de Sitter Geometries

de Sitter space can be described as a submanifold embedded in a higher dimension Minskowski space. Working in D = 4, take the D + 1 Minkowski space defined as

$$ds^{2} = -dx_{0}^{2} + dx_{1}^{2} + dx_{2}^{2} + dx_{3}^{2} + dx_{4}^{2}.$$
 (1)

Now let us constrain our coordinates to a hyperboloid

$$-x_0^2 + x_1^2 + x_2^2 + x_3^2 + x_4^2 = C^2 (2)$$