



Programming Language Syntax

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Read: Scott, Chapter 2.1



Lecture Outline

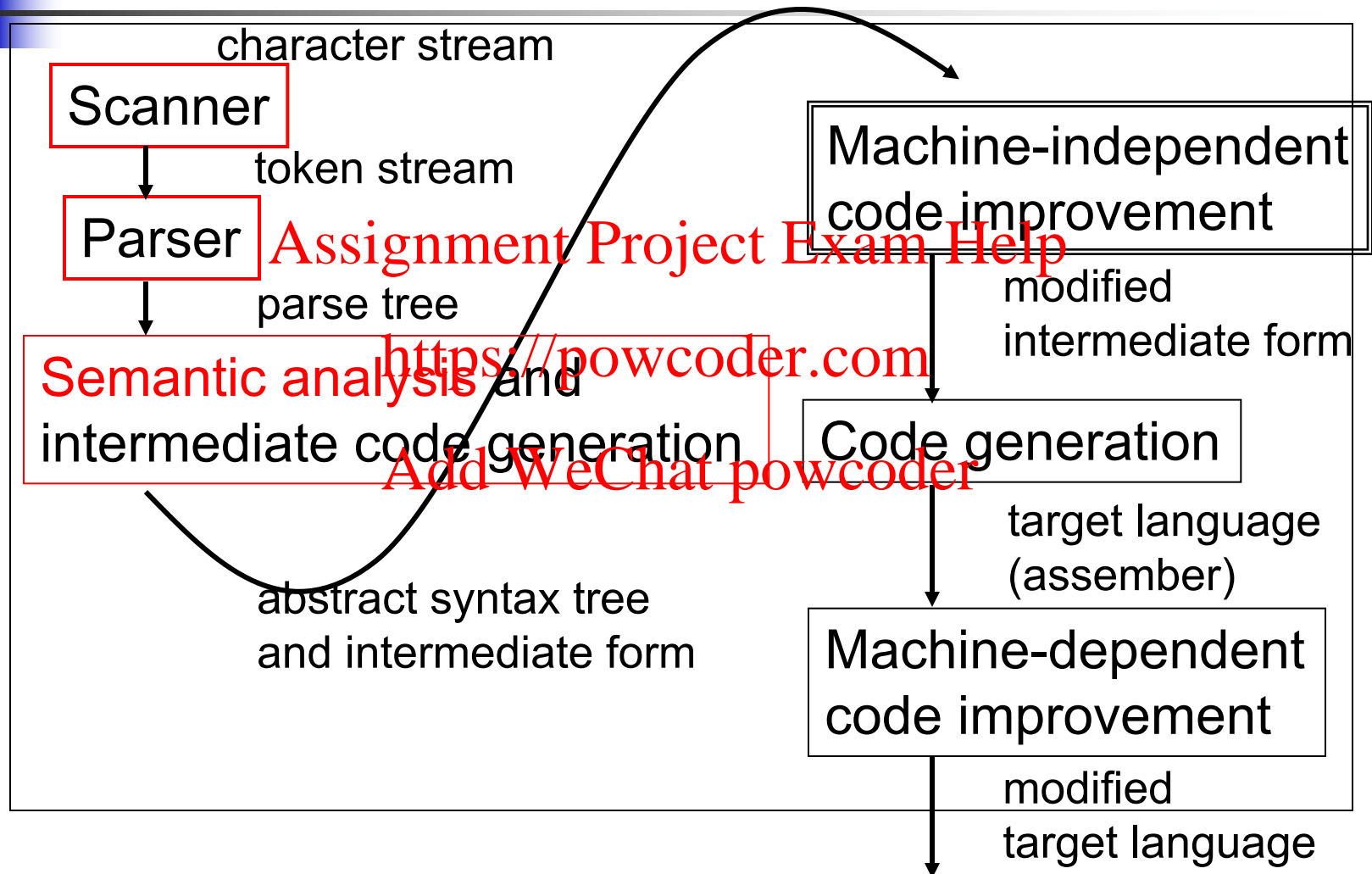
- Formal languages
- Regular expressions
- Context-free grammars
 - Derivation
 - Parse
 - Parse trees
 - Ambiguity
- Expression Grammars

