
S.V.T. Decomposition in Conformal to Flat Space

$$h_{00} = -2\phi$$

$$h_{0i} = w_i = \partial_i B + B_i$$

$$h_{ij} = -2\psi + S_{ij} = -2\psi + 2\partial_i \partial_j E + \partial_i E_j + \partial_j E_i + 2E_{ij}$$

where

$$\partial_i B^i = \partial_i E^i = 0$$

$$\partial_i E^{ij} = 0$$

$$\delta_{ij} E^{ij} = 0$$

$\Omega=1$ Gauge invariant quantities:

$$\psi = \psi$$

$$\mathcal{P} = \phi + \partial_0 B - \partial_0 \partial_0 E$$

$$\mathcal{F}_i = \partial_0 E_i - B_i$$

$$E_{ij} = E_{ij}$$

$\Omega=\Omega(t)$ Gauge invariant quantities:

$$C = \psi - \frac{\Omega'}{\Omega} (B - \partial_0 E)$$

$$\mathcal{P} = \phi + \frac{\Omega'}{\Omega} (B - \partial_0 E) + (\partial_0 B - \partial_0 \partial_0 E)$$

$$\mathcal{F}_i = \partial_0 E_i - B_i$$

$$E_{ij} = E_{ij}$$

 $\delta G_{\mu\nu}$

00	$6 \frac{\rho'}{\Omega} \partial_0 \psi - 2 \nabla^2 \psi + 2 \frac{\rho'}{\Omega} \nabla^2 (B - \partial_0 E)$
11	$-2 \partial_0 \partial_0 \psi - 2 \frac{\rho'}{\Omega} \partial_0 (\phi + 2\psi + E_{11}) + 2 [(\frac{\rho'}{\Omega})^2 - 2 \frac{\rho''}{\Omega}] (\phi + \psi - \partial_1 \partial_1 E - \partial_1 E_1 - E_{11}) -$ $(\nabla^2 - \partial_1 \partial_1) (\phi - \psi + \partial_0 B - \partial_0 \partial_0 E) - 2 \frac{\rho'}{\Omega} (\nabla^2 - \partial_1 \partial_1) (B - \partial_0 E) + (\partial_1 \partial_0 + 2 \frac{\rho'}{\Omega} \partial_1) (B_1 - \partial_0 E_1) + \square E_{11}$
22	$-2 \partial_0 \partial_0 \psi - 2 \frac{\rho'}{\Omega} \partial_0 (\phi + 2\psi + E_{22}) + 2 [(\frac{\rho'}{\Omega})^2 - 2 \frac{\rho''}{\Omega}] (\phi + \psi - \partial_2 \partial_2 E - \partial_2 E_2 - E_{22}) -$ $(\nabla^2 - \partial_2 \partial_2) (\phi - \psi + \partial_0 B - \partial_0 \partial_0 E) - 2 \frac{\rho'}{\Omega} (\nabla^2 - \partial_2 \partial_2) (B - \partial_0 E) + (\partial_2 \partial_0 + 2 \frac{\rho'}{\Omega} \partial_2) (B_2 - \partial_0 E_2) + \square E_{22}$
33	$-2 \partial_0 \partial_0 \psi - 2 \frac{\rho'}{\Omega} \partial_0 (\phi + 2\psi + E_{33}) + 2 [(\frac{\rho'}{\Omega})^2 - 2 \frac{\rho''}{\Omega}] (\phi + \psi - \partial_3 \partial_3 E - \partial_3 E_3 - E_{33}) -$ $(\nabla^2 - \partial_3 \partial_3) (\phi - \psi + \partial_0 B - \partial_0 \partial_0 E) - 2 \frac{\rho'}{\Omega} (\nabla^2 - \partial_3 \partial_3) (B - \partial_0 E) + (\partial_3 \partial_0 + 2 \frac{\rho'}{\Omega} \partial_3) (B_3 - \partial_0 E_3) + \square E_{33}$
01	$-2 \partial_1 \partial_0 \psi - 2 \frac{\rho'}{\Omega} \partial_1 \phi - [(\frac{\rho'}{\Omega})^2 - 2 \frac{\rho''}{\Omega}] (\partial_1 B + B_1) + \frac{1}{2} \nabla^2 (B_1 - \partial_0 E_1)$
02	$-2 \partial_2 \partial_0 \psi - 2 \frac{\rho'}{\Omega} \partial_2 \phi - [(\frac{\rho'}{\Omega})^2 - 2 \frac{\rho''}{\Omega}] (\partial_2 B + B_2) + \frac{1}{2} \nabla^2 (B_2 - \partial_0 E_2)$
03	$-2 \partial_3 \partial_0 \psi - 2 \frac{\rho'}{\Omega} \partial_3 \phi - [(\frac{\rho'}{\Omega})^2 - 2 \frac{\rho''}{\Omega}] (\partial_3 B + B_3) + \frac{1}{2} \nabla^2 (B_3 - \partial_0 E_3)$
12	$\partial_1 \partial_2 (\phi - \psi + \partial_0 B - \partial_0 \partial_0 E) + 2 \frac{\rho'}{\Omega} \partial_1 \partial_2 (B - \partial_0 E) + (\frac{1}{2} \partial_0 + \frac{\rho'}{\Omega}) (\partial_1 B_2 - \partial_1 \partial_0 E_2 + \partial_2 B_1 - \partial_2 \partial_0 E_1)$ $- [(\frac{\rho'}{\Omega})^2 - 2 \frac{\rho''}{\Omega}] (\partial_1 E_2 + \partial_2 E_1 + 2 \partial_1 \partial_2 E + 2 E_{12}) - 2 \frac{\rho'}{\Omega} \partial_0 E_{12} + \square E_{12}$
13	$\partial_1 \partial_3 (\phi - \psi + \partial_0 B - \partial_0 \partial_0 E) + 2 \frac{\rho'}{\Omega} \partial_1 \partial_3 (B - \partial_0 E) + (\frac{1}{2} \partial_0 + \frac{\rho'}{\Omega}) (\partial_1 B_3 - \partial_1 \partial_0 E_3 + \partial_3 B_1 - \partial_3 \partial_0 E_1)$ $- [(\frac{\rho'}{\Omega})^2 - 2 \frac{\rho''}{\Omega}] (\partial_1 E_3 + \partial_3 E_1 + 2 \partial_1 \partial_3 E + 2 E_{13}) - 2 \frac{\rho'}{\Omega} \partial_0 E_{13} + \square E_{13}$
23	$\partial_2 \partial_3 (\phi - \psi + \partial_0 B - \partial_0 \partial_0 E) + 2 \frac{\rho'}{\Omega} \partial_2 \partial_3 (B - \partial_0 E) + (\frac{1}{2} \partial_0 + \frac{\rho'}{\Omega}) (\partial_2 B_3 - \partial_2 \partial_0 E_3 + \partial_3 B_2 - \partial_3 \partial_0 E_2)$ $- [(\frac{\rho'}{\Omega})^2 - 2 \frac{\rho''}{\Omega}] (\partial_2 E_3 + \partial_3 E_2 + 2 \partial_2 \partial_3 E + 2 E_{23}) - 2 \frac{\rho'}{\Omega} \partial_0 E_{23} + \square E_{23}$