TD residual  $\delta_{t_i}^V$  for  $i = 0, 1, \dots$  by:

$$\delta_{t_i}^V := -V(s_{t_i}) + \bar{r}_{t_i} + \gamma^{t_{i+1}-t_i} V(s_{t_{i+1}}) \quad (3.13)$$

Then the k-step advantage estimation is given by:

$$\hat{A}_{t_i}^{(1)} := \delta_{t_i}^V = -V(s_{t_i}) + \bar{r}_{t_i} + \gamma^{t_{i+1}-t_i} V(s_{t_{i+1}}) \quad (3.14)$$

$$\hat{A}_{t_i}^{(2)} := \delta_{t_i}^V + \gamma^{t_{i+1}-t_i} \delta_{t_{i+1}}^V = -V(s_{t_i}) + \bar{r}_{t_i} + \gamma^{t_{i+1}-t_i} \bar{r}_{t_{i+1}} + \gamma^{t_{i+2}-t_i} V(s_{t_{i+2}}) \quad (3.15)$$

$$\hat{A}_t^{(3)} := \delta_t^V + \gamma \delta_{t+1}^V + \gamma^2 \delta_{t+2}^V = -V(s_t) + r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + \gamma^3 V(s_{t+3}) \quad (3.16)$$

$$\begin{aligned} \hat{A}_{t_i}^{(k)} &:= \sum_{d=0}^{k-1} \gamma^{t_{i+d}-t_i} \delta_{t_{i+d}}^V \\ &= -V(s_t) + \bar{r}_{t_i} + \gamma^{t_{i+1}-t_i} \bar{r}_{t_{i+1}} + \cdots + \gamma^{t_{i+k-1}-t_i} \bar{r}_{t_{i+k-1}} + \gamma^{t_{i+k}-t_i} V(s_{t_{i+k}}) \end{aligned} \quad (3.17)$$

We can define the unnormalized generalized advantage estimator as a exponentially-weighted sum of these k-step advantage estimators [11]:

$$\begin{aligned}\hat{A}_{t_i}^{GAE_{unnorm}(\lambda)} &:= \hat{A}_{t_i}^{(1)} + \lambda^{t_{i+1}-t_i} \hat{A}_{t_i}^{(2)} + \lambda^{t_{i+2}-t_i} \hat{A}_{t_i}^{(3)} + \dots + \lambda^{t_{i+k-1}-t_i} \hat{A}_{t_i}^{(k)} \\ &= \delta_{t_i}^V + \lambda^{t_{i+1}-t_i} (\delta_{t_i}^V + \gamma^{t_{i+1}-t_i} \delta_{t_{i+1}}^V) \\ &\quad + \lambda^{t_{i+2}-t_i} (\delta_t^V + \gamma^{t_{i+1}-t_i} \delta_{t_{i+1}}^V + \gamma^{t_{i+2}-t_i} \delta_{t_{i+2}}^V) + \dots\end{aligned}\tag{3.18}$$

$$+ \lambda^{t_{i+k-1}-t_i} \sum_{d=0}^{k-1} \gamma^{t_{i+d}-t_i} \delta_{t_{i+d}}^V\tag{3.19}$$

$$\begin{aligned}&= (\delta_{t_i}^V \sum_{b=0}^{k-1} \lambda^{t_{i+k-1}-t_i} + \gamma^{t_{i+1}-t_i} \delta_{t_{i+1}}^V \sum_{b=1}^k \lambda^{t_{i+b}-t_i} \\ &\quad + \gamma^{t_{i+2}-t_i} \delta_{t_{i+2}}^V \sum_{b=2}^k \lambda^{t_{i+b}-t_i} + \dots \\ &\quad + \gamma^{t_{i+k-1}-t_i} \delta_{t_{i+k-1}}^V \lambda^{t_{i+k-1}-t_i})\end{aligned}\tag{3.20}$$

$$= \sum_{d=0}^{k-1} \delta_{t_i}^V \gamma^{t_{i+d}-t_i} \sum_{b=0}^{k-1} \lambda^{t_{i+b}-t_i}\tag{3.21}$$

The normalized generalized advantage estimator is then given by:

$$\hat{A}_{t_i}^{GAE(\lambda)} = \frac{\hat{A}_{t_i}^{GAE_{unnorm}(\lambda)}}{\sum_{b=0}^{k-1} \lambda^{t_{i+b}-t_i}}\tag{3.22}$$

However, the unnormalized GAE estimator is usually used in practice instead of the normalized one, with a postprocessing step of batch normalization to adjust the scale of the advantages. This practical method usually lead to large advantage scales for experience data at the beginning of the episodes and small scales for the experience data near episode ends.

### 3.7 Training of the switcher agent

We train the switcher agent using a flat reinforcement learning method according to the return of the target task, because it needs to make decisions at every time step. However, we add an extra loss so that the switcher network will tend to reduce the number of decision points of the decision network:

$$J'(\theta_s) = J'(\theta_s) + \mathbb{E}[\pi_s(s)]\tag{3.23}$$

Where  $\pi_s$  is the output of the switcher network.

## 3.8 Efficient training of actuator policies

We have found that the straight-forward reuse of source task policies in the target task may not work.

For example, consider the target task as "dynamicg4" and the set of source tasks as "move0", "move1", "move2", "move3". When the goal direction in "dynamicg4" changes from  $(-1, 0)$  to  $(1, 0)$  the correct decider policy should be switching from "move1" to "move0". However, the actuator policy of "move0" fails to perform properly, because the initial state is sampled from the states generated by "move1" policy, rather than the original initial state distribution.

A straight-forward method to solve this problem is to perform joint training of actuator policy in the target task, with a uniform random decision policy and fixed-length switcher policy. However, this method makes the training much slower and much more ineffective.

There is a study [34] that proposes a method to improve the robustness of policies. The method basically artificially adds variance to the environments, so that the trained policy will be able to deal with a larger variety of circumstances. However, this method doesn't work in our case. Because simply increasing the variance of initial states will unnecessarily lead the agent to start with many unstable states that would otherwise not be encountered, and it is infeasible to manually design the generative model for all the possible states in the target task.

### 3.8.1 Domain randomization by cross-sampling initial states

We propose a novel method for training robust actuator agents, namely domain randomization by cross-sampling initial states. We train all the source tasks simultaneously. During the training, each actuator agent keeps a experience buffer that store its state history. At the beginning of each episode, the actuator environment randomly selects the initial state from the set of its initial state distribution and the experience buffer of other tasks. This will guarantee that each actuator agents will encounter states generated by other agents. The proposed method is also more efficient than the direct joint training method, and doesn't require domain-specific engineering. ]

# Chapter 4

## Experiments

### 4.1 Experiments on the basic source tasks

We discuss and compare the methods in solving the basic task "move0" in this section.

As is observed by many studies [30], one of the disadvantages with the traditional KL-divergence based is that the performance result could be inconsistent across different runs, due to the agent getting stuck at local minimum. One example is the performance of the ACKTR [10] method on the "move0" task. An example result is shown in Figure 4.1, where we train the same ACKTR agent on the task "move0" with batch-size 8000, KL-divergence 0.0001 and 20 parallel agents. It appears that one agent gets stuck at the a score below 300 while another continues to improve after reaching the score of 4000.