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Last Class: Compiler





Syntax and Semantics

- **Syntax** is the form or structure of expressions, statements, and program units of a given language
 - Syntax of a Java while statement:
 - `while (boolean_expr) statement`
- **Semantics** is the meaning of expressions, statements and program units of a given language
 - Semantics of `while (boolean_expr) statement`
 - Execute *statement* repeatedly (0 or more times) as long as *boolean_expr* evaluates to `true`



Formal Languages

- Theoretical foundations – Automata theory
- A **language** is a set of strings (also called sentences) over a finite alphabet
- A **generator** is a set of rules that generate the strings in the language
- A **recognizer** reads input strings and determines whether they belong to the language
- Languages are characterized by the complexity of generation/recognition rules
 - E.g., regular languages
 - E.g., context-free languages



Question

- What are the classes of formal languages?

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- The Chomsky hierarchy:

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- Regular languages
- Context-free languages
- Context-sensitive languages
- Recursively enumerable languages



Formal Languages

- Generators and recognizers become more complex as languages become more complex
 - Regular languages
 - Describe PL **tokens** (e.g., keywords, identifiers, numeric literals)
 - Generated by **Regular Expressions**
 - Recognized by a **Finite Automaton** (scanner)
 - Context-free languages
 - Describe more complex PL constructs (e.g., expressions and statements)
 - Generated by a **Context-free Grammar**
 - Recognized by a **Push-down Automaton** (parser)
 - Even more complex constructs



Formal Languages

- Main application of formal languages: enable proof of relative difficulty of computational problems
- Our focus: formal languages provide the formalism for describing PL constructs
 - A compelling application of formal languages!
 - Building a scanner
 - Building a parser
 - Central issue: build efficient, linear-time parsers

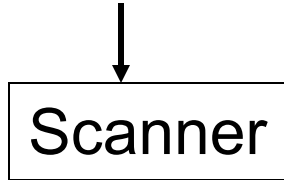
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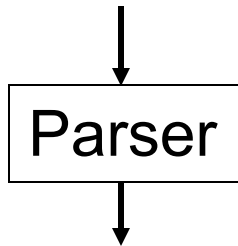
A Single Pass

*position = initial + rate * 60;*



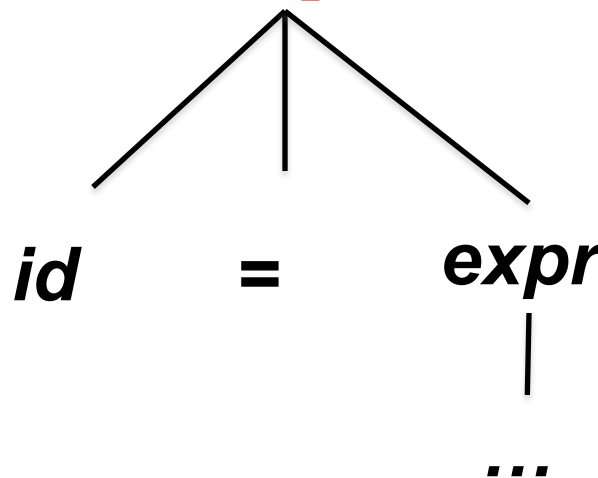
- Scanner emits next token
- Parser consumes the token and continues building the parse tree (typically bottom up)

id = ...



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 - Assignment Project Exam Help
- Context-free grammars
 - <https://powcoder.com>
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 - Parse trees
 - Ambiguity
- Expression Grammars



Regular Expressions

- Simplest structure
- Formalism to describe the simplest programming language constructs, the tokens
 - each symbols (e.g., “+”, “-”) is a token
 - an identifier (e.g., position, rate, initial) is a token
 - a numeric constant (e.g., 59) is a token
 - etc.
- Recognized by a finite automaton



Regular Expressions

- A Regular Expression is one of the following:
 - A character, e.g., **a**
 - The empty string, denoted by ϵ
 - Two regular expressions next to each other, $R_1 R_2$
 - Meaning: $R_1 R_2$ generates the language of strings that are made up of any string generated by R_1 , followed by any string generated by R_2
 - Two regular expressions separated by $|$, $R_1 | R_2$
 - Meaning: $R_1 | R_2$ generates the language that is the union of the strings generated by R_1 with the strings generated by R_2



Question

- What is the language defined by reg. exp.

