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23. Virtual Memory: Hierarchical Page Table

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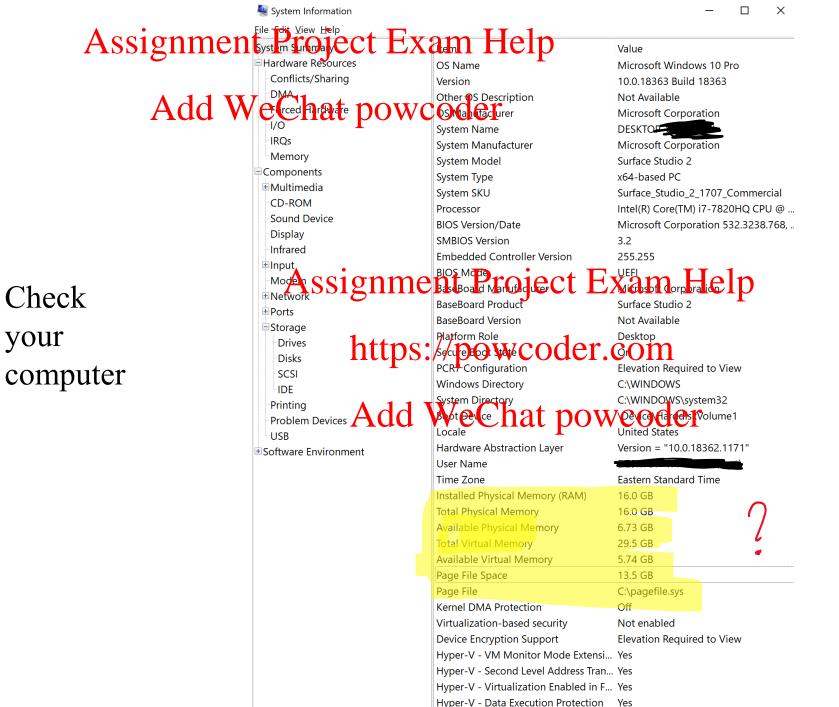
EECS 370 – Introduction to Computer Organization – Fall 2020

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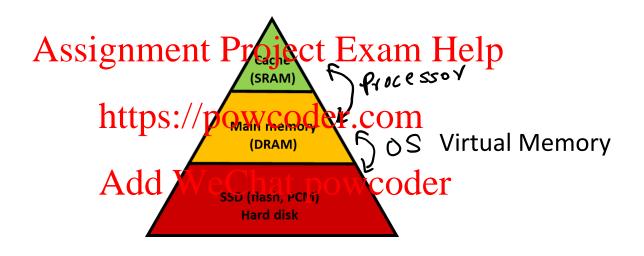
EECS Department
University of Michigan in Ann Arbor, USA

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Virtual Memory Role hat powcoder



Virtual Memory Roles powcoder

Capacity: Main memory is not enough

Problem:

Modern systems can afford ~128 GBs DRAM space = 2^37 bytes. Programs written in 64-bit ISA need 2^64 bytes!

Need to run many programs simultaneously on the same machine. Each program may require GBs of memory.

Solution:

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Provide an illusion of storage large enough for 2^64 bytes of data for all concurrently running programs Manage main memory like an attition of the country to disk.

Security features

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Isolation

Unrelated programs must not have access to each other's data

Permissions

Programs may want to share data and code (e.g., library)

Programs may want to disable read/write permissions to some portions of memory e.g., mark instructions are read-only, no read/write permission for unallocated heap