We observe that the conventional KL-divergence based trust region policy gradient methods in general could get stuck easily at some local minimum before the policy converges to the optimal solution. An experiment showing the performance of the original ACKTR algorithm is shown in Figure 4.2. We observe that the agents tend to get stuck around the total return of 3000. The reason might be that while the KL-divergence based trust-region method provides a theoretical guarantee on the monotonic improvement of performance, the agent might converge too early at local minimums and fails to make efficient exploration.

We propose that the proposed W-KTR method is less prone to the local minimum problem on the task "move0". The experiment comparing the performance of W-KTR agents with different parameters is shown in Figure 4.3. We can see that none of the agents get stuck at the local minimum around 3000, and their final performance can reach a total return of 6000. However, the W-KTR agent appears to have a much slower

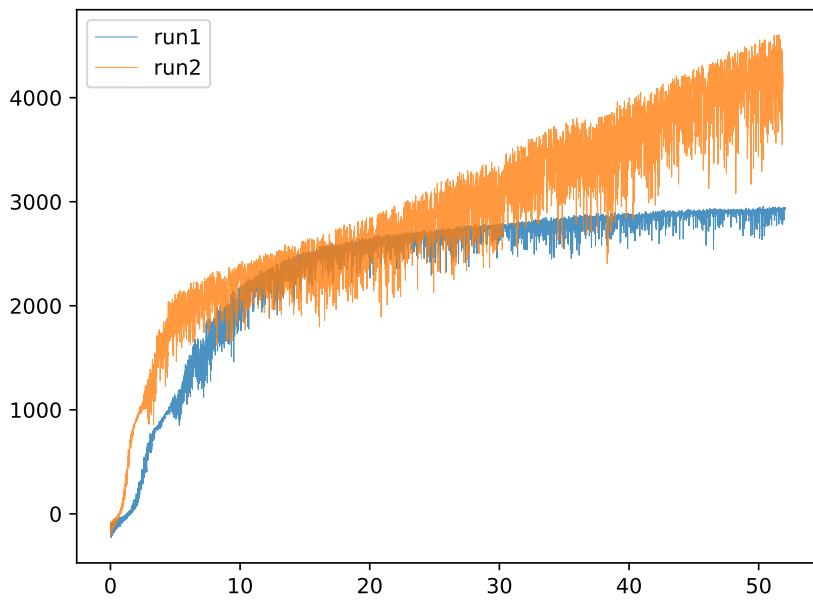


Figure 4.1: Inconsistent performance produced by ACKTR agents with the same parameters but different runs. The vertical axis is the total return averaged over the recent 20 episodes and the horizontal axis is the number of million time-steps

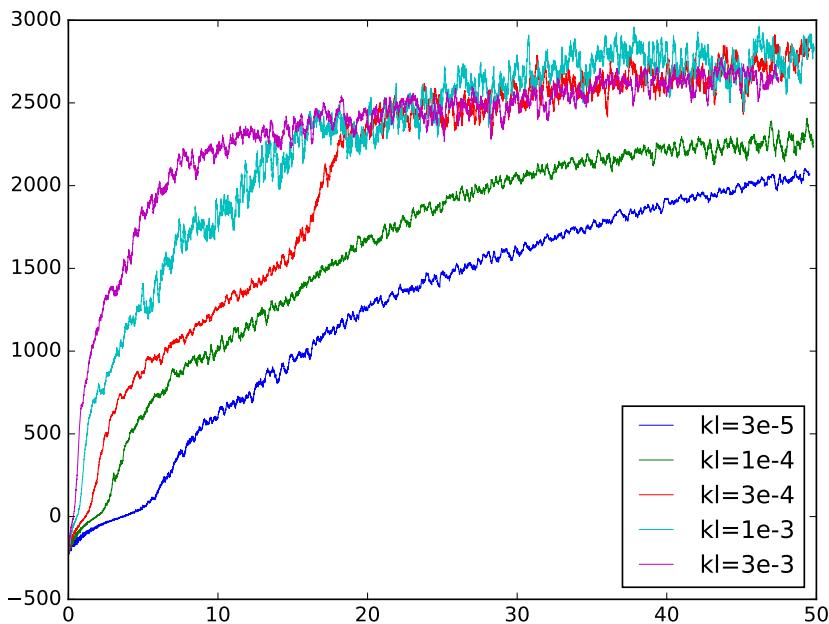


Figure 4.2: Performance of ACKTR agents with different KL-divergence constraints. All the agents are trained with batch-size 4000 and 20 parallel agents. The vertical axis is the total return averaged over the recent 200 episodes and the horizontal axis is the number of million time-steps

improvement rate before 50 million time-steps.

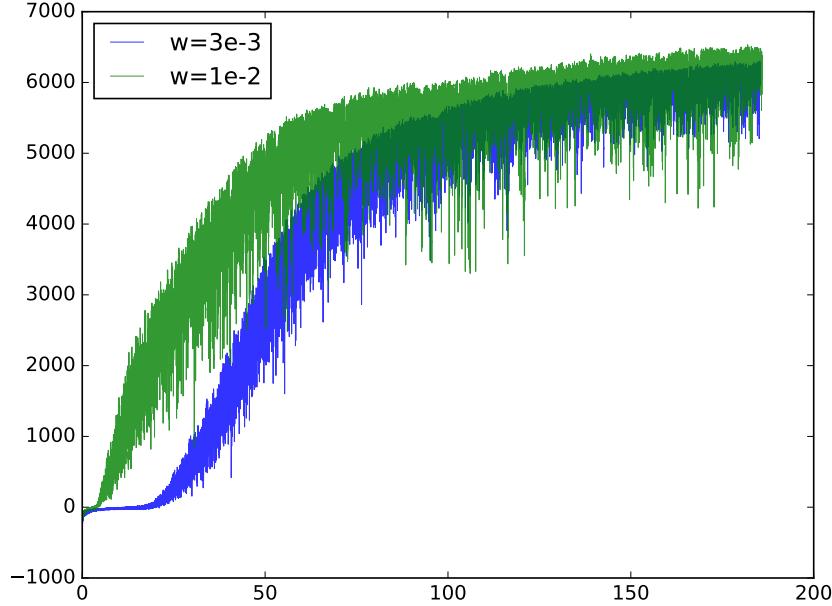


Figure 4.3: Performance of W-KTR agents with different W2-metric constraints. All the agents are trained with batch-size 4000 and 20 parallel agents. The vertical axis is the total return averaged over the recent 200 episodes and the horizontal axis is the number of million time-steps

One proposal to solve the slow initial improvement rate problem of W-KTR method is to apply a decaying Wasserstein constraint at the beginning. The performance of a proposed W-KTR agent with decaying Wasserstein constraint is shown in Figure 4.4. The agent can achieve much faster improvement rate in the first 50 million time-steps. The limitation is that there are more hyper-parameters to be tuned in this algorithm.

In conclusion, we have verified that the proposed W-KTR method can achieve the state-of-art final performance in the basic "move0" task, and is able to produce consistent final results across different runs.

