Class-wise Feature Distribution Matching Regularization for Domain Generalization

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Abstract

Domain generalization (DG) aims to learn a model that generalizes well to an unseen domain (target domain), which has a different distribution than known domains (source domains). Many of the previous works try to learn domain-invariant features. These methods adopt a loss that tries to match the whole distributions of the source domains. However, these works are sub-optimal because they rarely utilize task-specific information, such as class labels. Concerning the information, we propose a simple regularizing method called Class-wise Feature Distribution Matching (FDM). The proposed method induces a model to produce similar features when the labels of examples are the same, regardless of the examples' domains. By doing this, the model is expected to learn more task-specific and robust features than the previous works. To demonstrate the proposed methods, we conduct experiments on various settings. The proposed method consistently shows improvement compared to baseline. However, the analyses also reveal that domain-invariant features do not guarantee high performance.

1. Introduction

Deep learning has been remarkably successful in many areas [10, 14, 26, 19]. However, many studies find out deep learning methods are hard to generalize when they encounter an unseen domain, which has a different data distribution than domains used for training [16, 15, 16, 29, 7, 3, 20]. This problem called *domain shift* [30]. For alleviating the domain shift problem, many studies have been carried out on different assumptions. Domain Adaptation (DA) assumes there are two domains. The first is a fully-labeled source domain, and the other is a sparsely labeled or totally unlabeled target domain. Otherwise, domain generalization (DG) assumes there are some fully-labeled source domains, but the target domain is totally unavailable. DG is a challenge but important research area because general-
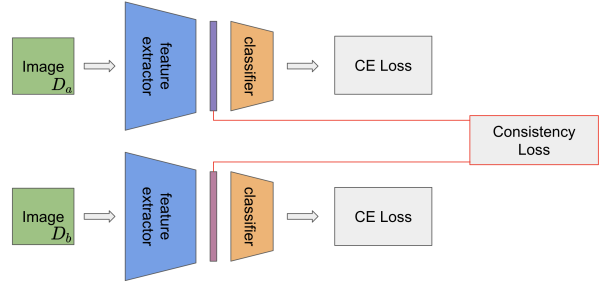

Figure 1: Overview

ization to other domains is crucial to make a safe artificial intelligence. Moreover, it is helpful to understand how deep neural networks see the world.

Existing DG studies can be classified into several categories depending on their strategies. Some methods proposed novel model architectures that are robust to domain shift [13, 15]. Others suggested learning algorithms aim to induce a model to fit in a more robust minimum [17, 16, 1]. The others adopted losses to learn domain-invariant features by matching feature distributions of the source domains [9, 22, 18]. Although these domain-invariant feature learning methods work well, the methods are sub-optimal because they do not utilize task-specific information such as class labels explicitly.

Our approach also aims to learn domain-invariant features, but the proposed method explicitly adopts the task-specific information. More specifically, we add a simple consistency loss that induces the model to produce similar features when the labels are the same. By using this constraint, the model is expected to learn features that are adequately semantic and constant across domains. Fig. 1 shows the overview of the proposed method.

To demonstrate the proposed method works, we conducted experiments on various datasets [6, 15] and models [12]. In the tests, the proposed regularization method consistently improves the performance of the model compared to the baseline method. However, an additional anal-

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ysis shows that domain-invariant features do not guarantee high performance.

We can summarize our contributions in this works as follows: 1)

2. Related Works

2.1. Multi-Domain Learning and Multi-Source Domain Adaptation

The primary purpose of Multi-Domain Learning (*MDL*) is to learn a single model that can compactly represent all domains with a smaller number of parameters [31, 24, 2, 25]. For this purpose, Bilen *et al.* [2] adopts domain-specific parameters of instance normalization and batch normalization while using shared parameters in other layers. Rebuffi *et al.* [24] transforms the standard residual network architecture to share a significant amount of parameters between different domains.

Multi-Source Domain Adaptation (*MSDA*) also uses a set of source domains, but it additionally utilizes the images of an unlabeled target domain. The main focus of MSDA is to train a model that works well on the target domain without labels of it. Even though many studies have been conducted on single-source domain adaptation, there are a limited number of researches on MSDA [32, 5, 11, 23]. Chang *et al.* [5] proposes a domain-specific batch normalization with shared weights parameters and extends their method to MSDA. Peng *et al.* [23] suggests a way to reduce the moment distance between different source domains as well as reducing the distance between target and source domains. The moment distance measures the difference between feature distributions of two domains without concerning the task at hand.