Page offset size = log(4KB)=12 bits

Page size = 4 KB



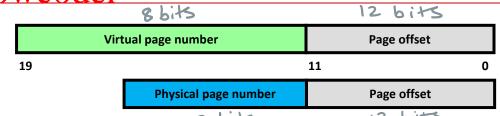
Virtual address

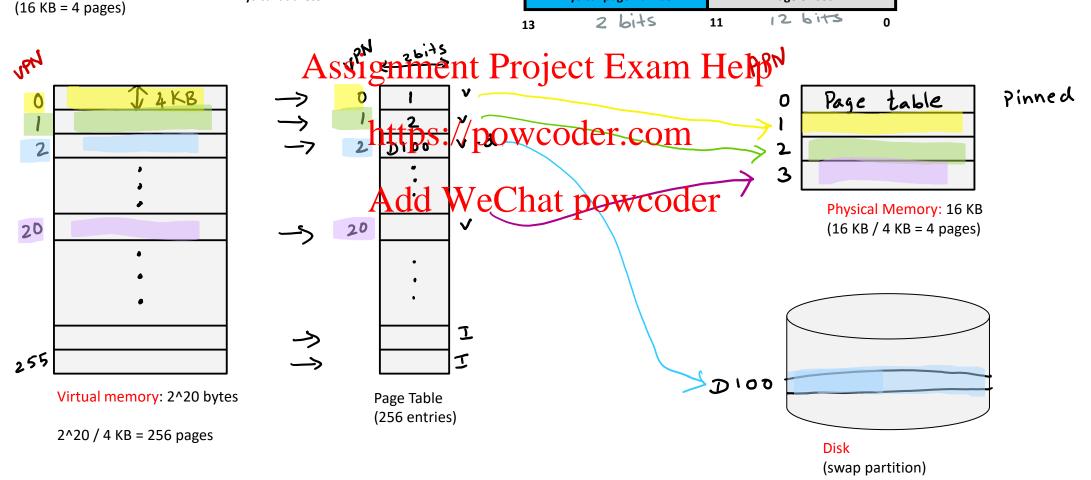
Physical address

Virtual memory

Physical Memory

 $(2^20 \text{ bytes} = 256 \text{ pages})$





Page Replacement: Approximating LRU

Page table indirection enables a fully associative mapping between virtual and physical pages.

How does OS implement LRU?

Precise LRU is expensive Assignment Project Exam Help

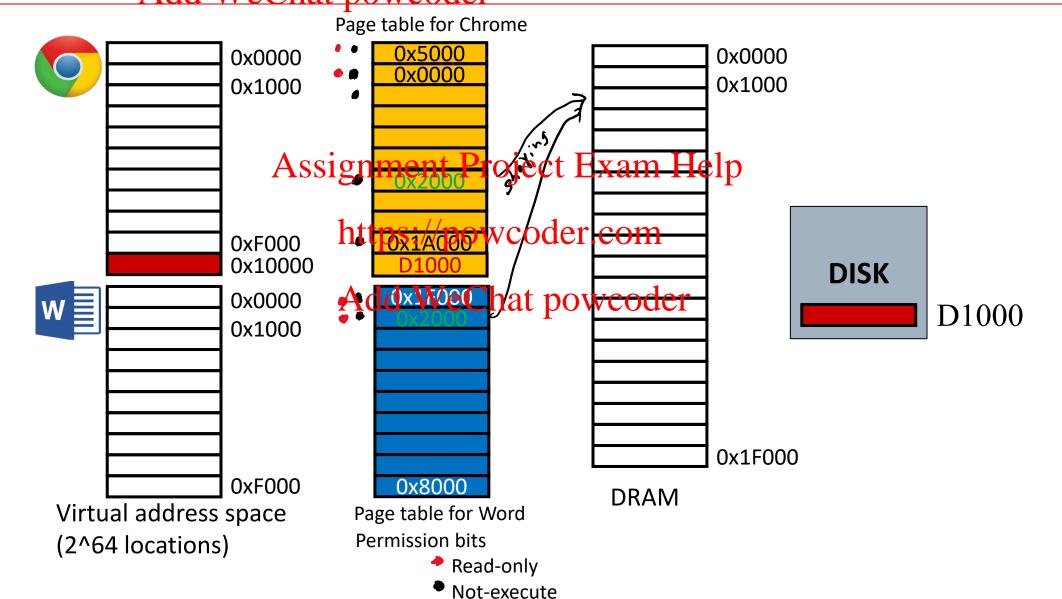
LRU is a heuristic anyway, so approximate LRU

Keep a "accessed" bit per page, cleated Siccal Onal God the Com

OS picks any "unaccessed" page (accessed bit not set) to evict

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Virtual Memory: Security: Isolation, Sharing, Permissions



Page Table Entry Contents Output Description:

Physical page number (PPN)

Allocated or not? (valid/invalid)

Main memory or disk?