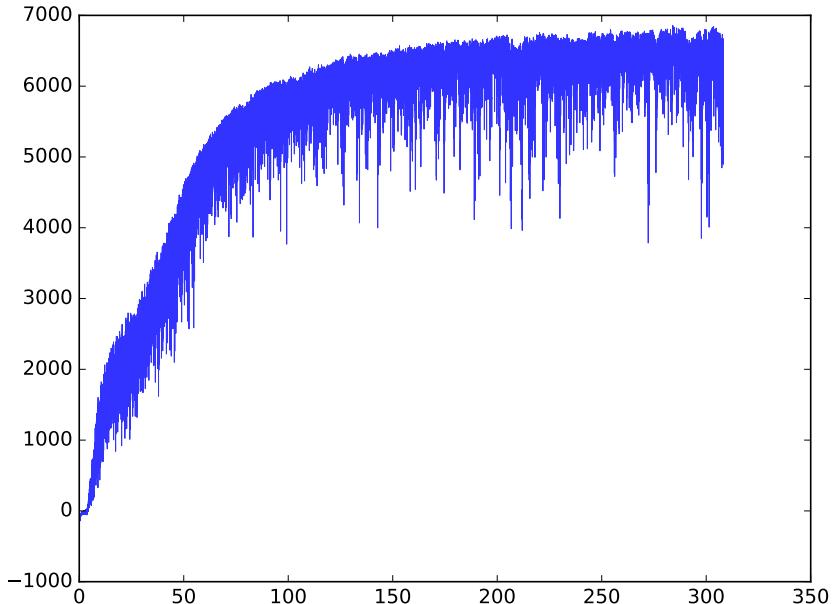


Figure 4.4: Performance of a W-KTR agent with a decaying W2-metric from 0.02 to 0.00003 in the first 15 million time-steps. The agent is trained with batch-size 4000 and 20 parallel agents. The vertical axis is the total return averaged over the recent 200 episodes and the horizontal axis is the number of million time-steps

## 4.2 Experiment on the flat reinforcement learning solution to multi-modality tasks

### 4.2.1 Discussion on conventional flat reinforcement learning methods

We observe contemporary end-to-end flat reinforcement learning methods fail to achieve good performance. We suggest that one of the important reason is the image features are much harder to learn than the state. The agent would tend to stuck at a local minimum when it has already learned the state features well, but has not been able to extract any useful information from the image. However, when the agent has finally learned the image features, the policy already converge to a relatively low-entropy distribution, and contemporary reinforcement learning methods cannot perform exploration again at this phase.

We take the task "movecont" as an example. In this task, a goal direction as sampled uniformly at random from the continuous range of angles:  $[0, 2\pi)$ , at the beginning of each episode. The agent can only indicate the goal direction from the image, where there

is a sphere object at the corresponding position.

A conventional method for encouraging exploration of reinforcement learning agents with continuous action space is entropy regularization. As we discussed in the section 3.3, the entropy regularization method is not an effective method in the general case because it simply adds constant biases on the policy parameters and may dominate the learning of the original task.

An experiment on the effectiveness of entropy regularization is shown in Figure 4.5. The agents are trained using ACKTR algorithm with 32 parallel agents, minibatch-size 2560 and KL-divergence constraint 0.0003. The result shows that the agent easily fails to learn the original task when the weight on entropy term is too large.

The change of average Standard Deviation of the policy distributions is shown in Figure 4.6. The agents' policy distributions appear to get stuck at certain level of standard deviation when the entropy term is not optimal.

### 4.2.2 Experiment on exceptional advantage regularization

We discuss the effectiveness of exceptional advantage regularization method on multi-modality tasks in this section.

We first demonstrate the general patterns of the distribution on the advantage values on the simple multi-modality task "moveg2". In this task, the goal direction is sampled from 2 opposite directions. The task is much more simple than the "movecont" task because the agent only needs to learn from the image whether it needs to go forward or backward.

The performance on the total return of an ACKTR agent is shown in Figure 4.7. The performance in terms of average reward per time-step is shown in Figure 4.8, and the average standard deviation is shown in Figre 4.9.

The distribution of advantage values at the first batch (batch 0) is shown in Figure 4.10. It can be seen that the advantage values are distributed uniformly across different values of log-likelihood because the critic model has not been trained. After the critic model has been trained for a reasonable amount of time, the marginal distribution advantage value tend to follow a normal distribution with zero mean. An example is shown in Figure 4.11, which is the distribution at batch 3000. However, the advantage values are likely to have higher values at low log-likelihood samples when the agent has just escaped from a local

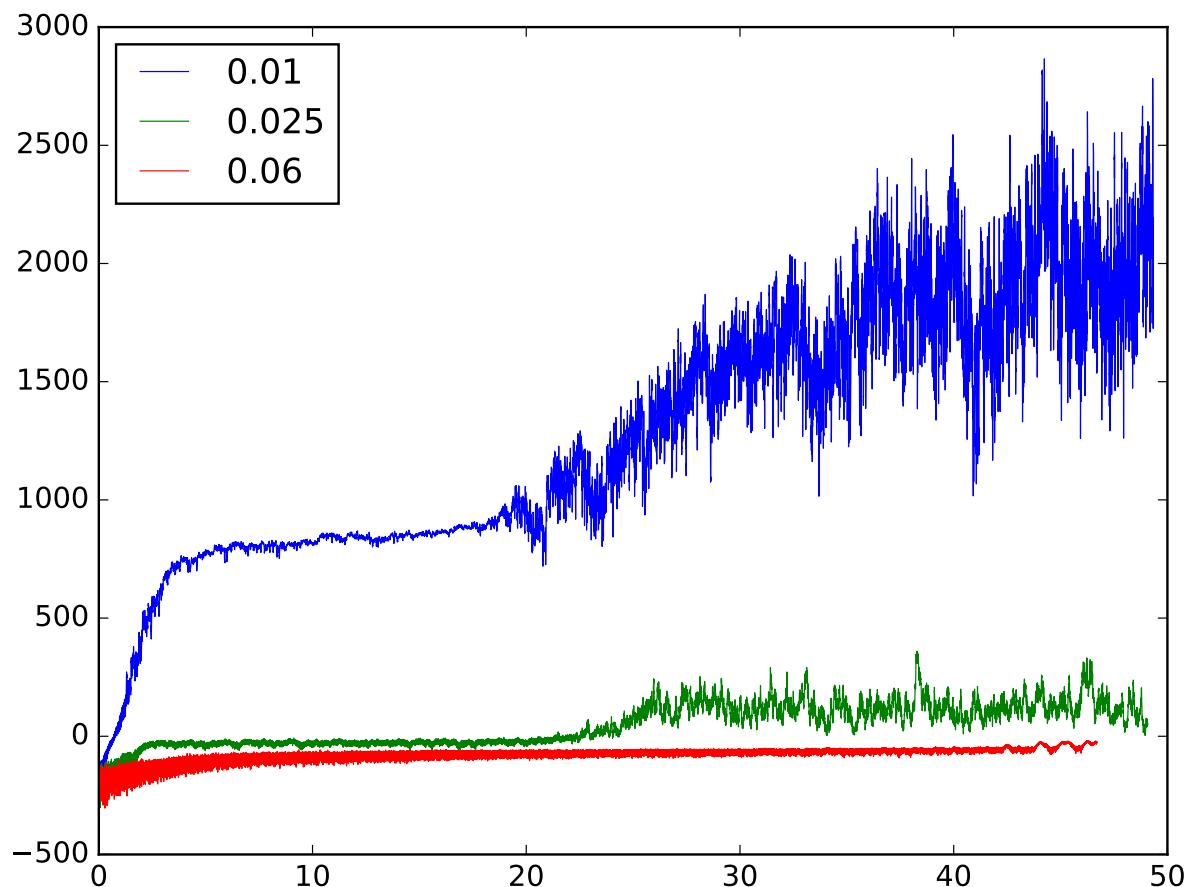


Figure 4.5: Performance of agents with different weight on entropy regularization term, the horizontal axis is the number of million timesteps and the vertical axis is the total episode reward averaged over the last 32 episodes

