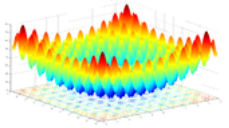
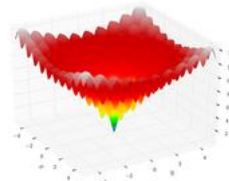
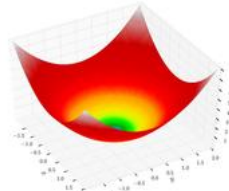
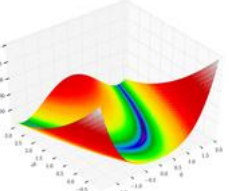
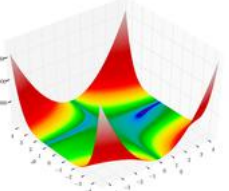
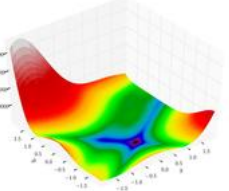
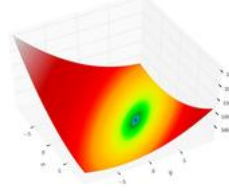
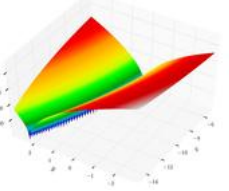
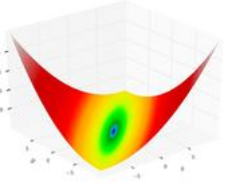
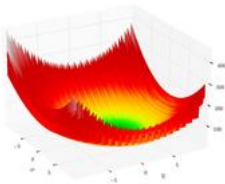
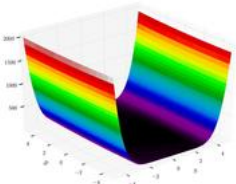
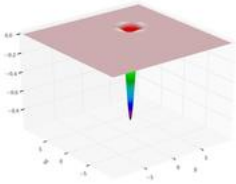
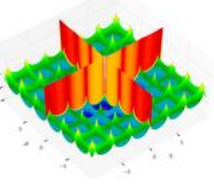
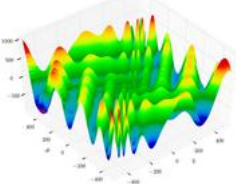
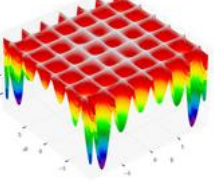
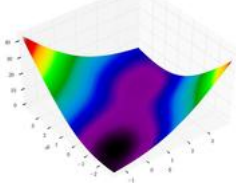
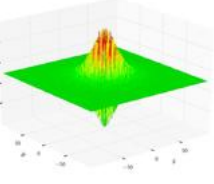
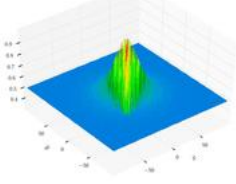
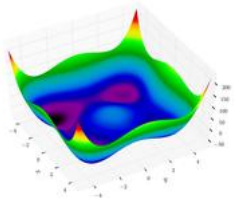
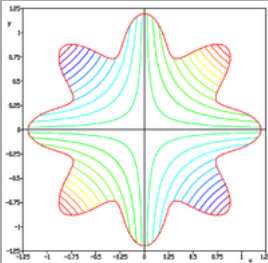