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Access permission bits

read-only

not-execute

https://powcoder.com

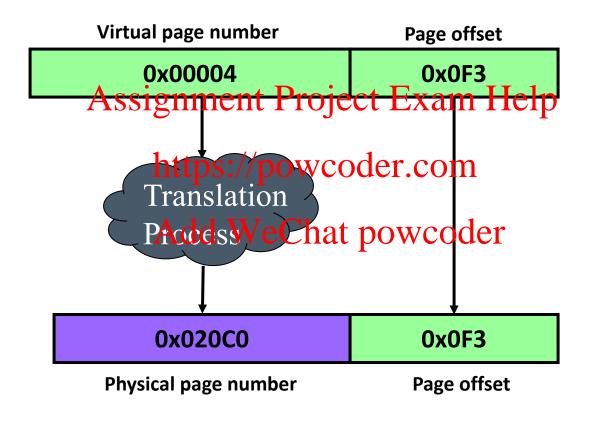
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Dirty page or not?

LRU meta-data

Address Translation Chat powcoder

Virtual address = 0x000040F3



Physical address = 0x020C00F3

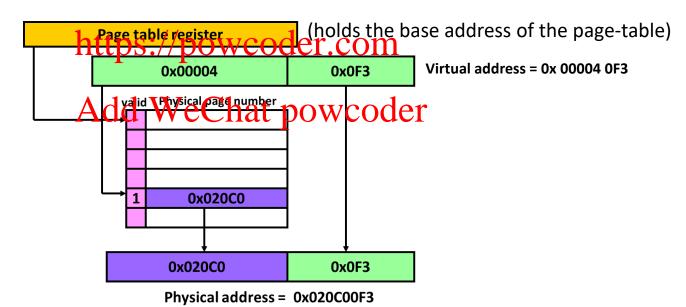
Page table for address translation

Single-level page table: an array-like structure.

a big array indexed by the virtual page number

Each page-table entry stores the physical page number (and some status bits like "valid").

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Single-level page table

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Next Problem: Page table is too large Help

Solution: Multi-lever Pagevrabler.com

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Problem: Single-level page table is too big

```
Example:
Assume 64-bit ISA. 4 KB pages. Assignment Project Exam Help
# virtual pages
# page-table entries
                                Add WeChat powcoder
Say, each page table entry is 4 bytes
Total page size = 2 ^ 52 entries * 4 bytes per entry = 2 ^ 54 bytes!
    = ~160,000 DRAMs each of 100 GB size (that is probably more DRAM than there is in UM!)
```

Observation Add WeChat powcoder

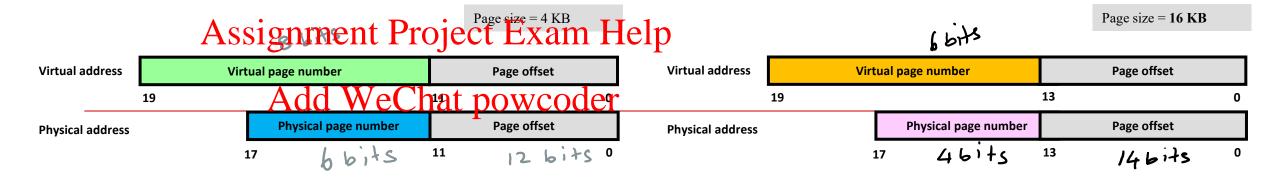
Problem: OS is allocating all page-table entries for a process when it starts.

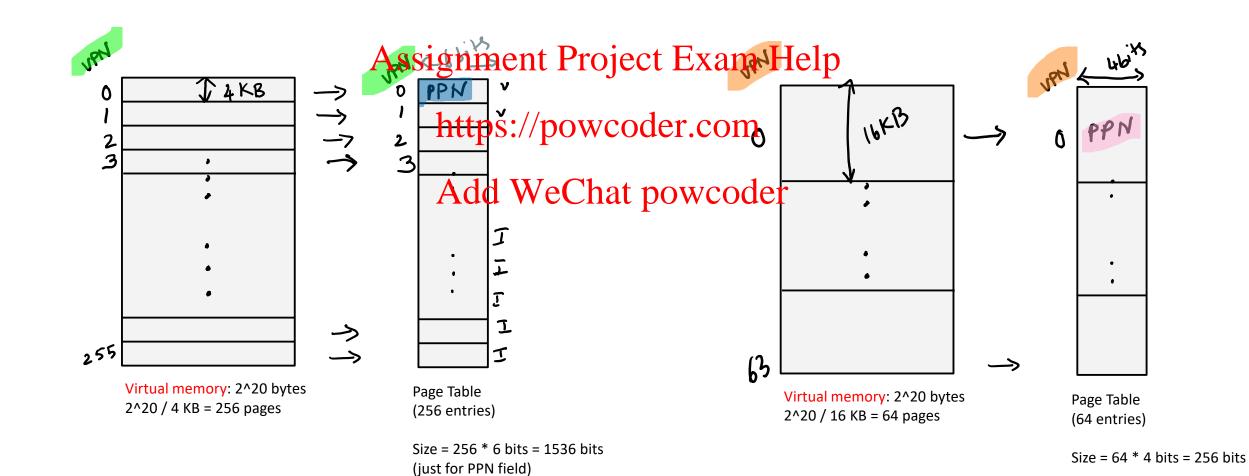
Most processes only use a very (very) small fraction of available virtual memory at any instant. Assignment Project Exam Help

