3D inversion for estimating total magnetization direction

using equivalent layer technique

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Running head: Determining total magnetization direction

ABSTRACT

We have developed a new methor for estimating the total magnetization direction of mag-

netic sources based on equivalent layer technique using total field anomaly data. In this

approach, we do not have to impose a strong information about the shape and the depth

of the sources, and do not require a regularly spaced data. Usually, this technique is used

for processing potential data estimating a 2D magnetic moment distribution over a ficti-

cious layer composed by dipoles below the observation plane. In certain conditions, when

the magnetization direction of equivalent sources is almost the same of true body, the esti-

mated magnetic property over the layer is all positive. The methodology uses a positivity

constraint to estimate a set of magnetic moment and a magnetization direction of the layer

through a iterative process. Mathematically, the algorithm solve a least squares problem

in two steps: the first one solve a linear problem for estimating a magnetic moment and

the second solve a non-linear problem for magnetization direction of the layer. We test the

methodology applying to synthetic data for different geometries and magnetization types

1

of sources. Moreover, we applied this method to field data from Goias Alkaline Province (GAP), center of Brazil, showing that the methodology can be a good tool for estimating the magnetization component of the alkaline intrusion complex in the Diorama region. The result for this complex suggests that this source has a remarkable strong remanent magnetization component. The magnetization direction estimated for this complex is  $-47^{\circ}$  and  $-111^{\circ}$  for inclination and declination, respectivelly.

## **METHODOLOGY**

Considering a Cartesian coordinate system with x-, y- and z-axis being oriented to north, east and downward, respectively. Let  $\Delta T(x_i, y_i, z_i)$  be the total field anomaly, at the i-th position  $(x_i, y_i, z_i)$ , produced by a continuous layer located below the observation plane on the depth  $z_c$ , where  $z_c > z_i$ , and  $p(x', y', z_c)$  is the distribution of magnetic dipoles per unit area over the layer surface. In this case, the total field anomaly produced by this continuous layer is given by the equation

$$\Delta T(x_i, y_i, z_i) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} p(x', y', z_c) [\gamma_m \hat{\mathbf{F}}_0^T \mathbf{H} \, \hat{\mathbf{h}}] dx' \, dy'.$$
 (1)

where  $\gamma_m$  is a constant proportional to the vaccum permeability,  $\hat{\mathbf{F}}_0$  is a unit vector with the same direction of the geomagnetic field  $\mathbf{F}_0$  and