

## Mid-exam Imperative Programming

Sept. 30 2016, 14:00-17:00h

- You can solve the problems in any order. Solutions must be submitted to the automated judgment system Justitia. For each problem, Justitia will test ten different inputs, and checks whether the outputs are correct.
- Grading: you get one grade point for free. The remaining nine points are based solely on the judgment given by Justitia. The first problem is worth one grade point. The remaining four problems are worth two grade points each, of which you score the full two points if you passed the complete test set of the problem (i.e. 10 test cases), or one grade point if you passed at least 5 (out of 10) test cases.
- Inefficient programs may be rejected by Justitia. In such cases, the error will be 'time limit exceeded'. The time limit for each problem is one second.
- The number of submissions to Justitia is unlimited. No points are subtracted for multiple submissions.
- There will be no assessment of programming style. However, accepted solutions are checked manually for cheating: for example, precomputed answers will not be accepted, even though Justitia accepts them.
- Note the hints that Justitia gives when your program fails a test.
- Needless to say: you are not allowed to work together. If plagiarism is detected, both parties (supplier of the code and the person that sends in a copy) will be excluded from any further participation in the course. You are not allowed to use mail, phones, tablets, calculators, etc. There is a calculator available on the exam computers (see icon on the desktop). You are allowed to consult the reader, the book, and submissions previously made to Justitia (from the labs or the midexam).
- For each problem, there are three examples of inputs and associated expected outputs. These examples are the first three test cases of a test set. The input files of these examples can be found in Justitia, together with the corresponding output files. These files are called `1.in`, `2.in`, `3.in` and `1.out`, `2.out` and `3.out`. These files can be used to test whether the output of your program matches the requested layout, so that there can be no misunderstanding about the layout and spaces in the output.

## Problem 1: Reversible multiples of seven

A positive integer that is divisible by 7, while the reversal of its digits is also divisible by 7 is called a *reversible multiple of seven*. For instance, 259 is such a number because  $259 = 7 \times 37$  and  $952 = 7 \times 136$ . Note that leading zeros in the reversal are ignored, so the reversal of 700 is 7. Hence, 700 is also a reversible multiple of seven.

The input of this problem consists of two integers  $a$ , and  $b$  such that  $1 \leq a \leq b \leq 10000000 = 10^7$ . The output should be the number of integers  $x$  such that  $a \leq x \leq b$  and  $x$  is a reversible multiple of seven. Note that there are no spaces in the output, and that the output ends with a newline (`\n`):

### Example 1:

**input:**

1 1000

**output:**

21

### Example 2:

**input:**

777 800

**output:**

1

### Example 3:

**input:**

700 705

**output:**

1

## Problem 2: Pangram

A *Pangram* is a sentence using every letter of the alphabet at least once. A famous English pangram is "THE QUICK BROWN FOX JUMPS OVER THE LAZY DOG".

Write a program that reads from the input a sentence, and outputs whether the sence is a *pangram*, or *no pangram*. The input consists of a sentence containing spaces and uppercase letters from the conventional 26 letter alphabet ('A', 'B', ..., 'Z'). The sentence ends with a dot ('.'). Make sure that the output of your program has the same format as in the following examples. Note that there are no spaces in the output, and that the output ends with a newline (`\n`):

### Example 1:

**input:**

THE QUICK BROWN FOX JUMPS OVER THE LAZY DOG.

**output:**

PANGRAM

### Example 2:

**input:**

AMAZINGLY FEW DISCOTHEQUES PROVIDE JUKEBOXES.

**output:**

PANGRAM

### Example 3:

**input:**

THIS SENTENCE IS CLEARLY NOT A PANGRAM.

**output:**

NO PANGRAM

### Problem 3: Hamming numbers

*Hamming numbers* are integers  $n$  of the form  $n = 2^i \times 3^j \times 5^k$ .

For example, 360 is such a number because it can be divided three times by 2, two times by 3, and once by 5 (i.e.  $360 = 2 \times 2 \times 2 \times 3 \times 3 \times 5$ ). The number 2520 is not a Hamming number, because it has a factor 7 ( $2520 = 360 \times 7$ ).