OS allocates physical pages on-demand on when a virtual page is accessed by the program.

Idea: Similarly, can we allocate pagadable of atspowdeodor?

i.e., only allocate space for a page-table entry only its corresponding virtual address is accessed.





Hierarchical Page Table: Goal Powcoder

Can we get the best of both worlds?

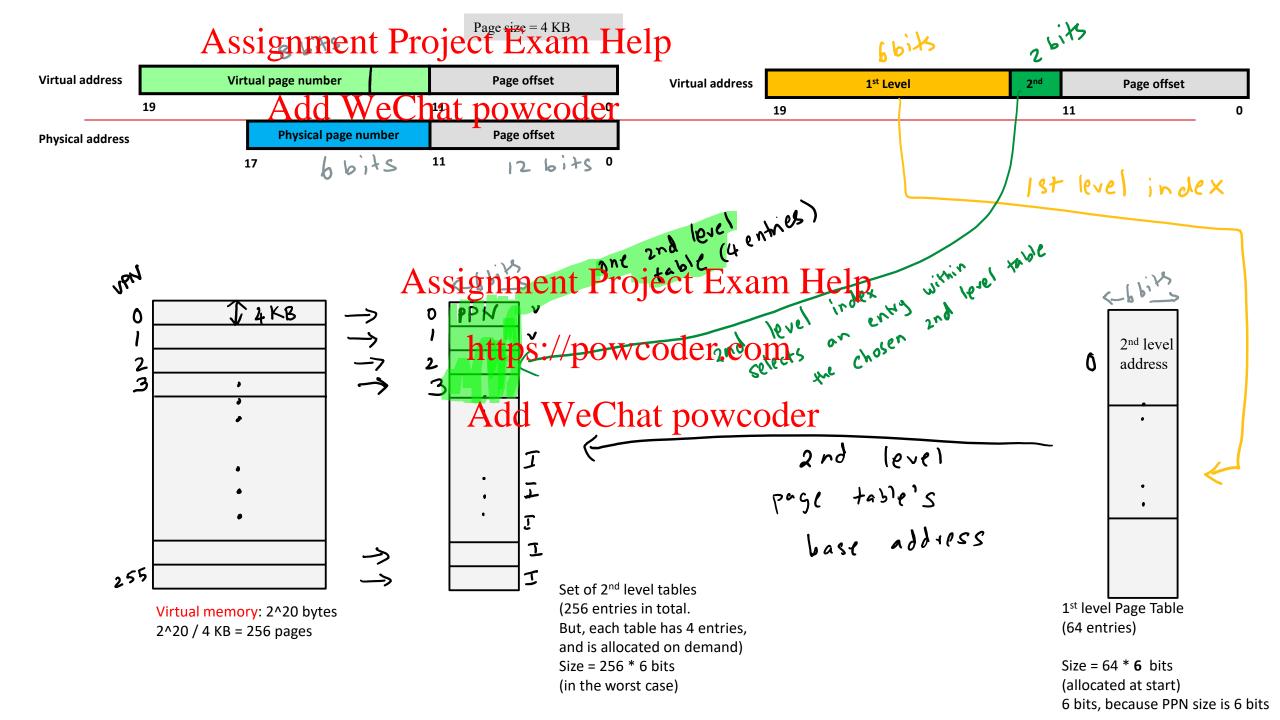
- Smaller pages (4 KB)
- Smaller page tables (as we would need for super pages at 16 KB) elp