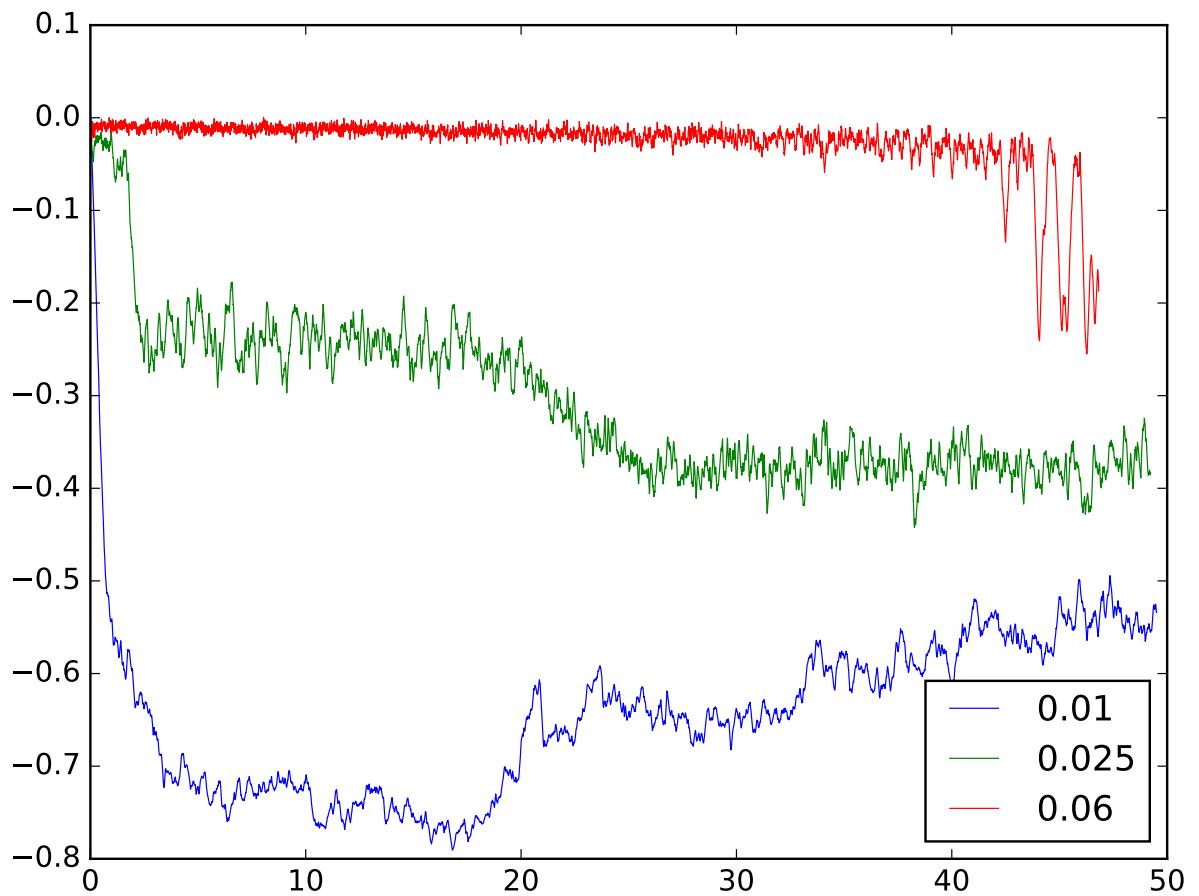


Figure 4.6: Logarithm of average standard deviation of the policy of agents in Figure 4.5, the horizontal axis is the number of million timesteps.

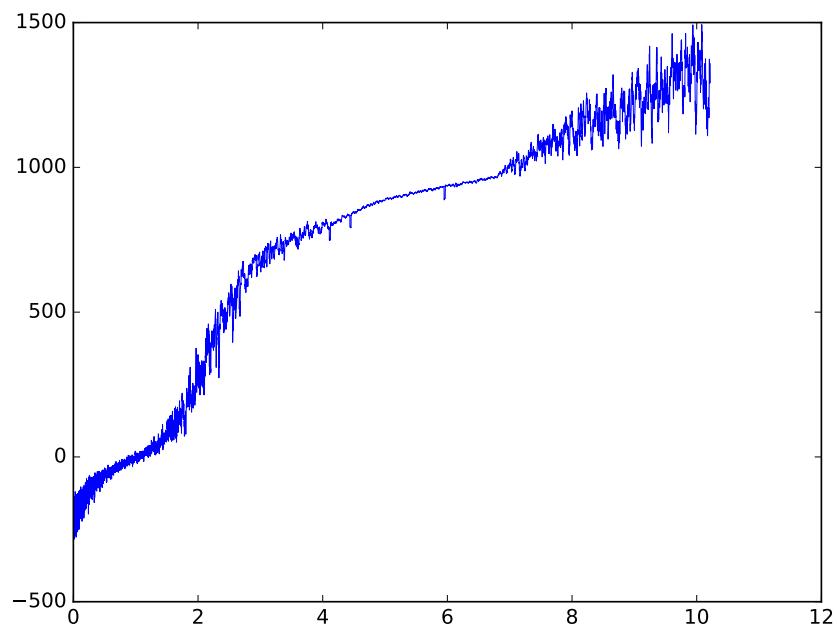


Figure 4.7: Performance of ACKTR agent on the "moveg2" task, the horizontal axis is the number of million timesteps and the vertical axis is the total episode reward averaged over the last 20 episodes

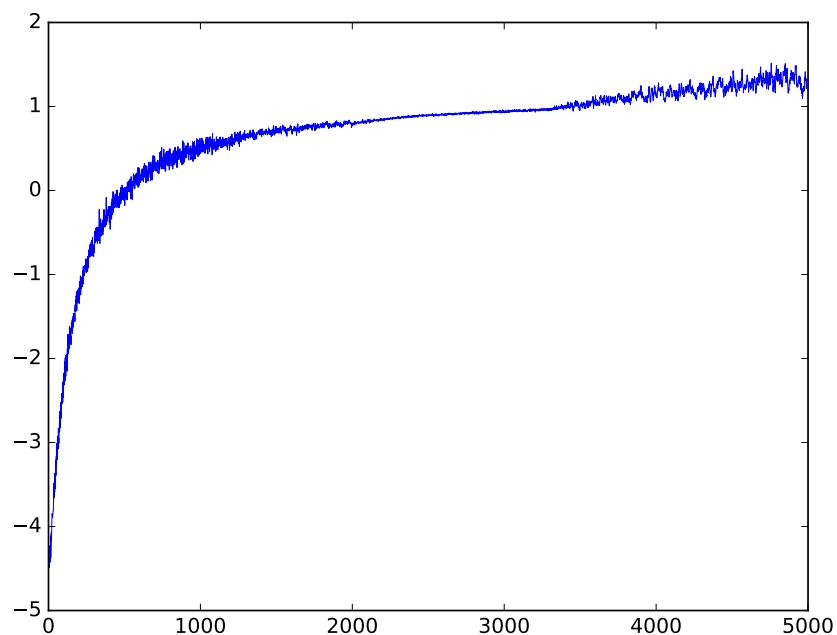


Figure 4.8: The avearge reward per time-step of ACKTR agent on the "moveg2" task, the horizontal axis is the number of training batches