(a | b) (a a | b b) ?

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- We saw concatenation and alternation. What operation is still missing?



Regular Expressions

- A Regular Expression is one of the following:
 - A character, e.g., **a**
 - The empty string, denoted by ϵ
 - $R_1 R_2$
 - $R_1 | R_2$
 - Regular expression followed by a Kleene star, R^*
 - Meaning: the concatenation of zero or more strings generated by R
 - E.g., a^* generates $\{\epsilon, a, aa, aaa, \dots\}$
 - E.g., $(a|b)^*$ generates all strings of **a**'s and **b**'s



Regular Expressions

■ Precedence

- Kleene * has highest precedence
- Followed by concatenation
- Followed by alternation |

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- E.g., **a b | c** is **(a b) | c** not **a (b | c)**
 - Generates {ab, c} not {ab, ac}
- E.g., **a b*** generates {a, ab, abb, ...} not { ϵ , ab, abab, ababab, ...}



Question

- What is the language defined by regular expression $(0 \mid 1)^* 1$?

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- What about $0^* (1 0^* 1 0^*)^* ?$

Regular Expressions in Programming Languages

- Describe tokens
- Let

letter → $a|b|c|\dots|z$

digit → $1|2|3|4|5|6|7|8|9|0$

- Which token is this?

1. *letter (letter | digit)** ?

2. *digit digit ** ?

3. *digit *. digit digit ** ?

Regular Expressions in Programming Languages

- Which token is this:

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number \rightarrow *integer* | *real*

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real \rightarrow *integer* *exponent* | *decimal* (*exponent* | ϵ)

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decimal \rightarrow *digit*^{*} (*.* *digit* | *digit* *.*) *digit*^{*}

exponent \rightarrow (*e* | *E*) (*+* | *-* | ϵ) *integer*

integer \rightarrow *digit* *digit*^{*}

digit \rightarrow 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0



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Context-Free Grammars

- Unfortunately, regular languages cannot specify all constructs in programming
- E.g., can we write a regular expression that specifies valid arithmetic expressions?
 - `id * (id + id * (number - id))`
 - Among other things, we need to ensure that parentheses are matched!
 - Answer is no. We need **context-free languages** and context-free grammars!



Grammar

- A grammar is a formalism to describe the strings of a (formal) language
- A grammar consists of a set of **terminals**, set of **nonterminals**, a set of **productions**, and a **start symbol**
 - **Terminals** are the characters in the alphabet
 - **Nonterminals** represent language constructs
 - **Productions** are rules for forming syntactically correct constructs
 - **Start symbol** tells where to start applying the rules

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Notation

Specification of identifier:

Regular expression: $\text{letter} (\text{letter} | \text{digit})^*$

BNF: $\langle \text{digit} \rangle ::= 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0$

$\langle \text{letter} \rangle ::= a | b | c | \dots | x | y | z$

$\langle \text{id} \rangle ::= \langle \text{letter} \rangle | \langle \text{id} \rangle \langle \text{letter} \rangle | \langle \text{id} \rangle \langle \text{digit} \rangle$

Textbook and slides:
(also BNF)

Nonterminals shown in *italic*

digit → 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0

letter → a | b | c | d | ... | z

id → letter | id letter | id digit

Terminals shown in **typewriter**



Regular Grammars

- Regular grammars generate regular languages
- The rules in regular grammars are of the form:
 - Each left-hand side (lhs) has exactly one nonterminal
 - Each right-hand side (rhs) is one of the following
 - A single terminal symbol or
 - A single nonterminal symbol or
 - A nonterminal followed by a terminal

e.g., $1\ 2^* \mid 0^+$

$S \rightarrow A \mid B$

$A \rightarrow 1 \mid A\ 2$

$B \rightarrow 0 \mid B\ 0$



Question

- Is this a regular grammar:

$$S \rightarrow 0 A$$

$$A \rightarrow S 1$$

$$S \rightarrow \varepsilon$$

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- No, this is a context-free grammar
 - It generates $0^n 1^n$, the canonical example of a context-free language
 - rhs should be nonterminal followed by a terminal, thus, $S \rightarrow 0 A$ is not a valid production



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Context-free Grammars (CFGs)

- **Context-free grammars** generate context-free languages
 - Most of what we need in programming languages can be specified with CFGs
- Context-free grammars have rules of the form:
 - Each left-hand-side has exactly one nonterminal
 - Each right-hand-side contains an arbitrary sequence of terminals and nonterminals
- A context-free grammar
 - e.g. $0^n 1^n, n \geq 1$
 $S \rightarrow 0 S 1$
 $S \rightarrow 0 1$



Question

- Examples of a non-context-free languages?