Idea:

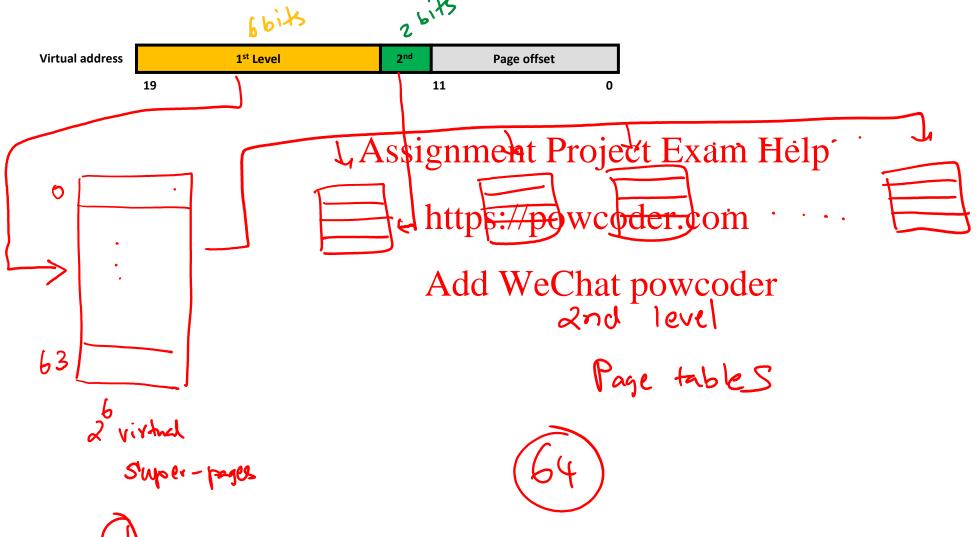
https://powcoder.com

Allocate super-page-table at the start WeChat powcoder

Allocate smaller page table for translating each smaller page within a super-page on-demand



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Hierarchical 2 level page table der

A tree-like hierarchical structure.

A 1st level page table entry (root of tree) contains location of a 2nd level page table (leaf)

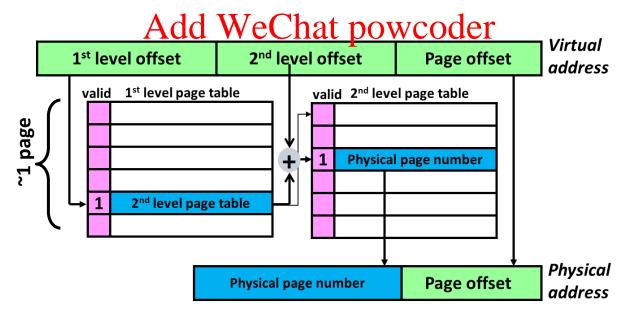
A 2nd level page table entry is same as an entry in the single-level page-table

Allocate 1st level page table when the process start Project Exam Help

Allocate a 2nd level page table on-demand only when the process accesses corresponding virtual address

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Can be generalized to n-level (multi-level) page-table



Hierarchical 2 level page table: Space benefits

2nd level page table size is proportional to the amount of virtual memory used by the process

Common case: siza of multi-level to rectable Exingle-level p

very few 2nd level page table would be allocated

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Worst case: size of multi-level page table = single-level page table + 1st level page-table

(single-level page tables are allocated)

1st level page-table is an additional overhead

Flat vs Hierarchical Chat powcoder

```
Flat (single-level)
     Pros:
         One page table lookup (one memory access) per address translation
     Cons:
         All page-table entries allocated at the start. Always takes up a lot of memory
Hierarchical (multi-level) -- Used in most modern systems
     Pros:
         Add WeChat powcoder
Allocates page-table entries on-demand. So, typically uses much less memory than single-level
     Cons:
         More page-table lookups (memory accesses) per address translation:
                   N page table lookups for N-level page table
```

Hierarchical page table: Example: 32bit Intel x86

	1 st level index	2 nd level index	Page offset	Virtual address
31	22	12	0	

Assume:

Size of 1st level index

Size of 2nd level index

Page offset size

Size of one page table entry

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12 bits (not important for this problem) https://powecoder.com

Derivation:

entries in the 1st level page table

entries in the 2nd level page table

Size of 1st level page table

Size of one 2nd level page table

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2^10

2^10

 $= 2^10 * 4 \text{ bytes} = 4 \text{ KB}$

 $= 2^10 * 4 bytes = 4 KB$

Computing Space for multi-level page table

N 2nd level page tables have been allocated. This means, 1 Jevel page table will have N valid entries.