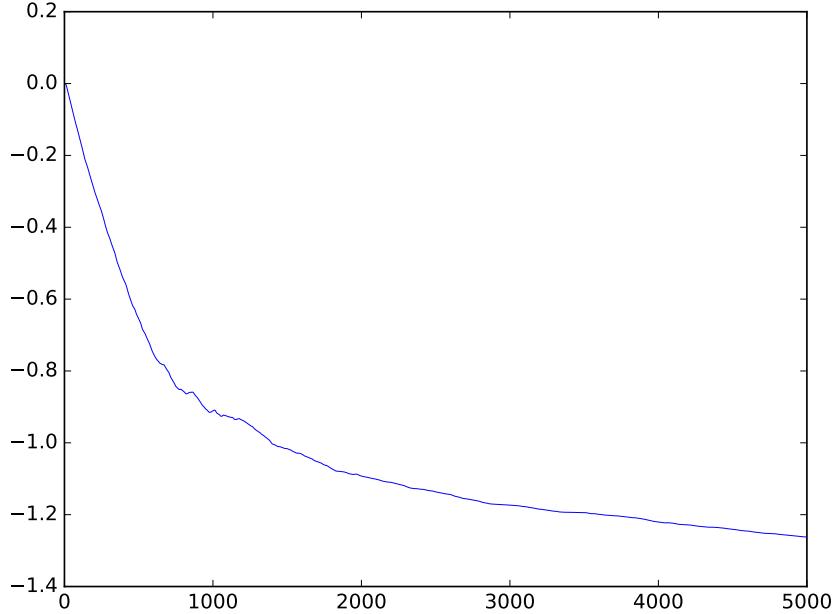


Figure 4.9: The logarithm of avearge standard deviation of ACKTR agent’s policy on the ”moveg2” task, the horizontal axis is the number of training batches

minimum. An example is Figure 4.12, which shows the the distribution of advantage values at batch 4900. It can be seen that the distribution becomes significantly different because many positive advantage points are spread across different log-likelihoods.

Intuitively, a large number of points with low log-likelihood but high advantage value indicates that the agent needs to increase the degree of exploration. However, the figure 4.9 on the change of standard deviation shows that the agent actually still keep decreasing the standard deviations of its policy even at this state. Therefore, the application of a exceptional advantage regularization term, could be useful in encouraging exploration in these cases.

We then verify the performance of exceptional advantage regularization on the ’move-cont’ task. The performance of an ACKTR agent with different weights exceptional advantage regularization on the in Figure 4.13, and the average standard deviation parameter of their policies are shown in Figure 4.14. All the agents are trained with batch-size 2560 and KL-divergence constraint 0.0003. The weight-0 agent is the same as the original ACKTR agent without any exploration regularization, and it could only achieve a total reward of around 2000 at the end of training. The agent with exceptional advantage regularization weight 0.04 can improve rapidly in the early phase before 40 million timestep, but gets stuck at around 3500. This shows that the exceptional advantage regularization

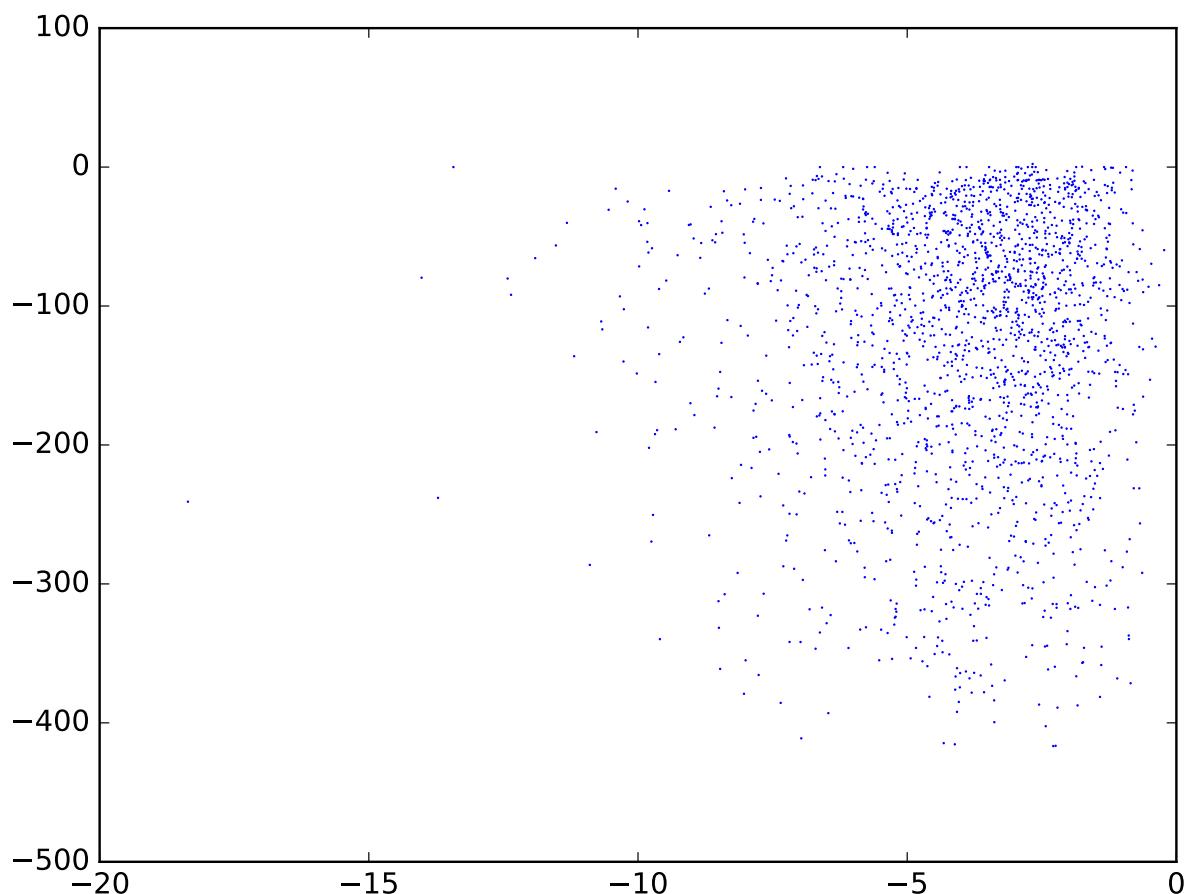


Figure 4.10: The distribution of advantage values of the ACKTR agent at batch 0 on the "moveg2" task, the horizontal axis is the log-likelihood value