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- E.g., $a^n b^m c^n d^m$ $n \geq 1, m \geq 1$
- E.g., wcw where w is in $(0|1)^*$
- E.g., $a^n b^n c^n$ $n \geq 1$ (canonical example)

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Context-free Grammars

- Can be used to generate strings in the context-free language (**derivation**)
- Can be used to recognize well-formed strings in the context-free language (**parse**)
- In Programming Languages and compilers, we are concerned with two special CFGs, called LL and LR grammars

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Derivation

Simple context-free grammar for expressions:

$expr \rightarrow id \mid (expr) \mid expr \ op \ expr$

$op \rightarrow + \mid *$

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We can generate (derive) expressions:

$expr \Rightarrow expr \ op \ \underline{expr}$

$\Rightarrow expr \ \underline{op} \ id$

$\Rightarrow \underline{expr} \ + \ id$

$\Rightarrow expr \ op \ \underline{expr} \ + \ id$ \longleftarrow sentential form

$\Rightarrow expr \ \underline{op} \ id \ + \ id$

$\Rightarrow \underline{expr} \ * \ id \ + \ id$

$\Rightarrow id \ * \ id \ + \ id$ \longleftarrow sentence, string or yield



Derivation

- A **derivation** is the process that starts from the start symbol, and at each step, replaces a nonterminal with the right-hand-side of a production <https://powcoder.com>
 - E.g., $expr\ op\ \underline{expr}\ id$ derives $expr\ op\ id$
We replaced the right (underlined) $expr$ with id due to production $expr \rightarrow id$
- An intermediate sentence is called a **sentential form**
 - E.g., $expr\ op\ id$ is a sentential form



Derivation

- The resulting sentence is called **yield**
 - E.g., **id*id+id** is the yield of our derivation
- What is a **left-most derivation**?
 - Replaces the **left-most** nonterminal in the sentential form at each step
- What is a **right-most derivation**?
 - Replaces the **right-most** nonterminal in the sentential form at each step
- There are derivations that are neither left- nor right-most

Question

- What kind of derivation is this:

$expr \Rightarrow expr\ op\ \underline{expr}$
 $\Rightarrow expr\ \underline{op}\ id$
 $\Rightarrow \underline{expr} + id$
 $\Rightarrow expr\ op\ \underline{expr + id}$
 $\Rightarrow expr\ \underline{op}\ id + id$
 $\Rightarrow \underline{expr} * id + id$
 $\Rightarrow id * id + id$

- A right-most derivation. At each step we replace the right-most nonterminal

Question

- What kind of derivation is this:

$expr \Rightarrow expr\ op\ expr$
 $\Rightarrow expr\ \underline{op}\ id$
 $\Rightarrow \underline{expr}\ +\ id$
 $\Rightarrow \underline{expr}\ op\ expr\ +\ id$
 $\Rightarrow id\ op\ \underline{expr}\ +\ id$
 $\Rightarrow id\ \underline{op}\ id\ +\ id$
 $\Rightarrow id\ * id\ +\ id$

- Neither left-most nor right-most

Parse

Recall our context-free grammar for expressions:

$expr \rightarrow id \mid (expr) \mid expr \ op \ expr$

$op \rightarrow + \mid *$

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- A parse is the reverse of a derivation

$id * id + id \Rightarrow expr * id + id$
 $\Rightarrow expr \ op \ \underline{id} \ + \ id$
 $\Rightarrow \underline{expr \ op \ expr} \ + \ id$
 $\Rightarrow expr \ \underline{+} \ id$
 $\Rightarrow expr \ op \ \underline{id}$
 $\Rightarrow \underline{expr \ op \ expr}$
 $\Rightarrow expr$