MDL and MSDA are closely related to DG since DG also utilizes a set of domains as training data. However, DG is different from MDL in that the primary focus of DG is to learn semantic and domain-invariant features, not to learn compact representations. Furthermore, DG is more challenging than MSDA because the target domain is totally unavailable in DG.

2.2. Domain Generalization

Even though existing DG methods basically aim to learn domain-invariant features, the methods can be classified into several groups based on their approaches. The first group proposes a novel architecture [13, 15]. The methods separate domain-specific parameters and domain-agnostic parameters. After that, they only extract and utilize the domain-agnostic parameters for the unseen domain. The second group of methods suggests optimization algorithms that adopt episodic learning or self-supervised learning [17, 16, 1, 4]. For example, MLDG [16] constructs an episode by splitting the source domains into train-

ing domains and test domains in each iteration. The final group of methods uses losses that aims to learn domain-invariant features [9, 22, 18]. These methods often adopt maximum mean distribution (*MMD*) constraints. However, MMD simply tries to match the feature distributions of all available source domains without concerning the task at hand. Therefore, methods that adopted MMD can be sub-optimal [28, 27]. Otherwise, we propose a regularizing method using a simple consistency loss that explicitly utilizes the task-specific information. By using this simple loss, we expect that the model can learn domain-invariant but semantic features.

3. Proposed Method

3.1. Problem Setting and Notation

In DG, we assume that there are n source domains $\mathcal{D} = \{\mathcal{D}_1, \mathcal{D}_2, \ldots, \mathcal{D}_n\}$ where $\mathcal{D}_i$ indicates i-th source domain which contains sample-label pairs $\{x_i^j, y_i^j\}$. Using the source domains, our goal is to train a model h that performs well on unseen target domain $\mathcal{D}_t$. We assume the model h consists of a feature extractor f and a classifier c.

3.2. Deep-All Method

The Deep-All Method is a simple but effective baseline. In this method, we just aggregate all examples of source domains and train the model using the aggregated samples. If we work on a classification task, we can use cross-entropy loss as follows:

$$L_{all} = \mathbb{E}_{\mathcal{D}_s \sim \mathcal{D}} \big[\mathbb{E}_{\mathbf{x}_i, y_i \sim \mathcal{D}_s} \big[\mathbf{y}_i^T \log h(\mathbf{x}_i) \big] \big] \qquad (1)$$

where $\mathbf{y}_i$ is a one-hot vector representation of y_i. This method is easy to train, but it has shown comparable performance than other works.

3.3. Class-wise Feature Distribution Matching Regularization

We propose a consistency loss called Class-wise Feature Distribution Matching Regularization (*FDM*), which tries to make a model generate similar features when the labels are the same. The FDM loss is calculated as follows: For each iteration, the feature extractor produces features of the source domains. After that, we calculate the averages of the features by classes. Lastly, the FDM loss is calculated as a consistency loss between the averages and the features that share the same label. The FDM loss is defined as follows:

$$L_{fdm} = \mathbb{E}_{\mathcal{D}_s \sim \mathcal{D}} \big[\mathbb{E}_{\mathbf{x}_i, y_i \sim \mathcal{D}_s} \big[d(f(\mathbf{x}_i), \mathbf{m}_{y_i}) \big] \big] \qquad (2)$$

where d measures the difference between $\mathbf{x}_i$ and $\mathbf{m}_{y_i}$. we used the square of Euclidean distance. $\mathbf{m}_{y_i}$ is the average feature of class y_i. For simplicity, $\mathbf{m}_{y_i}$ is calculated for
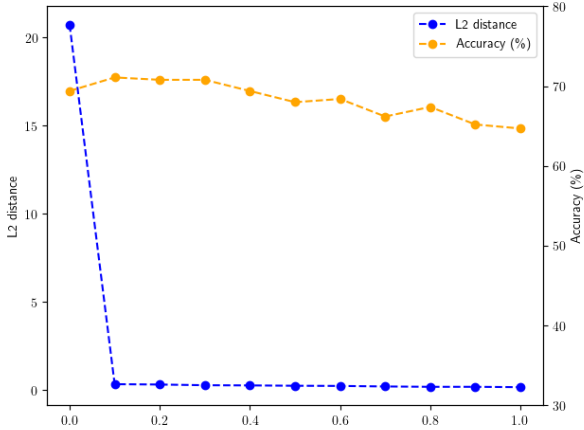
Figure 2: Analysis

each batch. The L_{fdm} regularize the feature extractor f to extract similar features when the classes are the same.