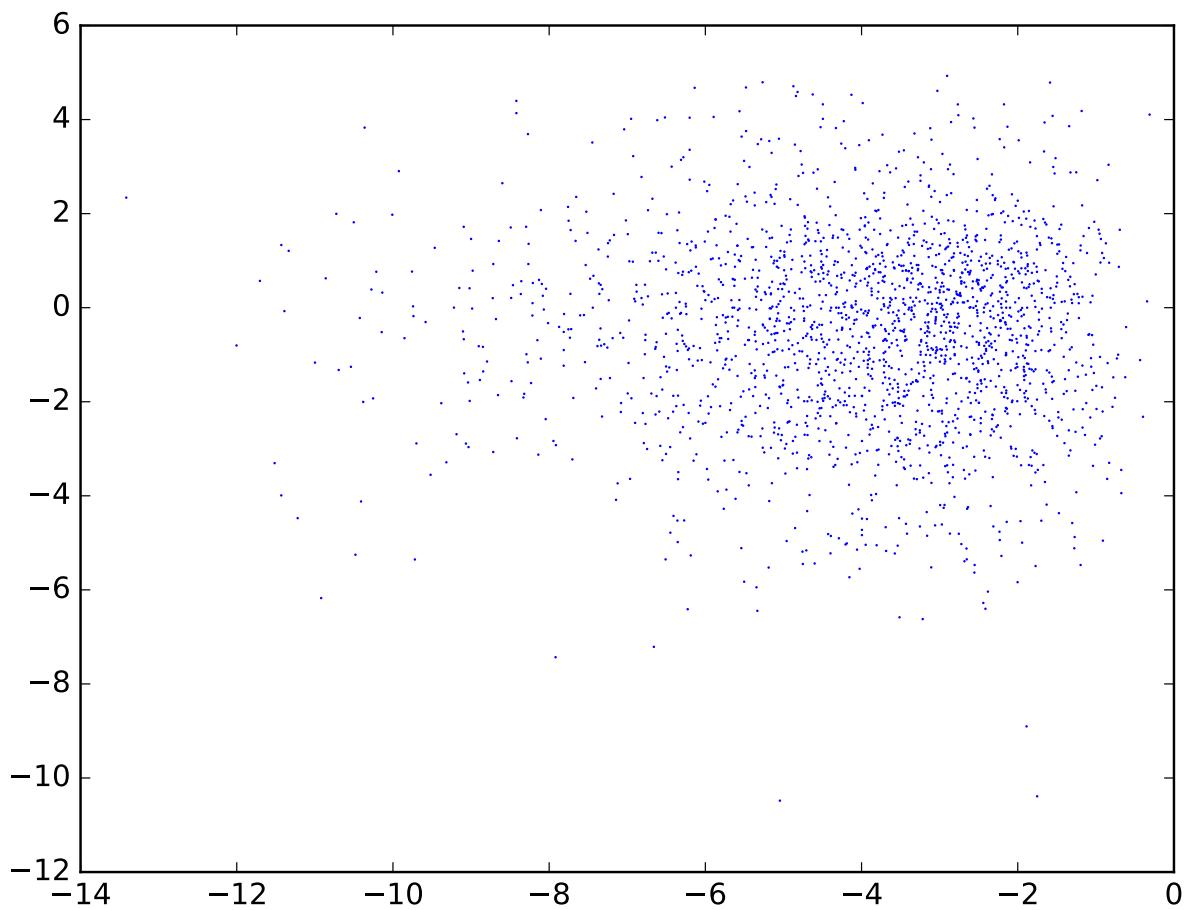


Figure 4.11: The distribution of advantage values of the ACKTR agent at batch 300 on the "moveg2" task, the horizontal axis is the log-likelihood value

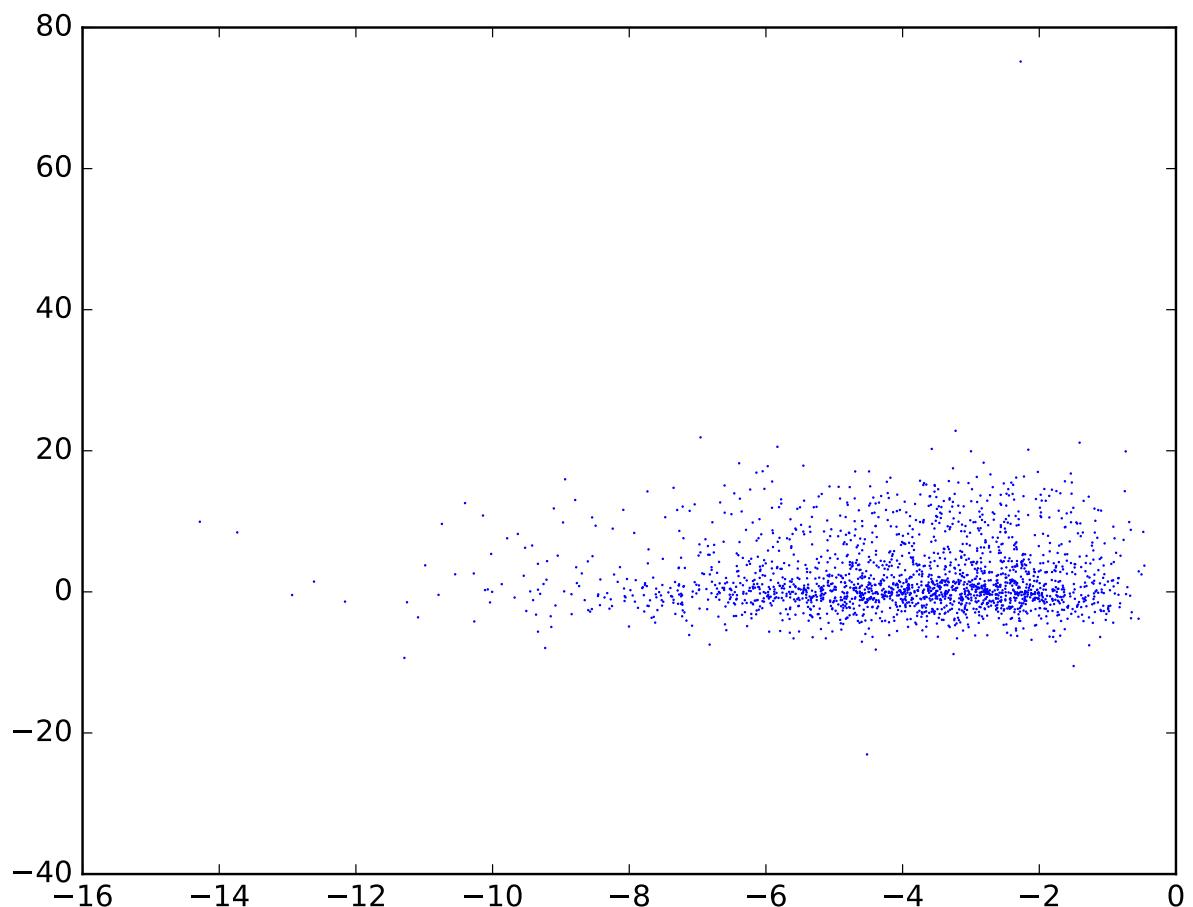


Figure 4.12: The distribution of advantage values of the ACKTR agent at batch 4900 on the "moveg2" task, the horizontal axis is the log-likelihood value

method could have adverse effect on the convergence of policy in the late phase of training, which is also indicated in by average std curve. The agent with exceptional advantage regularization weight 0.01 achieves the best final performance. Its average standard deviation shows that the agent manages to increase its policy entropy and re-explore the environment after it has escaped from a local minimum.