The first ten Hamming numbers are:

$1 = 2^0 \times 3^0 \times 5^0$	$6 = 2^1 \times 3^1 \times 5^0$
$2 = 2^1 \times 3^0 \times 5^0$	$8 = 2^3 \times 3^0 \times 5^0$
$3 = 2^0 \times 3^1 \times 5^0$	$9 = 2^0 \times 3^2 \times 5^0$
$4 = 2^2 \times 3^0 \times 5^0$	$10 = 2^1 \times 3^0 \times 5^1$
$5 = 2^0 \times 3^0 \times 5^1$	$12 = 2^2 \times 3^1 \times 5^0$

Of these numbers, the numbers 4, 6, 9, and 10 have a sum of the exponents that equals 2 ( $i+j+k = 2$ ).

The input of this problem consists of three integers  $a$ ,  $b$ , and  $n$  such that  $1 \leq a \leq b \leq 10000000 = 10^7$ . The output should be the number of Hamming numbers  $x$  (where  $a \leq x \leq b$ ) of which the sum of the exponents equals  $n$ . Note that there are no spaces in the output, and that the output line must end with a newline (`\n`):

**Example 1:**

**input:**

1 12 2

**output:**

4

**Example 2:**

**input:**

1 12 1

**output:**

3

**Example 3:**

**input:**

1 1000000 10

**output:**

57

### Problem 4: Smith numbers

A *prime number* is a natural number greater than 1 that has no positive divisors other than 1 and itself. A *composite number* is a natural number that is not a prime number. Each composite number can be uniquely expressed as a product of prime numbers. This product is called its *prime factorization*.

A *Smith number* is a *composite number* (i.e. a *non-prime number*) greater than 1 for which the sum of its digits is equal to the sum of the digits in its prime factorization.

For example, 825 is a Smith number, because its prime factorization is  $825 = 3 \times 5 \times 5 \times 11$ , and  $8 + 2 + 5 = 3 + 5 + 5 + 1 + 1$ .

Write a program that reads from the input a positive integer, and outputs YES if the number is a Smith number, and NO otherwise. Note that there are no spaces in the output, and that the output ends with a newline (`\n`):

**Example 1:**

**input:**

825

**output:**

YES

**Example 2:**

**input:**

42

**output:**

NO

**Example 3:**

**input:**

4937775

**output:**

YES

## Problem 5: Takuzu checker

A *Takuzu* is a number placement puzzle. The objective is to fill an  $8 \times 8$  grid with 1s and 0s, where there is an equal number of 1s and 0s in each row and column (hence four 0s and four 1s) and no more than two of either number adjacent to each other. Moreover, there can be no identical rows, nor can there be identical columns. An example of a Takuzu puzzle and its solutions are given in the following figure.

0				0		0	
0					1		
			1			0	
		0		0			
							1
0		0		0	0		
							1
	1						

0	0	1	1	0	1	0	1
0	1	1	0	0	1	1	0
1	0	0	1	1	0	0	1
1	1	0	1	0	0	1	0
0	0	1	0	1	1	0	1
0	1	0	1	0	0	1	1
1	0	1	0	1	0	1	0
1	1	0	0	1	1	0	0

Write a program that reads from the input a completely filled  $8 \times 8$  grid of 0s and 1s. There are 8 input lines, one for each row. A row consists of 8 characters ('0' and '1'), followed by a newline ('\n'). Your program should output **CORRECT** if the grid satisfies all the rules of a Takuzu puzzle, otherwise it should output **INCORRECT**. Of course, your output must be a a single line, without spaces, than ends with a newline (\n).

### Example 1:

#### input:

```
00110101
01100110
10011001
11010010
00101101
01010011
10101010
11001100
```

#### output:

CORRECT

### Example 2:

#### input:

```
00110111
01100110
10011001
11010010
00101101
01010011
10101010
11001100
```

#### output:

INCORRECT

### Example 3:

#### input:

```
00110101
01100110
10011001
11010010
00110101
01010011
10101010
11001100
```

#### output:

INCORRECT