Finally, overall loss function is defined as a weighted sum of L_{all} and L_{fdm} as follows:

$$L = L_{all} + \lambda L_{fdm} \qquad (3)$$

where λ is a hyperparameter that controlls the magnitude between the two losses. We found that using linear ramp-up on λ is helpful to stable training. Thus, we updated λ at epoch t with the following schedule:

$$\lambda^{(t)} = min(1, \frac{t}{T_r}) * \lambda_{max} \qquad (4)$$

where T_r is the ramp-up period, and λ_{max} is the maximum weight of the L_{fdm}.

4. Experiments

To demonstrate the effectiveness of the proposed method, we conduct an experiment on PACS dataset [15] using AlexNet [14]. We follow the experiment protocol of Li *et al.* [15]. We use a batch size 512, and λ is set to 0.1 for all tests. The results are shown in Table 1. As we can see, the Deep-All works better than many previous works, as Li *et al.* [17] mentioned before.

Nevertheless, the proposed method improves the performance of the Deep-All baseline. Furthermore, the proposed method shows better performance than the methods using MMD contraints [9, 22]. However, the improvement is quite marginal and sub-optimal compared to state-of-the-art, which indicates the proposed regularization is quite strong.

5. Future Works

We are planning to improve the proposed method further. According to the results, the proposed regularization seems too hard. Specifically, the proposed constraint prevents the model from learning more semantic features. Therefore, We are planning to find a way to soften or stabilize the regularization. Additionally, we will conduct more experiments and analysis using other datasets like VLCS [6] and other models such as ResNet [12].

6. Conclusion

We suggested a simple but effective regularization method called Class-wise Feature Distribution Matching Regularization. The experiments on the PACS dataset showed the proposed method can improve the performance of the baseline. Additionally, even though the FDM is sub-optimal compared to state-of-the-art, FDM is comparable or better than the majority of the previous works.

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Src.	Trgt.	D-MTAE [9]	DSN [3]	CrossGrad [29]	DICA [22]	DANN [8]	TF-CNN [15]	MetaReg [1]	MLDG [16]	Epi-FCR [17]	JiGen [4]	Deep-All	FDM
C,P,S	A	60.3	61.1	61.0	64.6	63.2	62.9	63.5	66.2	64.7	**67.6**	60.4	61.7
A,P,S	C	58.7	66.5	67.2	64.5	67.5	67.0	69.5	66.9	72.3	71.7	70.2	**73.1**
A,C,S	P	91.1	83.3	87.6	**91.8**	88.1	89.5	87.4	88.0	86.1	89.0	85.3	87.4
A,C,P	S	47.9	58.6	55.9	51.1	57.0	57.5	59.1	59.0	65.0	**65.2**	61.6	62.3
Ave.		64.5	67.4	67.9	68.0	69.0	69.2	69.9	70.0	72.0	**73.4**	69.4	71.1

Table 1: Cross-domain object classification results (accuracy. %) on PACS using AlexNet.

Src.	Trgt.	D-MTAE [9]	LRE-SVM [33]	CrossGrad [29]	DICA [22]	DANN [8]	MetaReg [1]	MLDG [16]	Epi-FCR [17]	Deep-All ([17])	Deep-All	FDM
L,C,S	V	63.9	60.6	65.5	63.7	66.4	65.0	67.7	67.1	65.4	59.7	59.3
V,C,S	L	60.1	59.7	60.0	58.2	64.0	60.2	61.3	64.3	60.6	54.1	54.3
V,L,S	C	89.1	88.1	92.0	79.7	92.6	92.3	94.4	94.1	93.1	87.7	88.0
V,L,C	S	61.3	54.9	64.7	61.0	63.6	64.2	65.9	65.9	65.8	61.4	64.0
Ave.		68.6	65.8	70.5	65.7	71.7	70.4	72.3	72.9	71.2	65.7	66.4

Table 2: Cross-domain object classification results (accuracy. %) on VLCS using AlexNet.

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Src.	Trgt.	CrossGrad [29]	DANN [8]	MetaReg [1]	MLDG [16]	Epi-FCR [17]	Deep-All	FDM
P,C,S	A	78.7	81.3	79.5	79.5	82.1	77.3	77.7
P,A,S	C	73.3	73.8	75.4	77.3	77.0	73.8	74.2
A,C,S	P	94.0	94.0	94.3	94.3	93.9	94.1	94.3
P,A,C	S	65.1	74.3	72.2	71.5	73.0	70.8	71.7
Ave.		77.8	80.8	80.4	80.7	81.5	79.0	79.5

Table 3: Cross-domain object classification results (accuracy. %) on PACS using ResNet-18.