Name	Plot	Formula	Minimum
Rastrigin function		$f(\mathbf{x}) = An + \sum_{i=1}^n [x_i^2 - A \cos(2\pi x_i)]$ <p>where: $A = 10$</p>	$f(0, 0) = 0$
Ackley's function		$f(x, y) = -20 \exp\left(-0.2 \sqrt{0.5 (x^2 + y^2)}\right) - \exp(0.5 (\cos(2\pi x) + \cos(2\pi y))) + e + 20$	$f(0, 0) = 0$
Sphere function		$f(\mathbf{x}) = \sum_{i=1}^n x_i^2$	$f(x_1, \dots, x_n) = f(0, \dots, 0)$
Rosenbrock function		$f(\mathbf{x}) = \sum_{i=1}^{n-1} [100(x_{i+1} - x_i^2)^2 + (x_i - 1)^2]$	$\text{Min} = \begin{cases} n=2 & \rightarrow f(1, 1) = \\ n=3 & \rightarrow f(1, 1, 1) \\ n>3 & \rightarrow f\left(\underbrace{1, \dots}_{(n) \text{ times}}\right) \end{cases}$
Beale's function		$f(x, y) = (1.5 - x + xy)^2 + (2.25 - x + xy^2)^2 + (2.625 - x + xy^3)^2$	$f(3, 0.5) = 0$
Goldstein-Price function		$f(x, y) = \left(1 + (x + y + 1)^2 (19 - 14x + 3x^2 - 14y + 6xy + 3y^2)\right) \left(30 + (2x - 3y)^2 (18 - 32x + 12x^2 + 48y - 36xy + 27y^2)\right)$	$f(0, -1) = 3$
Booth's function		$f(x, y) = (x + 2y - 7)^2 + (2x + y - 5)^2$	$f(1, 3) = 0$
Bukin function N.6		$f(x, y) = 100\sqrt{ y - 0.01x^2 } + 0.01 x + 10 .$	$f(-10, 1) = 0$
Matyas function		$f(x, y) = 0.26(x^2 + y^2) - 0.48xy$	$f(0, 0) = 0$
		$f(x, y) = \sin^2(3\pi x) + (x - 1)^2 (1 + \sin^2(3\pi y))$	

Lévi function N.13		$+(y-1)^2 (1 + \sin^2(2\pi y))$	$f(1, 1) = 0$
Three- hump camel function		$f(x, y) = 2x^2 - 1.05x^4 + \frac{x^6}{6} + xy + y^2$	$f(0, 0) = 0$
Easom function		$f(x, y) = -\cos(x) \cos(y) \exp\left(-\left((x-\pi)^2 + (y-\pi)^2\right)\right)$	$f(\pi, \pi) = -1$
Cross-in- tray function		$f(x, y) = -0.0001 \left(\left \sin(x) \sin(y) \exp\left(\left 100 - \frac{\sqrt{x^2 + y^2}}{\pi} \right \right) \right + 1 \right)^{0.1}$	$\text{Min} = \begin{cases} f(1.34941, -1.34941) \\ f(1.34941, 1.34941) \\ f(-1.34941, 1.34941) \\ f(-1.34941, -1.34941) \end{cases}$
Eggholder function		$f(x, y) = -(y+47) \sin\left(\sqrt{\left \frac{x}{2} + (y+47)\right }\right) - x \sin\left(\sqrt{ x - (y+47) }\right)$	$f(512, 404.2319) = -959.6$
Hölder table function		$f(x, y) = -\left \sin(x) \cos(y) \exp\left(\left 1 - \frac{\sqrt{x^2 + y^2}}{\pi} \right \right) \right $	$\text{Min} = \begin{cases} f(8.05502, 9.66459) \\ f(-8.05502, 9.66459) \\ f(8.05502, -9.66459) \\ f(-8.05502, -9.66459) \end{cases}$
McCormick function		$f(x, y) = \sin(x+y) + (x-y)^2 - 1.5x + 2.5y + 1$	$f(-0.54719, -1.54719) = -1.290833$
Schaffer function N. 2		$f(x, y) = 0.5 + \frac{\sin^2(x^2 - y^2) - 0.5}{(1 + 0.001(x^2 + y^2))^2}$	$f(0, 0) = 0$
Schaffer function N. 4		$f(x, y) = 0.5 + \frac{\cos^2(\sin(x^2 - y^2)) - 0.5}{(1 + 0.001(x^2 + y^2))^2}$	$f(0, 1.25313) = 0.29257$

Styblinski–Tang function		$f(\mathbf{x}) = \frac{\sum_{i=1}^n x_i^4 - 16x_i^2 + 5x_i}{2}$	$-39.16617n < f \left(\underbrace{-2.903534, \dots, -2.9034}_{(n) \text{ times}} \right)$
Simionescu function ^[10]		$f(x, y) = 0.1xy,$ subjected to: $x^2 + y^2 \leq \left(r_T + r_S \cos \left(n \arctan \frac{x}{y} \right) \right)^2$ where: $r_T = 1, r_S = 0.2$ and $n = 8$	$f(\pm 0.85586214, \mp 0.85586214) =$

Test functions for multi-objective optimization problems