Parse

- A parse starts with the string of terminals, and at each step, replaces the right-hand-side (rhs) of a production with the left-hand-side (lhs) of that production. E.g.,

... \Rightarrow $expr\ op\ expr$ \Rightarrow $expr + id$

Here we replaced $expr\ op\ expr$ (the rhs of production $expr \rightarrow expr\ op\ expr$) with $expr$ (the lhs of the production)

Parse Tree

$expr \rightarrow id \mid (expr) \mid expr \ op \ expr$

$op \rightarrow + \mid *$

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$expr \Rightarrow expr \ op \ expr$

$\Rightarrow expr \ op \ id$

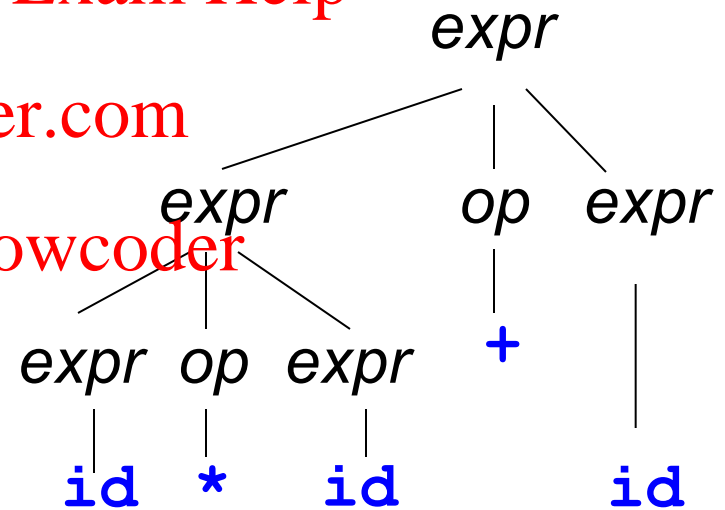
$\Rightarrow expr \ + \ id$

$\Rightarrow expr \ op \ expr \ + \ id$

$\Rightarrow expr \ op \ id \ + \ id$

$\Rightarrow expr \ * \ id \ + \ id$

$\Rightarrow id \ * \ id \ + \ id$



Internal nodes are nonterminals. Children are the rhs of a rule for that nonterminal.
Leaf nodes are terminals.



Ambiguity

■ Ambiguity

- A grammar is **ambiguous** if some string can be generated by two or more distinct parse trees
- There is no algorithm that can tell if an arbitrary context-free grammar is ambiguous
- Ambiguity arises in programming language grammars
 - Arithmetic expressions
 - If-then-else: the dangling else problem
- Ambiguity is bad

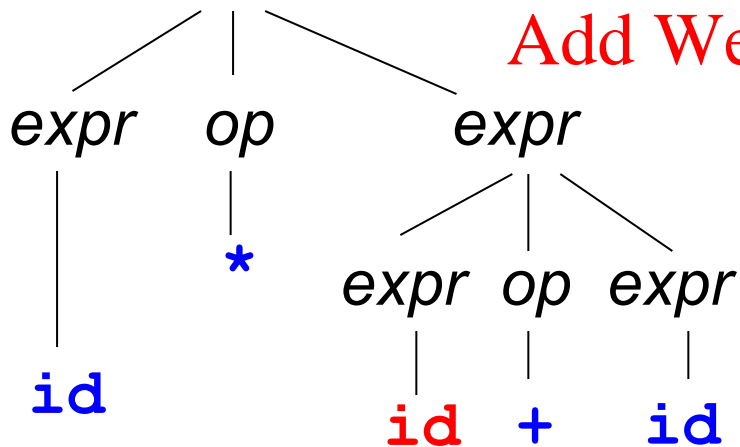
Ambiguity

$expr \rightarrow id \mid (expr) \mid expr \ op \ expr$

$op \rightarrow + \mid *$

- How many parse trees for $id + id * id$?