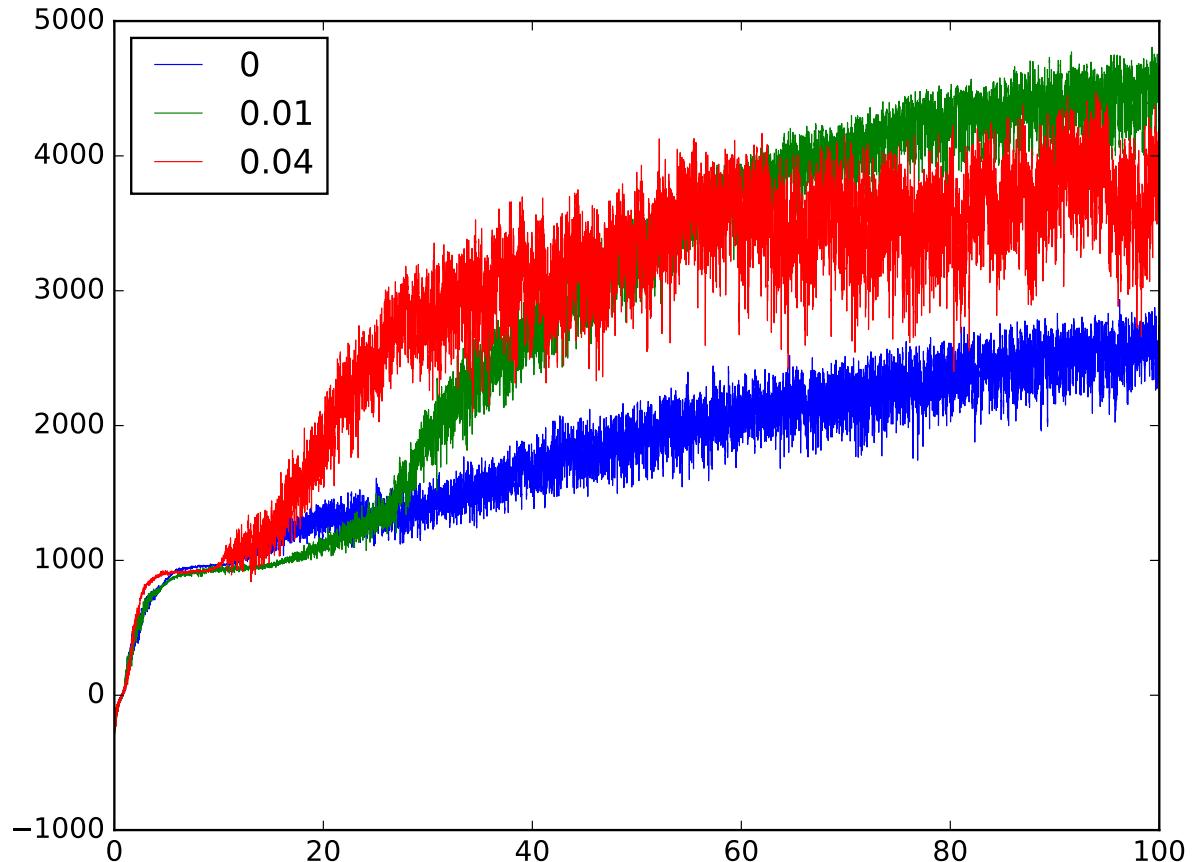


Figure 4.13: Performance of agents with different exceptional advantage regularization weights, the x-axis is the number of million time-steps and the y-axis is the total episode reward averaged over the last 32 episodes

#### 4.2.3 Experiment on the Robust Concentric Mixture Gaussian Policy

The effectiveness of robust concentric mixture Gaussian policy agent in exploration of task "movecont" is verified in this section.

The performance of an ACKTR mixture Gaussian policy agent is shown in Figure 4.15. The results shows that the mixture Gaussian policy agents have slower learning rates

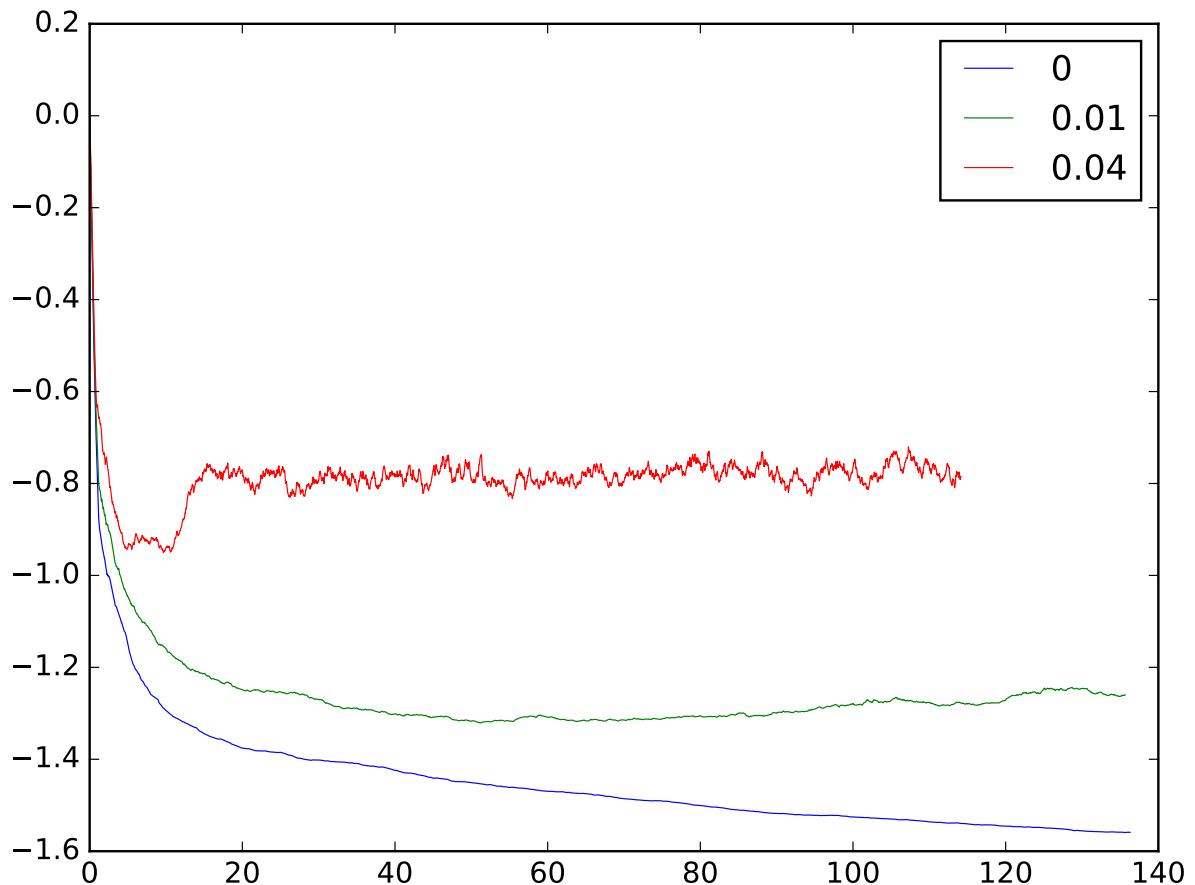


Figure 4.14: The logarithm of avearge standard deviation of agents with different exceptional advantage regularization weights, the horizontal axis is the number of million time-steps and the vertical axis is the total episode reward averaged over the last 32 episodes

compared to pure Gaussian policy agents. However, the agents are able to achieve a good fubak performance, with a total reward of around 4000 when the KL-divergence is set properly.