 $\frac{https://powcoder.com}{\text{Total size of the page table}}$ Total size of the page table = 1^{st} level page-table size + N * (size of one 2^{nd} level page table)

= 4 KB + N * And WeChat powcoder

(for the example in the previous slide)

Class Problem 1 (32 bit x86) wcoder

What is the least amount of memory that could be used? When would this happen?

What is the most memory that could be used? When would this happen?

Assignment Project Exam Help How much memory is used for this memory access pattern:

0x00000ABC https://powcoder.com 0x00000ABD

0x10000ABC

Add WeChat powcoder 0x20000ABC

How much memory if we used a single-level page table with 4KB pages? Assume entries are rounded to the nearest word (4B)

Class Problem 1 (32 bit x86) wcoder

1. What is the least amount of memory that could be used? When would this happen?

when N = 0 (true when no memory has been accessed -- before program runs)

= 4 KB

https://powcoder.com

2. What is the most memory that could be used? When would this happen?

All 2nd level page tables are allocated. That is, all chires of YMCeVer page table are valid.

So,
$$N = 2 ^ 10$$

(true when program uses all virtual pages (2²⁰ pages))

```
4 KB + N * 4 KB
= 4KB + 2 ^ 10 * 4 KB
= 4 KB + 4 MB
= 4100KB
```

Class Problem 1 (32 bit x86) wcoder

3. How much memory is used for this memory access pattern:

```
0x00000ABC // Page fault
0x00000ABD
0x10000ABC // Page fault Assignment Project Exam Help
0x20000ABC // Page fault
https://powcoder.com

N = 3
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4 KB + N * 4 KB
= 4KB + 3*4KB
= 16 KB
```

Class Problem 1 (32 bit x86) wcoder

4. What is the size of a **single-level page table**? Assume entries are rounded to the nearest word (4B)

```
# Virtual pages = Total virtual memory size / page size
= 2 ^ 32 / 2 Assignment Project Exam Help
= 2 ^ 20 pages https://powcoder.com

Each virtual page has an entry in the well-had powcoder.

Single-level page table size = # entries * size of each entry
= 2^20 * 4 bytes = 4 MB
```

~= Size of all 2-level page tables in the worst case

Class Problem 1: Summary powcoder

	2-level page table size	Single-level page table size
Best case Assign	nment Project Exan	4 MB
Worst case	4 KB + 4 MB	4 MB
For given access pattern (slide 25)	ttps://powcoder.com	n4 MB

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2-level page table

Only the first level (super) page table is allocated at the start.

2nd level page tables are allocated on-demand, whenever a new super-page is accessed by the program.

Single-level page table

The entire page table is allocated at the start.

Class Problem 2 Weight Class Problem 2 Weight

```
Design a two-level page-table for a 24-bit byte addressable ISA.
```

Physical memory size = 256KB

Page size = 512 Bytes.

Size of 1st level page table entry = 3 bytes (a physical memory address pointer to a 2L page table) ASSIGNMENT Project Exam Help

Size of one 2nd level page table = 1 page Size of a 2nd level page-table entry https://powcoder.com

2nd level page table entry contains physical page number + 1 valid bit
Size of 2nd level page table entry must be smallest basible in the level page table entry must be smallest basible in the level page table entry must be smallest basible in the level page table entry must be smallest basible in the level page.

Compute:

Number of entries in each 2nd level page table 2nd level page table index size 1st level page table index size Size of the 1st level page table

Class Problem 2 Weighar chical 2-level VM

Design a two-level page-table for a 24-bit byte addressable ISA.