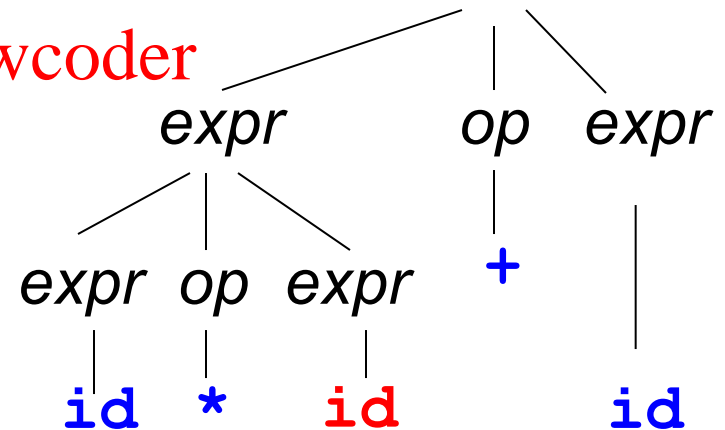
Tree 1:



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Tree 2:



- Which one is “correct”?

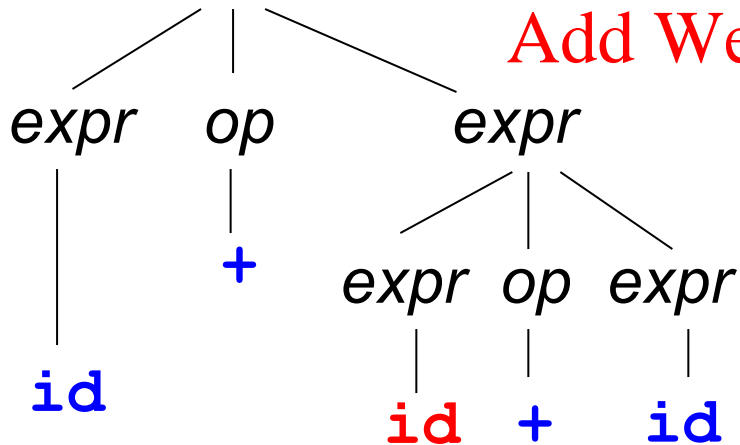
Ambiguity

$expr \rightarrow id \mid (expr) \mid expr \ op \ expr$

$op \rightarrow + \mid *$

- How many parse trees for $id + id + id$?

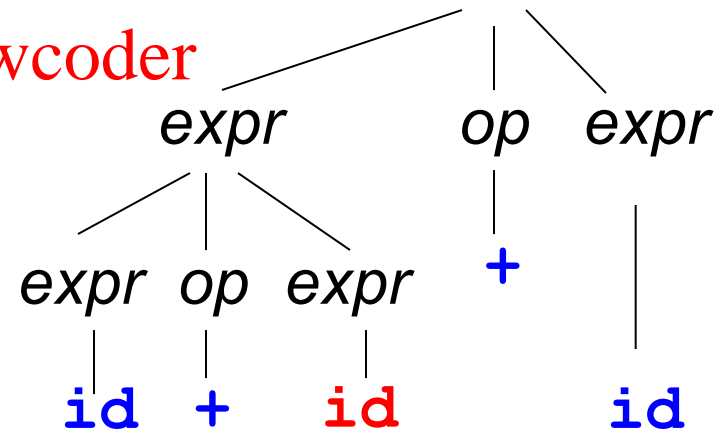
Tree 1:



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Tree 2:



- Which one is “correct”?



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Expression Grammars

- Generate expressions

- Arithmetic expressions

- Regular expressions

- Other

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- Terminals: operands, operators, and parentheses

$expr \rightarrow id \mid (expr) \mid expr \ op \ expr$

$op \rightarrow + \mid *$

Handling Ambiguity

Our ambiguous grammar, slightly simplified:

$$\text{expr} \rightarrow \text{id} \mid (\text{expr}) \mid \text{expr} + \text{expr} \mid \text{expr} * \text{expr}$$

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- Rewrite the grammar into unambiguous one:

$$\text{expr} \rightarrow \text{expr} + \text{term} \mid \text{term}$$
$$\text{term} \rightarrow \text{term} * \text{factor} \mid \text{factor}$$
$$\text{factor} \rightarrow \text{id} \mid (\text{expr})$$

- Forces left associativity of $+$ and $*$
- Forces higher precedence of $*$ over $+$