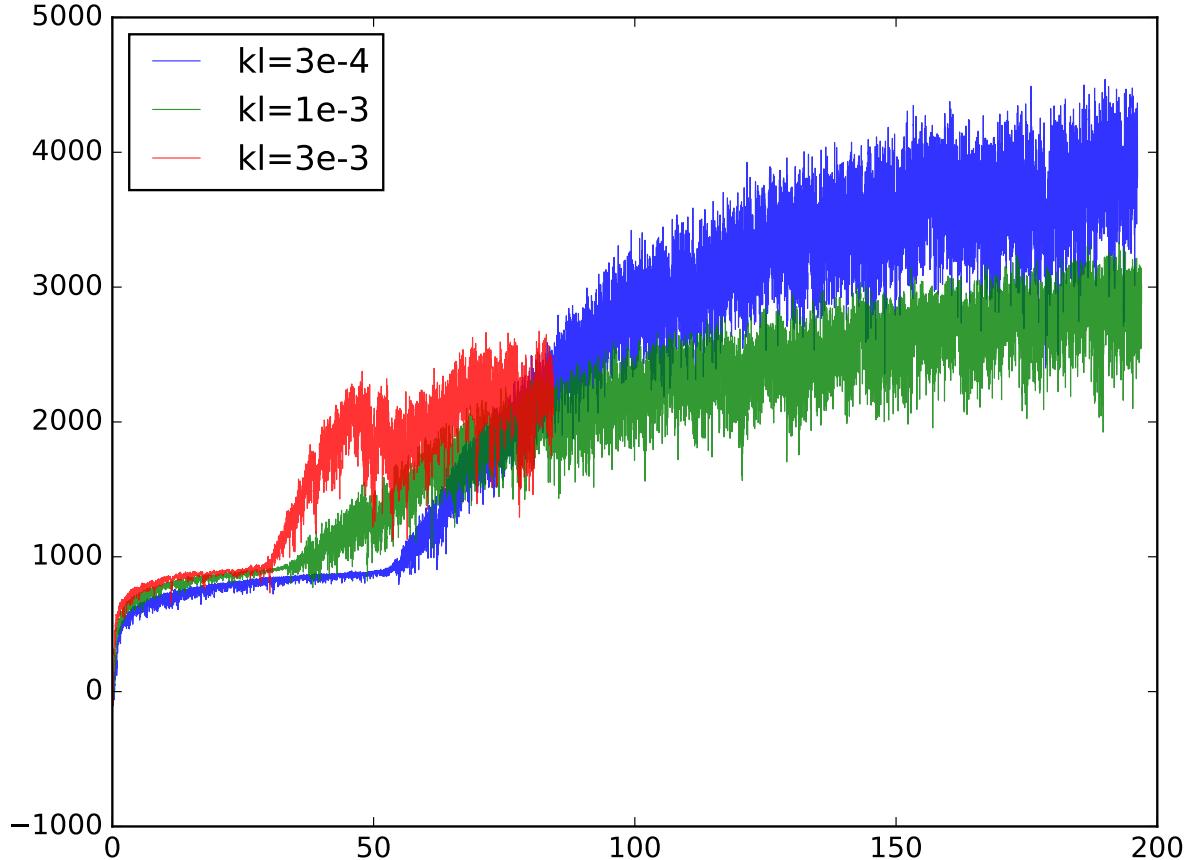


Figure 4.15: Performance of ACKTR agents with different KL-divergence constraints, the x-axis is the number of million time-steps and the y-axis is the total episode reward averaged over the last 32 episodes

### 4.3 Hierarchical reinforcement learning methods for multi-modality and sparse environments

This section will discuss the experiments on the proposed hierarchical reinforcement learning models.

In our experiment settings, we choose the set  $\{move0, move1, \dots, move7\}$  as source

tasks. We select "dynamicg4" as a representative target task for multi-modality environments and "reachcont" as a representative target task for multi-modality sparse environments.

The problem of hierarchical reinforcement learning is divided into two parts: learning robust actuator policies and learning the decider policies. The following two section will discuss these two problems.

### 4.3.1 Training of actuator agents

#### Domain randomization by cross-sampling initial states

We examine the efficiency of domain randomization by cross-sampling initial states in this section. A visualization on an experiment on the domain randomization by cross-sampling initial states method on the set of source tasks  $\{move0, move1, \dots, move7\}$  is shown in Figure 4.16.

The result shows that most of the actuator agents are able to learn efficiently, while some agents have much slower improvement rates. It is not expected that the agents have different learning behavior even they have the same parameters.

A possible reason might be the policy of other actuator agents can change the initial state distribution of the current agent, and its learning behavior might be influenced as a result. However, to learn a set of good actuator policies, this problem needs to be solved.

### 4.3.2 Training of decider agents

#### Training of decision policy

#### Training of switcher policy

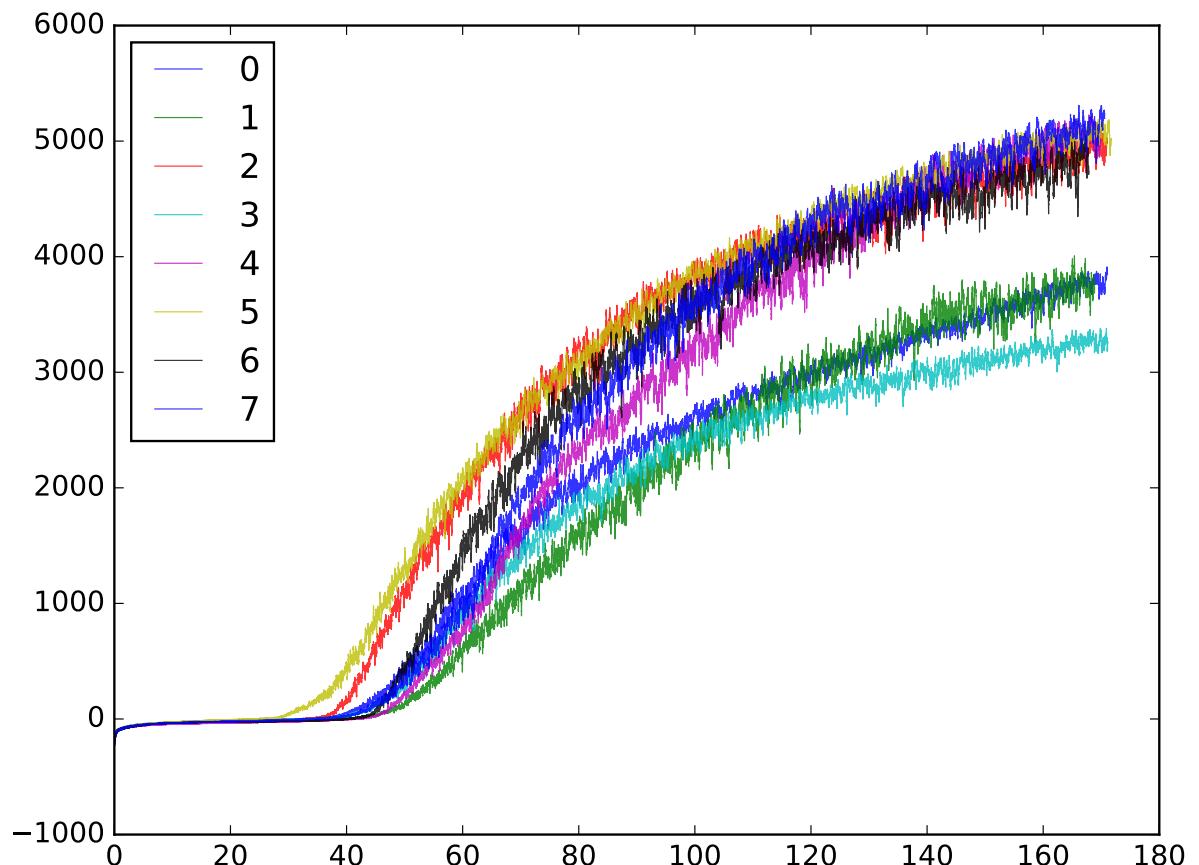


Figure 4.16: Performance of actuator agents with domain randomization by cross-sampling initial states, the x-axis is the number of million time-steps and the y-axis is the total episode reward averaged over the last 32 episodes

## **Chapter 5**

## **Discussion**

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