Physical memory size = 256KB

Page size = 512 Bytes.

$$\frac{28}{2} 28 \times 2 / 29 = \frac{3}{2} \text{ phy.}$$

Physical

Size of 1st level page table entry = 3 bytes (a physical memory address pointer to a 3L page table) ASSIGNMENT Project Exam Help

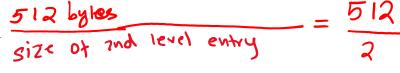
109(512)= 9

Size of one 2nd level page table = 1 page

Size of a 2nd level page-table entry

2nd level page table entry contains physical page number + 1 valid bit

Size of 2nd level page table entry must be smallest possible integer and bytes



= 256 entries

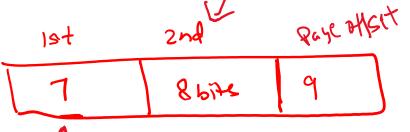
Compute:

Number of entries in each 2nd level page table

2nd level page table index size

1st level page table index size

Size of the 1st level page table ____



virtual addres:

Class Problem 2 Weighar power der VM

```
Page Offset size = log (512) = 9 bits
                                                                                                                         Page offset = 9b
                                                                                    Physical page number = 9b
Physical address size = log (256 K) = 18 bits
Physical page number (PPN) size = 18 bits (physical address size) – 9b (page offset)
                                      = 9 bits
                                        Assignment Project Exam Help
9b (PPN size) + 1 bit = ~2 bytes
2<sup>nd</sup> level page table entry size
                                                             1 page (given) = 512 bytes
Size of one 2<sup>nd</sup> level page table
                                                https://powcoder.com
#entries in 2<sup>nd</sup> level page table
                                                             512 \text{ bytes} / 2 \text{ bytes} = 256
2<sup>nd</sup> level index size
                                                Add We Chat powcoder
1<sup>st</sup> level index size
                                                 = 24 (virtual address size) - 8 (2<sup>nd</sup> level index size) - 9 (page offset size)
                                                 = 7 bits
1<sup>st</sup> level page table entry size
                                                 = 3 bytes (given)
1<sup>st</sup> level page table size
                                                 = 2^7 (\# entries) * 3 bytes = 384 bytes
```

 1^{st} level = 7b

 2^{nd} level = 8b

Page offset = 9b

Class Rroblemt Project Exam Help

Simulate for hierarchical 2-level page table in problem 2

Virtual Address	1 st level	2 nd level	Page offset	Page fault?	Physical page num.	Physical Address
0x000F0C						
0x001F0C	Assi	gnment	Project	Exar	n Help	
0x020F0C		https://p	owcode	r.cor	n	

1st level = 7b Add2Wtevellagbpoweegeeffset = 9b

Virtual address = 24b

Physical page number = 9b

Page offset = 9b

Physical address = 18b

Class Project Examples = 0000 0000 0000 1111 0000 1100

Simulate for hierarchical 2-level page table in problem 2

Virtual Address	1 st level	2 nd level	Page offset	Page fault?	Physical page num.	Physical Address
0x000F0C	0x00	0x07	0x10C	Υ	0x000	0x0010C
0x001F0C	Assi	gnment	Project	Exan	n Help	
0x020F0C		https://p	owcode	r.cor	n	

1st level = 7b Add2Wteellabpowcogteoffset = 9b

Virtual address = 24b

Physical page number = 9b

Page offset = 9b

Physical address = 18b

Class Project Exam Help

Simulate for hierarchical 2-level page table in problem 2

Virtual Address	1 st level	2 nd level	Page offset	Page fault?	Physical page num.	Physical Address
0x000F0C	0x00	0x07	0x10C	Υ	0x000	0x0010C
0x001F0C	0x0Assi	gaxorent	Project	Exar	nokbelp	0x0030C
0x020F0C		https://p	owcode	r.cor	n	

1st level = 7b Add2Wteellagbpoweggeoffset = 9b

Virtual address = 24b

Physical page number = 9b

Page offset = 9b

Physical address = 18b

Class Project Exam Help

Simulate for hierarchical 2-level page table in problem 2

Virtual Address	1 st level	2 nd level	Page offset	Page fault?	Physical page num.	Physical Address
0x000F0C	0x00	0x07	0x10C	Υ	0x000	0x0010C
0x001F0C	0x0Assi	gaxorent	Project	Exan	nokbelp	0x0030C
0x020F0C	0x01	1 1118 8://p	8×106de	r.cor	0x002	0x0050C

1st level = 7b Add2Weellabpoweegenffset = 9b

Virtual address = 24b

Physical page number = 9b

Page offset = 9b

Physical address = 18b