Rewriting Expression Grammars: Intuition

$expr \rightarrow id \mid (expr) \mid expr + expr \mid expr * expr$

- A new nonterminal, *term*
- $expr * expr$ becomes *term*. Thus, $expr * expr$ gets pushed down the tree, forcing higher precedence of $*$
- $expr + expr$ becomes $expr + term$. Pushes leftmost $+$ down the tree, forcing operand to associate with $+$ on its left
 - $expr \rightarrow expr + expr$ becomes $expr \rightarrow expr + term \mid term$

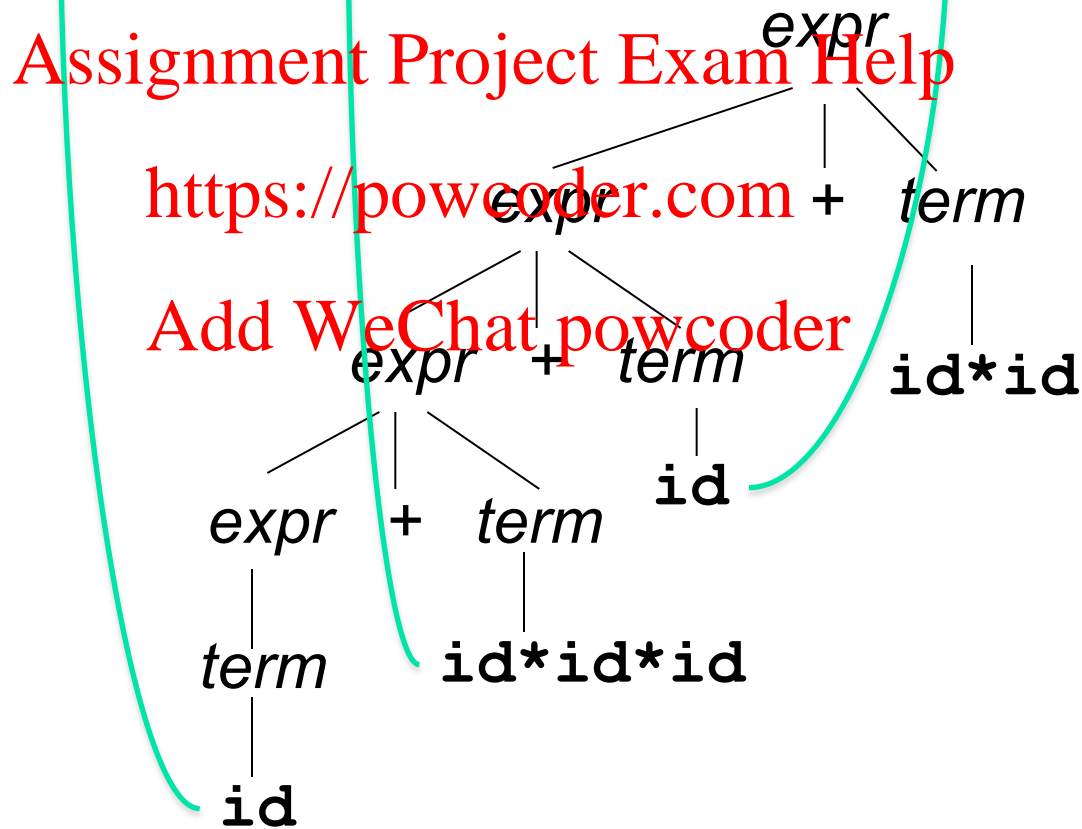
Rewriting Expression Grammars: Intuition

E.g., look at $\text{id} + \text{id} * \text{id} * \text{id} + \text{id} + \text{id} * \text{id}$

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Rewriting Expression Grammars: Intuition

- Another new nonterminal, *factor* and productions:

- $term \rightarrow term * factor \mid factor$

- $factor \rightarrow id \mid (expr)$

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Exercise

$expr \rightarrow expr \times expr \mid expr \wedge expr \mid id$

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- How many parse trees for $id \times id \wedge id \times id$?
 - No need to draw them all
- Rewrite this grammar into an equivalent unambiguous grammar where
 - ^ has higher precedence than \times
 - ^ is right-associative
 - \times is left-associative

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The End

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